Get logic'd

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1 Day 1

If I am deceived, I exist.
If I am not deceived, I do not exist.
I exist.

2 Day 2,3,4

An argument is **valid** if and only if the truth of its premises guarantees the truth of the conclusion. (i.e. there is no case in which all premises are true and the conclusion is false)

An argument is **vacuously valid** if and only if it is valid and has inconsistent premises.

An argument is **sound** if it is both valid and the premises are true.

An argument is **consistent** if and only if there is a case that all sentences are true.

An argument is **defeasibly valid** if and only if, if the premises are true, it's reasonable to expect the conclusion to be true as well.

A **counterexample** to an argument is a circumstance in which the premises are true and the conclusion is false.

1.

A He must have gone to King's Pyland or to Mapleton
   He is not at King's Pyland
   He is at Mapleton

B The argument is not valid because having gone to King's Pyland or to Mapleton is not equivalent to being at King's Pyland or Mapleton. The first premise does not guarantee that He is eitehr at King's Pyland or at Mapleton, just that he must have gone to one of the two. For example, He could have gone to Mapleton and then gone to San Francisco. In this case, both premises are true and the conclusion is false. The argument is not sound because it is not valid.

C *A*:He must have gone to King's Pyland.
 B:He must have gone to Mapleton.
 C:He is at King's Pyland.
 D:He is at Mapleton.

$A \lor B$
$\underline{\neg C}$
D

	P	M	$P \lor M$	$\neg P$	M
	T	T	T	F	T
D	T	F	T	F	F
	F	T	T	T	T
	F	F	F	T	F
	1				

2.

A The patient will die unless we operate.
 We will operate.
 The patient will not die.

B The first premise states that if !A then B(if we do not operate then the patient will die), and then it states A, which does not imply !B. Therefore, the argument is invalid, and therefore not sound.

C *D*:The patient will die.
 O:We will operate.

$\neg O \implies D$
$\underline{O}$
$\neg O$

3.

A If I am right, then I am a fool.
 If I am a fool, I am not right.
 I am no fool.

B If I am a fool, then I am not right. The first premise does not relate to a situation in which I am not right. Therefore, a situation in which I am a fool would have true premises but a false conclusion. THerefore, the argument is invalid, and therefore not sound.

C *R*:I am right.
 F:I am a fool.

$R \implies F$
$\underline{F \implies \neg R}$
$\neg F$

	R	F	$R \implies F$	$F \implies \neg R$	$\neg F$
	T	T	T	F	F
D	T	F	F	T	T
	F	T	T	T	F
	F	F	T	T	T

invalid

4.

A If I am right, then I'm a fool.
   If I am a fool, I am not right
   I'm not right.

B If I am right, then the argument is contradictory, making the premises
   false. If I am not right, then all premises are true and the conclusion is
   true. Therefore, the argument is valid and sound.

C R:I am right.
   F:I am a fool.

   $R \implies F$
   $F \implies \neg R$
   $\neg R$

	R	F	$R \implies F$	$F \implies \neg R$	$\neg R$	
	T	T	T	F	F	
D	T	F	F	T	F	Valid
	F	T	T	T	T	
	F	F	T	T	T	

5.

A If Einstein's theory of relativity is correct, light bends in the vicinity of
   the sun.
   Light bends in the vicinity of the sun.
   Einstein's theory of relativity is correct.

B If Einstein's theory is false, premise number 2 could still be true for some
   other reason, so both premises are false and the argument is invalid and
   not sound.

C E:Einstein's theory of relativity is correct.
   L:Light bends in the vicinity of the sun.

   $E \implies L$
   L
   E

	E	L	E $\implies$ L	L	E
	T	T	T	T	T
D	T	F	F	F	T
	F	T	T	T	F
	F	F	T	F	F

6.

A Congress will agree to the cut only if the President announces his support first.
The President won't announce his support first.
Congress won't agree to the cut

B Valid
Sound-ness is difficult to determine.

C C:Congress will agree to the cut.
S:The president announces his support first.

$$C \implies S$$
$$\neg S$$
$$\neg C$$

7.

A If you are ambitious, you'll never achieve all your goals.
Iff you have ambition, life has meaning
If you achieve all your goals, life has no meaning.

B Valid
Sound-ness is difficult to determine

C A:You are ambitious.
G:You achieve all your goals.
L:Life has meaning.

$$A \implies \neg G$$
$$A \implies L$$
$$G \implies \neg L$$

	A	G	L	A $\implies$ ¬G	L $\implies$ A	G $\implies$ ¬L
	T	T	T	F	T	F
	T	T	F	F	F	T
	T	F	T	T	T	T
D	T	F	F	T	F	T
	F	T	T	T	F	F
	F	T	F	T	T	T
	F	F	T	T	F	T
	F	F	F	T	T	T

A If Adams wins the election, Brown will retire to private life.
   If Brown dies before the election, Adams will win it.
   ‾‾
   If Brown dies before the election, he will retire to private life.

B Valid
   Not Sound

C A:Adams wins the election.
   B:Brown will retire to private life.
   D:Brown dies before the election.

   $A \implies B$
   $\underline{D \implies A}$
   $D \implies B$

8.

A Holmes is right and the Moriarty is guilty or Holmes is wrong and Thin
   is guilty.
   They are either both guilty or both innocent.
   Holmes is right
   ‾‾‾‾‾‾‾‾‾‾‾‾‾‾
   Thin is guilty

B Valid
   Sound-ness is difficult to determine

C H:Holmes is right.
   T:Thin is guily.
   M:Moriarty is guilty.

   $(H \wedge M) \vee (\neg H \wedge T)$
   $(M \wedge T) \vee (\neg M \wedge \neg T)$
   $\underline{H}$
   T

D

H	T	M	$(H \wedge M) \vee (\neg H \wedge T)$	$(M \wedge T) \vee (\neg M \wedge \neg T)$	H	T
T	T	T	T	T	T	T
T	T	F	F	F	T	T
T	F	T	T	F	T	F
T	F	F	F	T	T	F
F	T	T	T	T	F	T
F	T	F	T	F	F	T
F	F	T	F	F	F	F
F	F	F	F	T	F	F

   valid

9.

A Mittens meows exactly when she is Hungry.
Mittens is meowing.
Mittens isn't hungry

The end of the earth is at hand.

B invalid
sound-ness is difficult to determine

C M:Mittens meows.
H:She is hungry.
E:End of the earth is at hand.

$M \iff H$
M
$\neg H$

E

10.

A God cannot be conceived.
If God can be conceived and does not exist in our reality, then something is conceivable that is greater t

If God can be conceived, God exists in reality.

B Valid

Sound-ness is difficult to determine

C C:God can be conceived.
E:God exists in our reality.
G:Something is conceivable that is greater than god.

$\neg C$
$(C \wedge \neg E) \implies G$

$C \implies E$

	C	E	G	$\neg C$	$(C \wedge \neg E) \implies G$	$C \implies E$
	T	T	T	F	T	T
	T	T	F	F	T	T
	T	F	T	F	T	F
D	T	F	F	F	F	F
	F	T	T	T	T	T
	F	T	F	T	T	T
	F	F	T	T	T	T
	F	F	F	T	T	T

Valid

11.

A God is omnipotent iff he can do everythang.
   If he can't make a stone so big he can't lift it, he can't do everything.
   If he can make a stone so big he can't life it, he can't do everything.
   God is either not omnipotent or does not exist in reality.

B Valid
   Sound-ness is controvertial

C O:God is omnipotent.
   E:God can do everything.
   S:God can make a stone so big he can't lift it.
   G:God exists in out reality.

   $O \iff E$
   $\neg S \implies \neg E$
   $S \implies \neg E$
   $\neg O \lor \neg G$

12.

A If the objects of mathematics are material things, then mathematics can't
   consist entirely of necessary truths.
   Mathematical objects are immaterial only if the mind has access to a realm
   beyond the reach of the senses.
   Mathematics does consist of necessary truths.
   Mathematics does consist of necessary truths, although the mind has no access to any realm beyond the
   The objects of mathematics are neither material nor immaterial.

B Invalid
   Sound-ness is difficult to determine

C O:The objects of mathematics are material things.
   T:Mathematics consists entirely of necessary truths.
   M:The mind has access to a realm beyond the reach of the senses.

   $O \implies \neg T$
   $O \implies M$
   T
   $T \land \neg M$
   $\neg O \land \neg\neg O$

O	T	M	$O \implies \neg T$	$O \implies M$	T	$T \wedge \neg M$	$\neg O \wedge \neg\neg O$
T	T	T	F	T	T	F	F
T	T	F	F	F	T	T	F
T	F	T	T	T	F	F	F
T	F	F	T	F	F	F	F
F	T	T	T	T	T	F	F
F	T	F	T	T	T	T	F
F	F	T	T	T	F	F	F
F	F	F	T	T	F	F	F

(D marks the fourth data row)

Valid!

13.

A If the president pursues arms limitations talks, then if he gets the goreign policy mechanism working more harmoniously, the European Left will acquiesce to the placement of additional nuclear weapons in Europe.
The European left will never acquiesce to that.
The President won't get the foreign policy mechanism working more harmoniously, or he won't pursue arms limitation talks.

B Invalid
Sound-ness is difficult to determine

C P:The president pursues arms limitation talks.
F:The president gets the foreign policy mechanism working more harmoniously.
L:The European Left will acquiesce to the placement of additional nuclear weapons in Europe.

$P \implies (F \implies L)$
$\underline{\neg L}$
$\neg P \vee \neg F$

P	F	L	$P \implies (F \implies L)$	$\neg L$	$\neg P \vee \neg F$
T	T	T	T	F	F
T	T	F	F	T	F
T	F	T	T	F	T
T	F	F	T	T	T
F	T	T	T	F	T
F	T	F	T	T	T
F	F	T	T	F	T
F	F	F	T	T	T

(D marks the fourth data row)   Valid

14.

A If we continue to run a large trade deficit, then the government will yield to calls for protectionism.
We won't continue to run a large deficit only if our economy slows down or foreign economies recover.

If foreign economies don't recover, then the government will resist calls for protectionism only if our economy slows down.

B Valid
Sound-ness is difficult to determine

C D:We will continue to run a large trade deficit.
G:The government will yield to calls for protectionism.
E:Our economy slows down.
F:Foreign economies recover.

$$D \implies G$$
$$\neg D \implies (E \vee F)$$
$$\overline{\neg F \implies (\neg G \implies E)}$$

D	G	E	F	$D \implies G$	$\neg D \implies (E \vee F)$	$\neg F \implies (\neg G \implies E)$
T	T	T	T	T	T	T
T	T	T	F	T	T	T
T	T	F	T	T	T	T
T	F	T	T	F	T	T
T	F	T	F	F	T	T
T	F	F	T	F	T	T
T	F	F	F	F	T	F
F	T	T	T	T	T	T
F	T	T	F	T	T	T
F	T	F	T	T	T	T
F	F	T	T	T	T	T
F	F	T	F	T	T	T
F	F	F	T	T	T	T
F	F	F	F	T	F	F

D

valid

15.

A We cannot both maintain high educational standards and accept almost every high school graduate unless we fail large numbers of students when (and only when) many students do poorly.
We will continue to maintain high standards
We will placate the legislature and admit almost all high school graduates.
We can't both placate the legislature and fail large numbers of students.
Not many students will do poorly.

B Valid
Sound-ness is difficult to determine

C E:We maintain high educational standards.
A:We accept almost every high school student.
F:We fail large numbers of students.

S:Students do poorly.
P:We will placate the legislature.

$$\neg(E \wedge F) \vee (F \iff S)$$
$$E$$
$$P \wedge A$$
$$\underline{\neg(P \wedge F)}$$
$$\neg S$$

3 Claims

1. True, an argument is only made invalid if the conclusion is made false.

2. False, if you remove false premises and leave true ones, then the argument can become invalid.

3. O moving to either 1 or 7 would make no difference, since the two situations are equivalent after a simple translation.

4. $(A \wedge B) \implies C$
   There is a case where $(A \wedge B)$ are true but C is false, therefore there is a case where the prepositions are true but the conclusion is false, making the argument invalid.

5. There are no cases where $(A \wedge B)$ are true but C is false, so $(A \wedge B) \implies C$ is always true. The argument A, B, therefore C is valid, therefore there is no case in which A and B are true but C is false, because A and B are premises and C is the conclusion. The only case in which $(A \wedge B) \implies C$ is false would be when $(A \wedge B)$ is true but C is false, which we just established will never happen. Therefore, the statement $(A \wedge B) \implies C$ is always true.

4 Other