

$$T(n) = \begin{cases} T(1) = P \\ T(n) = 8T\left(\frac{n}{2}\right) + qn \end{cases}$$

$$T(n) = 8 + \left(\frac{n}{2}\right) + qn$$

$$= 8 \left(8 + \left(\frac{n}{4}\right) + \frac{qn}{2} \right) + qn = 8 \left(8 \left(8 + \left(\frac{n}{8}\right) + \frac{qn}{4} \right) + \frac{qn}{2} \right) + qn$$

$$= 8^i T\left(\frac{n}{2^i}\right) + qn \left(\frac{8^2}{4} + \frac{8^1}{2} + \frac{8^0}{1} \right)$$

$$= 8^i T\left(\frac{n}{2^i}\right) + qn \left(4^2 + 4^1 + 4^0 \right)$$

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$$= 8^i T\left(\frac{n}{2^i}\right) + qn \left(1 \left(\frac{4^i - 1}{4 - 1} \right) \right) = 8^i T\left(\frac{n}{2^i}\right) + qn \left(\frac{4^i - 1}{3} \right)$$

$$\Rightarrow T(1) = P \quad \Rightarrow 8^{\log_2^n} \cdot T(1) + qn \left(\frac{4^{\log_2^n} - 1}{3} \right)$$

$$= 2^{\log_2^n} \cdot 2^{\log_2^n} \cdot 2^{\log_2^n} \cdot P + qn \left(\frac{(2 \cdot 2^{\log_2^n}) - 1}{3} \right) =$$

$$= n \cdot n \cdot n \cdot P + qn \left(\frac{n^2 - 1}{3} \right) = P \cdot n^3 + \frac{qn^3 - qn}{3}$$

$$= Pn^3 + \frac{qn^3}{3} - \frac{qn}{3} \Rightarrow \boxed{\Theta(n^3)}$$