

1 One-step error probability

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#= This script answers the first question "One-step error probability" of Homework 1 =#

#= All the scrips are written in julia, since I didn't want to be bothered with the =#
#= slow programing languages such as python or matlab. I will do my best to make the =#
#= scripts understandable for someone with no experience with Julia. The performance =#
#= in this scrips are outstanding compared to the equivalent scripts that are written =#
#= with python or matlab, it only takes 5 seconds to execute this script on my laptop =#

using Distributions # used for random sampling

#= The main script computes the error probability for different values for P =#
function main()
    P = [12,24,48,70,100,120]
    trials = 1e5
    for pt in P
        P_error(pt, trials)
    end
end

#= This function computes the error probability for a given value for P patterns =#
#= and a given value for trials =#
function P_error(P, trials)
    N = 120

    # generate the patterns X =#
    X = generate_patterns(N, P)

    # Compute the weights W =#
    zero_dig = false
    W = hebbs_rule(X, zero_dig)

    total_errors = 0
    for t in 1:trials
        # sample a random pixle from a random pattern
        i = sample(1:N)
        = sample(1:P)

        # perform a asynchronous update
        S_i = async_update(W, X[], i)

        # check wheter the pixle changed or not
        if S_i != X[][i]
            total_errors += 1
        end
    end

    # compute P_error and print it
    total_errors /= trials
    print(total_errors, ", ")
end

#= Generates a pattern of length N, where each element is = 1 with p=1/2 and -1 otherwise =#
function generate_pattern(N)
    sample([-1, 1], N)
end

#= Generates a list of P patterns and returns it =#
function generate_patterns(N, P)
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    #= Initialize a empty list and append(push!) each pattern to it =#
    X = []
    for it in 1:P
        push!(X, generate_pattern(N))
    end

    return X
end

#= A function that computes the weights for a hopfield network using Hebb's rule =#
#= Inputs the patterns and a boolean that says wheter the diagonal should be zero or not =#
function hebbs_rule(X, zero_dig)
    P = length(X)
    N = length(X[1])
    W = zeros{Int, N, N}
    for it in 1:N
        for jt in 1:N
            for pt in 1:P
                W[it,jt] += X[pt][it] * X[pt][jt]
            end
        end
    end
    W /= N

    # if we want the diagonal to equal zero we need this extra loop
    if zero_dig
        for it in 1:N
            W[it,it] = 0
        end
    end

    return W
end

#= This function performs a asynchronous update on the pattern S at index i =#
#= using the weights W. Then returns the value, if the local field is equal =#
#= to 0, then it returns 1 =#
function async_update(W, S, i)
    N = length(S)

    #= Compute the localfield =#
    local_field = 0
    for j in 1:N
        local_field += W[i, j] * S[j]
    end

    #= Return the sign of the local field =#
    s_i = sign(local_field)
    if s_i == 0
        return 1
    else
        return s_i
    end
end

main()

```