Mapping Scotland’s Sickening: Using Lexis Surface Visualisations to compare mortality patterns between populations

# Abstract

# Introduction

This paper will present hundreds of thousands of mortality rates, recorded at over one hundred different ages and over more than sixty years, covering populations in Scotland and those of our nearest neighbours, and selected other populations from across the globe. However it will contain no statistical models, no tables, and very few numbers. It will do this by presenting a series of maps of demographic data, known as Lexis surfaces, which show how something – mortality rates, in this case – varies by both age and by year. Conceptually, Lexis surfaces are to population data as spatial maps are to physical landscapes: in spatial maps, the height of a landscape is shown as a function of both its latitude and its longitude; the Lexis surfaces presented here show mortality as a function of both age and of year. Mortality hazards can be thought to vary continuously over both age and year, much as height varies continuously with both latitude and longitude. And just as it usually makes little sense to try to understand the height of physical landscapes only as a function of their latitude or longitude alone, so this paper will argue that important patterns and features in mortality landscapes are often missed when public health research aims to understand population health, and differences between population, by looking only at how mortality risks vary as a function of age or time alone.

## Thinking in slices: Life expectancy, age schedules, drift and cohorts

A life expectancy is a common way that many individual age-specific mortality risks are summarised as a function of year alone. Life expectancies are important summary statistics, and show that, on average, one population tends to live less long than another population in a given year. It is known, for example, that the general trend has been for life expectancies to have increased in richer countries for more than a century. (Leon, 2011) Plotting life expectancies against time for many populations can also show how both relative and absolute inequalities can increase despite outcomes improving for everyone, but at a faster rate for some populations than others. For example, life expectancy at birth, for countries submitting data to the Human Mortality Database (HDM) tended to increase faster for females than males for much of the Twentieth Century, leading to a gap in life expectancy by sex opening up until the 1970s, before starting to narrow again in more recent decades, in large part due to falling rates of cardiovascular disease death in men over 60 years of age. (Glei & Horiuchi, 2007; White et al., 2014) Similarly, much of Scotland’s partly deserved status as ‘Sick Man of Europe’ is due to its life expectancy trends improving more slowly than those of European neighbours, rather than falling in absolute terms. (McCartney, Walsh, Whyte, & Collins, 2012; Whyte & Ajetunmobi, 2012) Throughout the UK, and in England & Wales in particular, there has been an unprecedented stalling in life expectancies since 2011, leading public health researchers to suggest the effects of austerity are to blame, and for actuarial models to be revised substantially. (Fransham & Dorling, 2017; Seekings, 2017)

The risk of dying, known as the force of mortality, also varies in characteristic ways with age, according to a ‘schedule’ that tends to be simple and predictable over some ages, but more complicated and unpredictable at other ages. After around the age of 50, the risk of dying in the next year has tended to increase exponentially with each additional year of age, resulting in a schedule that appears as a straight line when the logarithm of mortality is plotted as a function of age, at least until very old age. Much of this increasing mortality hazard with age has been labelled ‘senescent’, the results of chronic and cumulative deterioration of bodily structure and function with age, of cells imperfectly copying themselves, each time with some errors, which eventually accumulate and become catastrophic for bodily functioning. Long because the biology of ageing was understood, however, the straight line schedule of log mortality against age was noted by insurers, academics, and actuaries, and today is usually referred to as the Gompertz curve, after the author of a publication written in 1825. (Gompertz, 1825) However, not all deaths are caused by old age; others are caused by accidents, violence, childbirth, and other things that ‘just happen’ to bodies whatever state of repair or disrepair they are in. To represent this hazard of death, a baseline hazard has been added at all ages, producing the next simplest age-mortality schedule, known as the Gompertz-Makeham model, named additionally after the author of a paper published in an actuarial journal in 1860. (Makeham, 1860) There is also a distinct and high hazard within the first year of life, and within this first year concentrated in the first months, weeks and days. Historically the risk of dying in infancy was similar to the risk of dying at very old age, producing empirical schedules of hazard against age that were high in the first year, low in childhood, then rising again with adulthood, and because of this shape referred to as ‘bathtub curves’. Adding yet more complexity to the age schedule is the observation that the ‘baseline risk’ does not appear constant at all ages, or the same between sexes. Instead, the mortality hazard appears to diverge between in the first few years of adulthood: jumping up sharply for males at the start of childhood, largely due to violent and accidental deaths, and historically for females between around the ages of 25 and 30 years, due to the risk of death in childbirth. These additional risks in early adulthood have been described as ‘the accident hump’, although these deaths are not all accidental. Relatively few models have attempted to parametrically fit the whole age schedule, with the most comprehensive and complicated models, incorporating up to eight parameters being proposed in 1980 (Heligman & Pollard, 1980), and a somewhat simpler five parameter model, first developed for modelling mortality risks in other animals, being proposed by Siler in 1979 (Siler, 1979), and applied to humans over subsequent years. (Gage & Dyke, 1986)

Age-specific mortality risks have been constantly changing over time, however, and so any attempts to predict both healthy and overall life expectancies for populations that are not already extinct needs to account for how these age-specific risks will evolve over coming years and decades. Perhaps the most widely used modelling framework for doing this was proposed by Lee & Carter in 1992, and involves making the assumption that the logarithm of age-specific mortality rates will tend to ‘drift’ downwards over time at a constant rate. (Lee & Carter, 1992) Methodologically, it has been noted that the Lee-Carter model is a form of principle component analysis (PCA) which summarises the age-year surface of values using only the first principle component, the ‘drift parameter’, (Girosi & King, 2007) and that there may be additional value in characterising populations using additional principle components. (Giordano, Russolillo, & Haberman, 2008) Conceptually, the Lee-Carter model is based around the Gompertz-Makeham model, assuming its log-linear shape will tend to evolve according to a constant tempo, the ‘drift parameter’. For this reason, Lee-Carter models tend to be less effective in estimating mortality rate changes at younger ages (before around age 50), but are often nevertheless relatively effective at estimating future life expectancies because the majority of deaths that occur in richer countries tend to be at these older ages.

An additional complication in thinking about mortality patterns relates to efforts to uniquely model and estimate age-period-cohort (APC) effects. All populations exist and age as cohorts, ageing one year per year, and some specific cohorts appear distinct in their mortality risks than cohorts from neighbouring birth years. For example, people born around the time of the ‘Spanish Flu’ of 1918 appear to have somewhat higher mortality risks at any given age than might be expected from trends observed in earlier and later cohorts, (Almond, 2006; J Minton, Vanderbloemen, & Dorling, 2013) and people born in England and Wales in the 1950s to have a somewhat lower mortality risk as they age than might be expected from broader trends. (Willets, 2003) There have been various attempts to uniquely partition away cohort effects from age effects and period effects in statistical models (for example (Yang, Fu, & Land, 2004; Yang, Schulhofer‐Wohl, Fu, & Land, 2008)), but doing so is logically impossible, because each of the three effects cannot be uniquely identified (Wilmoth, 2006), leading to effects to do so being branded ‘futile’. (Bell & Jones, 2014)

## Thinking in surfaces: Visualising and intuiting the geography of mortality using Lexis surfaces

This paper argues that a more intuitive, and often more productive, way of thinking about and exploring mortality is by visualising log mortality rates by both age and year at once. This can be done by producing level plots, or contour plots, in which year runs across the horizontal axis, age along the vertical axis, and the ‘cells’ at each age-year ‘coordinate’ are shaded, coloured, or otherwise marked graphically according to the corresponding age-year specific log mortality hazards. Conceptually Lexis surfaces are maps of age-time much as topographic maps are maps of latitude-longitude. In epidemiology, Lexis surfaces represented as shaded contour maps have been used to identify both mortality surfaces in selected European countries, (J Minton et al., 2013) but their use in demography dates back at least to the 1980s, (Vaupel, Gambill, & Yashin, 1987) and they are based on the Lexis diagram as discussed in 1875 (Lexis, 1875).

Figure 1a presents a blank Lexis surface, with some additional bands as annotation. The Lexis surface is arranged with equal projection along both axes, such that one year in time is as wide as one year in age as tall. Because of this cohorts run diagonally from bottom left to top right at 45 degree angles. The background of the Lexis surface marks out decades as vertical lines, decadal age groups as horizontal lines, and birth cohort decades as diagonal lines. Within this figure, a specific age band, decade band, and cohort band is highlighted with green, red, and blue colours respectively. In addition to thinking about patterns on Lexis surfaces in terms of bands of parallel horizontal (age), vertical (period) and diagonal (cohort) lines, it is also often useful to look for and identify specific regions within the surface that do not strictly run across the entirety of any of these three planes. These regions can sometimes be usefully interpreted as representing either age-period interaction effects, or age-cohort interaction effects, two examples of which are marked in the figure. Within the demographic time-frame of a century or longer, a common example of an age-period interaction is a war, during which the mortality risks of young adult males tend to rise sharply, before falling back more slowly. Examples of age-cohort interactions are perhaps less common, but potentially include any *additional* additional mortality risk experienced by 1918 birth cohorts as infants, i.e. the observation of an even higher mortality rate in the first year of life for this cohort even when the whole life-course log mortality multiplier associated with membership of this cohort is taken into account. Particularly high mortality and morbidity risks in the first year of life can be signals of one of the main mechanisms through which persistent life-course cohort effects emerge, namely through interuterine and perinatal exposure to deleterious environments at these earliest life-course stages, often referred to as a Barker Effect, (Barker, 2004) after research by Barker and colleagues demonstrating links between low birthweight and a range of early onset morbidities in adulthood. (Gluckman, Hanson, & Pinal, 2005; Hales & Barker, 1992) The importance of later stages in the life course, beyond infancy, for either establishing or accelerating mortality and morbidity hazards at later age, has also been recognised in life-course epidemiology, (Ben-Shlomo, 2002) and ongoing research into the associations between deprivation, gender and cohort membership in Scotland seems to highlight the importance of young adulthood as an important life-course stage, and the macroeconomic conditions established young adults are exposed to at this stage, in establishing persistently elevated hazards of suicides and drug-related deaths throughout the later life-course. (J Minton, 2017a; Parkinson, Minton, Lewsey, Bouttell, & McCartney, 2017a, 2017b) Given the role of critical stages in life-course epidemiology, the value of identifying changes in mortality risk at younger age, as potential determinants of changes in older ages, therefore seems clear.

Figure 1b presents an impressionistic schematic of different patterns and trends that are often observed within Lexis surfaces of log mortality rates for rich world populations. Regions within this surface are coloured blue where trends in age-specific mortality tend to be improving, red where they tend to be worsening or relatively bad, and purple where the trends are more inconsistent over time and population. Arrows point upwards to indicate these improving trends, as on Lexis surfaces the corresponding ‘bands’ of mortality hazards appear to be moving upwards over time, and downwards where the mortality rates are high and/or worsening. For researchers concerned predominantly with life expectancy alone, the two most important age-year regions to note are at the bottom and top of the map, labelled ‘Falling Infant Mortality’ and ‘Lee-Carter Drift’. Mortality hazards within the first age of life have tended to fall, exponentially, since the early twentieth century in most European and North American countries; improvements in many other regions of the world have tended to have started later, but occurred even more quickly, over the middle and later parts of the twentieth century and beyond. Though the force of mortality in the first year is still much higher than over the next few years of age, it is a small fraction of levels that were typical and unchanged for the vast majority of recorded human history.

Because of this fall in infant mortality, the importance of Lee-Carter Drift as a primary determinant of future longevity has tended to rise. On the schematic of Figure 1b this is represented as applying mainly from around the age of 50 years, and until old age, but not the oldest ages. Below this age range, mortality trends tend to be more erratic, to differ more between populations and change over time. For male populations in particular, such trends may tend to be more responsive to relatively short term macroeconomic, cultural and social changes that occur within particular countries and regional population groups. For this reason, although changes in mortality rates at these younger adult ages may not contribute greatly to the sum total of mortality that occurs in any given year, they can still be important to explore, both as potential signals of period specific societal phenomena, such as violent conflicts and economic recessions, and also – via cohort effects which emerge from exposures to environmental conditions at later life-stage critical periods – as forerunners of lagged effects which may manifest as elevated mortality hazards in older age (‘scarring’). Finally, after the first year of age, mortality hazards within childhood tend to be very low, likely lower than at any previous time in human history, and to be continuing to fall; this makes the increase in mortality hazards for males, in particular, in the first few years of adulthood appear all the more abrupt and stark.

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| 1. Age, period and cohort bands, and age-period and age-cohort interactions | 1. Examples of key features often identified in Lexis surfaces of log mortality |

Figure 1 Lexis surface illustrations

# Methods

The data and methods used in this paper are largely as described in a previous paper on quantifying ‘excess deaths’ in Scotland compared with neighbouring regions over time and at different ages. (Jon Minton et al., 2017) The earlier paper used one year by one year ‘Lexis squares’ of both exposures (adjusted population counts) and death counts for a range of countries, extracted from the Human Mortality Database (HMD), covering ages in single years up to 109 years old, and years from 1950 to the last available period. In the earlier paper, populations from individual countries were nested into narrower and broader geographic regions, allowing nested comparison of Scottish age-year specific mortality rates to be compared with both our nearest neighbours (the rest of the United Kingdom), and more distant neighbours (the rest of Western Europe). This earlier paper introduced a variation of the Lexis surface, the comparative level plot (CLP), which is essentially a Lexis surfaces of differences in mortality risks between two Lexis surfaces, each covering the same range of ages and years, but for two different populations, A and B. Though it can sometimes be more intuitive to present differences between populations on the Lexis surface as ratios (B/A), (Vanderbloemen, Dorling, & Minton, 2016) CLPs instead are coloured according to differences in log mortality (Log(B) – Log(A)). Log differences of zero are represented by white cells, cells where B has a higher mortality than A by red shades, and where A has a higher mortality than A by blue shades. The magnitude of the difference between B and A is therefore indicated by the degree of shade, with deeper reds and blues indicating greater differences, and lighter shades indicating smaller differences. An advantage of visualising log mortality differences is that mortality differences of A/B and B/A will therefore be of the same shade, with A/B appearing as blue as B/A appears red. (For example, 10 and 0.1 can be represented as 101 and 10-1 respectively, and it is the magnitude of these exponents, 1 and 1, which determine the cells’ shade, whereas the sign of the exponents, positive and negative, which determine the cells’ colour.)

This paper differs from the earlier paper, however, in three ways: firstly, the previous paper also calculated life-table estimates of the effect of excess Scottish mortality risks at different ages; this paper will focus only on describing and engaging with the Lexis surfaces themselves, and as by design more impressionistic rather than actuarial in intent. Secondly, this paper will focus as much on presenting Lexis surfaces of log mortality for individual populations, as much as the CLPs showing differences in log mortality between two populations; for brevity, Lexis surfaces of log mortality will be referred to as Shaded Level Plots (SLPs), and Lexis surfaces of differences between two populations as CLPs. Thirdly, the figures within this paper will present all individual age-year specific log mortality values largely ‘as-is’, without any smoothing of values to make neighbouring values more similar. Such smoothing of neighbouring values often becomes necessary when contour lines are used, as sudden discontinuities within the surfaces tend to a result in maps that are heavily overplotted with contours, obscuring underlying patterns. However, the SLP Lexis surfaces presented here use colour and shade alone, which removes the overplotting issues that result from using contour lines.

Using colour and shade alone often creates a different interpretative risk, however, as illustrated in the famous Checkershadow Illusion, in which two equally dark grey cells either light if surrounded by darker cells, or dark if surrounded by lighter cells, highlighting the perceptual challenge of correctly decoding specific values from slight variations in cell shade. (Jonathan Minton, 2014) To reduce the risk of incorrectly inferring the value of a cell from its shade and colour, a colour scheme designed mainly to work with categorical data from the RColorBrewer package, called ‘Paired’, is used in the SCPs. (Neuwirth, 2014) This colour scheme comprises a sequence of six qualitatively dissimilar colours – blue, green, red, orange, purple, and brown – and within each of these six colours the palette cycles between a light and then a dark variant: light blue, dark blue, light green, dark green, and so on. Colours and shades between these 12 colour values are then interpolated to produce hundreds of separate colour/shade combinations for the overall palette. Adjacent groups of colours in this palette are dissimilar enough that it becomes possible to identify relatively narrow bands of values in the Lexis surfaces. Log mortality values are mapped to the palette with base 10, so -1 means 10-1 and so 0.1, -2 means 10-2 and so 0.01, and so on. A continuity correction of 10-5 is added to all values because log10 of 0 is negative infinity, and so cannot be plotted.

For the CLPs the RColorBrewer ‘RdBu’ is used. This palette comprises: dark red, light red, white, light blue, and dark blue. The middle of this palette, corresponding to white, is mapped to 0, no difference in log10 mortality values between populations, with blues implying that the first of the two populations (‘B’) being compared has a lower mortality rate than the second of the two populations (‘A’), and red implying that B has a higher mortality rate than A. The shade of red or blue indicates the size of the difference log10B – log10A for each particular age-year cell.

# Results

The results section will first present an SLP for populations in the British Isles, and then a CLP showing how age-year specific mortality rates in Scotland compare with our neighbours. It will then present SLPs and CLPs for a selection of other population groups. In both series of comparisons schematic representations of the figures will be drawn alongside the SLPs and CLPs themselves. These schematic representations contain labelled regions, coloured according to whether the values within broadly indicate improvements (blue) or deteriorations (red) in mortality risks (SLPs) or mortality inequalities (CLPs) in the corresponding SLP and CLP regions. Purple shades are used to indicate other regions in the Lexis surfaces that are useful to mention as, for example, they may indicate anomalies with the population data being visualised.

## Lexis Plots of the British Isles

Figure 2a shows the SLP for British Isles populations, and Figure 2b presents CLPs for Scotland as compared with each of these other British Isles populations. Figure 3a presents a schematic representation of some key features identified in Figure 2a, and Figure 3b a schematic representation of key features identified in Figure 2b.

### SLPs for the British Isles

As should be expected, the overall impression from the SLPs from Figure 2a is that the Lexis surfaces for these neighbouring populations are broadly similar. Each Lexis surface corresponds broadly to the schematic representation of general mortality patterns presented in Figure 1b, with infancy distinct from the rest of childhood, childhood distinct from early adulthood, and mortality from around the age of 50 distinct from earlier ages.

Impressionistically, the mortality surface for England & Wales appears ‘smoother’ than the other surfaces, with the surface for Northern Ireland appearing the most ‘noisy’ or ‘speckled’, and Scotland’s and the Republic of Ireland’s mortality surfaces appearing somewhat between Northern Ireland and England & Wales in its degree of apparent smoothness. It should be reiterated that these plots show the data ‘as-is’, with no additional smoothing applied, and instead this apparent smoothness or otherwise is a result of the population sizes of these four countries or regions, with England & Wales having the largest total population, and Northern Ireland the smallest. This difference in apparent smoothness may invite almost philosophical questions about what the mortality surfaces of a hypothetical ‘Mega Scotland’, ‘Mega Northern Ireland’, or ‘Micro England & Wales’ may look like: i.e. how these surfaces would look if the underlying age-year specific forces of mortality observed in these populations were unchanged, but the total population sizes were either much larger in the first two examples, or much smaller in the last example. Pondering this question also raises interesting thoughts about whether data from whole populations should sometimes be thought about as ‘samples’ from infinitely sized hypothetical ‘hyper-populations’, and related to this whether and how standard errors for these age-year specific point estimates should be calculated. Given such issues are not the focus of this paper, they will not be addressed further, but are raised for broader consideration and reflection in later research.

Within Figure 3a, two regions are labelled S1 and S2, where ‘S’ indicates ‘senescence’. These two regions divide the region of Lee-Carter Drift indicated in Figure 1b into broadly two distinct time periods. Within the schematic of Figure 3a this divide is placed at around 1980, but the main point is to highlight that, for many of the populations shown in Figure 3a, the degree of Lee-Carter Drift appears somewhat discontinuous. There appear to be marked differences in the degree of discontinuity between genders within each of the countries/regions mapped. Typically, the Drift appears more continuous throughout the period mapped for females than for males, where the ‘two part’ S1/S2 structure of mortality shifts is more apparent. The longer and less interrupted period of continuing older adult mortality risks for females in much of the twentieth century, compared with much more modest improvements for males of the same ages over the same periods, is the key reason why mortality gaps in life expectancy increased between genders in many rich world nations, due in large part to historically higher rates of smoking in males, and poorer cardiovascular mortality; conversely, the more rapid improvements in older ages for males have led to a closing in the sex gaps in life expectancy. There also appear to be slight differences in when S1 gave way to S2 between countries/regions within the same gender, with perhaps the S2 improvement phase beginning around three or four years earlier for English & Welsh populations than for Scottish populations. However this is a more speculative inference than for the sex mortality comparisons.

Towards the start of the period, and in particular at pre- Lee-Carter Drift ages, a region is labelled ‘DX’, shorthand for ‘Demographic Transition’. During much of the first half of the Twentieth century there were very rapid improvements in mortality risks at most ages in richer countries, of a degree not realised before or afterwards, and despite the presence of the two World Wars over these two generations. The region ‘DX’ appears to indicate the last few years of this period of rapid improvement, and is most apparent at these younger adult ages, perhaps in part due to changes in industrial activity towards less hazardous forms of labour for males, and in a sense to less hazardous forms of labour for females as well, due to improved medical care reducing the risk of death from childbirth.

The region labelled ‘CB’, or ‘Childhood Buffer’, is also marked in Figure 3a, and in Figure 2a produces a chevron-like appearance within childhood ages, with colours/shades indicating higher mortality giving way to colours/shades indicating successively lower mortality risks. For all countries/regions, it is apparent that this buffer is more distinct and localised to before adulthood ages for males than for females, with much more consistent and sharp discontinuities after adulthood for males, and more gradual increases for females reaching adulthood.

A somewhat irregular region ‘T’ is labelled, short for ‘Troubles’, the colloquial name given to the civil conflict in Northern Ireland. This is visible in male young adult all-cause mortality at younger adult ages in Northern Ireland, as a patch of dark red colours which appear after around 1972, compared with lighter pink shades, indicating lower mortality risks, at the same ages from the late 1950s to this turning point. These darker red cells at these ages then give way to slightly lighter pinks, and some green cells, over the subsequent decades. A somewhat subtler version of this same ‘disruptive’ pattern is also visible for Northern Irish females, and no corresponding sudden shift in mortality risks at these ages are visible for the other populations, including for the Republic of Ireland. This finding is the subject of an upcoming paper, (J Minton, 2017b) which also models this pattern and estimates the age distribution and total number of ‘excess deaths’ that resulted from this conflict using this all-cause mortality data alone.

The three final features to discuss are the red diagonal dashed line, which runs from slightly over the age of twenty years, up through S1 and S2; and the two regions R1, and within this R2 (‘Recent’). The diagonal red line indicates the ‘scarred cohort’ of those born around 1918; this is perhaps most visible for populations in England & Wales, and least visible within Northern Ireland, but in all cases indicates that cohorts born around the time of the Spanish Flu epidemic faced somewhat higher mortality rates as they aged than would be expected by broader trends. For all ages within this age range, with R1, covering around the 2000s, there some indications of age-specific mortality rates either stalling (England & Wales, Northern Ireland), or worsening slightly (Scotland), for males in particular. Within the Republic of Ireland, by contrast, mortality rates look to have improved slightly instead. Within R2, covering the most recent years, and younger adults, there are hints that mortality rates may be improving, and that this improvement is possibly seen more for both genders.

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| 1. *SCP of Scotland, England & Wales, Northern Ireland, and the Republic of Ireland* | 1. *CLP of Scotland compared with other populations in the British Isles* |

Figure 2 Shaded Level Plot of log10 mortality rates for Scotland, England & Wales, Northern Ireland, and the Republic of Ireland

### CLPs for the British Isles

The schematic map for discussing the CLP shown in Figure 2b is shown in Figure 3b. The purple region marked ‘I’ (Ireland) corresponds to the horizontal striation visible at many older ages when Scottish populations are compared with corresponding populations in the Republic of Ireland. These horizontal disruptions are also visible in the SLPs for the Republic of Ireland over the same age-year regions as well. Many of these stria appear to be spaced exactly ten years apart, with consecutive bands by single age that are blue-tinged in the CLPs at age 40, 50, 60, 70 and 80 years, then red-tinged at age 41, 52, 61, 71 and 81 years. As these relate to somewhat older data, it appears likely these stria are data artefacts, probably due to either death counts, or population counts, or both, for Irish populations up to the 1970s only being made available to the HMD at five or ten year age groups. The HMD employ a range of methods to interpolate data over these coarser age categories into one year by one year Lexis squares, but such methods will always be imperfect, and the striated appearance of the data appears to indicate this.

The red region ‘DX’ highlights the observation that, for females aged in their twenties in particular, mortality rates seemed slightly higher in Scotland than in England & Wales, as well as being lower than corresponding rates in the Republic of Ireland. Above the region marked DX a red diagonal stria is also visible for both genders, up to around the age of 45 years. This could be suggestive that some of the 1918 cohort effect was experienced slightly more severely for Scottish populations than English and Welsh populations; or given this stria disappears after around one decade, it could also be an artefact of, perhaps, slightly less accurate population estimates in Scotland for this cohort than for England & Wales.

The shape ‘T’ (‘Troubles’) is coloured blue in the schematic, to indicate that mortality rates in young adulthood in Scotland suddenly became relatively better after 1972 than for males of the same age in Northern Ireland. Of course this relative improvement was not due to any improvement in Scottish male mortality at these ages, but the sudden increase in mortality hazards in young Northern Irish adult males. This finding, of sudden apparent comparative improvement in Scottish mortality, was what led to the previously mentioned paper on Northern Ireland being written. (J Minton, 2017b)

The gradated red triangle ‘L’, for ‘Lag’, indicates a broad tendency firstly for trends in mortality rates improvement to lag slightly behind those of England & Wales, and secondly for much of this lag to have occurred for generations born after around the 1930s. There are indications of this broad lag operating along generational lines by looking at the changing comparative mortality for both genders in Scotland at around the age of 80 years, which move from lighter to darker red shades, and also noting a fairly subtle triangular pattern in these darker red shades when Scotland is compared with either England & Wales, or the Republic of Ireland. The transition in comparative mortality trends for Scottish populations compared with Irish is perhaps particularly stark for females, in that mortality risks were historically somewhat lower in Scotland compared with Ireland up to the end of the 1960s, and remained so at older ages up to the late 1990s. This pattern is discussed, and the implications quantified, in more detail elsewhere. (Jon Minton et al., 2017)

The final region indicated in the schematic is ‘R1’ (Recent), where perhaps the largest comparative relative mortality disadvantages in Scotland are apparent. This appears as a slightly irregularly shaped ‘cloud’ of darker red shades in both the English/Welsh, and the Irish comparison, and is much more marked for males than females. This recent growth in increased relative mortality disadvantage is also discussed in more detail elsewhere (Jon Minton et al., 2017) and is likely related to worsening trends in some forms of cause-specific mortality in young adult males including suicides and drug-related deaths. (Parkinson, Minton, Lewsey, Bouttell, & McCartney, 2017a, 2017b) Although it should be noted deaths from these causes and at these ages are relatively rare, a particular source of concern with regard to healthy ageing is if the same factors which lead to elevated mortality risks at these ages also carry over to relative mortality hazard multipliers later in the life course, and so are portents of less healthy aging trajectories for ‘Generation X’ and later cohorts.

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| 1. *Schematic representation of SLPs for British Isles populations* | 1. *Schematic representation of CLPs comparing Scottish populations against other British Isles populations* |

Figure 3 Schematic representations of SLPs and CLPs for Scotland and other British Isles populations

## Comparative Level Plot: Scotland and its Neighbours

## Lexis Plots of other populations

## Comparative Level Plots: Selected Other Populations

## Scottish Disadvantage

### Age groups

#### Older Age

#### Younger Age

## Healthy ageing

### Compression of Mortality

### Compression of Morbidity

## Life course

### Life course stages

#### Infancy

#### Adulthood

#### Senescence

### Barker & Critical Period

## Different model types

### Life Expectancies

#### Conditional and Unconditional

#### Period or Cohort

#### Extrapolation if Cohort

### Life course structures

#### Gompertz

#### Gompertz-Makeham

#### Siler

#### Non-Parametric

#### Heligman Pollard

### Drift Models:

#### Lee-Carter

#### Quasi-Spatial (Girosi & King)

## Lexis surfaces

### Concept

### Origins

### Applications

### Variants

## Ways of Reasoning about data

### Reasoning: Inductive, Deductive, Abductive

### Case-based and variable-based

### Lexis surfaces as case-based approach

## Aim

### Use Lexis surfaces to apply case-based reasoning to populations, and population comparisons

### To understand accumulation of Scottish disadvantage over the life course

### To understand additional selected phenomena

# Results

## Lexis Plots of the British Isles

## Comparative Level Plot: Scotland and its Neighbours

## Lexis Plots of other populations

## Comparative Level Plots: Selected Other Populations

# Discussion

## Implications for Practice

### Conclusions regarding Scotland

### Conclusions regarding other countries

## Implications for Research

### Case-based reasoning

### Modelling approaches

### Lexis surfaces in an abductive research workflow

### Interactive Lexis surfaces

## Final summary