Volatility analysis

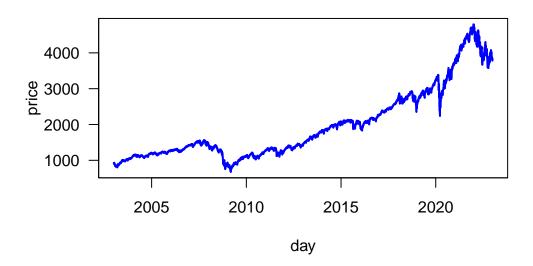
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2024-01-01

Data

We are analysing SP-500 returns from 2003-01-03 to 2022-12-30, 5034 observations. If you like thousand commas in your numbers, then 5,034 observations.

The SP-500 index



Analysis of SP-500 volatility

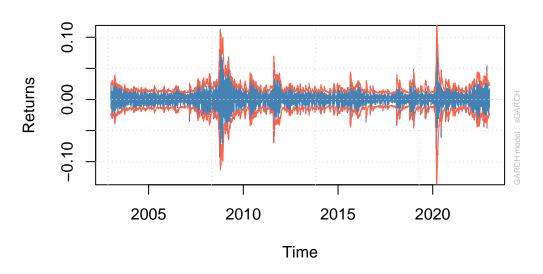
When we estimate a GARCH(1,1), we get these parameters

	Estimate	Std. Error	t value	$\Pr(> t)$
0	0.0000024 0.1202890 0.8594914	0.0097730	3.140765 12.308242 80.579245	

Note that since alpha+beta=0.98<1 , the model is covariance stationary. Note that since $\alpha+\beta=0.98<1$, the model is covariance stationary. The Log Likelihood is 16,443.07 .

Returns with 2 times volatility

Series with 2 Conditional SD Superimposed



Some VaR analysis

```
Portfolio = 1000

sigma = 0.01

p = 0.05

VaR = -qnorm(p) * Portfolio * sigma
```

Risk is \$16.4 according to the VaR.