# logistic\_regression

May 30, 2025

# 1 Logistic Regression

This notebook presents a comprehensive workflow for optimizing a logistic regression model to detect breast cancer from clinical features. The process includes systematic dataset preprocessing, feature selection, and multi-stage hyperparameter optimization using cross-validation and MLflow tracking. Emphasis is placed on maximizing recall to minimize false negatives, which is critical in medical diagnostics. The methodology combines randomized and grid search strategies, mutual information analysis for hyperparameter impact, and rigorous evaluation of model performance. The resulting model achieves high recall, f1, and roc-auc, demonstrating robust generalization and suitability for clinical application.

# 1.1 Setup

```
[1]: import os
     import warnings
     import random
     import itertools
     from typing import Any, Dict, List
     import joblib
     from tqdm import tqdm
     import mlflow
     import numpy as np
     import mlflow.sklearn
     import matplotlib.pyplot as plt
     import seaborn as sns
     import pandas as pd
     from sklearn.linear_model import LogisticRegression
     from sklearn.metrics import (
         accuracy_score,
         precision_score,
         recall_score,
         f1_score,
         roc_auc_score,
         make_scorer,
     from sklearn.model_selection import (
         StratifiedKFold,
```

```
train_test_split,
    cross_validate,
)
from sklearn.exceptions import ConvergenceWarning
from sklearn.feature_selection import mutual_info_regression
from sklearn.preprocessing import OrdinalEncoder
```

```
[2]: # Suppress warnings from Python's multiprocessing module. This is a known issue_
on Apple Silicon Macs. It does not affect the code's functionality.

warnings.filterwarnings(
    "ignore", category=UserWarning, module="multiprocessing.resource_tracker"
)
```

```
[3]: mlflow.set_tracking_uri(os.path.join(os.path.dirname(os.getcwd()), "mlruns"))
```

# 1.1.1 Helper Functions

- sample\_param\_combinations: Randomly samples a specified number of hyperparameter combinations from a parameter grid for efficient randomized search.
- all\_param\_combinations: Generates all possible hyperparameter combinations from a parameter grid using a cartesian product, supporting exhaustive grid search.
- total\_param\_combinations: Calculates the total number of possible hyperparameter combinations in a given parameter grid.

```
[4]: def sample_param_combinations(
    param_grid: Dict[str, Any], n_iter: int = 50, seed: int = 42
) -> List[Dict[str, Any]]:
    """
    Sample parameter combinations from a given parameter grid.

Args:
    param_grid (dict): Dictionary of parameter names and their possible_
    values.
        n_iter (int): Number of combinations to sample.
        seed (int): Random seed for reproducibility.

Returns:
    list[dict]: List of sampled parameter combinations.

"""

random.seed(seed)

all_keys = list(param_grid.keys())
all_values = [param_grid[k] for k in all_keys]

all_combos = list(itertools.product(*all_values))
```

```
random.shuffle(all_combos)
         sampled_combos = all_combos[:n_iter]
         return [dict(zip(all_keys, values)) for values in sampled_combos]
[5]: def all_param_combinations(param_grid: Dict[str, Any]) -> List[Dict[str, Any]]:
         Generate every possible hyperparameter combination from a parameter grid_{\sqcup}
      \hookrightarrowusing cartesian product.
         Arqs:
             param\_grid (Dict[str, Any]): Mapping of parameter names to iterables of
      ⇔possible values.
         Returns:
              (List[Dict[str, Any]]): A list of dicts, each representing one unique
      \neg combination \ of \ parameters.
         11 11 11
         keys = list(param_grid.keys())
         values_lists = [param_grid[k] for k in keys]
         all_combos = itertools.product(*values_lists)
         return [dict(zip(keys, combo)) for combo in all_combos]
[6]: def total_param_combinations(param_grid: Dict[str, Any]) -> int:
         Calculate the total number of possible hyperparameter combinations.
         Args:
             param_grid(dict) : Dictionary of parameter names to lists of possible ⊔
      \hookrightarrow values.
         Returns:
             int: Total number of combinations.
         total = 1
         for values in param_grid.values():
             total *= len(values)
         return total
```

# 1.2 Dataset Selection

To determine the best preprocessing strategy for binary classification of breast cancer data, multiple pipelines will be evaluated. These pipelines vary by scaling method—Power Transformer (PT), Quantile Transformer (QT), MinMaxScaler, and StandardScaler (STD)—and by feature selection method: none (all), mutual information (mi), and sequential feature selection (sfs). The primary performance metric will be **recall**, given the critical nature of detecting positive (cancerous) cases. Secondary metrics include F1-score, accuracy, precision, and ROC AUC.

Metric Importance Ranking 1. Recall \* Why: Missing a cancer case (false negative) can be life-threatening, so recall must be prioritized to catch as many actual positives as possible.

#### 2. ROC AUC

• Why: Provides an overall measure of classification quality across all thresholds, important when dealing with imbalanced data.

#### 3. F1 Score

• Why: Balances recall and precision, useful when both false positives and false negatives matter, but especially when class distribution is uneven. False positives are not as grave as false negative but should also be reduced as much as possible (without sacrificing recall), to avoid unnecessary secondary testing.

## 4. Precision

- Why: Important to reduce false positives, but secondary to recall in medical contexts.
- 5. Accuracy
  - Why: Can be misleading in imbalanced datasets, where high accuracy might still mean missing many positive cases.

```
[9]: # Get all versions of preprocessed data
data_path = os.path.join(os.path.dirname(os.getcwd()), "data", "processed_data")
files = [f for f in os.listdir(data_path) if os.path.isfile(os.path.

→join(data_path, f))]
files
```

```
[5]: mlflow.set_experiment(experiment_name="LR-Dataset_Selection")
```

2025/05/20 15:10:24 INFO mlflow.tracking.fluent: Experiment with name 'LR-Dataset\_Selection' does not exist. Creating a new experiment.

```
[5]: <Experiment:
    artifact_location='/Users/jonas/git/ml_project/mlruns/864561007828072332',
    creation_time=1747746624622, experiment_id='864561007828072332',
    last_update_time=1747746624622, lifecycle_stage='active', name='LR-Dataset_Selection', tags={}>
```

```
[]: # Default hyperparameters will be used for dataset selection
     params = {
         "penalty": "12",
         "dual": False,
         "tol": 1e-4,
         "C": 1.0,
         "fit_intercept": True,
         "intercept_scaling": 1.0,
         "class_weight": None,
         "solver": "lbfgs",
         "max_iter": 100,
         "warm_start": False,
         "l1_ratio": None,
     }
     best_dataset = None
     best_score = 0.0
     best_run = None
     for i, file in enumerate(tqdm(files, desc="Processing ML Runs")):
         # Load and split data
         df = pd.read_parquet(os.path.join(data_path, file))
         X = df.drop("Diagnosis", axis=1)
         y = df["Diagnosis"]
         X_train, X_test, y_train, y_test = train_test_split(
             X, y, train_size=0.8, test_size=0.2, random_state=42
         with mlflow.start_run():
             mlflow.set_tags(
                 tags={
                     "Model": "LogisticRegression",
                     "Experiment Type": "Dataset Selection",
                     "Dataset": file,
                 }
             )
             mlflow.log_params(params)
```

```
# Create and train model
      model = LogisticRegression(n_jobs=-1, random_state=42, verbose=0,_
→**params)
      model.fit(X_train, y_train)
      # Get predictions
      y_pred_train = model.predict(X_train)
      y_prob_train = model.predict_proba(X_train)[:, 1]
      y_pred_test = model.predict(X_test)
      y_prob_test = model.predict_proba(X_test)[:, 1]
      # Calculate and log metrics
      mlflow.log_metrics(
          {
              "accuracy_train": float(
                  accuracy_score(y_true=y_train, y_pred=y_pred_train)
              ),
               "precision_train": float(
                  precision_score(y_true=y_train, y_pred=y_pred_train)
              ),
              "recall train": float(
                  recall_score(y_true=y_train, y_pred=y_pred_train)
              "f1_train": float(f1_score(y_true=y_train,_
→y_pred=y_pred_train)),
              "roc_auc_train": float(
                  roc_auc_score(y_true=y_train, y_score=y_prob_train)
              ),
               "accuracy_test": float(
                  accuracy_score(y_true=y_test, y_pred=y_pred_test)
              ),
               "precision_test": float(
                  precision_score(y_true=y_test, y_pred=y_pred_test)
              ),
              "recall_test": float(recall_score(y_true=y_test,__
→y_pred=y_pred_test)),
              "f1_test": float(f1_score(y_true=y_test, y_pred=y_pred_test)),
              "roc_auc_test": float(
                  roc_auc_score(y_true=y_test, y_score=y_prob_test)
              ),
          }
      )
      input_example = X_train.iloc[:5]
      mlflow.sklearn.log_model(model, "model", input_example=input_example)
```

```
# Check if current model performs better than current best model
             if best_score < recall_score(y_true=y_test, y_pred=y_pred_test):</pre>
                 best_score = recall_score(y_true=y_test, y_pred=y_pred_test)
                 best_dataset = file
                 best_run = mlflow.active_run().info.run_id # type: ignore
         mlflow.end_run()
     print("")
     print(f"Best dataset: {best_dataset}")
     print(f"Best score: {best score}")
     print(f"Best run: {best_run}")
    Processing ML Runs: 100%|
                                   | 12/12 [00:44<00:00, 3.68s/it]
    Best dataset: processed_data_pt_sfs.parquet
    Best score: 0.7368421052631579
    Best run: c100974268ed427cbc671cfd9d903ac2
[6]: # Get data from runs
     runs_metadata = mlflow.search_runs(experiment_names=["LR-Dataset_Selection"])
     runs_metadata = runs_metadata[
         sorted(
             Γ
                 "metrics.f1_test",
                 "metrics.roc_auc_test",
                 "metrics.precision_train",
                 "metrics.precision_test",
                 "metrics.roc_auc_train",
                 "metrics.recall_test",
                 "metrics.recall_train",
                 "metrics.accuracy_test",
                 "metrics.accuracy_train",
                 "metrics.f1_train",
                 "tags.Dataset",
             ]
         )
       # type: ignore
     runs_metadata["tags.Dataset"] = runs_metadata["tags.Dataset"].apply(
         lambda x: str(x).replace("processed_data_", "").replace(".parquet", "")
     runs_metadata.columns = [
         col.split(".")[1] if "." in col else col for col in runs_metadata.columns
     ]
```

runs\_metadata

```
[6]:
         accuracy_test accuracy_train
                                                     f1_train precision_test \
                                           f1_test
     0
              0.851485
                                  0.9050
                                          0.782609
                                                     0.866197
                                                                      0.870968
     1
                                  0.8850
                                          0.760563
                                                     0.839161
                                                                      0.818182
              0.831683
     2
              0.742574
                                  0.8050
                                          0.551724
                                                     0.651786
                                                                      0.800000
     3
              0.831683
                                  0.8875
                                          0.760563
                                                     0.842105
                                                                      0.818182
     4
              0.861386
                                  0.9050
                                          0.800000
                                                     0.868056
                                                                      0.875000
     5
              0.792079
                                  0.8900
                                          0.720000
                                                     0.843972
                                                                      0.729730
     6
              0.811881
                                  0.8925
                                          0.707692
                                                     0.837736
                                                                      0.851852
     7
              0.752475
                                  0.8225 0.561404
                                                     0.687225
                                                                      0.842105
     8
              0.762376
                                  0.8225
                                          0.571429
                                                     0.675799
                                                                      0.888889
     9
              0.772277
                                  0.8850
                                          0.646154
                                                     0.827068
                                                                      0.777778
     10
              0.792079
                                  0.8850
                                          0.666667
                                                                      0.840000
                                                     0.823077
     11
              0.831683
                                  0.9125
                                          0.753623
                                                     0.875445
                                                                      0.838710
         precision_train
                           recall_test
                                         recall_train roc_auc_test roc_auc_train
     0
                0.872340
                              0.710526
                                             0.860140
                                                             0.925647
                                                                             0.963538
     1
                0.839161
                              0.710526
                                             0.839161
                                                             0.912281
                                                                             0.952600
     2
                0.901235
                              0.421053
                                                                             0.909553
                                             0.510490
                                                             0.868421
     3
                0.845070
                              0.710526
                                             0.839161
                                                             0.916458
                                                                             0.953199
     4
                0.862069
                              0.736842
                                             0.874126
                                                             0.925647
                                                                             0.963702
     5
                0.856115
                              0.710526
                                             0.832168
                                                             0.889724
                                                                             0.941362
     6
                0.909836
                              0.605263
                                             0.776224
                                                             0.876775
                                                                             0.951892
     7
                0.928571
                              0.421053
                                             0.545455
                                                             0.878028
                                                                             0.927621
     8
                0.973684
                              0.421053
                                             0.517483
                                                             0.865079
                                                                             0.925227
     9
                0.894309
                              0.552632
                                             0.769231
                                                                             0.948328
                                                             0.901003
     10
                              0.552632
                0.914530
                                             0.748252
                                                             0.867586
                                                                             0.951321
     11
                0.891304
                              0.684211
                                             0.860140
                                                             0.923977
                                                                             0.961770
            Dataset
     0
             pt_all
     1
             qt_sfs
     2
          minmax_mi
     3
             qt_all
     4
             pt_sfs
     5
              qt mi
     6
            std_all
     7
         minmax all
     8
         minmax_sfs
             std_mi
     9
     10
            std_sfs
     11
              pt_mi
[]: # Get available metrics
     metrics = [c for c in runs metadata.columns if "Dataset" not in c]
                                                                              # type:
      \hookrightarrow ignore
     metrics
```

```
[]: ['accuracy_test',
      'accuracy_train',
      'f1_test',
      'f1_train',
      'precision_test',
      'precision_train',
      'recall_test',
      'recall_train',
      'roc_auc_test',
      'roc_auc_train']
[]: # Plot metrics
    fig, axes = plt.subplots(nrows=5, ncols=2, figsize=(16, 20))
     axes = axes.flatten()
     palette = sns.color_palette("tab10", n_colors=runs_metadata["Dataset"].
      →nunique()) # type: ignore
     for idx, metric in enumerate(metrics):
         ax = axes[idx]
         sns.barplot(
             x="Dataset", y=metric, data=runs_metadata, hue="Dataset", ax=ax,
      →palette=palette # type: ignore
         ax.set_xlabel("Dataset")
         ax.set_ylabel(metric)
         ax.set_title(f"{metric} by Dataset")
         ax.set_ylim(0.0, 1.0)
         ax.tick_params(axis="x", rotation=45)
         plt.tight_layout()
     plt.show()
```



- Best Recall: The highest test recall (0.7368) was achieved by the pt\_sfs dataset (Power Transformer + SFS), closely followed by pt\_all and others in the PT and QT families.
- Best Overall Balance: pt\_sfs not only had the best recall but also maintained high scores in:

- Accuracy (0.8614)
- F1-score (0.8000)
- Precision (0.8750)
- ROC AUC (0.9256)
- Underperformers: All minmax variants significantly underperformed in recall (0.4211), indicating that MinMaxScaler is not a suitable preprocessing method for this task.
- StandardScaler Performance: While std\_all and its variants offered reasonable performance, they did not surpass the PT or QT transformations in any major metric.
- Overfitting Consideration: The PT and QT models show a consistent train-test performance gap, though not alarmingly high. pt\_sfs has a recall of 0.7368 on test vs. 0.8741 on train, which is acceptable given the improved generalization.

Based on the evaluation, pt\_sfs (Power Transformer + Sequential Feature Selection) is the best preprocessing setup for this task. It offers the highest recall with strong support from other metrics, making it a reliable choice for a classification problem where identifying all positive cases is critical.

```
[]: # Get scores of best run
     runs metadata[runs metadata["Dataset"] == "pt sfs"]
[]:
                       accuracy_train f1_test
        accuracy_test
                                                f1_train
                                                          precision_test
             0.861386
                                           0.8
                                                0.868056
                                0.905
                                                                    0.875
     4
        precision_train recall_test
                                      recall_train roc_auc_test
                                                                  roc_auc_train \
                                          0.874126
               0.862069
                            0.736842
                                                        0.925647
                                                                        0.963702
      Dataset
     4 pt_sfs
```

# 1.3 Hyperparameter Optimization

To systematically find the best hyperparameter configuration, a three-step optimization strategy will be used:

- Broad Exploration (Randomized Search)
- Focused Tuning (Grid Search)
- Fine Adjustment (Grid Search)

This staged approach ensures a balance between exploration of the full parameter space and exploitation of the most promising regions, while being mindful of computational efficiency.

Cross-validation is used because it provides a reliable estimate of model generalization and guides robust hyperparameter tuning by averaging performance metrics over multiple train—test splits.

# 1.3.1 Setup

```
[7]: os.environ["PYTHONWARNINGS"] = "ignore::UserWarning,ignore::RuntimeWarning"
```

```
[8]: mlflow.set_experiment(experiment_name="LR-Hyperparameter_Optimization")
[8]: <Experiment:
    artifact_location='/Users/jonas/git/ml_project/mlruns/166928110039040565',
     creation time=1748025393932, experiment id='166928110039040565',
     last_update_time=1748025393932, lifecycle_stage='active', name='LR-
    Hyperparameter_Optimization', tags={}>
[9]: # Load and split data
     data path = os.path.join(os.path.dirname(os.getcwd()), "data", "processed data")
     df = pd.read_parquet(os.path.join(data_path, "processed_data_pt_sfs.parquet"))
     X = df.drop("Diagnosis", axis=1)
     y = df["Diagnosis"]
     X_train, X_test, y_train, y_test = train_test_split(
         X, y, train_size=0.8, test_size=0.2, random_state=42
     )
     cv = StratifiedKFold(n_splits=5, shuffle=True, random_state=42)
     scorer = make_scorer(recall_score)
```

```
[10]: # Prepare CV and scoring
```

```
[11]: # Define scoring functions
      scoring = {
          "recall": "recall",
          "precision": "precision",
          "f1": "f1",
          "accuracy": "accuracy",
          "roc_auc": "roc_auc",
      }
```

# **Broad Hyperparameter Exploration**

The first step aims to broadly sample the hyperparameter space to identify regions where the model performs well. Rather than exhaustively trying all combinations (which is computationally expensive), randomized sampling will be used to cover more ground quickly.

Parameters: \* penalty: Type of regularization (11, 12, elasticnet, or None). \* tol: Tolerance for stopping criteria. \* C: Inverse of regularization strength, sampled on a log scale. \* solver: Optimization algorithm. \* fit intercept: Whether to fit the intercept. \* max iter: Number of iterations before solver termination. \* class\_weight: Option to balance classes, which can help boost recall. \* warm\_start: Whether to reuse the solution of the previous call to fit as initialization. \* 11 ratio: Elastic Net mixing parameter, relevant only for penalty='elasticnet'.

Starting with a broad search allows for: \* Discovery of effective combinations that might be missed in a narrowly defined grid. \* Understanding which hyperparameters have the most influence on model performance. \* Avoiding overfitting to a local minimum early in the optimization process.

The insights from this step guide the design of a more focused and efficient search in the next phase.

A custom implementation of random search will be used for integration with mlflow.

Certain hyperparameter combinations will cause errors, thus multiple valid parameter grids will be defined and tested in as much runs.

Run 1 The first set of runs focuses on hyperparameter combinations that can use 12 as the penalty term.

```
[22]: # Define the parameter grid - penalty=12
      param grid = {
          "penalty": ["12"],
          "tol": [1e-4, 1e-3, 1e-2, 1e-1],
          "C": np.logspace(-4, 4, 20),
          "solver": [
              "lbfgs",
              "liblinear",
              "saga",
              "newton-cg",
              "newton-cholesky",
              "sag",
              "saga",
          ],
          "fit intercept": [True, False],
          "max iter": [100, 200, 500, 1000, 10000],
          "class_weight": [None, "balanced"],
          "warm start": [False, True], # Useless when using liblinear solver
      }
      param_samples = sample_param_combinations(param_grid, n_iter=5000)
      print(
          "Number of total possible parameter combinations: ",
          total_param_combinations(param_grid),
      print("Number of sampled parameter combinations: ", len(param samples))
      print("")
      print(param_samples[0])
     Number of total possible parameter combinations:
                                                        22400
     Number of sampled parameter combinations: 5000
     {'penalty': '12', 'tol': 0.001, 'C': np.float64(3792.690190732246), 'solver':
     'liblinear', 'fit_intercept': False, 'max_iter': 1000, 'class_weight':
     'balanced', 'warm_start': False}
[28]: # Suppress warnings for convergence
      warnings.filterwarnings("ignore", category=ConvergenceWarning)
      best_score = -np.inf
      best_run = None
      best_params = None
```

```
for i, params in enumerate(tqdm(param samples, desc="Processing ML Runs")):
    with mlflow.start_run():
        mlflow.set_tags(
            tags={
                "Model": "LogisticRegression",
                "Experiment Type": "Hyperparameter Optimization",
                "Dataset": "processed_data_pt_sfs.parquet",
            }
        )
        # Log params
        for k, v in params.items():
            mlflow.log_param(k, v)
        model = LogisticRegression(verbose=0, random_state=42, n_jobs=1)
        model.set_params(**params)
        # Get model scores
        cv_results = cross_validate(
            model,
            X_train,
            y_train,
            cv=cv,
            scoring=scoring,
            return_train_score=True,
            n_{jobs=-1},
        )
        mean_scores = {
            f"train_{metric}": np.mean(cv_results[f"train_{metric}"])
            for metric in scoring.keys()
        }
        mean_scores.update(
            {
                f"test_{metric}": np.mean(cv_results[f"test_{metric}"])
                for metric in scoring.keys()
            }
        )
        for metric, value in mean_scores.items():
            mlflow.log_metric(metric, value)
        # Update best score
        if mean_scores["test_recall"] > best_score:
```

Run 2 The first set of runs focuses on hyperparameter combinations that can use 11 as the penalty term.

```
[38]: # Define the parameter grid - penalty=11
      param_grid = {
          "penalty": ["11"],
          "tol": [1e-4, 1e-3, 1e-2, 1e-1],
          "C": np.logspace(-4, 4, 20),
          "solver": ["liblinear", "saga", "saga"],
          "fit_intercept": [True, False],
          "max_iter": [100, 200, 500, 1000, 10000],
          "class_weight": [None, "balanced"],
          "warm start": [False, True], # Useless when using liblinear solver
      }
      param_samples = sample_param_combinations(param_grid, n_iter=5000)
      print(
          "Number of total possible parameter combinations: ",
          total_param_combinations(param_grid),
      print("Number of sampled parameter combinations: ", len(param samples))
      print("")
      print(param_samples[0])
     Number of total possible parameter combinations:
     Number of sampled parameter combinations: 5000
```

{'penalty': '11', 'tol': 0.001, 'C': np.float64(0.08858667904100823), 'solver':

```
'liblinear', 'fit_intercept': False, 'max_iter': 200, 'class_weight':
     'balanced', 'warm_start': True}
[30]: # Suppress warnings for convergence
      warnings.filterwarnings("ignore", category=ConvergenceWarning)
      best_score = -np.inf
      best_run = None
      best_params = None
      for i, params in enumerate(tqdm(param_samples, desc="Processing ML Runs")):
          with mlflow.start run():
              mlflow.set_tags(
                  tags={
                      "Model": "LogisticRegression",
                      "Experiment Type": "Hyperparameter Optimization",
                      "Dataset": "processed_data_pt_sfs.parquet",
                  }
              )
              # Log params
              for k, v in params.items():
                  mlflow.log_param(k, v)
              model = LogisticRegression(verbose=0, random_state=42, n_jobs=1)
              model.set params(**params)
              # Get model scores
              cv_results = cross_validate(
                  model,
                  X_train,
                  y_train,
                  cv=cv,
                  scoring=scoring,
                  return_train_score=True,
                  n_{jobs=-1},
              )
              mean scores = {
                  f"train_{metric}": np.mean(cv_results[f"train_{metric}"])
                  for metric in scoring.keys()
              mean_scores.update(
                  {
                      f"test_{metric}": np.mean(cv_results[f"test_{metric}"])
```

```
for metric in scoring.keys()
            }
        )
        for metric, value in mean_scores.items():
            mlflow.log_metric(metric, value)
         # Update best score
        if mean scores["test recall"] > best score:
            best_score = mean_scores["test_recall"]
            best_params = params
            best_run = mlflow.active_run().info.run_id # type: ignore
    mlflow.end_run()
print(f"Best Score: {best_score}")
print(f"Best Params: {best_params}")
print(f"Best Run: {best_run}")
Processing ML Runs: 100%|
                              | 5000/5000 [17:29<00:00, 4.76it/s]
Best Score: 0.9433497536945812
Best Params: {'penalty': '11', 'tol': 0.0001, 'C':
np.float64(545.5594781168514), 'solver': 'saga', 'fit_intercept': False,
```

Run 3 The first set of runs focuses on hyperparameter combinations that can use elasticnet as the penalty term.

'max\_iter': 500, 'class\_weight': 'balanced', 'warm\_start': False}

Best Run: 751ff56508864f04a0dd2a829f459cd3

```
[39]: # Define the parameter grid - penalty=elasticnet
param_grid = {
    "penalty": ["elasticnet"],
    "tol": [1e-4, 1e-3, 1e-2, 1e-1],
    "C": np.logspace(-4, 4, 20),
    "solver": ["saga"],
    "fit_intercept": [True, False],
    "max_iter": [100, 200, 500, 1000, 10000],
    "class_weight": [None, "balanced"],
    "warm_start": [False, True], # Useless when using liblinear solver
    "l1_ratio": [0.0, 0.25, 0.5, 0.75, 1.0],
}

param_samples = sample_param_combinations(param_grid, n_iter=5000)
print(
```

```
"Number of total possible parameter combinations: ",
          total_param_combinations(param_grid),
      print("Number of sampled parameter combinations: ", len(param samples))
      print("")
      print(param_samples[0])
     Number of total possible parameter combinations:
                                                        16000
     Number of sampled parameter combinations: 5000
     {'penalty': 'elasticnet', 'tol': 0.01, 'C': np.float64(0.0006951927961775605),
     'solver': 'saga', 'fit_intercept': False, 'max_iter': 500, 'class_weight': None,
     'warm_start': True, 'l1_ratio': 0.0}
[40]: # Suppress warnings for convergence
      warnings.filterwarnings("ignore", category=ConvergenceWarning)
      best_score = -np.inf
      best_run = None
      best_params = None
      for i, params in enumerate(tqdm(param_samples, desc="Processing ML Runs")):
          with mlflow.start_run():
              mlflow.set_tags(
                  tags={
                      "Model": "LogisticRegression",
                      "Experiment Type": "Hyperparameter Optimization",
                      "Dataset": "processed_data_pt_sfs.parquet",
                  }
              )
              # Log params
              for k, v in params.items():
                  mlflow.log_param(k, v)
              model = LogisticRegression(verbose=0, random_state=42, n_jobs=1)
              model.set_params(**params)
              # Get model scores
              cv_results = cross_validate(
                  model,
                  X_train,
                  y_train,
                  cv=cv.
                  scoring=scoring,
```

```
return_train_score=True,
                  n_{jobs=-1},
              )
              mean_scores = {
                  f"train_{metric}": np.mean(cv_results[f"train_{metric}"])
                  for metric in scoring.keys()
              }
              mean_scores.update(
                      f"test_{metric}": np.mean(cv_results[f"test_{metric}"])
                      for metric in scoring.keys()
                  }
              )
              for metric, value in mean_scores.items():
                  mlflow.log_metric(metric, value)
              # Update best score
              if mean_scores["test_recall"] > best_score:
                  best_score = mean_scores["test_recall"]
                  best_params = params
                  best_run = mlflow.active_run().info.run_id # type: ignore
          mlflow.end run()
      print(f"Best Score: {best score}")
      print(f"Best Params: {best_params}")
      print(f"Best Run: {best_run}")
     Processing ML Runs: 100%|
                                    | 5000/5000 [27:43<00:00, 3.01it/s]
     Best Score: 0.9433497536945812
     Best Params: {'penalty': 'elasticnet', 'tol': 0.0001, 'C':
     np.float64(545.5594781168514), 'solver': 'saga', 'fit intercept': False,
     'max_iter': 200, 'class_weight': 'balanced', 'warm_start': False, 'l1_ratio':
     0.0}
     Best Run: df79d65931d542e491f5bd30fab18297
     Evaluation
[46]: # Get data from 100 best runs by recall (and other metrics)
      runs_metadata = mlflow.
      search_runs(experiment_names=["LR-Hyperparameter_Optimization"])
      runs_metadata = runs_metadata[
          sorted(
```

```
"metrics.test_f1",
            "metrics.test_roc_auc",
            "metrics.train_precision",
            "metrics.test_precision",
            "metrics.train_roc_auc",
            "metrics.test_recall",
            "metrics.train_recall",
            "metrics.test_accuracy",
            "metrics.train_accuracy",
            "metrics.train_f1",
            "params.fit_intercept",
            "params.C",
            "params.class_weight",
            "params.solver",
            "params.penalty",
            "params.warm_start",
            "params.max_iter",
            "params.tol",
            "params.l1_ratio",
        ]
    )
] # type: ignore
runs_metadata = runs_metadata.sort_values(
    by=[
        "metrics.test recall",
        "metrics.test_roc_auc",
        "metrics.test_f1",
        "metrics.train_recall",
        "metrics.train_roc_auc",
        "metrics.train_f1",
        "metrics.test_precision",
        "metrics.test_accuracy",
        "metrics.train_precision",
        "metrics.train_accuracy",
    ],
    ascending=False,
).head(
    100
) # type: ignore
runs metadata.columns = [
    col.split(".")[1] if "." in col else col for col in runs_metadata.columns
runs_metadata
```

[46]: test\_accuracy test\_f1 test\_precision test\_recall test\_roc\_auc \
10204 0.675 0.689615 0.541048 0.971675 0.926493

```
14813
                0.675 0.689615
                                         0.541048
                                                       0.971675
                                                                      0.926493
11244
                0.855
                       0.827583
                                         0.732723
                                                       0.957635
                                                                      0.966431
12718
                0.855
                       0.827583
                                         0.732723
                                                       0.957635
                                                                      0.966431
12084
                0.855
                       0.827583
                                         0.732723
                                                       0.957635
                                                                      0.966158
8209
                0.860
                       0.829426
                                         0.744018
                                                       0.943350
                                                                      0.965748
                       0.829426
                                                                      0.965748
9171
                0.860
                                         0.744018
                                                       0.943350
9178
                0.860
                       0.829426
                                         0.744018
                                                       0.943350
                                                                      0.965748
9882
                0.860
                       0.829426
                                         0.744018
                                                       0.943350
                                                                      0.965748
                       0.829426
                                         0.744018
                                                       0.943350
                                                                      0.965748
9995
                0.860
       train_accuracy
                                   train_precision
                                                      train_recall
                                                                     train_roc_auc
                        train_f1
10204
                0.6650
                         0.679225
                                           0.533823
                                                          0.956278
                                                                           0.928088
14813
                0.6650
                         0.679225
                                           0.533823
                                                          0.956278
                                                                          0.928088
11244
                0.8600
                         0.828283
                                           0.737932
                                                          0.944027
                                                                           0.967808
12718
                0.8600
                         0.828283
                                           0.737932
                                                          0.944027
                                                                           0.967808
12084
                0.8600
                         0.828245
                                           0.737831
                                                          0.944027
                                                                           0.967817
8209
                0.8625
                         0.830567
                                           0.742654
                                                          0.942273
                                                                           0.967443
                0.8625
9171
                                           0.742654
                                                          0.942273
                                                                           0.967443
                         0.830567
9178
                0.8625
                         0.830567
                                           0.742654
                                                          0.942273
                                                                           0.967443
9882
                0.8625
                         0.830567
                                           0.742654
                                                          0.942273
                                                                           0.967443
9995
                0.8625
                                           0.742654
                                                          0.942273
                                                                           0.967443
                         0.830567
                              C class weight fit intercept 11 ratio max iter
10204
       0.00026366508987303583
                                    balanced
                                                        True
                                                                  None
                                                                             500
       0.00026366508987303583
14813
                                    balanced
                                                        True
                                                                  None
                                                                             100
             78.47599703514607
                                    balanced
                                                       False
                                                                             500
11244
                                                                  None
12718
             78.47599703514607
                                    balanced
                                                       False
                                                                  None
                                                                            1000
12084
              206.913808111479
                                    balanced
                                                       False
                                                                  None
                                                                             100
8209
             545.5594781168514
                                                       False
                                                                            1000
                                    balanced
                                                                  None
                                                       False
9171
             545.5594781168514
                                    balanced
                                                                  None
                                                                           10000
9178
             545.5594781168514
                                    balanced
                                                       False
                                                                  None
                                                                             200
9882
             545.5594781168514
                                    balanced
                                                       False
                                                                  None
                                                                            1000
9995
             545.5594781168514
                                    balanced
                                                       False
                                                                  None
                                                                             500
                                     tol warm_start
      penalty
                          solver
10204
           12
                                     0.1
                                                True
                             sag
           12
                                      0.1
                                               False
14813
                             sag
           12
11244
                newton-cholesky
                                      0.1
                                               False
12718
           12
                newton-cholesky
                                      0.1
                                                True
                newton-cholesky
12084
           12
                                      0.1
                                                True
8209
                                  0.0001
                                               False
           11
                            saga
            11
                                                True
9171
                            saga
                                  0.0001
9178
           11
                            saga
                                  0.0001
                                               False
```

```
      9882
      11
      saga 0.0001
      True

      9995
      11
      saga 0.0001
      False
```

[100 rows x 19 columns]

In order to properly understand which hyperparameters have the highest impact on the main target metrics and thus should be inspected deeper, mutual information is used.

```
[52]: # Create a DataFrame to store mutual information scores
                    mi_scores_df = pd.DataFrame(columns=["feature", "test_recall", "test_roc_auc", "test_recall", "test_roc_auc", "test_recall", "test_roc_auc", "test_recall", "test_recall "test_recall", "test_recall", "test_recall", "test_recall", "test_recall", "test_recall", "test_recall", "test_recall
                        ⇔"test_f1"]) # type: iqnore
                    main_metrics = ["test_recall", "test_roc_auc", "test_f1"]
                    hyperparameters = [
                                  "penalty",
                                  "C",
                                 "solver",
                                 "fit_intercept",
                                 "max_iter",
                                 "class_weight",
                                  "tol",
                                  "warm_start",
                                 "l1_ratio",
                    ]
                    # Iterate over each metric and calculate mutual information scores
                    for metric in main_metrics:
                                 X = runs_metadata[hyperparameters].copy()
                                                                                                                                                                             # type: ignore
                                 y = runs_metadata[metric] # type: ignore
                                 # Encode categorical variables
                                 encoder = OrdinalEncoder()
                                 X_encoded = encoder.fit_transform(X.astype(str))
                                 mi_scores = mutual_info_regression(X_encoded, y)
                                 mi_scores_df[metric] = mi_scores
                                 mi_scores_df["feature"] = X.columns
                    mi_scores_df = mi_scores_df.sort_values(by=main_metrics, ascending=False)
                    mi_scores_df
```

```
[52]: feature test_recall test_roc_auc test_f1
6 tol 0.509626 0.762341 0.534317
2 solver 0.347469 0.706628 0.359293
0 penalty 0.161953 0.351322 0.060001
```

```
4
        max_iter
                     0.119997
                                    0.000000 0.000000
8
                     0.097790
        l1_ratio
                                    0.111444
                                              0.070845
                     0.066494
1
                                    0.704387
                                              0.182688
3
  fit_intercept
                     0.022492
                                    0.016291
                                              0.002822
5
    class_weight
                     0.002570
                                    0.000000 0.000000
                     0.000000
                                    0.000000
7
      warm_start
                                              0.000000
```

- tol shows the highest influence across all three metrics, suggesting that model convergence criteria have a major effect on detecting positive cancer cases.
- solver also has a relatively strong impact on all metrics. This implies solver choice significantly affects the classifier's ability to discriminate between classes.
- penalty and l1\_ratio have moderate influence, suggesting regularization method and strength impact the model's ability to generalize but are less critical.
- max\_iter shows some impact on *recall*, but none on *roc\_auc* or *f1* likely due to early convergence or saturation.
- C shows weak but non-negligible influence, especially on *roc\_auc*.
- fit\_intercept, class\_weight, and warm\_start have very low to zero mi, meaning they have minimal impact on performance.

```
[57]: # Get data from the 10 best runs by recall (and other metrics)
top_ten_runs = runs_metadata.head(10) # type: ignore
top_ten_runs
```

	top_ten_runs						
[57]:		test_accuracy	test_f1	test_precision	test_recall	test_roc_auc \	
	10204	0.675	0.689615	0.541048	0.971675	0.926493	
	14813	0.675	0.689615	0.541048	0.971675	0.926493	
	11244	0.855	0.827583	0.732723	0.957635	0.966431	
	12718	0.855	0.827583	0.732723	0.957635	0.966431	
	12084	0.855	0.827583	0.732723	0.957635	0.966158	
	12802	0.855	0.827583	0.732723	0.957635	0.966158	
	10709	0.855	0.827583	0.732723	0.957635	0.966158	
	12082	0.855	0.827583	0.732723	0.957635	0.966158	
	12013	0.855	0.827583	0.732723	0.957635	0.966158	
	13880	0.855	0.827583	0.732723	0.957635	0.966158	
		train_accuracy	$train_f1$	train_precision	n train_recal	l train_roc_auc	\
	10204	0.665	0.679225	0.533823	0.95627	0.928088	
	14813	0.665	0.679225	0.533823	0.95627	0.928088	
	11244	0.860	0.828283	0.737932	0.94402	0.967808	
	12718	0.860	0.828283	0.737932	0.94402	0.967808	
	12084	0.860	0.828245	0.737831	0.94402	7 0.967817	
	12802	0.860	0.828245	0.737831	0.94402	7 0.967817	
	10709	0.860	0.828245	0.737831	0.94402	7 0.967800	
	12082	0.860	0.828245	0.737831	0.94402	0.967800	
	12013	0.860	0.828245	0.737831	0.94402	7 0.967800	

13880		0.860	0.828245	5	0.737	331 0.	944027	0.9678	300
			Cc	:lass	_weight fi	t_intercept	l1_ratio	max_iter	\
10204	0.00026	36650898	7303583	ba	alanced	True	None	500	
14813	0.00026	36650898	7303583	ba	alanced	True	None	100	
11244	78	.4759970	3514607	ba	alanced	False	None	500	
12718	78	.4759970	3514607	ba	alanced	False	None	1000	
12084	2	06.91380	8111479	ba	alanced	False	None	100	
12802	2	06.91380	8111479	ba	alanced	False	None	100	
10709	54	5.559478	1168514	ba	alanced	False	None	100	
12082	545.5594781168514			ba	alanced	False	None	100	
12013			10000.0	ba	alanced	False	None	10000	
13880			10000.0	ba	alanced	False	None	200	
	penalty		solver		warm_star	t			
10204	12		sag	0.1	Tru	е			
14813	12		sag	0.1	Fals	е			
11244	12	newton-	cholesky	0.1	Fals	е			
12718	12	newton-	cholesky	0.1	Tru	е			
12084	12	newton-	cholesky	0.1	Tru	е			
12802	12	newton-	cholesky	0.1	Fals	е			
10709	12	newton-	cholesky	0.1	Fals	е			
12082	12	newton-	cholesky	0.1	Tru	е			
12013	12	newton-	cholesky	0.1	Tru	е			
13880	12	newton-	cholesky	0.1	Tru	е			

tol: All top results used a tolerance of 0.1, the upper bound of the tested range. Given its consistent use in high-performing models, 0.1 will serve as the baseline for further analysis, though variations around this value may still be worth exploring.

solver: While sag achieved the two top recall scores, the remaining 8/10 top runs used newton-cholesky, which provided superior overall metrics with only a marginal recall drop. Thus, newton-cholesky is selected for continued optimization.

penalty: All top-performing models used *l2 regularization*, confirming its effectiveness for this classification task. It will be fixed as the penalty method in subsequent tuning.

max\_iter: A broad range of max\_iter values (100 to 10,000) appears in top results, indicating potential sensitivity. It will be further fine-tuned in future searches.

11\_ratio: Not used in top runs due to exclusive use of l2 penalty, which does not require it. This parameter will be excluded moving forward.

C: The inverse regularization strength varies widely across top results, suggesting strong interaction with other hyperparameters. It will remain a tuning parameter.

fit\_intercept: All top newton-cholesky runs used fit\_intercept=False. This setting appears beneficial and will be set to False by default in further analysis.

class\_weight: Every top-performing run used balanced class weighting, reinforcing its relevance in handling class imbalance for breast cancer detection.

warm\_start: This parameter is split in the top results and, based on mutual information results, appears uninfluential. It will be disregarded in further tuning.

# 1.3.3 Focused Hyperparameter Optimization

The first step in hyperparameter optimization gave indications as to regions where the model performs well. The second step will use a more focused approach building upon these finding. This step will use grid search for exploration.

The insights from this step guide the design of an exhaustive search in the next phase.

A custom implementation of grid search will be used for integration with mlflow.

```
[16]: # Define the parameter grid
      param_grid = {
          "penalty": ["12"],
          "tol": [1e-2, 0.05, 1e-1, 0.25, 0.5, 0.75, 1, 2.5, 5, 10],
          "C": np.logspace(-6, 6, 100),
          "solver": [
              "newton-cholesky",
          ],
          "fit_intercept": [False],
          "max_iter": [100, 200, 300, 500, 1000, 2000, 5000, 10000],
          "class_weight": ["balanced"],
          "warm_start": [False], # Use default value
          "l1_ratio": [None], # Use default value
      }
      param_samples = all_param_combinations(param_grid)
      print(
          "Number of total parameter combinations: ",
          total_param_combinations(param_grid),
      print("")
      print(param_samples[0])
```

Number of total parameter combinations: 8000

```
{'penalty': 'l2', 'tol': 0.01, 'C': np.float64(1e-06), 'solver': 'newton-
cholesky', 'fit_intercept': False, 'max_iter': 100, 'class_weight': 'balanced',
'warm_start': False, 'l1_ratio': None}
```

```
[17]: # Suppress warnings for convergence
warnings.filterwarnings("ignore", category=ConvergenceWarning)

best_score = -np.inf
best_run = None
best_params = None
```

```
for i, params in enumerate(tqdm(param_samples, desc="Processing ML Runs")):
    with mlflow.start_run():
        mlflow.set_tags(
            tags={
                "Model": "LogisticRegression",
                "Experiment Type": "Hyperparameter Optimization",
                "Dataset": "processed_data_pt_sfs.parquet",
                "Stage": "Focused",
            }
        )
        # Log params
        for k, v in params.items():
            mlflow.log_param(k, v)
        model = LogisticRegression(verbose=0, random_state=42, n_jobs=1)
        model.set_params(**params)
        # Get model scores
        cv_results = cross_validate(
            model,
            X_train,
            y_train,
            cv=cv,
            scoring=scoring,
            return_train_score=True,
            n_{jobs=-1},
        )
        mean_scores = {
            f"train_{metric}": np.mean(cv_results[f"train_{metric}"])
            for metric in scoring.keys()
        }
        mean_scores.update(
            {
                f"test_{metric}": np.mean(cv_results[f"test_{metric}"])
                for metric in scoring.keys()
            }
        )
        for metric, value in mean_scores.items():
            mlflow.log_metric(metric, value)
        # Update best score
        if mean_scores["test_recall"] > best_score:
```

```
best_score = mean_scores["test_recall"]
    best_params = params
    best_run = mlflow.active_run().info.run_id # type: ignore

mlflow.end_run()

print(f"Best Score: {best_score}")
print(f"Best Params: {best_params}")
print(f"Best Run: {best_run}")
```

Processing ML Runs: 100%| | 8000/8000 [1:25:43<00:00, 1.56it/s]

Best Score: 0.9576354679802955

Best Params: {'penalty': '12', 'tol': 0.1, 'C': np.float64(43.287612810830616), 'solver': 'newton-cholesky', 'fit\_intercept': False, 'max\_iter': 100, 'class\_weight': 'balanced', 'warm\_start': False, 'l1\_ratio': None}

Best Run: a5f9749564aa41b78b25f2672fd5618a

#### Evaluation

```
[7]: # Get data from all runs
     runs_metadata = mlflow.search_runs(
         filter_string="tags.Stage = 'Focused'",
         experiment_names=["LR-Hyperparameter_Optimization"],
     )
     runs_metadata = runs_metadata[
         sorted(
             Γ
                 "metrics.test f1",
                 "metrics.test roc auc",
                 "metrics.train precision",
                 "metrics.test_precision",
                 "metrics.train_roc_auc",
                 "metrics.test_recall",
                 "metrics.train_recall",
                 "metrics.test_accuracy",
                 "metrics.train_accuracy",
                 "metrics.train_f1",
                 "params.fit_intercept",
                 "params.C",
                 "params.class_weight",
                 "params.solver",
                 "params.penalty",
                 "params.warm start",
                 "params.max_iter",
                 "params.tol",
```

```
"params.l1_ratio",
        ]
    )
] # type: ignore
runs_metadata = runs_metadata.sort_values(
    by=[
        "metrics.test_recall",
        "metrics.test_roc_auc",
        "metrics.test_f1",
        "metrics.train_recall",
        "metrics.train_roc_auc",
        "metrics.train_f1",
        "metrics.test_precision",
        "metrics.test_accuracy",
        "metrics.train_precision",
        "metrics.train_accuracy",
    ],
   ascending=False,
) # type: ignore
runs_metadata.columns = [
    col.split(".")[1] if "." in col else col for col in runs_metadata.columns
]
{\tt runs\_metadata}
```

[7]:		test_accuracy	test_f1	test_precision	test_recall	test_roc_auc \	
	5080	0.8575	0.829954	0.736184	0.957635	0.966568	
	5081	0.8575	0.829954	0.736184	0.957635	0.966568	
	5082	0.8575	0.829954	0.736184	0.957635	0.966568	
	5083	0.8575	0.829954	0.736184	0.957635	0.966568	
	5084	0.8575	0.829954	0.736184	0.957635	0.966568	
		***	•••	•••			
	5331	0.8275	0.792441	0.703018	0.915271	0.940073	
	5332	0.8275	0.792441	0.703018	0.915271	0.940073	
	5333	0.8275	0.792441	0.703018	0.915271	0.940073	
	5334	0.8275	0.792441	0.703018	0.915271	0.940073	
	5335	0.8275	0.792441	0.703018	0.915271	0.940073	
		train_accuracy	$train_f1$	train_precision	train_recal	l train_roc_auc	\
	5080	0.860000	0.828283	0.737932	0.94402	7 0.967791	
	5081	0.860000	0.828283	0.737932	0.94402	7 0.967791	
	5082	0.860000	0.828283	0.737932	0.94402	7 0.967791	
	5083	0.860000	0.828283	0.737932	0.94402	7 0.967791	
	5084	0.860000	0.828283	0.737932	0.94402	7 0.967791	
		•••	•••	•••	•••	•••	
	5331	0.838125	0.802321	0.713028	0.91778	0.942218	
	5332	0.838125	0.802321	0.713028	0.91778	0.942218	
	5333	0.838125	0.802321	0.713028	0.91778	0.942218	

```
5335
                                          0.838125 0.802321
                                                                                                             0.713028
                                                                                                                                                 0.917788
                                                                                                                                                                                      0.942218
                                                                C class_weight fit_intercept l1_ratio max_iter penalty
            5080 57.2236765935022
                                                                                balanced
                                                                                                                         False
                                                                                                                                                   None
                                                                                                                                                                       10000
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            5081 57.2236765935022
                                                                               balanced
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            5082 57.2236765935022
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            5083 57.2236765935022
                                                                               balanced
                                                                                                                         False
                                                                                                                                                   None
                                                                                                                                                                          1000
                                                                                                                                                                                                  12
            5084 57.2236765935022
                                                                                                                                                                                                  12
                                                                               balanced
                                                                                                                          False
                                                                                                                                                   None
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                                                                                                                                 •••
            5331
                                                                                                                                                                                                  12
                                                         0.01
                                                                               balanced
                                                                                                                          False
                                                                                                                                                  None
                                                                                                                                                                          1000
            5332
                                                         0.01
                                                                               balanced
                                                                                                                         False
                                                                                                                                                   None
                                                                                                                                                                            500
                                                                                                                                                                                                  12
            5333
                                                         0.01
                                                                               balanced
                                                                                                                          False
                                                                                                                                                   None
                                                                                                                                                                            300
                                                                                                                                                                                                  12
            5334
                                                         0.01
                                                                               balanced
                                                                                                                         False
                                                                                                                                                   None
                                                                                                                                                                            200
                                                                                                                                                                                                  12
                                                         0.01
                                                                               balanced
                                                                                                                         False
                                                                                                                                                                                                  12
            5335
                                                                                                                                                   None
                                                                                                                                                                            100
                                                 solver
                                                                       tol warm_start
            5080 newton-cholesky 0.25
                                                                                              False
            5081 newton-cholesky 0.25
                                                                                              False
            5082 newton-cholesky 0.25
                                                                                              False
            5083 newton-cholesky 0.25
                                                                                              False
            5084 newton-cholesky
                                                                                              False
                                                                     0.25
                                                                                              False
            5331 newton-cholesky 0.25
            5332 newton-cholesky 0.25
                                                                                              False
            5333 newton-cholesky 0.25
                                                                                              False
                                                                                              False
            5334 newton-cholesky 0.25
            5335 newton-cholesky 0.25
                                                                                              False
            [8000 rows x 19 columns]
[8]: # Create a DataFrame to store mutual information scores
            mi_scores_df = pd.DataFrame(columns=["feature", "test_recall", "test_roc_auc", "test_recall", "test_roc_auc", "test_recall", "test_roc_auc", "test_recall", "test_reca

¬"test_f1"]) # type: ignore
            main_metrics = ["test_recall", "test_roc_auc", "test_f1"]
            hyperparameters = [
                      "C".
                      "max_iter",
                      "tol",
            ]
            # Iterate over each metric and calculate mutual information scores
            for metric in main_metrics:
                      X = runs_metadata[hyperparameters].copy() # type: ignore
```

0.713028

0.917788

0.942218

5334

0.838125 0.802321

```
y = runs_metadata[metric] # type: ignore

# Encode categorical variables
encoder = OrdinalEncoder()
X_encoded = encoder.fit_transform(X.astype(str))

mi_scores = mutual_info_regression(X_encoded, y)

mi_scores_df[metric] = mi_scores
mi_scores_df["feature"] = X.columns

mi_scores_df = mi_scores_df.sort_values(by=main_metrics, ascending=False)
mi_scores_df
```

```
[8]:
         feature
                  test_recall test_roc_auc
                                               test_f1
               C
                     1.435892
                                   2.879903
                                             2.284884
     2
             tol
                     0.472347
                                   0.700198
                                             0.605220
                     0.000000
                                   0.000000 0.000000
     1 max iter
```

- C emerged as the single strongest driver of performance (MI 1.44 for recall, 2.88 for ROC AUC, 2.28 for F1). The best runs cluster tightly around C 57.2, yielding test recall 0.9576, ROC AUC 0.9666, and F1 0.8300.
- tol is the next most influential (MI 0.47 0.70), with the top-performing models using tol = 0.25—the middle of the refined range.
- max\_iter shows zero mutual information, and varying it between 500 and 10 000 had no effect on any metric, indicating that once the solver runs long enough to converge, extra iterations are wasted.

## 1.3.4 Exhaustive Hyperparameter Optimization

The final step of hyperparameter optimization focuses on exhaustively optimizing hyperparameters still showing variance in results (C and tol), while continuing to use previously found optimal settings for other hyperparameters. This step will use grid search with very narrow ranges for these hyperparameters.

```
), # Generate 100 samples from a normal distribution with mean=50 and \Box
       \hookrightarrow std = sqrt(mean)
          "solver": [
              "newton-cholesky",
          ],
          "fit intercept": [False],
          "max iter": [
              300
          ], # Algorithm converged at 100 iterations, so a lower value with a buffer
       ⇔will be used
          "class_weight": ["balanced"],
          "warm start": [False], # Use default value
          "l1_ratio": [None], # Use default value
      }
      param_samples = all_param_combinations(param_grid)
      print(
          "Number of total parameter combinations: ",
          total_param_combinations(param_grid),
      )
      print("")
      print(param_samples[0])
     Number of total parameter combinations: 10000
     {'penalty': '12', 'tol': np.float64(0.28104463456320206), 'C':
     np.float64(39.99181750403116), 'solver': 'newton-cholesky', 'fit_intercept':
     False, 'max_iter': 300, 'class_weight': 'balanced', 'warm_start': False,
     'l1_ratio': None}
[13]: # Suppress warnings for convergence
      warnings.filterwarnings("ignore", category=ConvergenceWarning)
      best_score = -np.inf
      best_run = None
      best_params = None
      for i, params in enumerate(tqdm(param_samples, desc="Processing ML Runs")):
          with mlflow.start_run():
              mlflow.set_tags(
                  tags={
                      "Model": "LogisticRegression",
                      "Experiment Type": "Hyperparameter Optimization",
                      "Dataset": "processed_data_pt_sfs.parquet",
                      "Stage": "Exhaustive",
```

```
# Log params
        for k, v in params.items():
            mlflow.log_param(k, v)
        model = LogisticRegression(verbose=0, random_state=42, n_jobs=1)
        model.set_params(**params)
        # Get model scores
        cv_results = cross_validate(
            model,
            X_train,
            y_train,
            cv=cv,
            scoring=scoring,
            return_train_score=True,
            n_{jobs=-1},
        )
        mean_scores = {
            f"train_{metric}": np.mean(cv_results[f"train_{metric}"])
            for metric in scoring.keys()
        }
        mean_scores.update(
            {
                f"test_{metric}": np.mean(cv_results[f"test_{metric}"])
                for metric in scoring.keys()
            }
        )
        for metric, value in mean_scores.items():
            mlflow.log_metric(metric, value)
        # Update best score
        if mean_scores["test_recall"] > best_score:
            best_score = mean_scores["test_recall"]
            best_params = params
            best_run = mlflow.active_run().info.run_id # type: ignore
    mlflow.end_run()
print(f"Best Score: {best_score}")
print(f"Best Params: {best_params}")
print(f"Best Run: {best_run}")
```

```
Processing ML Runs: 100% | 10000/10000 [2:52:20<00:00, 1.03s/it]

Best Score: 0.9576354679802955

Best Params: {'penalty': '12', 'tol': np.float64(0.28104463456320206), 'C': np.float64(39.99181750403116), 'solver': 'newton-cholesky', 'fit_intercept': False, 'max_iter': 300, 'class_weight': 'balanced', 'warm_start': False, 'l1_ratio': None}

Best Run: ea26546874894a96b23f4083fdf1bbcd
```

## Evaluation

```
[15]: # Get data from all runs
      runs_metadata = mlflow.search_runs(
          filter_string="tags.Stage = 'Exhaustive'",
          experiment_names=["LR-Hyperparameter_Optimization"],
      runs_metadata = runs_metadata[
          sorted(
              Γ
                  "metrics.test f1",
                  "metrics.test_roc_auc",
                  "metrics.train_precision",
                  "metrics.test_precision",
                  "metrics.train_roc_auc",
                  "metrics.test_recall",
                  "metrics.train_recall",
                  "metrics.test_accuracy",
                  "metrics.train_accuracy",
                  "metrics.train_f1",
                  "params.fit_intercept",
                  "params.C",
                  "params.class_weight",
                  "params.solver",
                  "params.penalty",
                  "params.warm_start",
                  "params.max iter",
                  "params.tol",
                  "params.l1_ratio",
              ]
      ] # type: ignore
      runs_metadata = runs_metadata.sort_values(
          by=[
              "metrics.test_recall",
              "metrics.test_roc_auc",
              "metrics.test_f1",
              "metrics.train recall",
```

```
"metrics.train_roc_auc",
               "metrics.train_f1",
               "metrics.test_precision",
               "metrics.test_accuracy",
               "metrics.train_precision",
               "metrics.train_accuracy",
          ],
          ascending=False,
        # type: ignore
      runs metadata.columns = [
          col.split(".")[1] if "." in col else col for col in runs_metadata.columns
      runs metadata
[15]:
             test_accuracy
                              test_f1
                                        test_precision
                                                        test_recall
                                                                       test_roc_auc
                             0.829954
      8
                     0.8575
                                              0.736184
                                                            0.957635
                                                                           0.966568
      9
                     0.8575
                             0.829954
                                              0.736184
                                                            0.957635
                                                                           0.966568
                             0.829954
      35
                     0.8575
                                              0.736184
                                                            0.957635
                                                                           0.966568
                                              0.736184
      37
                     0.8575
                             0.829954
                                                            0.957635
                                                                           0.966568
      70
                     0.8575
                             0.829954
                                              0.736184
                                                            0.957635
                                                                           0.966568
      9269
                     0.8550
                             0.825057
                                              0.737747
                                                            0.943596
                                                                           0.966566
      5989
                     0.8550
                             0.825057
                                              0.737747
                                                            0.943596
                                                                           0.966566
      9289
                     0.8550
                             0.825057
                                              0.737747
                                                            0.943596
                                                                           0.966566
      10000
                        NaN
                                  NaN
                                                   NaN
                                                                 NaN
                                                                                NaN
      10001
                        NaN
                                  {\tt NaN}
                                                   NaN
                                                                 NaN
                                                                                NaN
             train_accuracy
                              train_f1
                                         train_precision
                                                           train_recall
                                                                          train_roc_auc
      8
                        0.86
                              0.828283
                                                                               0.967791
                                                0.737932
                                                               0.944027
      9
                        0.86 0.828283
                                                0.737932
                                                               0.944027
                                                                               0.967791
                        0.86
      35
                              0.828283
                                                0.737932
                                                               0.944027
                                                                               0.967791
      37
                        0.86
                              0.828283
                                                0.737932
                                                               0.944027
                                                                               0.967791
      70
                        0.86
                              0.828283
                                                0.737932
                                                               0.944027
                                                                               0.967791
                                                                               0.967740
      9269
                        0.86
                              0.828037
                                                0.738599
                                                               0.942288
      5989
                        0.86
                              0.828037
                                                0.738599
                                                               0.942288
                                                                               0.967732
                        0.86
                                                               0.942288
      9289
                              0.828037
                                                0.738599
                                                                               0.967732
      10000
                         NaN
                                   NaN
                                                                    NaN
                                                                                    NaN
                                                      NaN
      10001
                         NaN
                                   NaN
                                                      NaN
                                                                    NaN
                                                                                    NaN
                               C class_weight fit_intercept l1_ratio max_iter
      8
              56.05565394866111
                                      balanced
                                                        False
                                                                             300
                                                                  None
      9
              46.84266249492223
                                      balanced
                                                        False
                                                                  None
                                                                             300
      35
                                      balanced
                                                        False
             56.812097938219075
                                                                  None
                                                                             300
      37
               58.1925079056889
                                      balanced
                                                        False
                                                                  None
                                                                             300
      70
              46.43988950812103
                                      balanced
                                                        False
                                                                  None
                                                                             300
```

9269 5989 9289 10000 10001	36.432 36.432 39.991	23862116495 23862116495 81750403116	balanced balanced balanced balanced balanced	False False False False	None None None None	300 300 300 300 300
]	penalty	solver		tol warm	_start	
8	12	newton-cholesky	0.23533830416	340533	False	
9	12	newton-cholesky	0.23533830416	340533	False	
35	12	newton-cholesky	0.23533830416	340533	False	
37	12	newton-cholesky	0.23533830416	340533	False	
70	12	newton-cholesky	0.23533830416	340533	False	
	•••	•••	•••	•••		
9269	12	newton-cholesky	0.29796467057	720568	False	
5989	12	newton-cholesky	0.296154161249	71317	False	
9289	12	newton-cholesky	0.29796467057	720568	False	
10000	12	newton-cholesky	0.281044634563	320206	False	
10001	12	newton-cholesky	0.281044634563	320206	False	

[10002 rows x 19 columns]

The metrics obtained from the best run of the exhaustive hyperparameter optimization are identical to those from the previous optimization step. This outcome indicates that a (near-)optimal solution has been reached, and further significant improvements with this algorithm are unlikely.

Final Model Performance Metrics

Metric	Test Set	Train Set
Accuracy	0.8575	0.8600
F1 Score	0.8300	0.8283
Precision	0.7362	0.7379
Recall	0.9576	0.9440
ROC AUC	0.9666	0.9678

# **Optimal Hyperparameters**

Hyperparameter	Value
$\overline{\mathrm{C}}$	56.06
class_weight	balanced
$fit\_intercept$	False
l1_ratio	None
$\max_{}$ iter	300
penalty	12
solver	newton-cholesky
tol	0.235
warm_start	False

These results demonstrate that the logistic regression model, with the specified preprocessing and hyperparameter configuration, achieves high recall and ROC AUC, making it well-suited for the detection of positive cases in this binary cancer-detection classification task. The absence of further improvement in the exhaustive search confirms the robustness and optimality of the selected solution.

```
[]: # Save the best model
model = LogisticRegression(verbose=0, random_state=42, n_jobs=1, **best_params)
# type: ignore
model.fit(X_train, y_train)

# Save the model
model_path = os.path.join(
    os.path.dirname(os.getcwd()), "artifacts", "logistic_regression.pkl"
)
joblib.dump(model, model_path)

# Log the model to MLflow
mlflow.sklearn.log_model(
    model,
    "model",
    input_example=X_train.iloc[:5],
    registered_model_name="LogisticRegression",
)
```

Successfully registered model 'LogisticRegression'. Created version '1' of model 'LogisticRegression'.

[]: <mlflow.models.model.ModelInfo at 0x12675ec00>

## 1.4 Summary

This notebook presents a systematic approach to selecting preprocessing strategies and optimizing hyperparameters for a logistic regression model aimed at binary classification of breast cancer data. The primary goal is to maximize recall, ensuring the detection of as many positive (cancerous) cases as possible, with secondary consideration given to ROC AUC, F1-score, precision, and accuracy.

## 1.4.1 Methodology

# Preprocessing and Dataset Selection

- Multiple data preprocessing pipelines were evaluated, varying by:
  - Scaling method: Power Transformer (PT), Quantile Transformer (QT), MinMaxS-caler, StandardScaler (STD)
  - Feature selection: None (all), mutual information (mi), sequential feature selection (sfs)
- Each pipeline was assessed using default logistic regression hyperparameters.
- Performance metrics: Recall (primary), F1-score, accuracy, precision, ROC AUC.

The pt\_sfs dataset (Power Transformer + Sequential Feature Selection) achieved the highest recall and strong overall metrics, making it the optimal preprocessing strategy.

**Hyperparameter Optimization** A three-stage optimization strategy was employed:

**Broad Exploration (Randomized Search)** - Random sampling of a wide hyperparameter space for penalty, tolerance, regularization strength, solver, and other parameters.

Focused Tuning (Grid Search) - Grid search was performed in promising regions identified in the broad search.

**Exhaustive Fine Adjustment** - Narrow grid search around optimal values. - Confirmed that further improvements were negligible, indicating convergence to a (near-)optimal solution.

# 1.4.2 Results Final Model Performance

Metric	Test Set	Train Set
Accuracy	0.8575	0.8600
F1 Score	0.8300	0.8283
Precision	0.7362	0.7379
Recall	0.9576	0.9440
ROC AUC	0.9666	0.9678
F1 Score Precision Recall	0.8300 $0.7362$ $0.9576$	0.8283 0.7379 0.9440

# **Optimal Hyperparameters**

Hyperparameter	Value
$\overline{\mathrm{C}}$	56.06
class_weight	balanced
fit_intercept	False
l1_ratio	None
max_iter	300
penalty	12
solver	newton-cholesky
tol	0.235
warm_start	False

Mutual Information Analysis showed that solver, penalty, tolerance, and C had the highest impact on model performance (primarily recall, f1, and roc-auc)

The final model achieves high recall, f1, and roc-auc, making it suitable for medical applications where minimizing false negatives is critical.