The Definition of Red JonPRL, the people's refinement logic

The JonPRL Group January 21, 2016

Contents

	Signatures		
	1.1	Grammar	4
	1.2	Static Semantics	4

Chapter 1

Signatures

Decisively Smash The Formalist Clique!

Chairman Jon

A *signature* is a collection of definitions, including terms, tactics and theorems.

1.1 Grammar

The grammar of Red JonPRL signatures is presented in Figure 1.1. Note that an optional production of sort s is formatted $\langle s \rangle$ in the rules.

```
sigexp ::= \langle \cdot \rangle
                                                                                empty signature
                                                                                signature extension
                     sigexp.\ sigdec
    sigdec ::= Def opid \langle [params] \rangle \langle (args) \rangle : sortid = [term]
                                                                                operator definition
                     Tac opid\langle [params]\rangle\langle (args)\rangle = [term]
                                                                                tactic definition
                     Thm opid\langle [params]\rangle\langle (args)\rangle : [term] by [term]
                                                                                theorem declaration
                                                                                empty parameter list
  params
              ::=
                     params, symbind
                                                                                parameter list extension
                    \langle \cdot \rangle
                                                                                empty argument list
      args
                     args, metabind
                                                                                argument list extension
 symbind
                    symid: sortid
                                                                                symbol binding
             ::=
metabind
                    metaid:valence
                                                                                metavariable binding
                     \langle\langle \{sortlist\}\rangle\langle [sortlist]\rangle.\rangle sortid
  valence
                                                                                valence
  sortlist
                                                                                empty sort list
             ::=
                                                                                sort list extension
                     sortlist, sortid
```

Figure 1.1: Grammar of signature expressions. The identifier sorts *opid*, *sortid*, *symid* and *metaid* can be assumed to be arbitrary strings; the sort *term* is left uninterpreted.

1.2 Static Semantics

The static semantics for Red JonPRL signatures begins with a specification of the class of *semantic* objects that will serve as the meanings for the *syntactic* objects defined in Section 1.1. We assume an ambient abstract binding tree signature such that at least the following facts hold:

$$\frac{\mathsf{tac}\; sort}{\Upsilon \Vdash \mathsf{prove} : (.\,\mathsf{exp}\,, \mathsf{tac})\,\mathsf{thm}} \frac{\mathsf{opid}\; sort}{\mathsf{opid}\; sort}$$

Then, our semantic objects are defined as in Figure 1.2.

Figure 1.2: Specification of the semantic objects.

A natural semantics hinges on the elaboration judgment $E \vdash A \Longrightarrow A'$, which means that the syntactic object A elaborates to the semantic object A' in the environment E. Let the $\Upsilon_{\Sigma} \in \text{Params}$ be defined as follows:

$$\Upsilon_{\Sigma}(\vartheta) \triangleq \left\{ egin{array}{ll} \mathtt{opid} & \mathit{if} & \vartheta \in \mathbf{dom}(\Sigma) \\ \bot & \mathit{otherwise} \end{array}
ight.$$

Symbol Bindings

$$\Sigma \vdash symbind \Longrightarrow (a, \tau)$$

$$\frac{\Sigma \vdash symid \Longrightarrow \mathbf{a} \quad \Sigma \vdash sortid \Longrightarrow \tau}{\Sigma \vdash symid : sortid \Longrightarrow (\mathbf{a}, \tau)}$$
(1.1)

Metavariable Bindings

$$\Sigma \vdash metabind \Longrightarrow (\mathbf{m}, v)$$

$$\frac{\Sigma \vdash metaid \Longrightarrow \mathfrak{m} \quad \Sigma \vdash metaid \Longrightarrow v}{\Sigma \vdash metaid \Longrightarrow (\mathfrak{m}, v)}$$

$$(1.2)$$

Parameters

$$\Sigma \vdash params \Longrightarrow \Upsilon$$

$$\overline{\Sigma \vdash \langle \, \cdot \, \rangle \Longrightarrow \{\}} \tag{1.3}$$

$$\frac{\Sigma \vdash params \Longrightarrow \Upsilon \quad \Sigma \vdash symbind \Longrightarrow (a, \tau)}{\Sigma \vdash params, symbind \Longrightarrow \Upsilon \cup a \mapsto \tau}$$
(1.4)

Arguments

$$\Sigma \vdash args \Longrightarrow \Theta$$

$$\overline{\Sigma \vdash \langle \, \cdot \, \rangle \Longrightarrow \{\}} \tag{1.5}$$

$$\frac{\Sigma \vdash args \Longrightarrow \Theta \quad \Sigma \vdash metabind \Longrightarrow (\mathfrak{m}, v)}{\Sigma \vdash args, metabind \Longrightarrow \Theta \cup \mathfrak{m} \mapsto v}$$
 (1.6)

Operator Identifiers

$$\Sigma \vdash opid \Longrightarrow \vartheta$$

$$\frac{\vartheta \not\in \mathbf{dom}(\Sigma)}{\Sigma \vdash opid \Longrightarrow \vartheta} \tag{1.7}$$

Declarations

$$\Sigma \vdash sigdec \Longrightarrow (\vartheta, D)$$

$$\begin{array}{cccc} \Sigma \vdash params \Longrightarrow \Upsilon & \Sigma \vdash sortid \Longrightarrow \tau & \Sigma \vdash opid \Longrightarrow \vartheta \\ \Sigma \vdash args \Longrightarrow \Theta & \Sigma \vdash term \Longrightarrow M & \Theta \triangleright \Upsilon_{\Sigma} \oplus \Upsilon \parallel \cdot \vdash M : \tau \\ \hline \Sigma \vdash \mathsf{Def} \ opid \langle [params] \rangle \langle (args) \rangle : sortid = [term] \Longrightarrow (\vartheta, \langle \Upsilon, \Theta, \tau, M \rangle) \end{array} \tag{1.8}$$

$$\begin{array}{ccc} \Sigma \vdash params \Longrightarrow \Upsilon \\ \Sigma \vdash args \Longrightarrow \Theta \\ \Sigma \vdash term \Longrightarrow M \end{array} & \begin{array}{c} \Sigma \vdash opid \Longrightarrow \vartheta \\ \Theta \rhd \Upsilon_\Sigma \oplus \Upsilon \parallel \cdot \vdash M : \texttt{tac} \end{array} \\ \hline \Sigma \vdash \mathsf{Tac} \ opid \langle \lceil params \rceil \rangle \langle (args) \rangle = \lceil term \rceil \Longrightarrow (\vartheta, \langle \Upsilon, \Theta, \texttt{tac}, M \rangle) \end{array}$$

Signatures

 $\vdash sigexp \Longrightarrow \Sigma$

(1.9)

$$\overline{\vdash \langle \cdot \rangle \Longrightarrow \{\}} \tag{1.11}$$

$$\frac{\vdash sigexp \Longrightarrow \Sigma \quad \Sigma \vdash sigdec \Longrightarrow (\vartheta, D)}{\vdash sigexp. \ sigdec \Longrightarrow \Sigma \cup \vartheta \mapsto D}$$
(1.12)