Beeldverwerken assignment 2

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 $Theory\ Questions$

1 Convolution

Everything outside of the signal f is considered 0

1.
$$f * g = \{4 \underline{3} 1\}$$

2.
$$f * g = \{0 \ 0 \ 0 \ 1 \ \underline{3} \ 4 \ 4 \ 3\}$$

3.
$$f * g = \{0 \ 0 \ 0 \ 0 \ \underline{1} \ 0 \ 0 \ 0\}$$

$$6. \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$7. \begin{bmatrix} 0 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$8. \begin{bmatrix} 0 & 0 & 1 \\ \bar{0} & 0 & 0 \end{bmatrix}$$

9. Not possible

10.
$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

- 11. Not possible
- 12. Not possible

13.
$$\frac{1}{6}$$
 [1 1 1 1 1]

```
\begin{bmatrix} 0.0113 & 0.0149 \end{bmatrix}
                  0.0176 \quad 0.0186
                                     0.0176 \quad 0.0149
                                                        0.0113
0.0149
         0.0197
                  0.0233
                            0.0246
                                     0.0233
                                              0.0197
                                                        0.0149
0.0176
         0.0233
                            0.0290
                                     0.0275
                                              0.0233
                                                        0.0176
                  0.0275
0.0186
                            0.0307
                                     0.0290
                                              0.0246
                                                        0.0186
0.0176
                                                        0.0176
         0.0233
                  0.0275
                            0.0290
                                     0.0275
                                              0.0233
0.0149
         0.0197
                  0.0233
                            0.0246
                                     0.0233
                                              0.0197
                                                        0.0149
0.0113
         0.0149
                  0.0176
                            0.0186
                                     0.0176
                                              0.0149
                                                        0.0113
```

15. Unsharp masking is simply blurring an image and then substracting that blurred image from the original. A kernel for a blur could be something like shown above or a gaussian.(An example of unsharp masking is provided in the matlab code)

```
16. g = 1/2\{1 \ 0 \ -1\}
```

- 17. ...
- 18. Not possible, since this would require more than one convolution kernel.
- 19. Not possible, a convolution kernel cannot specify differences between point.
- 20. The applied filters are shown in the matlab file.
- 21.

22.
$$f(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{||x||^2}{2\sigma^2}}$$

- 23.
- 24.
- 25.
- 26.
- 27.

2 Implementation of Gaussian derivatives

This part was entirely made in matlab.

3 The Canny Edge Detector

1.
$$f(x,y) = A \sin(Vx) + B \cos(Wy)$$

 $f'_x(x,y) = AV \cos(Vx)$
 $f'_y(x,y) = -BW \sin(Wy)$
 $f'_{xx}(x,y) = -AV \sin(Vx)$
 $f'_{yy}(x,y) = -BW \cos(Wy)$
 $f'_{xy}(x,y) = 0$