

$$T(n) = \begin{cases} T(1) = 1 \\ T(n) = T(n-1) + 3n + 2 \end{cases}$$

$$T(n) = T(n-1) + 3n + 2$$

$$\text{~~T(n)~~ = (T(n-2) + 3(n-1)) + 3n + 2$$

$$= (T(n-3) + 3(n-2) + 2) + 3(n-1) + 2 + 3n + 2$$

$$= T(n-3) + 3(n-2) + \underbrace{3(n-1) + 3(n-2) + 2 + 2 + 2}_{\text{SOMA DE P.A.}}$$

$$T(i) = T(n-i) + 3[(n-2) + (n-1) + (n-0)] + 2i$$

$$T(n-i) + 3 \left[i \left(\frac{n + n - i + 1}{2} \right) \right] + 2i$$

$$T(n-i+1) = T(n-i) + 3i \left(\frac{2n-i+1}{2} \right) + 2i \Rightarrow \begin{matrix} T(1) = 1 \\ n-i = 1 \\ \boxed{i = n-1} \end{matrix}$$

$$= T(1) + 3(n-1) \left(\frac{2n - (n-1) + 1}{2} \right) + 2(n-1)$$

$$= 1 + (3n-3) \left(\frac{n+2}{2} \right) + 2n-2 = \frac{3n^2 + 6n - 3n - 6}{2} + 2n - 1$$

$$= \frac{3n^2}{2} + \frac{3n}{2} - 3 + 2n - 1 = \frac{3n^2}{2} + \frac{7n}{2} - 4 \Rightarrow \boxed{\Theta(n^2)}$$