# Dependently Typed Languages in Statix

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# My Thesis

- Followed Compiler Construction A+B from Eelco
- Open question from Eelco: How powerful is Statix?

# Background: What are Dependent Types?

Types may depend on values!

### Example

```
concat : (A: Set) \rightarrow (n m : Nat) \rightarrow Vec A n \rightarrow Vec A m \rightarrow Vec A (n + m)
```

- Proof assistants
- For example: Agda, Coq, Lean, ...

### Research Question

How suitable is Statix for defining a dependently-typed language?

- Will it be easier than doing it in Haskell?
- Defining system F was a challenge<sup>1</sup>, will it even be possible?

<sup>&</sup>lt;sup>1</sup>Hendrik van Antwerpen et al. Scopes as types.

### Why is this important?

### Spoofax perspective

Developing a language with a complex type system tests the boundaries of what Spoofax can do.

#### Dependent Types perspective

Using a language workbench helps with rapid prototyping.

## Primary Contribution: Calculus of Constructions in Statix

A lambda calculus with dependent types.

```
Example 1
(\v: Type. v) Type
```

### Example 2

```
let f = \T: Type. \x: T. x;
f (T: Type -> Type) (\y: Type. y)
```

# Type Checking

### Type checking relation

```
typeOfExpr : scope * Expr -> Expr
```

#### How do we use scopes?

A scope is used as a replacement for an environment and a context. One edge p. One relation name → NameEntry, NameEntry is either:

- NType: Stores a type (Corresponds to a context)
- NSubst: Stores a substitution (Corresponds to an environment)

### Type Checking: Requires Evaluation

### Example 1

```
let T = if false then Int else Bool end;
let b: T = true;
```

#### Evaluation relation

```
betaHeadReduce : scope * Expr -> scope * Expr
betaReduce : scope * Expr -> Expr
exectBetaEq : (scope * Expr) * (scope * Expr)
```

# Type Checking: From inference rules to Statix code

$$\frac{\langle s \mid e \rangle : t_e \qquad \langle \mathsf{sPutSubst}(s, x, (s, e)) \mid b \rangle : t_b}{\langle s \mid \mathsf{Let}(x, e, b) \rangle : t_b}$$

### Equivalent Statix code

```
typeOfExpr (s, Let(x, e, b)) = bt :-
typeOfExpr (s, e) == et,
typeOfExpr (sPutSubst (s, x, (s, e)), b) == bt
```

#### Extra contributions

#### **Features**

- 1 Implemented Inference
- 2 Implemented Inductive Data Types
- 3 Implemented Universes
- 4 Interpreter
- 6 Compiler to Clojure

#### **Evaluation**

- ① Comparison with implementation in Haskell
- 2 Comparison with implementation in LambdaPi
- 3 Evaluation of Spoofax

#### Conclusions

Spoofax is a great tool for developing dependently typed languages!

- We can use scopes to represent environments and contexts
- Statix can still use improvements