

### **INDEFINITE INTEGRALS-IV**

1.  $\int \frac{dx}{(9+x^2)} = ?$

- (a)  $\tan^{-1} \frac{x}{3} + C$       (b)  $\frac{1}{3} \tan^{-1} \frac{x}{3} + C$       (c)  $3 \tan^{-1} \frac{x}{3} + C$       (d) none of these

2.  $\int \frac{dx}{(4+16x^2)} = ?$

- (a)  $\frac{1}{32} \tan^{-1} 4x + C$       (b)  $\frac{1}{16} \tan^{-1} \frac{x}{2} + C$       (c)  $\frac{1}{8} \tan^{-1} 2x + C$       (d)  $\frac{1}{4} \tan^{-1} \frac{x}{2} + C$

3.  $\int \frac{dx}{(9+4x^2)} dx = ?$

- (a)  $\frac{1}{2} \tan^{-1} \frac{2x}{3} + C$       (b)  $\frac{1}{6} \tan^{-1} \frac{2x}{3} + C$       (c)  $\frac{1}{6} \tan^{-1} \frac{3x}{2} + C$       (d) none of these

4.  $\int \frac{\sin x}{(1+\cos^2 x)} dx = ?$

- (a)  $-\tan^{-1} (\cos x) + C$       (b)  $\cot^{-1} (\cos x) + C$       (c)  $-\cot^{-1} (\cos x) + C$       (d)  $\tan^{-1} (\cos x) + C$

5.  $\int \frac{\cos x}{(1+\sin^2 x)} dx = ?$

- (a)  $-\tan^{-1} (\sin x) + C$       (b)  $\tan^{-1} (\cos x) + C$       (c)  $\tan^{-1} (\sin x) + C$       (d)  $-\tan^{-1} (\cos x) + C$

6.  $\int \frac{e^x}{(e^{2x}+1)} dx = ?$

- (a)  $\cot^{-1}(e^x) + C$       (b)  $\tan^{-1}(e^x) + C$       (c)  $2 \tan^{-1}(e^x) + C$       (d) none of these

7.  $\int \frac{3x^5}{(1+x^{12})} dx = ?$

- (a)  $\tan^{-1} x^6 + C$       (b)  $\frac{1}{4} \tan^{-1} x^6 + C$       (c)  $\frac{1}{2} \tan^{-1} x^6 + C$       (d) none of these

8.  $\int \frac{2x^3}{(4+x^8)} dx = ?$

(a)  $\frac{1}{2} \tan^{-1} \frac{x^4}{2} + C$  (b)  $\frac{1}{4} \tan^{-1} \frac{x^4}{2} + C$  (c)  $\frac{1}{2} \tan^{-1} x^4 + C$  (d) none of these

9.  $\int \frac{dx}{(x^2 + 4x + 8)} = ?$

(a)  $\frac{1}{2} \tan^{-1} \left( \frac{x+2}{2} \right) + C$  (b)  $\frac{1}{2} \tan^{-1} \left( \frac{x+2}{2} \right) + C$  (c)  $\frac{1}{2} \tan^{-1} (x+2) + C$

(d)  $\tan^{-1} \left( \frac{x+2}{2} \right) + C$

10.  $\int \frac{dx}{(2x^2 + x + 3)} = ?$

(a)  $\frac{1}{\sqrt{23}} \tan^{-1} \left( \frac{4x+1}{\sqrt{23}} \right) + C$

(b)  $\frac{1}{\sqrt{23}} \tan^{-1} \left( \frac{x+1}{\sqrt{23}} \right) + C$

(c)  $\frac{2}{\sqrt{23}} \tan^{-1} \left( \frac{4x+1}{\sqrt{23}} \right) + C$

(d) none of these.

11.  $\int \frac{dx}{(e^x + e^{-x})} = ?$

(a)  $\tan^{-1} (e^x) + C$  (b)  $\tan^{-1} (e^{-x}) + C$  (c)  $-\tan^{-1} (e^{-x}) + C$  (d) none of these

12.  $\int \frac{x^2}{(9 + 4x^2)} = ?$

(a)  $\frac{x}{4} - \frac{1}{8} \tan^{-1} \frac{x}{3} + C$

(b)  $\frac{x}{4} - \frac{3}{8} \tan^{-1} \frac{x}{3} + C$

(c)  $\frac{x}{4} - \frac{3}{8} \tan^{-1} \frac{2x}{3} + C$

(d) none of these .

13.  $\int \frac{(x^2 - 1)}{(x^2 + 4)} dx = ?$

(a)  $x - 5 \tan^{-1} \frac{x}{2} + C$  (b)  $x - \frac{5}{2} \tan^{-1} \frac{x}{2} + C$  (c)  $x - \frac{5}{2} \tan^{-1} \frac{5x}{2} + C$  (d) none of these

14.  $\int \frac{dx}{(4 + 9x^2)} = ?$

(a)  $\frac{2}{3} \tan^{-1} \frac{3x}{2} + C$  (b)  $\frac{1}{6} \tan^{-1} 3x + C$  (c)  $\frac{1}{6} \tan^{-1} \frac{3x}{2} + C$  (d) none of these

15.  $\int \frac{dx}{(4x^2 - 4x + 3)} = ?$

(a)  $\frac{1}{\sqrt{2}} \tan^{-1} \left( \frac{2x-1}{\sqrt{2}} \right) + C$  (b)  $\frac{1}{2\sqrt{2}} \tan^{-1} \left( \frac{2x-1}{\sqrt{2}} \right) + C$

(c)  $-\frac{1}{\sqrt{2}} \tan^{-1} \left( \frac{2x-1}{\sqrt{2}} \right) + C$  (d) none of these

16.  $\int \frac{dx}{(\sin^4 x + \cos^4 x)} = ?$

(a)  $\frac{1}{\sqrt{2}} \tan^{-1} \left( \frac{\tan^2 x - 1}{\sqrt{2} \tan x} \right) + C$  (b)  $\frac{1}{\sqrt{2}} \tan^{-1} \left( \frac{\tan^2 x - 1}{\tan x} \right) + C$

(c)  $\frac{1}{\sqrt{2}} \tan^{-1} \left( \frac{1}{\sqrt{2} \tan x} \right) + C$  (d) none of these

17.  $\int \frac{(x^2 + 1)}{(x^4 + x^2 + 1)} dx = ?$

(a)  $\tan \frac{(x^2 - 1)}{\sqrt{3}} + C$  (b)  $\frac{1}{\sqrt{3}} \tan^{-1} \frac{(x^2 - 1)}{\sqrt{3}} + C$

(c)  $\frac{1}{\sqrt{3}} \tan^{-1} \frac{(x^2 - 1)}{\sqrt{3}x} + C$  (d) none of these

18.  $\int \frac{\sin 2x}{(\sin^4 x + \cos^4 x)} dx = ?$

(a)  $\tan^{-1} (\tan^2 x) + C$  (b)  $x^2 + C$  (c)  $-\tan^{-1} (\tan^2 x) + C$  (d) none of these

19.  $\int \frac{dx}{(1 - 9x^2)} = ?$

(a)  $\frac{1}{3} \log \left| \frac{1+3x}{1-3x} \right| + C$  (b)  $\frac{1}{3} \log \left| \frac{1-3x}{1+3x} \right| + C$  (c)  $\frac{1}{6} \log \left| \frac{1+3x}{1-3x} \right| + C$  (d)  $\frac{1}{6} \log \left| \frac{1-3x}{1+3x} \right| + C$

20.  $\int \frac{dx}{(16 - 4x^2)} = ?$

$$(a) \frac{1}{8} \log \left| \frac{2-x}{2+x} \right| + C \quad (b) \frac{1}{16} \log \left| \frac{2-x}{2+x} \right| + C \quad (c) \frac{1}{8} \log \left| \frac{2+x}{2-x} \right| + C \quad (d) \frac{1}{16} \log \left| \frac{2+x}{2-x} \right| + C$$

21.  $\int \frac{x^2}{(1-x^6)} dx = ?$

$$(a) \frac{1}{6} \log \left| \frac{1+x^3}{1-x^3} \right| + C \quad (b) \frac{1}{6} \log \left| \frac{1-x^3}{1+x^3} \right| + C \quad (c) \frac{1}{3} \log \left| \frac{1-x^3}{1+x^3} \right| + C \quad (d) \text{none of these}$$

22.  $\int \frac{x}{(1-x^4)} dx = ?$

$$(a) \frac{1}{4} \log \left| \frac{1+x^2}{1-x^2} \right| + C \quad (b) \frac{1}{4} \log \left| \frac{1-x^2}{1+x^2} \right| + C \quad (c) \frac{1}{2} \log \left| \frac{1+x^2}{1-x^2} \right| + C \quad (d) \text{none of these}$$

23.  $\int \frac{x^2}{(a^6-x^6)} dx = ?$

$$(a) \frac{1}{3a^3} \log \left| \frac{a^3+x^3}{a^3-x^3} \right| + C \quad (b) \frac{1}{6a^3} \log \left| \frac{a^3+x^3}{a^3-x^3} \right| + C \quad (c) \frac{1}{6a^3} \log \left| \frac{a^3-x^3}{a^3+x^3} \right| + C$$

(d) none of these

24.  $\int \frac{dx}{(3-2x-x^2)} = ?$

$$(a) \frac{1}{4} \log \left| \frac{3+x}{3-x} \right| + C \quad (b) \frac{1}{4} \log \left| \frac{1+x}{1-x} \right| + C \quad (c) \frac{1}{4} \log \left| \frac{3+x}{1-x} \right| + C \quad (d) \text{none of these}$$

25.  $\int \frac{dx}{(\cos^2 x - 3 \sin^2 x)} = ?$

$$(a) \frac{1}{\sqrt{3}} \log \left| \frac{\sqrt{3} + \tan x}{\sqrt{3} - \tan x} \right| + C \quad (b) \frac{1}{\sqrt{3}} \log \left| \frac{1 - \sqrt{3} \tan x}{1 + \sqrt{3} \tan x} \right| + C$$

$$(c) \frac{1}{2\sqrt{3}} \log \left| \frac{1 + \sqrt{3} \tan x}{1 - \sqrt{3} \tan x} \right| + C \quad (d) \text{none of these}$$

26.  $\int \frac{\cos ec^2 x}{(1 - \cot^2 x)} dx = ?$

(a)  $\frac{1}{2} \log \left| \frac{1 + \cot x}{1 - \cot x} \right| + C$  (b)  $-\frac{1}{2} \log \left| \frac{1 + \cot x}{1 - \cot x} \right| + C$  (c)  $\frac{1}{2} \log \left| \frac{1 - \cot x}{1 + \cot x} \right| + C$  (d) none of these

27.  $\int \frac{dx}{(4x^2 - 1)} = ?$

(a)  $\frac{1}{2} \log \left| \frac{2x-1}{2x+1} \right| + C$  (b)  $\frac{1}{2} \log \left| \frac{2x+1}{2x-1} \right| + C$  (c)  $\frac{1}{4} \log \left| \frac{2x-1}{2x+1} \right| + C$  (d) none of these

28.  $\int \frac{x}{(x^4 - 16)} dx = ?$

(a)  $\frac{1}{4} \log \left| \frac{x^2 + 4}{x^2 - 4} \right| + C$  (b)  $\frac{1}{16} \log \left| \frac{x^2 + 4}{x^2 - 4} \right| + C$  (c)  $\frac{1}{16} \log \left| \frac{x^2 - 4}{x^2 + 4} \right| + C$  (d) none of these

29.  $\int \frac{dx}{(\sin^2 x - 4 \cos^2 x)} = ?$

(a)  $\frac{1}{4} \log \left| \frac{\tan x - 2}{\tan x + 2} \right| + C$  (b)  $\frac{1}{4} \log \left| \frac{\tan x + 2}{\tan x - 2} \right| + C$  (c)  $\frac{1}{4} \log \left| \frac{1 - \tan x}{1 + \tan x} \right| + C$

(d) none of these

30.  $\int \frac{dx}{(4 \sin^2 x + 5 \cos^2 x)} = ?$

(a)  $\frac{1}{2} \tan^{-1} \left( \frac{\tan x}{\sqrt{5}} \right) + C$  (b)  $\frac{1}{\sqrt{5}} \tan^{-1} \left( \frac{\tan x}{\sqrt{5}} \right) + C$  (c)  $\frac{1}{\sqrt[3]{5}} \tan^{-1} \left( \frac{2 \tan x}{\sqrt{5}} \right) + C$

(d) none of these

31.  $\int \frac{\sin x}{\sin 3x} dx = ?$

(a)  $\frac{1}{\sqrt[3]{3}} \log \left| \frac{\sqrt{3} + \sin x}{\sqrt{3} - \sin x} \right| + C$  (b)  $\frac{1}{\sqrt[3]{3}} \log \left| \frac{\sqrt{3} + \cos x}{\sqrt{3} - \cos x} \right| + C$

(c)  $\frac{1}{\sqrt[3]{3}} \log \left| \frac{\sqrt{3} + \tan x}{\sqrt{3} - \tan x} \right| + C$  (d) none of these

32.  $\int \frac{(x^2 + 1)}{(x^4 + 1)} dx = ?$

$$(a) \frac{1}{2} \tan^{-1} \left( \frac{x^2 + 1}{\sqrt{2}x} \right) + C$$

$$(b) \frac{1}{2} \tan^{-1} \left( \frac{x^2 - 1}{\sqrt{2}x} \right) + C$$

$$(c) \frac{1}{\sqrt{2}} \log \left( \frac{x^2 + 1}{x^2 - 1} \right) + C$$

(d) none of these

### **ANSWERS: INDEFINITE INTEGRALS-IV**

1.(b)	2.(c)	3.(b)	4.(a)	5.(c)	6.(b)
7.(c)	8.(b)	9.(a)	10.(c)	11.(a)	12.(c)
13.(b)	14.(c)	15.(b)	16.(a)	17.(c)	18.(a)
19.(c)	20.(d)	21.(a)	22.(a)	23.(b)	24.(c)
25.(c)	26.(b)	27.(c)	28.(c)	29.(a) n	30.(C)
31.(c)	32.(b)				