

Phenomenological aspects of the UMSSM

Jonathan Da Silva

Particle Physics group, University of Manchester, United Kingdom



Liverpool High Energy Theory seminar, University of Liverpool, February 05, 2014

G. Bélanger, JDS and A. Pukhov, JCAP 1112 (2011) 014, [[arXiv:1110.2414](https://arxiv.org/abs/1110.2414)]

JDS, PhD thesis : [[arXiv:1312.0257](https://arxiv.org/abs/1312.0257)]

G. Bélanger, JDS et al., in progress

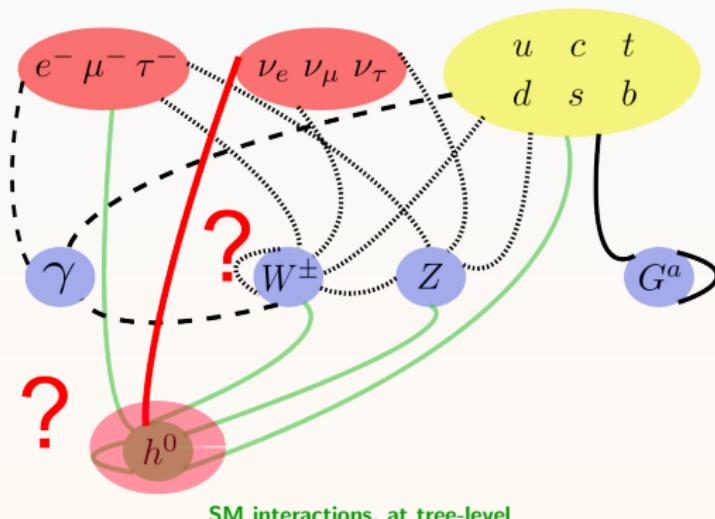
Outline

Introduction

Drawbacks of the Standard Models

* Particle Physics (SM)

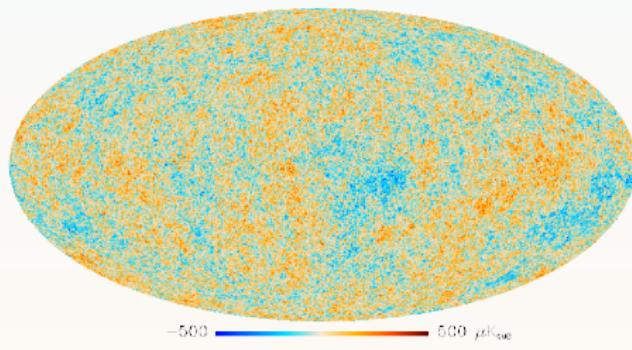
- * **Hierarchy problem** between EW (~ 100 GeV) and Planck ($\sim 10^{19}$ GeV) scales
Quadratic divergences to the Higgs boson mass squared
- * **Grand Unification (GUT)**
- * **Neutrino sector** (Dirac, Majorana ??)
- * ...



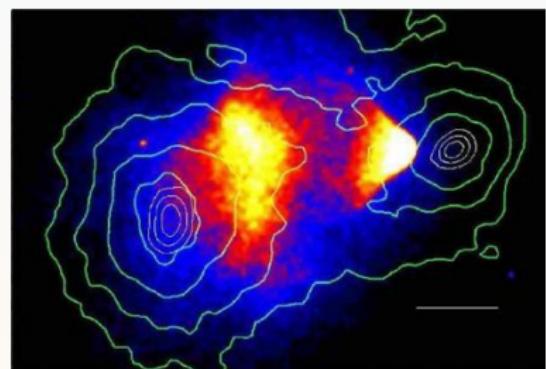
Drawbacks of the Standard Models

* Cosmology (Λ CDM)

- Simple cosmological model which fits even the most accurate measurements (Planck satellite)
- But needs **Dark Energy** and **Dark Matter** (DM, other evidence : rotation curves of galaxies, galaxy clusters, ...)



P.A.R. Ade et al., [arXiv:1303.5062]



D. Clowe et al., [astro-ph/0608407]

Drawbacks of the Standard Models

* Cosmology (Λ CDM)

- ★ Simple cosmological model which fits even the most accurate measurements (Planck satellite)
- ★ But needs **Dark Energy** and **Dark Matter** (DM, other evidence : rotation curves of galaxies, galaxy clusters, ...)
- ★ DM made of particles \neq SM particles :
 - ✗ baryons : BBN, CMB, ...
 - ✗ charged leptons : we would have seen DM (overproduction of γ , ...)
 - ✗ neutrinos : too light \Rightarrow low relic density + HDM

Drawbacks of the Standard Models

* Cosmology (Λ CDM)

- ★ Simple cosmological model which fits even the most accurate measurements (Planck satellite)
- ★ But needs **Dark Energy** and **Dark Matter** (DM, other evidence : rotation curves of galaxies, galaxy clusters, ...)
- ★ DM made of particles \neq SM particles :
 - ✗ baryons : BBN, CMB, ...
 - ✗ charged leptons : we would have seen DM (overproduction of γ , ...)
 - ✗ neutrinos : too light \Rightarrow low relic density + HDM

⇒ Example of DM candidate which gives the right abundance :
Weakly Interacting Massive Particle (WIMP)

✓ Candidates can be found beyond the Standard Model
Here : **Supersymmetry (SUSY)**

Supersymmetry

- * Fermions \Leftrightarrow bosons \Rightarrow solution to the Hierarchy problem
- * Unification at GUT scale
- * LSP/DM (supersymmetry breaking, R-Parity)

The lightest supersymmetric particle (LSP) is stable, at the GeV-TeV scale, and can be weakly charged under the SM gauge group

Supersymmetry

- * Fermions \Leftrightarrow bosons \Rightarrow solution to the Hierarchy problem
- * Unification at GUT scale
- * LSP/DM (supersymmetry breaking, R-Parity)

The lightest supersymmetric particle (LSP) is stable, at the GeV-TeV scale, and can be weakly charged under the SM gauge group

\Rightarrow DM candidates in supersymmetric models

- * Examples with the Minimal Supersymmetric Standard Model (MSSM) :

u	c	t
d	s	b
ν_{eL}	$\nu_{\mu L}$	$\nu_{\tau L}$
e	μ	τ

g	A^0
Z	$h^0 H^0$
W^\pm	h_\pm

|

$\tilde{\chi}_1^0$
$\tilde{\chi}_2^0$
$\tilde{\chi}_3^0$
$\tilde{\chi}_4^0$
$\tilde{\chi}_1^\pm$
\tilde{g}
$\tilde{\chi}_2^\pm$

\tilde{u}	\tilde{c}	\tilde{t}
\tilde{d}	\tilde{s}	\tilde{b}
$\tilde{\nu}_{eL}$	$\tilde{\nu}_{\mu L}$	$\tilde{\nu}_{\tau L}$
\tilde{e}	$\tilde{\mu}$	$\tilde{\tau}$

Drawbacks of the MSSM

* The μ -problem :

MSSM superpotential, $\mathcal{W}_{\text{MSSM}} \supset \mu H_u H_d$, μ SUSY preserving :
 natural values are $\mu = 0$ (chargino mass) or very large, e.g. $\mu \sim M_{\text{Pl}}$, but :
 minimization condition of the MSSM potential \Rightarrow

$$\sin 2\beta = \frac{2b}{m_{H_u}^2 + m_{H_d}^2 + 2|\mu|^2},$$

$$M_Z^2 = \frac{|m_{H_d}^2 - m_{H_u}^2|}{\sqrt{1 - \sin^2 2\beta}} - m_{H_u}^2 - m_{H_d}^2 - 2|\mu|^2$$

No fine-tuned cancellation to obtain the expected Z boson mass needs $b, m_{H_u}^2, m_{H_d}^2$
 and $\mu \sim (10 - 100) \times M_Z^2$:

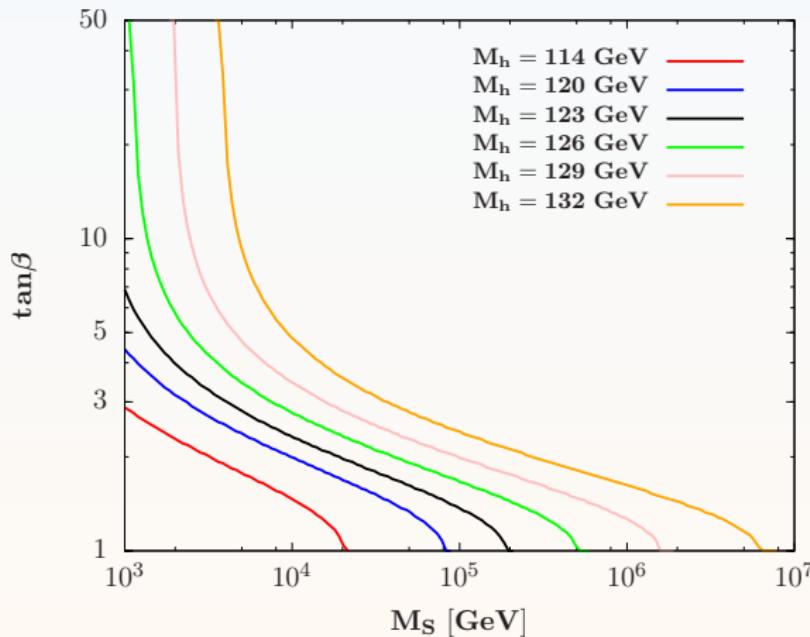
✓ SUSY breaking parameters $b, m_{H_u}^2$ and $m_{H_d}^2$

✗ μ

\Rightarrow MSSM does not account for EW scale μ term

Drawbacks of the MSSM

- * The μ -problem
- * TeV-scale values of the SUSY-breaking scale M_S :
SM-like Higgs boson mass ≈ 125 GeV + very small $\tan\beta$, i.e. $\approx 1 \Rightarrow$ tricky
 \Rightarrow Higgs boson mass of 125 GeV requires large $\tan\beta$



A. Djouadi, J. Quevillon, [[arXiv:1304.1787](https://arxiv.org/abs/1304.1787)]

Possible solutions

- ★ Generating an effective μ term thanks to a Yukawa coupling λ between H_u , H_d and a new scalar field S

$$\mathcal{W}_{\text{MSSM}} \rightarrow \mathcal{W}_{\text{MSSM}}|_{\mu=0} + \lambda S H_u H_d$$

- ★ Avoiding very small λ (new $U(1)_{\text{PQ}}$ global symmetry \rightarrow axion searches), the NMSSM looks in its simplest form like

$$\mathcal{W}_{\text{NMSSM}} = \mathcal{W}_{\text{MSSM}}|_{\mu=0} + \lambda S H_u H_d + \frac{1}{3} \kappa S^3$$

- ★ In the NMSSM (U. Ellwanger, C. Hugonie and A. M. Teixeira, [arXiv:0910.1785]), $m_h \approx 125$ GeV can be achieved with $\tan \beta \approx 2$

But NMSSM has drawbacks that can be debated ($\mathcal{W}_{\text{NMSSM}}$ invariant under a discrete \mathbb{Z}_3 symmetry \rightarrow domain walls, S. A. Abel, S. Sarkar and P. L. White, [arXiv:hep-ph/9506359])

Possible solutions

- * Generating an effective μ term thanks to a Yukawa coupling λ between H_u , H_d and a new scalar field S

$$\mathcal{W}_{\text{MSSM}} \rightarrow \mathcal{W}_{\text{MSSM}}|_{\mu=0} + \lambda S H_u H_d$$

- * Avoiding very small λ (new $U(1)_{\text{PQ}}$ global symmetry \rightarrow axion searches), the NMSSM looks in its simplest form like

$$\mathcal{W}_{\text{NMSSM}} = \mathcal{W}_{\text{MSSM}}|_{\mu=0} + \lambda S H_u H_d + \frac{1}{3} \kappa S^3$$

- * In the NMSSM (U. Ellwanger, C. Hugonie and A. M. Teixeira, [arXiv:0910.1785]), $m_h \approx 125$ GeV can be achieved with $\tan \beta \approx 2$

But NMSSM has drawbacks that can be debated ($\mathcal{W}_{\text{NMSSM}}$ invariant under a discrete \mathbb{Z}_3 symmetry \rightarrow domain walls, S. A. Abel, S. Sarkar and P. L. White, [arXiv:hep-ph/9506359])

- * Promoting the new $U(1)_{\text{PQ}}$ global symmetry to a new Abelian gauge symmetry

The model

E₆ inspired model

- ★ Models with extended gauge symmetries are well motivated within the context of Beyond the Standard model (GUT scale models, extra-dimension motivations, superstring models, strong dynamics models, little Higgs models,...)
- ★ One of the most analysed U(1) extension originates from a string-inspired E₆ grand unified gauge group ([P. Langacker and J. Wang, \[arXiv:hep-ph/9804428\]](#), [S.F. King, S. Moretti and R. Nevzorov, \[arXiv:hep-ph/0510419\]](#),...)
$$E_6 \rightarrow SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_\chi \times U(1)_\psi$$

E₆ inspired model

- ★ Models with extended gauge symmetries are well motivated within the context of Beyond the Standard model (GUT scale models, extra-dimension motivations, superstring models, strong dynamics models, little Higgs models,...)
- ★ One of the most analysed U(1) extension originates from a string-inspired E₆ grand unified gauge group ([P. Langacker and J. Wang, \[arXiv:hep-ph/9804428\]](#), [S.F. King, S. Moretti and R. Nevzorov, \[arXiv:hep-ph/0510419\]](#),...)
 $E_6 \rightarrow SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_\chi \times U(1)_\psi$
- ★ Low energy gauge symmetry considered : $SU(3)_c \times SU(2)_L \times U(1)_Y \times U'(1)$
 Coupling constants : g_3, g_2, g_Y and $g'_1 = \sqrt{\frac{5}{3}} g_Y$
- ★ U'(1) charge :

$$Q' = \cos \theta_{E_6} Q'_\chi + \sin \theta_{E_6} Q'_\psi, \quad \theta_{E_6} \in [-\pi/2, \pi/2]$$

- ★ MSSM fields + RH (s)neutrinos + new gauge boson (gaugino) + new singlet (singlino) + $\mathcal{O}(\text{TeV}) = \text{UMSSM}$

Q'_Q	Q'_u	Q'_d	Q'_L	Q'_ν	Q'_e	Q'_{H_u}	Q'_{H_d}	Q'_S
$\sqrt{40} Q'_\chi$	-1	-1	3	3	-5	-1	2	-2
$\sqrt{24} Q'_\psi$	1	1	1	1	1	-2	-2	4

Content

* Superpotential :

$$\mathcal{W}_{\text{UMSSM}} = \mathcal{W}_{\text{MSSM}}|_{\mu=0} + \lambda \mathbf{S} \mathbf{H_u} \mathbf{H_d} + \tilde{\nu}_R^* \mathbf{y}_\nu \tilde{\mathbf{L}} \mathbf{H_u} + \mathcal{O}(\text{TeV})$$

- * As the NMSSM, this model **solves the μ -problem** : $\mu = \lambda \frac{v_s}{\sqrt{2}}$
- * Higgs sector : MSSM fields + 1 singlet \Rightarrow 3 CP-even Higgs bosons $h_i, i \in \{1, 2, 3\}$
New D-terms for the SM-like Higgs boson :
 $m_{h_1}^2 \leq M_Z^2 \cos^2 2\beta + \frac{1}{2} \lambda^2 v^2 \sin^2 2\beta + g_1'^2 v^2 (Q'_{H_d} \cos^2 \beta + Q'_{H_u} \sin^2 \beta)^2 + \Delta m_h^2$
- * Gauge sector : Physical abelian gauge bosons : Z_1 and Z_2 , mixing between the Z of the SM and the Z' , α_Z is the mixing angle $\Rightarrow \tan \beta$ constrained

$$\begin{aligned} Z_1 &= \cos \alpha_Z Z + \sin \alpha_Z Z', \\ Z_2 &= -\sin \alpha_Z Z + \cos \alpha_Z Z', \end{aligned}$$

- * Gauginos sector : 6 neutralinos in the basis $(\tilde{B}, \tilde{W}^3, \tilde{H}_d^0, \tilde{H}_u^0, \tilde{S}, \tilde{B}')$

Content

* To sum up :

u	c	t
d	s	b

ν_{eL}	$\nu_{\mu L}$	$\nu_{\tau L}$
e	μ	τ



g	A^0
Z_1	$h_{1,2}$
W^\pm	h_\pm



$\tilde{\chi}_1^0$	$\tilde{\chi}_1^\pm$
$\tilde{\chi}_2^0$	\tilde{g}
$\tilde{\chi}_3^0$	$\tilde{\chi}_2^\pm$
$\tilde{\chi}_4^0$	



\tilde{u}	\tilde{c}	\tilde{t}
\tilde{d}	\tilde{s}	\tilde{b}

$\widetilde{\nu_{eL}}$	$\widetilde{\nu_{\mu L}}$	$\widetilde{\nu_{\tau L}}$
\widetilde{e}	$\widetilde{\mu}$	$\widetilde{\tau}$



Content

* To sum up :

u	c	t
d	s	b

ν_{eL}	$\nu_{\mu L}$	$\nu_{\tau L}$
e	μ	τ



g	A^0
Z_1	$h_{1,2}$
W^\pm	h_\pm



$\tilde{\chi}_1^0$	$\tilde{\chi}_1^\pm$
$\tilde{\chi}_2^0$	\tilde{g}
$\tilde{\chi}_3^0$	$\tilde{\chi}_2^\pm$
$\tilde{\chi}_4^0$	



\tilde{u}	\tilde{c}	\tilde{t}
\tilde{d}	\tilde{s}	\tilde{b}

$\widetilde{\nu_{eL}}$	$\widetilde{\nu_{\mu L}}$	$\widetilde{\nu_{\tau L}}$
\widetilde{e}	$\widetilde{\mu}$	$\widetilde{\tau}$



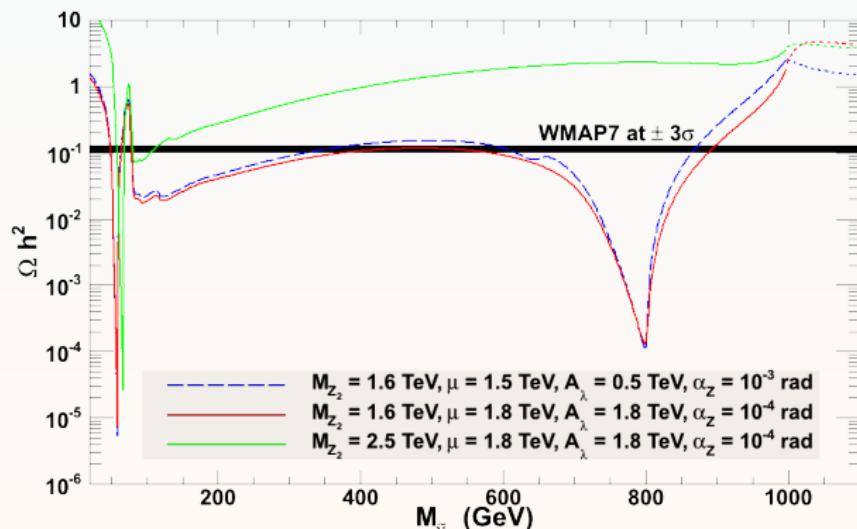
* Right-Handed (RH) sneutrinos : are they viable DM candidates ?

RH sneutrino DM candidate

WIMP annihilation

Parameter space regions with $\Omega_{\text{WIMP}} h^2 \approx 0.1 \Rightarrow$ need to increase the annihilation cross section : interesting WIMP mass from 50 GeV to TeV-scale :

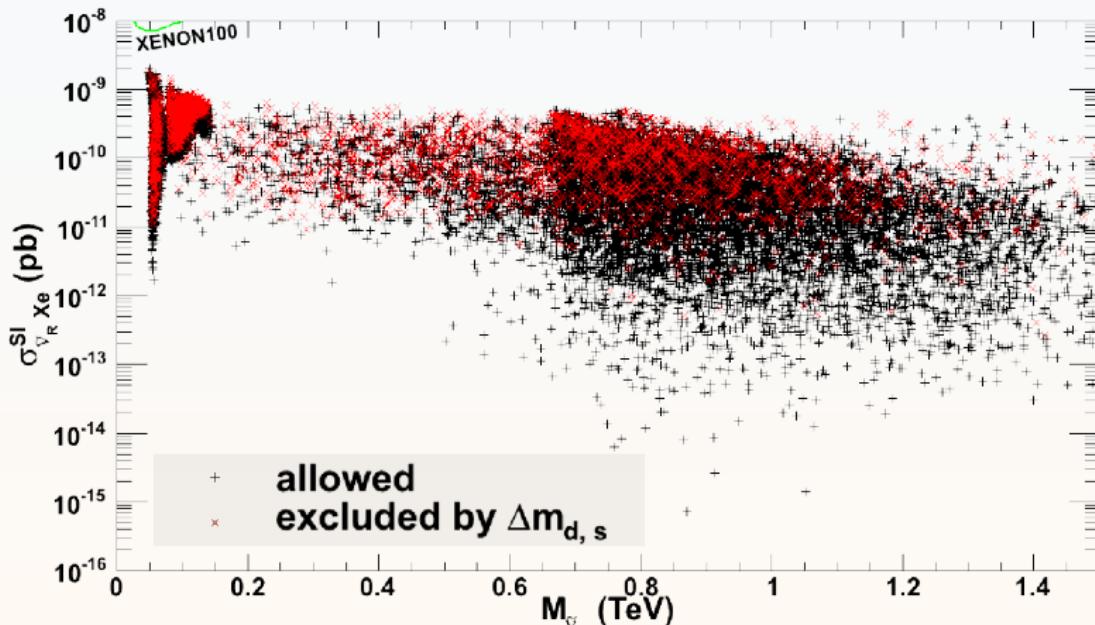
- * WIMP mass near $m_{h_1}/2$
- * WIMP mass near $M_{Z_2}/2$ (also $m_{h_1}/2$)
- * WIMP mass near $m_{h_1}/2$ or above W pair threshold
- * Coannihilation processes (mainly higgsino-like)



Scattering on nucleons

For some $U'(1)$ models we can have a good suppression of the gauge boson or/and Higgs boson contribution

here $U(1)_\psi \Rightarrow \theta_{E_6} = \pi/2$

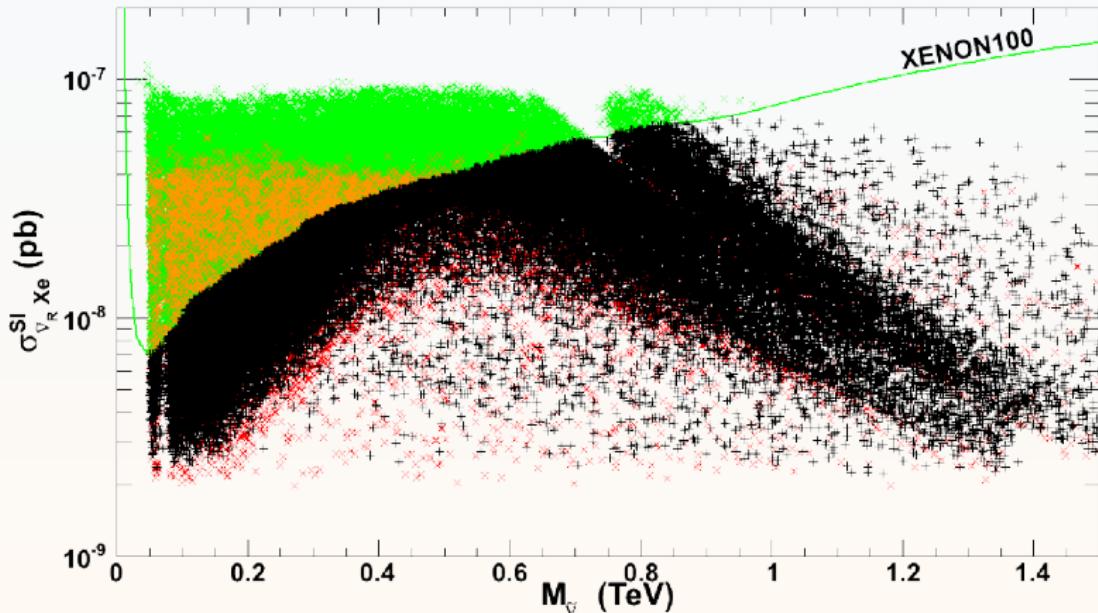


Scattering on nucleons

For other models, huge constraints on the parameter space appear

here $U(1)_\eta \rightarrow \tan \theta_{E_6} = -\sqrt{5}/3$

OK, $\Delta m_{d,s}$, XENON100, both

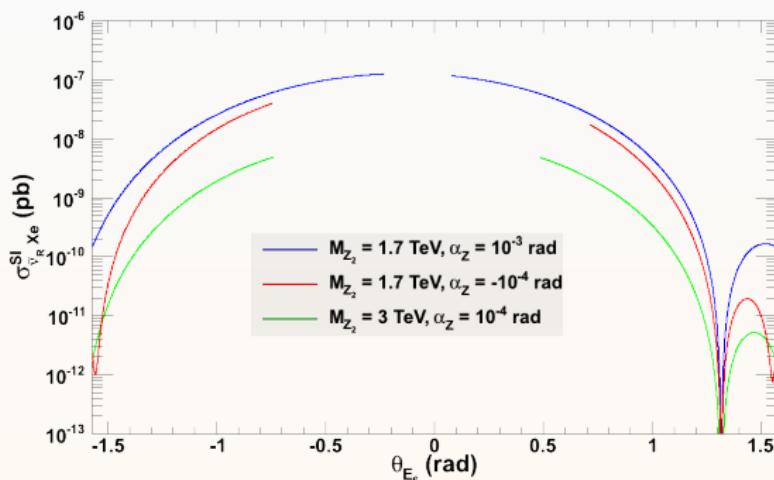


Scattering on nucleons

Abelian gauge boson contribution to direct detection cross section :

$$\sigma_{\tilde{\nu}_R N}^{Z_1, Z_2} = \frac{\mu_{\tilde{\nu}_R N}^2}{\pi} (g'_1 Q'_\nu)^2 [(y(1 - 4s_W^2) + y')Z + (-y + 2y')(\mathbf{A} - \mathbf{Z})]^2$$

$$\text{with } y = \frac{g_Y \sin \alpha_Z \cos \alpha_Z}{4 \sin \theta_W} \left(\frac{1}{M_{Z_2}^2} - \frac{1}{M_{Z_1}^2} \right), \quad y' = -\frac{g'_1 Q'_V^d}{2} \left(\frac{\sin^2 \alpha_Z}{M_{Z_1}^2} + \frac{\cos^2 \alpha_Z}{M_{Z_2}^2} \right)$$

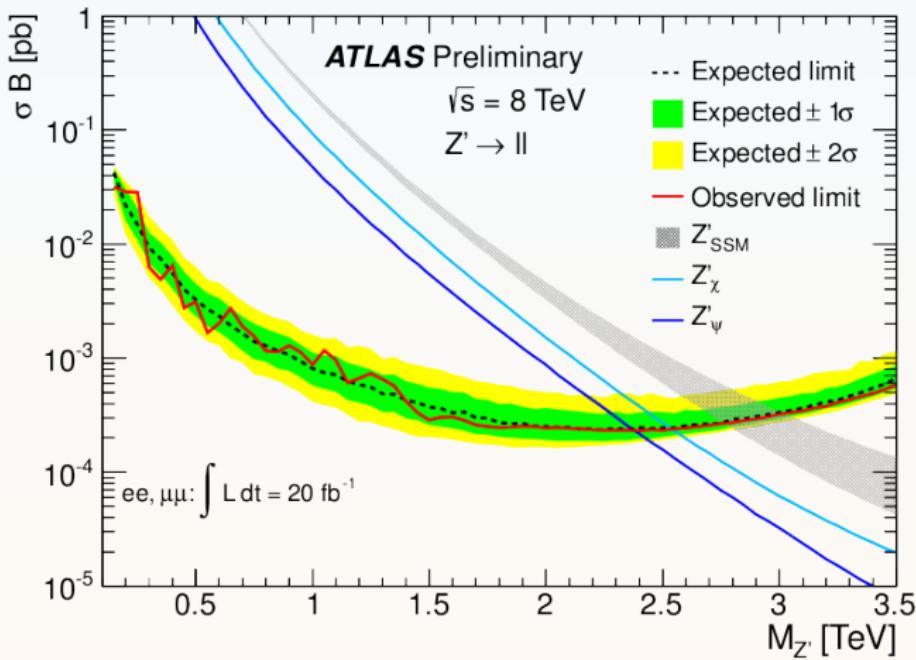


⇒ stringent constraints for small $|\theta_{E_6}|$ because of Q_V^d term

Low $\tan \beta$ region

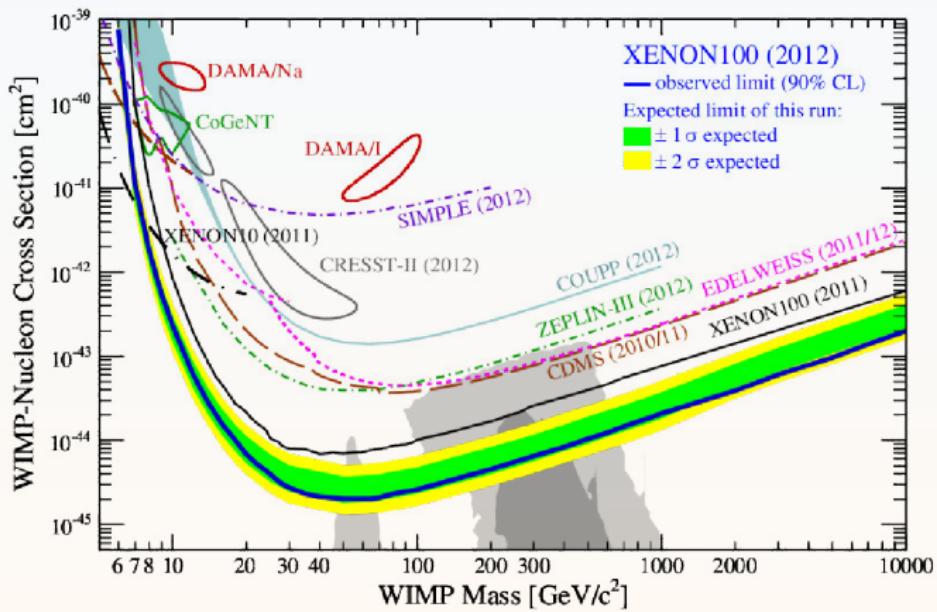
Constraints - Z'

- * Z' heavy \Rightarrow heavy singlet-like Higgs boson $\Rightarrow h_2$ mostly doublet-like



Constraints - DM

- ★ DM observables for either neutralino or RH sneutrino DM candidate :
- ★ $\Omega_{\text{LSP}} h^2 < 0.1221$ (2σ Planck+WP+highL+BAO upper bound)
- ★ SI WIMP-nucleon cross section limits from XENON100 (a posteriori)



E. Aprile et al., XENON100 Collaboration, [arXiv:1207.5988]

Constraints - Higgs + low energy observables

- ★ Theoretical uncertainties (see **B. C. Allanach, A. Djouadi, J. L. Kneur, W. Porod, P. Slavich, [arXiv:hep-ph/0406166]**)
 $\rightarrow m_{h_1} \in [120.63, 130.63] \text{ GeV}$
- ★ Higgs boson signal strengths and low energy observables (a posteriori)
 \Rightarrow Modification of the NMSSMTools code : [UMSSMTools](#)
 Limits on signal strengths using **G. Bélanger, B. Dumont, U. Ellwanger, J. F. Gunion, S. Kraml, [arXiv:1306.2941]** : $\chi^2_i \lesssim 6$ with $h_1 \rightarrow i, \quad i \in \gamma\gamma, VV^*, b\bar{b}, \tau^+\tau^-$

Observable	Value
$\mathcal{B}(B^\pm \rightarrow \tau^\pm \nu_\tau)$	$(0.99 \pm 0.25) \times 10^{-4}$ UTfit
$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$	$(2.95^{+0.74}_{-0.67}) \times 10^{-9}$ LHCb + CMS
ΔM_s	$17.719 \pm 0.043 \text{ ps}^{-1}$ HFAG
ΔM_d	$0.507 \pm 0.004 \text{ ps}^{-1}$ HFAG
$\mathcal{B}(\bar{B}^0 \rightarrow X_s \gamma)$	$(3.55 \pm 0.24 \pm 0.09) \times 10^{-4}$ HFAG

Scan

Scanning the parameter space :

- ★ Nuisance parameters :

- ★ $m_t = 175.5 \pm 1$ GeV PDG 2012

- ★ Quark content of the nucleon (from G. Bélanger, F. Boudjema, A. Pukhov, A. Semenov, [arXiv:1305.0237])

Parameter	Value
m_u/m_d	0.46 ± 0.05
m_s/m_d	27.5 ± 0.3
$\sigma_{\pi N}$	34 ± 2 MeV
σ_s	42 ± 5 MeV

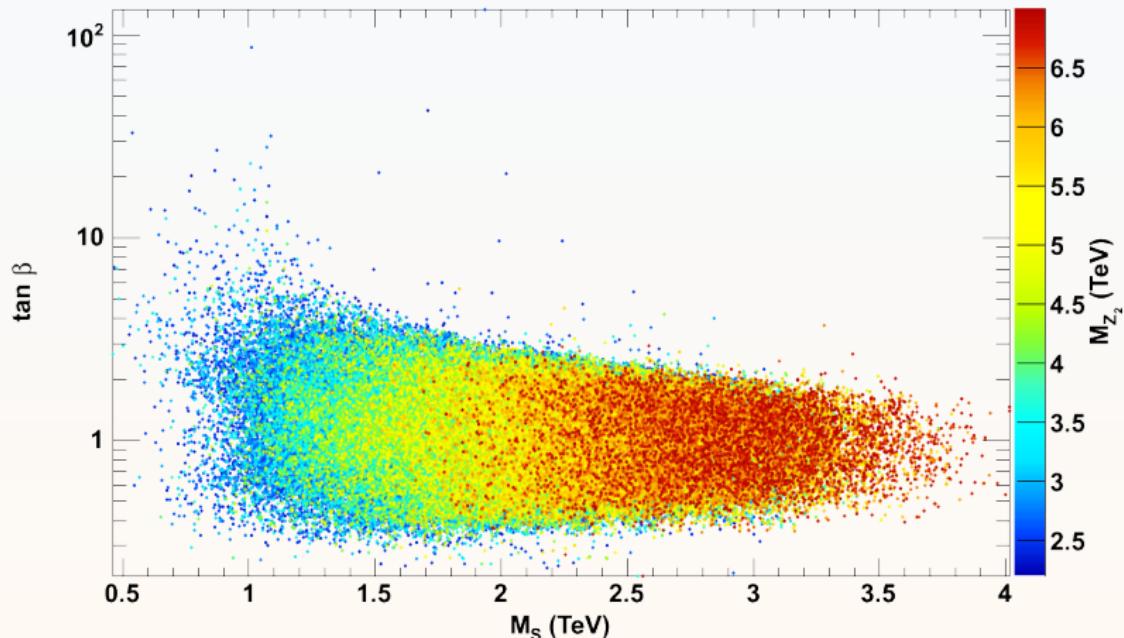
- ★ UMSSM parameters :

Parameter	Range	Parameter	Range
$m_{\tilde{\nu}_R}$	[0.05, 2] TeV	A_λ	[0, 4] TeV
M_{Z_2}	[2.2, 7] TeV	A_t, A_b, A_τ	[-4, 4] TeV
α_Z	$[-10^{-3}, 10^{-3}]$ rad	$m_{\tilde{Q}_3}, m_{\tilde{u}_3}, m_{\tilde{d}_3}, m_{\tilde{L}_3}, m_{\tilde{e}_3}$	[0, 3] TeV
θ_{E_6}	$[-\pi/2, \pi/2]$ rad	μ, M_1, M'_1	[0.1, 2] TeV

First and second generation sfermion soft mass terms at 3 TeV

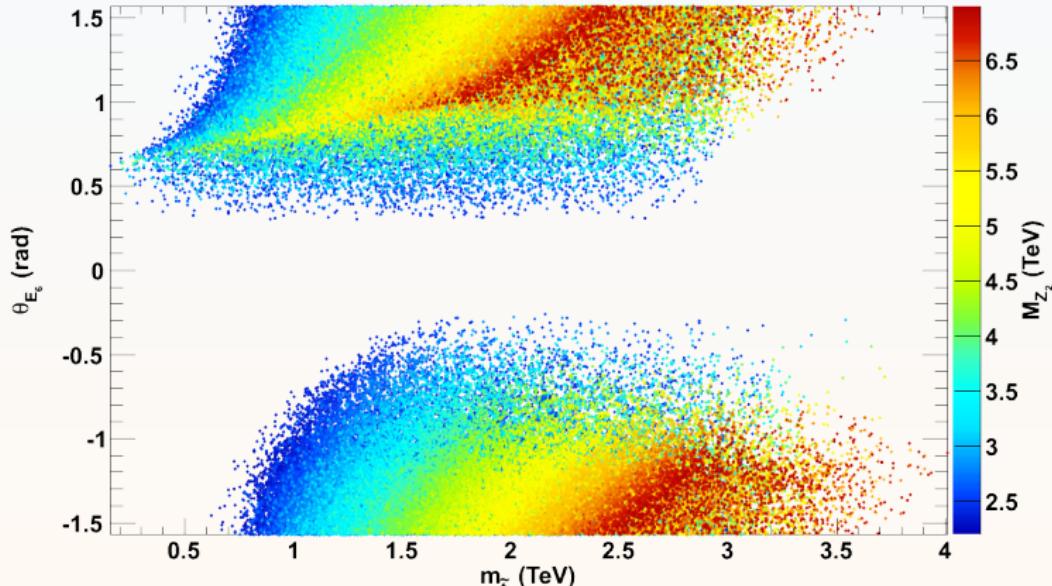
$\tan \beta$

- * $\tan \beta \approx 1 + \text{TeV-scale } M_S \Rightarrow \text{expected } m_{h_1} :$
large contribution from pure UMSSM as well as one-loop stop terms



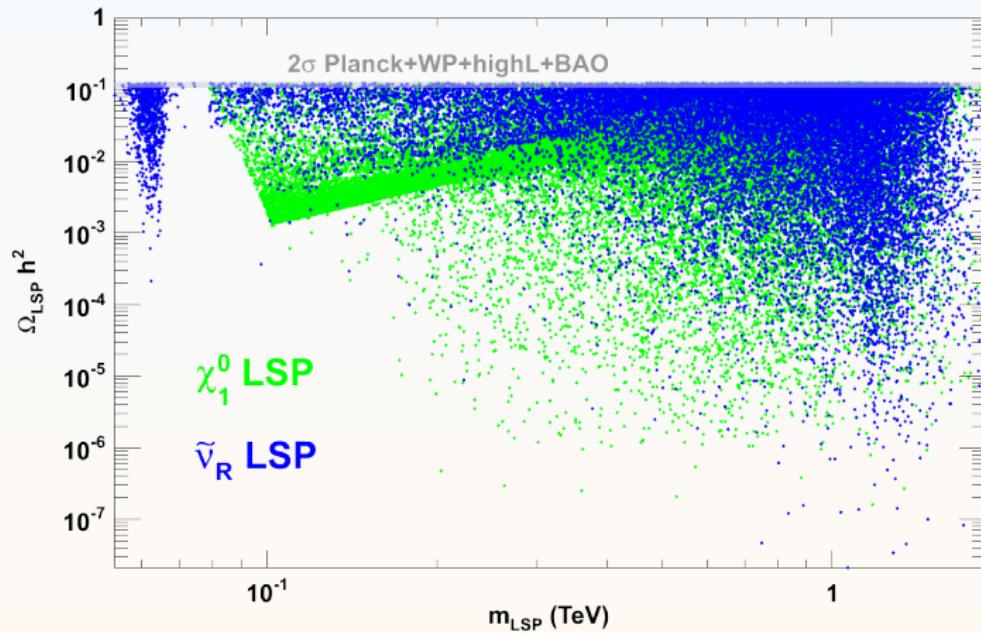
Sfermion masses

- Important UMSSM contribution to sfermion masses (dependent on θ_{E_6}) :
- $$\Delta_f = \frac{1}{2} g_1'^2 Q'_f (Q'_{H_d} v_d^2 + Q'_{H_u} v_u^2 + Q'_S v_s^2)$$
- \Rightarrow Condition on neutral LSP put strong constraints on θ_{E_6}



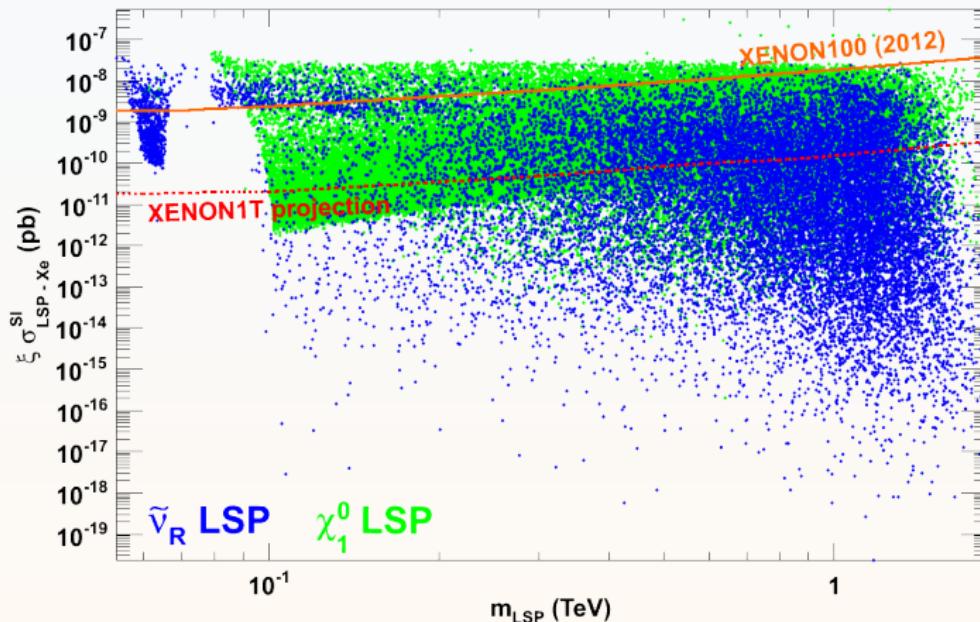
LSP abundance

★ \widetilde{B} , \widetilde{H} and $\widetilde{\nu}_R$ LSP with the experimentally allowed abundance



Direct detection

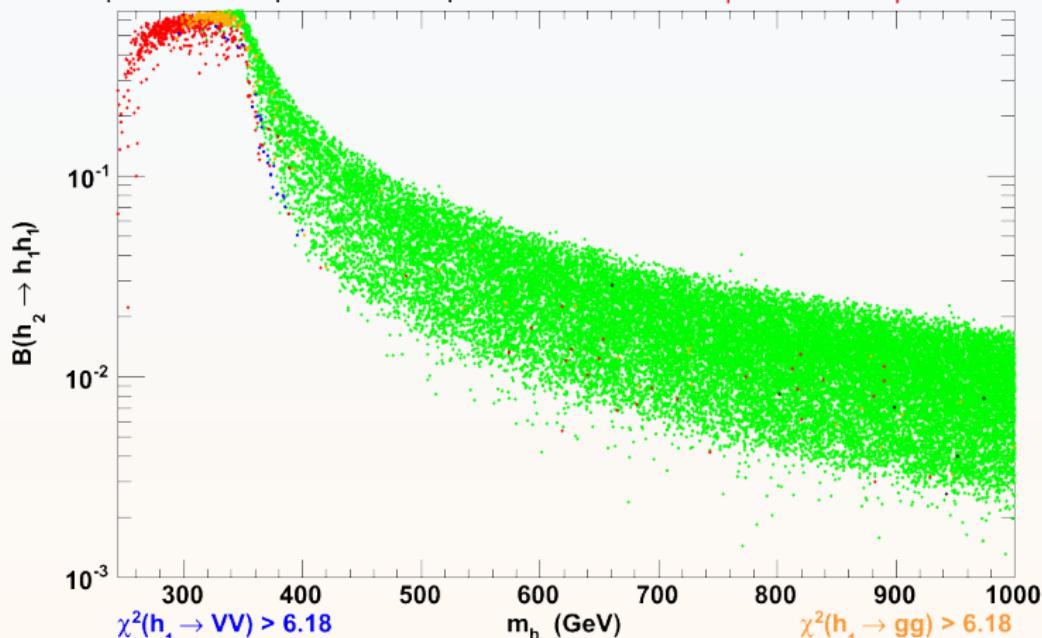
- \tilde{B} , \tilde{H} and $\tilde{\nu}_R$ LSP with the wanted abundance
- DM direct detection experiments can probe entirely some regions, especially for $\tilde{\nu}_R$ LSP



h_1 signal strength and h_2 bounds

- * h_1 signal strength mostly compatible with current limits, but also useful to exclude "light" h_2 ($\lesssim 300$ GeV); large branching ratio into SM-like Higgs boson for such h_2

$$\chi^2(h_1 \rightarrow gg) \& \chi^2(h_1 \rightarrow VV) \& \chi^2(h_1 \rightarrow \tau\tau) > 6.18 \quad \chi^2(h_1 \rightarrow gg) \& \chi^2(h_1 \rightarrow VV) > 6.18$$



Conclusions

Conclusions

- ★ RH sneutrinos are viable DM candidates in the UMSSM
- ★ New D-terms in the UMSSM \Rightarrow low $\tan\beta$ values still allowed for TeV-scale M_S
 \Rightarrow sfermion sector impacted
- ★ χ_1^0 or $\tilde{\nu}_R$ LSP that does not overclose the Universe exclude a large region of the parameter space
- ★ Viable or excluded regions depend strongly on θ_{E_6}
- ★ XENON1T would probe entirely some scenarios
- ★ Study of the SM-like Higgs boson puts bounds on the second CP-even Higgs boson :
 $m_{h_2} \lesssim 300$ GeV excluded in the UMSSM

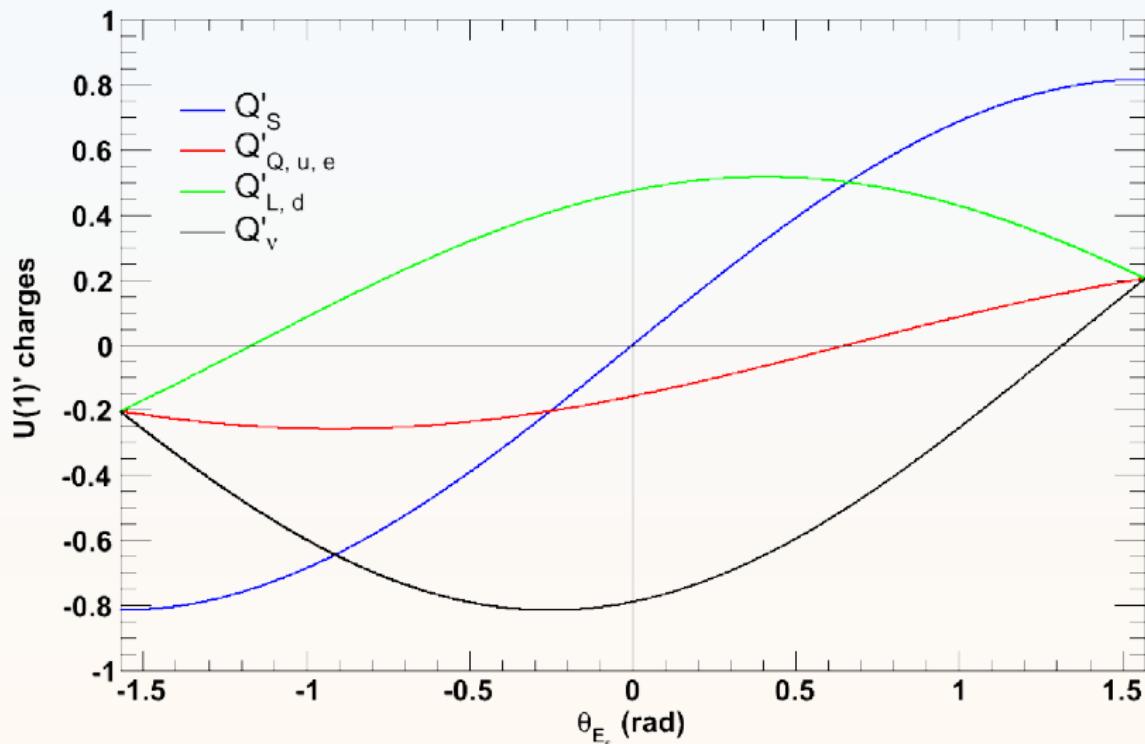
Conclusions

- ★ RH sneutrinos are viable DM candidates in the UMSSM
- ★ New D-terms in the UMSSM \Rightarrow low $\tan\beta$ values still allowed for TeV-scale M_S
 \Rightarrow sfermion sector impacted
- ★ χ_1^0 or $\tilde{\nu}_R$ LSP that does not overclose the Universe exclude a large region of the parameter space
- ★ Viable or excluded regions depend strongly on θ_{E_6}
- ★ XENON1T would probe entirely some scenarios
- ★ Study of the SM-like Higgs boson puts bounds on the second CP-even Higgs boson :
 $m_{h_2} \lesssim 300$ GeV excluded in the UMSSM

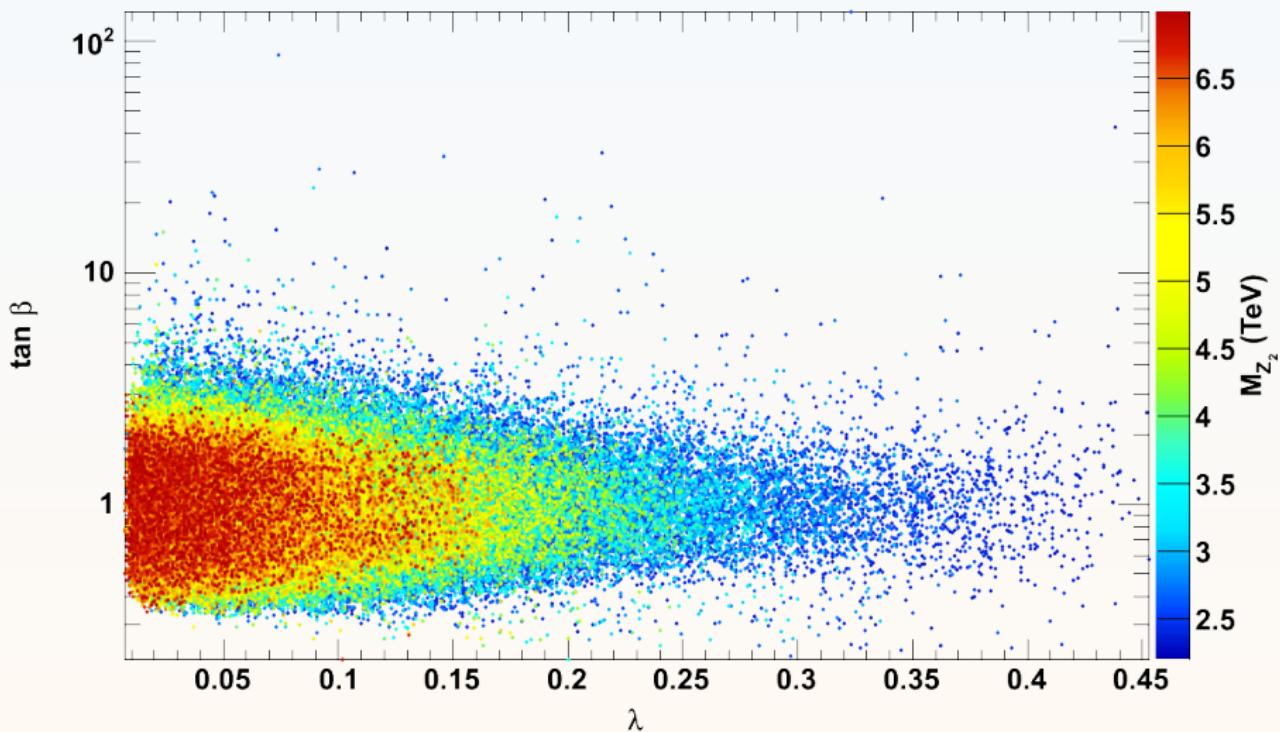
Thanks for your attention !

BACKUP

BACKUP



BACKUP



BACKUP

New contribution from the Z' to $\Delta\rho$: $\Delta\rho < 2 \times 10^{-3} \rightarrow -6.5 \times 10^{-4} \lesssim \alpha_Z \lesssim 6.9 \times 10^{-4}$

