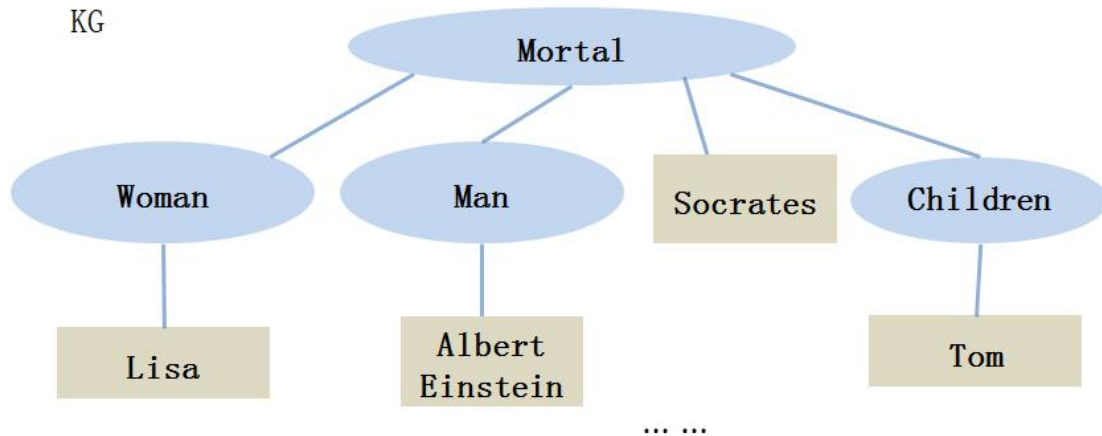


Homework 4

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1) Given the following KG, please answer the question “Is Albert Einstein a mortal?” using query rewriting on the query $Mortal(Albert\ Einstein)$ (this query is used for checking whether Albert Einstein is a mortal) .



Solution:

$$Mortal(x) \vee Woman \vee Man(x) \vee Children(x)$$

2) The following ontology is inconsistent. Please remove one axiom in it to make it consistent and provide a model of the new ontology.

$Highvalue_Company \sqsubseteq Solvent_Company$

$Solvent_Company \sqsubseteq \neg Bankrupt_Enterprise$

$Highvalue_Company(Lehman_Brothers_Holdings)$

$Bankrupt_Enterprise(Lehman_Brothers_Holdings)$

Solution:

A. Remove ‘ $Bankrupt_Enterprise(Lehman_Brothers_Holdings)$ ’;

Model:

$$\begin{aligned}\Delta &= \{lbh\} \\ I_I(Lehman_Brothers_Holdings) &= lbh, \\ I_C(Highvalue_Company) &= \{lbh\}, \\ I_C(Solvent_Company) &= \{lbh\}, \\ I_C(Bankrupt_Enterprise) &= \{\}\end{aligned}$$

B. Remove ‘ $Solvent_Company \sqsubseteq \neg Bankrupt_Enterprise$ ’;

Model:

$$\begin{aligned}\Delta &= \{lbh\} \\ I_I(Lehman_Brothers_Holdings) &= lbh, \\ I_C(Highvalue_Company) &= \{lbh\}, \\ I_C(Bankrupt_Enterprise) &= \{lbh\}, \\ I_C(Solvent_Company) &= \{lbh\}\end{aligned}$$

C. Remove ‘Highvalue_Company(Lehman_Brothers_Holdings)’;

Model:

$$\begin{aligned}\Delta &= \{\text{lbh}\} \\ I_l(\text{Lehman_Brothers_Holdings}) &= \text{lbh}, \\ I_c(\text{Bankrupt_Enterprise}) &= \{\text{lbh}\}, \\ I_c(\text{Highvalue_Company}) &= \{\}, \\ I_c(\text{Solvent_Company}) &= \{\}\end{aligned}$$

D. Remove ‘Highvalue_Company \sqsubseteq Solvent_Company’;

Model:

$$\begin{aligned}\Delta &= \{\text{lbh}\} \\ I_l(\text{Lehman_Brothers_Holdings}) &= \text{lbh}, \\ I_c(\text{Bankrupt_Enterprise}) &= \{\text{lbh}\}, \\ I_c(\text{Highvalue_Company}) &= \{\text{lbh}\}, \\ I_c(\text{Solvent_Company}) &= \{\}\end{aligned}$$

3) Why TransE cannot handle symmetric relation and one-to-many relation?

Solution:

① For an arbitrary triple $\langle \mathbf{h}, \mathbf{r}, \mathbf{t} \rangle$, the symmetric relation can be described as:

$$\begin{cases} \mathbf{h} + \mathbf{r} = \mathbf{t} \\ \mathbf{t} + \mathbf{r} = \mathbf{h} \end{cases}$$

So that, this will hold only if:

$$\begin{cases} \mathbf{r} = 0 \\ \mathbf{h} = \mathbf{t} \end{cases}$$

This is not a condition for any triple, so TransE cannot handle symmetric relation.

② For two arbitrary triples $\langle \mathbf{h}, \mathbf{r}, \mathbf{t}_1 \rangle$ and $\langle \mathbf{h}, \mathbf{r}, \mathbf{t}_2 \rangle$ with different vector \mathbf{t}_1 and \mathbf{t}_2 , the one-to-many relation will be described as:

$$\mathbf{t}_1 = \mathbf{h} + \mathbf{r} = \mathbf{t}_2$$

So that, this will hold only if:

$$\mathbf{t}_1 = \mathbf{t}_2$$

This is contrary to the original conditions, so TransE cannot handle one-to-many relation.