

**ONE MARK QUESTION FOR PRACTICES**

**CHAPTERWISE/TOPICWISE**

**RELATION AND FUNCTIONS**

1. Let  $A = \{1, 2, 3\}$  and let  $R = \{(1, 1), (2, 2), (3, 3), (1, 3), (3, 2), (1, 2)\}$ . The  $R$  is
  - (a) reflexive and symmetric but not transitive
  - (b) reflexive and transitive but not symmetric
  - (c) symmetric and transitive but not reflexive
  - (d) an equivalence relation
2. Let  $A = \{a, b, c\}$  and Let  $R = \{(a, a), (a, b), (b, a)\}$ . Then  $R$  is
  - (a) reflexive and symmetric but not transitive
  - (b) reflexive and transitive but not symmetric
  - (c) symmetric and transitive but not reflexive
  - (d) an equivalence relation
3. Let  $A = \{1, 2, 3\}$  and let  $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 1), (2, 3), (3, 2)\}$ . The  $R$  is
  - (a) reflexive and symmetric but not transitive
  - (b) reflexive and transitive but not symmetric
  - (c) symmetric and transitive but not reflexive
  - (d) an equivalence relation
4. Let  $S$  be the set of all straight lines in a plane. Let  $R$  be the relation  $S$  defined by  $aRb \Leftrightarrow a \perp b$ . Then  $R$  is
  - (a) reflexive but neither symmetric nor transitive
  - (b) symmetric but neither reflexive nor transitive
  - (c) transitive but neither reflexive nor symmetric
  - (d) an equivalence relation
5. Let  $S$  be the set of all straight lines in a plane. Let  $R$  be the relation  $S$  defined by  $aRb \Leftrightarrow a \parallel b$ . Then  $R$  is

- ( a ) reflexive and symmetric but not transitive
  - ( b ) reflexive and transitive but not symmetric
  - ( c ) symmetric and transitive but not reflexive
  - ( d ) an equivalence relation
6. Let  $Z$  be the set of all integers and let  $R$  be a relation on  $Z$  defined by  $aRb \Leftrightarrow (a-b)$  is divisible by 3. Then  $R$  is
- ( a ) reflexive and symmetric but not transitive
  - ( b ) reflexive and transitive but not symmetric
  - ( c ) symmetric and transitive but not reflexive
  - ( d ) an equivalence relation
7. Let  $N$  be the set of all natural numbers and let  $R$  be a relation on  $N$  defined by  $aRb \Leftrightarrow a$  is factor of  $b$ . Then  $R$  is
- ( a ) reflexive and symmetric but not transitive
  - ( b ) reflexive and transitive but not symmetric
  - ( c ) symmetric and transitive but not reflexive
  - ( d ) an equivalence relation
8. Let  $Z$  be the set of all integers and let  $R$  be a relation on  $Z$  defined by  $aRb \Leftrightarrow (a \geq b)$ . Then  $R$  is
- ( a ) symmetric and transitive but not reflexive
  - ( b ) reflexive and symmetric but not transitive
  - ( c ) reflexive and transitive but not symmetric
  - ( d ) an equivalence relation
9. Let  $S$  be the set of all real numbers. Let  $R$  be the relation  $S$  defined by  $aRb \Leftrightarrow |a| \leq b$
- Then  $R$  is
- ( a ) reflexive but neither symmetric nor transitive
  - ( b ) symmetric but neither reflexive nor transitive
  - ( c ) transitive but neither reflexive nor symmetric

( d ) None of these

10. Let  $S$  be the set of all real numbers. Let  $R$  be the relation  $S$  defined by  $aRb \Leftrightarrow |a - b| \leq 1$ . Then  $R$  is
- (a) reflexive and symmetric but not transitive
  - (b) reflexive and transitive but not symmetric
  - (c) symmetric and transitive but not reflexive
  - (d) an equivalence relation
11. Let  $S$  be the set of all real numbers and let  $R$  be a relation on  $S$ , defined by  $a R b \Leftrightarrow (1 + ab) > 0$ . Then,  $R$  is
- (a) reflexive and symmetric but not transitive
  - (b) reflexive and transitive but not symmetric
  - (c) symmetric and transitive but not reflexive
  - (d) none of these
12. Let  $S$  be the set of all triangles in a plane and let  $R$  be a relation on  $S$  defined by  $\Delta_1 S \Delta_2 \Leftrightarrow \Delta_1 \equiv \Delta_2$ . Then,  $R$  is
- (a) Reflexive and symmetric but not transitive
  - (b) Reflexive and transitive but not symmetric
  - (c) Symmetric and transitive but not reflexive
  - (d) An equivalence relation
13. Let  $S$  be the set of all real numbers and let  $R$  be a relation on  $S$  defined by  $a R b \Leftrightarrow a^2 + b^2 = 1$ . Then,  $R$  is
- (a) symmetric but neither reflexive nor transitive
  - (b) reflexive but neither symmetric nor transitive
  - (c) transitive but neither reflexive nor symmetric
  - (d) none of these
14. Let  $R$  be a relation on  $N \times N$ , defined by  $(a,b) R (c,d) \Leftrightarrow a + d = b + c$ . Then,  $R$  is
- (a) reflexive and symmetric but not transitive

- ( b ) reflexive and transitive but not symmetric
  - ( c ) symmetric and transitive but not reflexive
  - ( d ) an equivalence relation
15. Let  $A$  be the set of all points in a plane and let  $O$  be the origin, Let  $R = \{(P, Q) : OP = OQ\}$ . Then,  $R$  is
- ( a ) reflexive and symmetric but not transitive
  - ( b ) reflexive and transitive but not symmetric
  - ( c ) symmetric and transitive but not reflexive
  - ( d ) an equivalence relation
16.  $F : \mathbb{N} \rightarrow \mathbb{N} : f(x) = 2x$  is
- (a) one-one and onto
  - (b) one-one and into
  - (c) many-one and onto
  - (d) many-one and into
17.  $f : \mathbb{N} \rightarrow \mathbb{N} : f(x) = x^2 + x + 1$  is
- (a) one-one and onto
  - (b) one-one and into
  - (c) many-one and onto
  - (d) many-one and into
18.  $f : \mathbb{R} \rightarrow \mathbb{R} : f(x) = x^2$  is
- (a) one-one and onto
  - (b) one-one and into
  - (c) many-one and onto
  - (d) many-one and into
19.  $f : \mathbb{R} \rightarrow \mathbb{R} : f(x) = x^3$  is
- (a) one-one and onto
  - (b) one-one and into

- (c) many-one and onto  
(d) many-one and into
20.  $f : \mathbb{R}^+ \rightarrow \mathbb{R}^+ : f(x) = e^x$  is  
(a) many – one and into  
(b))many – one and onto  
(c) one-one and into  
(d) one-one and onto
21.  $f : \left[-\frac{\pi}{2}, \frac{\pi}{2}\right] \rightarrow [-1, 1] : f(x) = \sin x$  is  
(a) one-one and into  
(b) one-one and onto  
(c) many-one and into  
(d) many-one and onto
22.  $f : \mathbb{R} \rightarrow \mathbb{R} : f(x) = \cos x$  is  
(a) one-one and into  
(b) one-one and onto  
(c) many-one and into  
(d) many-one and onto
23.  $f : \mathbb{C} \rightarrow \mathbb{R} : f(z) = |z|$  is  
(a) one-one and into  
(b) one-one and onto  
(c) many-one and into  
(d) many-one and onto
24. Let  $A = \mathbb{R} - [3]$  and  $B = \mathbb{R} - [1]$ . Then,  $f : A \rightarrow B : f(x) = \frac{x-2}{x-3}$  is  
(a) one-one and into  
(b) one-one and onto

(c) many-one and into

(d) many-one and onto

25. Let  $f : \mathbb{N} \rightarrow \mathbb{N} : f(n) = \begin{cases} \frac{n+1}{2} \\ \frac{n}{2} \end{cases}$  Then,  $f$  is

(a) One-one and into

(b) One-one and onto

(c) Many-one and into

(d) Many-one and onto

26. Let  $A$  and  $B$  be two non-empty sets and let  $f : (A \times B) \rightarrow (B \times A) : f(a,b) = (b,a)$ . Then,  $f$  is

(a) one-one and onto

(b) one-one and into

(c) many-one and onto

(d) many-one and into

27. Let  $f : \mathbb{Q} \rightarrow \mathbb{Q} : f(x) = (2x + 3)$ , Then,  $f^{-1}(y) = ?$

(a)  $(2y - 3)$

(b)  $1/(2y - 3)$

(c)  $\frac{1}{2}(y - 3)$

(d) none of these

28. Let  $f : \mathbb{R} - \{-4/3\} \rightarrow \mathbb{R} - \{4/3\} : f(x) = \frac{4x}{3x+4}$ . Then,  $f^{-1}(y) = ?$

(a)  $4y/(4-3y)$

(b)  $4y/(4+3y)$

(c)  $4y/(3y-4)$

(d) none of these

29. Let  $f : \mathbb{N} \rightarrow \mathbb{X} : f(x) = 4x^2 + 12x + 15$ . Then,  $f^{-1}(y) = ?$

(a)  $\frac{1}{2}(\sqrt{y-4}+3)$

(b)  $\frac{1}{2}(\sqrt{y-6}-3)$

(c)  $\frac{1}{2}(\sqrt{y-4}+5)$

(d) none of these

30. If:  $f(x) = \frac{4x+3}{6x-4}$ ,  $x \neq 2/3$  then  $(f \circ f)(x) = ?$

(a)  $x^2$

(b)  $(2x - 3)$

(c)

$\frac{4x-6}{3x+4}$

(d) none of these

31. If  $f(x) = (x^2 - 1)$  and  $g(x) = (2x + 3)$  then  $(g \circ f)(x) = ?$   
 (a)  $(2x^2 + 3)$  (b)  $(3x^2 + 2)$  (c)  $(2x^2 + 1)$  (d) none of these
32. If  $f\left(x + \frac{1}{x}\right) = x^2 + \frac{1}{x^2}$ , then  $f(x) = ?$   
 (a)  $x^2$  (b)  $(x^2 - 1)$  (c)  $(x^2 - 2)$  (d) none of these
33. If  $f(x) = \frac{1}{1-x}$ , then  $(f \circ f \circ f)(x) = ?$   
 (a)  $1/(1 - 3x)$  (b)  $x/(1 + 3x)$  (c)  $x$  (d) none of these
34. If  $f(x) = \sqrt[3]{3-x^3}$  then  $(f \circ f)(x) = ?$   
 (a)  $x^{1/3}$  (b)  $x$  (c)  $(1 - x^{1/3})$  (d) none of these
35. If  $f(x) = x^2 - 3x + 2$  then  $(f \circ f)(x) = ?$   
 (a)  $x^4$  (b)  $x^4 - 6x^3$  (c)  $x^4 - 6x^3 + 10x^2$  (d) none of these
36. If  $f(x) = 8x^3$  and  $g(x) = x^{1/3}$  then  $(g \circ f)(x) = ?$   
 (a)  $x$  (b)  $2x$  (c)  $x/2$  (d)  $3x^2$
37. If  $f(x) = x^2$ ,  $g(x) = \tan x$  and  $h(x) = \log x$  then  $\{h \circ (g \circ f)\}(\sqrt{\pi/4}) = ?$   
 (a) 0 (b) 1 (c)  $1/x$  (d)  $\frac{1}{2} \log \frac{\pi}{4}$
38. If  $f = \{(1,2), (3,5), (4,1)\}$  and  $g = \{(2,3), (5,1), (1,3)\}$  then  $(g \circ f) = ?$   
 (a)  $\{(3,1), (1,3), (3,4)\}$  (b)  $\{(1,3), (3,1), (4,3)\}$   
 (c)  $\{(3,4), (4,3), (1,3)\}$  (d)  $\{(2,5), (5,2), (1,3)\}$
40. Let  $f(x) = \sqrt{9-x^2}$  Then, Dom  $(f) = ?$   
 (a)  $[-3, 3]$  (b)  $(-\infty, -3]$  (c)  $[3, \infty)$  (d)  $(-\infty, -3] \cup (4, \infty)$
41. Let  $f(x) = \sqrt{\frac{x-1}{x-4}}$ . Then, dom  $(f) = ?$   
 (a)  $[1,4)$  (b)  $[1,4]$  (c)  $(-\infty, 4]$  (d)  $(-\infty, 1] \cup (4, \infty)$
42. Let  $f(x) = e^{\sqrt{x^2-1}} \cdot \log(x-1)$ , Then, dom  $(f) = ?$

- (a)  $(-\infty, 1]$  (b)  $[-1, \infty)$  (c)  $(1, \infty)$  (d)  $(-\infty, -1] \cup (1, \infty)$
43. Let  $f(x) = \frac{x}{x^2 - 1}$ . Then,  $\text{dom}(f) = ?$   
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{1\}$  (c)  $\mathbb{R} - \{-1\}$  (d)  $\mathbb{R} - \{-1, 1\}$
44. Let  $f(x) = \frac{\sin^{-1} x}{x}$ , Then,  $\text{dom}(f)$   
 (a)  $(-1, 1)$  (b)  $[-1, 1]$  (c)  $[-1, 1] - [0]$  (d) none of these
45. Let  $f(x) = \cos^{-1} 2x$ . Then,  $\text{dom}(f) = ?$   
 (a)  $[-1, 1]$  (b)  $[-\frac{1}{2}, \frac{1}{2}]$  (c)  $[-\frac{\pi}{2}, \frac{\pi}{2}]$  (d)  $[-\frac{\pi}{4}, \frac{\pi}{4}]$
46. Let  $f(x) = \cos^{-1}(3x - 1)$ , Then,  $\text{dom}(f) = ?$   
 (a)  $(0, \frac{2}{3})$  (b)  $[0, \frac{2}{3}]$  (c)  $[-\frac{2}{3}, \frac{2}{3}]$  (d) none of these
47. Let  $f(x) = \sqrt{\cos x}$ , Then,  $\text{dom}(f) = ?$   
 (a)  $[0, \frac{\pi}{2}]$  (b)  $[\frac{3\pi}{2}, 2\pi]$  (c)  $[0, \frac{\pi}{2}] \cup [\frac{3\pi}{2}, 2\pi]$  (d) none of these
48. Let  $f(x) = x^2$ , Then,  $\text{dom}(f)$  and  $\text{range}(f)$  are respectively  
 (a)  $\mathbb{R}$  and  $\mathbb{R}$  (b)  $\mathbb{R}^+$  and  $\mathbb{R}^+$  (c)  $\mathbb{R}$  and  $\mathbb{R}^+$  (d)  $\mathbb{R}$  and  $\mathbb{R} - (0)$
49. Let  $f(x) = x^3$ , Then,  $\text{dom}(f)$  and  $\text{range}(f)$  are respectively  
 (a)  $\mathbb{R}$  and  $\mathbb{R}$  (b)  $\mathbb{R}^+$  and  $\mathbb{R}^+$  (c)  $\mathbb{R}$  and  $\mathbb{R}^+$  (d)  $\mathbb{R}^+$  and  $\mathbb{R}$
50. Let  $f(x) = \log(1 - x) + \sqrt{x^2 - 1}$ . Then,  $\text{dom}(f) = ?$   
 (a)  $(1, \infty)$  (b)  $(-\infty, -1]$  (c)  $[-1, 1)$  (d)  $(0, 1)$
51. Let  $f(x) = \frac{1}{(1 - x^2)}$ . Then  $\text{range}(f) = ?$   
 (a)  $(-\infty, 1]$  (b)  $[1, \infty)$  (c)  $[-1, 1]$  (d) none of these
52. Let  $f(x) = \frac{x^2}{(1 + x^2)}$ . Then,  $\text{range}(f) = ?$



- (a)  $[1, \infty)$  (b)  $[0, 1)$  (c)  $[-1, 1]$  (d)  $(0, 1]$
53. The range of  $f(x) = x + \frac{1}{x}$  is  
 (a)  $[-2, 2]$  (b)  $[2, \infty)$  (c)  $(-\infty, -2]$  (d) none of these
54. The range of  $f(x) = a^x$ , where  $a > 0$  is  
 (a)  $[-\infty, 0]$  (b)  $[-\infty, 0)$  (c)  $[0, \infty)$  (d)  $(0, \infty)$
55. If  $f(x) = x^2 - 1$  and  $g(x) = \sqrt{x}$ , then  $g \circ f(1)$  is :  
 (a)  $-1$  (b)  $0$  (c)  $1$  (d)  $2$ .
56. If  $f(x) = x^2 + 2$  and  $g(x) = 3x + 1$ , then  $f \circ g(2)$  is :  
 (A) 19 (B) 50 (C) 51 (D) 49.
57. If  $f(x) = e^x$  and  $g(x) = \log(x)$  then  $(f \circ g)(1)$  is :  
 (A)  $e$  (B)  $0$  (C)  $1$  (D)  $2$ .
58.  $f(x) = \begin{cases} 3x-1, & \text{when } x > 1 \\ -x, & \text{when } x \leq 1, \end{cases}$  the value of  $f(0)$  is :  
 (a)  $-1$  (b)  $0$  (c)  $1$  (d)  $2$ .
59. If the function  $f(x)$  is defined as :  
 $f(x) = \begin{cases} 3x+1, & \text{when } x > 1 \\ -x, & \text{when } x \leq 1, \end{cases}$  the value of  $f(2)$  is :  
 (a)  $-2$  (b)  $2$  (c)  $4$  (d)  $7$
60. If  $f(x) = \begin{cases} 3x-1, & \text{when } x > 1 \\ -x, & \text{when } x < 1, \end{cases}$  the value of  $f(-2)$  is :  
 (a)  $2$  (b)  $-2$  (c)  $-7$  (d)  $5$
61. Let  $S = \{1, 4, 5\}$  and  $f : S \rightarrow S$  is defined by  $f = \{(1, 1), (4, 5), (5, 4)\}$ .  $f^{-1}$  is equal to  
 (a)  $\{(1, 1), (5, 4), (4, 5)\}$   
 (b)  $\{(1, 1), (4, 4), (5, 5)\}$   
 (c) does not exist

(d) None of these.

62. If  $f : R \rightarrow R$  is given by  $f(x) = 4x - 1$  and  $g : R \rightarrow R$  is given by

$g(x) = x^3 + 2$ , then the value of  $(f \circ g)(1)$  is :

(a) 29 (b) 11 (c) 31 (d) none of these.

63. If  $f : R \rightarrow R$  given by  $f(x) = x^3 + 5$ , then  $f^{-1}(x)$  is :

(a)  $(x - 5)^{1/3}$  (b)  $(x + 5)^{1/3}$  (c)  $(x - 5)^3$  (d) none of these.

### **RELATION AND FUNCTIONS : ANSWERS**

1.b	2.c	3.a	4.b	5.d	6.d	7.b	8.c	9.c	10.a
11.a	12.d	13.a	14.d	15.d	16.b	17.b	18.d	19.a	20.d
21.b	22.c	23.c	24.b	25.d	26.a	27.c	28.a	29.b	30.a
31.c	32.c	33.c	34.b	35.d	36.b	37.a	38.b	39.a	40.d
41.c	42.d	43.c	44.b	45.b	46.c	47.c	48.c	49.a	50.b
51.b	52.b	53.d	54.d	55.b	56.c	57.c	58.b	59.a	60.a
61.a	62.b	63.a							