104

Tangent Line Exercises (With SOLUTIONS!)

Jonathan D. Doane Calc. 1

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Preview

101.
$$2\cos(x)$$
 at $x_1 = -\frac{\pi}{3}$

102.
$$x-2$$
 at $x_1 = 1$

103.
$$\sin(x)$$
 at $x_1 = \pi$

104.
$$-6\tan(x)$$
 at $x_1 = \frac{\pi}{6}$

| n. | f(x) | x_1 | y_1 | f'(x) | m | tangent line |
|------|-------------|------------------|--------------|---------------|------------|--|
| 101. | $2\cos(x)$ | $-\frac{\pi}{3}$ | 1 | $-2\sin(x)$ | $\sqrt{3}$ | $y = \sqrt{3}\left(x + \frac{\pi}{3}\right) + 1$ |
| 102. | x-2 | 1 | -1 | 1 | 1 | y = x - 2 |
| 103. | $\sin(x)$ | π | 0 | $\cos(x)$ | -1 | $y = \pi - x$ |
| 104. | $-6\tan(x)$ | $\frac{\pi}{6}$ | $-2\sqrt{3}$ | $-6\sec^2(x)$ | -8 | $y = -8x - 2\sqrt{3} + \frac{4\pi}{3}$ |

Find the equation of the tangent line for each of the following:

1.
$$-2\sin(x)$$
 at $x_1 = -\frac{\pi}{6}$

2.
$$x + 4$$
 at $x_1 = -2$

3.
$$\frac{1}{(x+8)^2}$$
 at $x_1 = -7$

4.
$$-2\tan(x)$$
 at $x_1 = -\frac{2\pi}{3}$

5.
$$-\sin(x)$$
 at $x_1 = -\frac{\pi}{3}$

6.
$$-4\tan(x)$$
 at $x_1 = -\frac{\pi}{3}$

7.
$$\tan(x)$$
 at $x_1 = -\pi$

8.
$$\frac{1}{(x+9)^2}$$
 at $x_1 = -7$

9.
$$\frac{1}{x+5}$$
 at $x_1 = -4$

10.
$$-2\sin(x)$$
 at $x_1 = \frac{\pi}{6}$

11.
$$\frac{1}{(x+3)^2}$$
 at $x_1 = -2$

12.
$$(x+3)^2$$
 at $x_1 = -1$

13.
$$\frac{1}{x+1}$$
 at $x_1 = 0$

14.
$$x-8$$
 at $x_1 = 9$

15.
$$-\sin(x)$$
 at $x_1 = -\frac{3\pi}{4}$

16.
$$-2\cos(x)$$
 at $x_1 = -\frac{\pi}{6}$

17.
$$\sin(x)$$
 at $x_1 = -\frac{2\pi}{3}$

18.
$$\frac{1}{x+5}$$
 at $x_1 = -3$

19.
$$2\sin(x)$$
 at $x_1 = \frac{\pi}{3}$

20.
$$(x+5)^2$$
 at $x_1 = -6$

- **21.** $-2\cos(x)$ at $x_1 = -\frac{\pi}{4}$
- **22.** $-\cos(x)$ at $x_1 = \frac{\pi}{6}$
- 23. $\frac{1}{x+8}$ at $x_1 = -7$
- **24.** $-2\tan(x)$ at $x_1 = \frac{2\pi}{3}$
- **25.** x-2 at $x_1 = 3$
- **26.** $-9\tan(x)$ at $x_1 = 0$
- **27.** $2\tan(x)$ at $x_1 = \frac{\pi}{3}$
- **28.** $\sin(x)$ at $x_1 = 2\pi$
- **29.** $\sin(x)$ at $x_1 = \frac{\pi}{6}$
- **30.** x + 9 at $x_1 = -10$
- **31.** $\cos(x)$ at $x_1 = \frac{\pi}{2}$
- 32. $\frac{1}{x+3}$ at $x_1 = -4$
- **33.** $(x+6)^2$ at $x_1 = -5$
- **34.** $-7\tan(x)$ at $x_1 = \frac{\pi}{3}$
- **35.** $2\cos(x)$ at $x_1 = \frac{\pi}{2}$
- **36.** $-7\tan(x)$ at $x_1 = -\frac{\pi}{6}$
- 37. $(x+2)^2$ at $x_1 = -3$
- **38.** $2\cos(x)$ at $x_1 = -\frac{\pi}{6}$
- **39.** x-2 at $x_1 = 3$
- **40.** $\frac{1}{x+8}$ at $x_1 = -9$

- $(x-7)^2$ at $x_1 = 6$ **41**.
- $5 \tan{(x)}$ at $x_1 = -\frac{\pi}{3}$ **42**.
- $\frac{1}{(x+1)^2} \qquad \text{at } x_1 = -2$ **43**.
- $\sin(x)$ at $x_1 = -\frac{\pi}{2}$ 44.
- at $x_1 = \frac{2\pi}{3}$ **45**. $\sin(x)$
- $-\cos(x)$ at $x_1 = \frac{\pi}{4}$ **46**.
- $\frac{1}{x+6}$ **47.** at $x_1 = -5$
- $(x+8)^2$ at $x_1 =$ 48. -6
- $(x-2)^2 \qquad \text{at } x_1 =$ 49. 3
- 50. $-2\cos(x)$ at $x_1 =$ 0
- $-4\tan(x)$ at $x_1 =$ 51.
- **52**. $-\sin(x)$ at $x_1 =$ 2π
- **53**. $\sin(x)$ at $x_1 =$
- $\frac{1}{r-4}$
- 6 **54.** at $x_1 =$

55.

56. x - 5 at $x_1 =$ 6

 $-\cos(x)$ at $x_1 = -\frac{\pi}{4}$

- $-2\cos(x)$ 57. at $x_1 =$ π
- $\sin(x)$ at $x_1 =$ **58.**
- $2\cos(x)$ at $x_1 =$ 59.
- x 7 at $x_1 =$ 60. 8

61.
$$\frac{1}{x-2}$$
 at $x_1 = 3$

62.
$$\frac{1}{x+9}$$
 at $x_1 = -8$

63.
$$\cos(x)$$
 at $x_1 =$

64.
$$-2\sin(x)$$
 at $x_1 =$

65.
$$\frac{1}{x-1}$$
 at $x_1 = 3$

66.
$$-\sin(x)$$
 at $x_1 = \frac{2\pi}{3}$

67.
$$-2\cos(x)$$
 at $x_1 = 2\pi$

68.
$$-2\cos(x)$$
 at $x_1 = \frac{\pi}{4}$

69.
$$-3\tan(x)$$
 at $x_1 = -\frac{2\pi}{3}$

70.
$$\sin(x)$$
 at $x_1 = -\frac{\pi}{2}$

71.
$$\sin(x)$$
 at $x_1 = \frac{3\pi}{4}$

72.
$$(x-9)^2$$
 at $x_1 = 8$

73.
$$\sin(x)$$
 at $x_1 = -\frac{\pi}{6}$

74.
$$x + 7$$
 at $x_1 = -5$

75.
$$x-4$$
 at $x_1 = 6$

76.
$$\sin(x)$$
 at $x_1 = -\frac{\pi}{2}$

77.
$$-\sin(x)$$
 at $x_1 = -\frac{\pi}{6}$

78.
$$\frac{1}{(x-1)^2}$$
 at $x_1 = 2$

79.
$$\frac{1}{x-10}$$
 at $x_1 = 12$

80.
$$2\cos(x)$$
 at $x_1 = -\frac{\pi}{6}$

81.
$$2\tan(x)$$
 at $x_1 = \frac{2x}{3}$

82.
$$-8\tan(x)$$
 at $x_1 = 0$

83.
$$2\sin(x)$$
 at $x_1 = \frac{3\pi}{4}$

84.
$$(x+8)^2$$
 at $x_1 = -9$

85.
$$-2\sin(x)$$
 at $x_1 = -\frac{\pi}{6}$

86.
$$6 \tan(x)$$
 at $x_1 = \pi$

87.
$$x + 8$$
 at $x_1 = -7$

88.
$$2\cos(x)$$
 at $x_1 = \pi$

89.
$$\frac{1}{x+7}$$
 at $x_1 = -6$

90.
$$\cos(x)$$
 at $x_1 = -\pi$

91.
$$-2\cos(x)$$
 at $x_1 = 2\pi$

92.
$$\frac{1}{(x+6)^2}$$
 at $x_1 = -7$

92.
$$\frac{(x+6)^2}{(x+6)^2}$$
 at $x_1 = -x$

 $7\tan(x) \qquad \text{at } x_1 = -2\pi$

93.

94.
$$\frac{1}{(x-4)^2}$$
 at $x_1 = 5$

95.
$$\cos(x)$$
 at $x_1 = -\frac{\pi}{4}$

96.
$$3\tan(x)$$
 at $x_1 = \frac{2\pi}{3}$

97.
$$\frac{1}{x-4}$$
 at $x_1 = 3$

98.
$$2\cos(x)$$
 at $x_1 = \frac{2}{5}$

99.
$$2\sin(x)$$
 at $x_1 = \frac{37}{4}$

100.
$$2\cos(x)$$
 at $x_1 = -\frac{\pi}{3}$

- **101.** $2\cos(x)$ at $x_1 = -\frac{\pi}{3}$
- **102.** x-2 at $x_1 = 1$
- **103.** $\sin(x)$ at $x_1 = \pi$
- **104.** $-6\tan(x)$ at $x_1 = \frac{\pi}{6}$

Solutions

| n. | f(x) | x_1 | y_1 | f'(x) | m | tangent line |
|-----|---------------------|-------------------|-----------------------|----------------------|----------------------|--|
| 1. | $-2\sin(x)$ | $-\frac{\pi}{6}$ | 1 | $-2\cos(x)$ | $-\sqrt{3}$ | $y = -\sqrt{3}\left(x + \frac{\pi}{6}\right) + 1$ |
| 2. | x + 4 | -2 | 2 | 1 | 1 | y = x + 4 |
| 3. | $\frac{1}{(x+8)^2}$ | -7 | 1 | $-\frac{2}{(x+8)^3}$ | -2 | y = -2x - 13 |
| 4. | $-2\tan(x)$ | $-\frac{2\pi}{3}$ | $-2\sqrt{3}$ | $-2\sec^2(x)$ | -8 | $y = -8x - \frac{16\pi}{3} - 2\sqrt{3}$ |
| 5. | $-\sin(x)$ | $-\frac{\pi}{3}$ | $\frac{\sqrt{3}}{2}$ | $-\cos(x)$ | $-\frac{1}{2}$ | $y = -\frac{x}{2} - \frac{\pi}{6} + \frac{\sqrt{3}}{2}$ |
| 6. | $-4\tan(x)$ | $-\frac{\pi}{3}$ | $4\sqrt{3}$ | $-4\sec^2(x)$ | -16 | $y = -16x - \frac{16\pi}{3} + 4\sqrt{3}$ |
| 7. | $\tan(x)$ | $-\pi$ | 0 | $\sec^2(x)$ | 1 | $y = x + \pi$ |
| 8. | $\frac{1}{(x+9)^2}$ | -7 | $\frac{1}{4}$ | $-\frac{2}{(x+9)^3}$ | $-\frac{1}{4}$ | $y = -\frac{x}{4} - \frac{3}{2}$ |
| 9. | $\frac{1}{x+5}$ | -4 | 1 | $-\frac{1}{(x+5)^2}$ | -1 | y = -x - 3 |
| 10. | $-2\sin(x)$ | $\frac{\pi}{6}$ | -1 | $-2\cos(x)$ | $-\sqrt{3}$ | $y = -\sqrt{3}\left(x - \frac{\pi}{6}\right) - 1$ |
| 11. | $\frac{1}{(x+3)^2}$ | -2 | 1 | $-\frac{2}{(x+3)^3}$ | -2 | y = -2x - 3 |
| 12. | $(x+3)^2$ | -1 | 4 | 2x + 6 | 4 | y = 4x + 8 |
| 13. | $\frac{1}{x+1}$ | 0 | 1 | $-\frac{1}{(x+1)^2}$ | -1 | y = 1 - x |
| 14. | x - 8 | 9 | 1 | 1 | 1 | y = x - 8 |
| 15. | $-\sin(x)$ | $-\frac{3\pi}{4}$ | $\frac{\sqrt{2}}{2}$ | $-\cos(x)$ | $\frac{\sqrt{2}}{2}$ | $y = \frac{\sqrt{2}\left(x + \frac{3\pi}{4}\right)}{2} + \frac{\sqrt{2}}{2}$ |
| 16. | $-2\cos(x)$ | $-\frac{\pi}{6}$ | $-\sqrt{3}$ | $2\sin(x)$ | -1 | $y = -x - \sqrt{3} - \frac{\pi}{6}$ |
| 17. | $\sin(x)$ | $-\frac{2\pi}{3}$ | $-\frac{\sqrt{3}}{2}$ | $\cos(x)$ | $-\frac{1}{2}$ | $y = -\frac{x}{2} - \frac{\pi}{3} - \frac{\sqrt{3}}{2}$ |
| 18. | $\frac{1}{x+5}$ | -3 | $\frac{1}{2}$ | $-\frac{1}{(x+5)^2}$ | $-\frac{1}{4}$ | $y = -\frac{x}{4} - \frac{1}{4}$ |
| 19. | $2\sin(x)$ | $\frac{\pi}{3}$ | $\sqrt{3}$ | $2\cos(x)$ | 1 | $y = x - \frac{\pi}{3} + \sqrt{3}$ |
| 20. | $(x+5)^2$ | -6 | 1 | 2x + 10 | -2 | y = -2x - 11 |

| n. | f(x) | x_1 | y_1 | f'(x) | m | tangent line |
|-----|-----------------|------------------|-----------------------|----------------------|----------------------|--|
| 21. | $-2\cos(x)$ | $-\frac{\pi}{4}$ | $-\sqrt{2}$ | $2\sin(x)$ | $-\sqrt{2}$ | $y = -\sqrt{2}\left(x + \frac{\pi}{4}\right) - \sqrt{2}$ |
| 22. | $-\cos(x)$ | $\frac{\pi}{6}$ | $-\frac{\sqrt{3}}{2}$ | $\sin(x)$ | $\frac{1}{2}$ | $y = \frac{x}{2} - \frac{\sqrt{3}}{2} - \frac{\pi}{12}$ |
| 23. | $\frac{1}{x+8}$ | -7 | 1 | $-\frac{1}{(x+8)^2}$ | -1 | y = -x - 6 |
| 24. | $-2\tan(x)$ | $\frac{2\pi}{3}$ | $2\sqrt{3}$ | $-2\sec^2(x)$ | -8 | $y = -8x + 2\sqrt{3} + \frac{16\pi}{3}$ |
| 25. | x-2 | 3 | 1 | 1 | 1 | y = x - 2 |
| 26. | $-9\tan(x)$ | 0 | 0 | $-9\sec^2(x)$ | -9 | y = -9x |
| 27. | $2\tan(x)$ | $\frac{\pi}{3}$ | $2\sqrt{3}$ | $2\sec^2(x)$ | 8 | $y = 8x - \frac{8\pi}{3} + 2\sqrt{3}$ |
| 28. | $\sin(x)$ | 2π | 0 | $\cos(x)$ | 1 | $y = x - 2\pi$ |
| 29. | $\sin(x)$ | $\frac{\pi}{6}$ | $\frac{1}{2}$ | $\cos(x)$ | $\frac{\sqrt{3}}{2}$ | $y = \frac{\sqrt{3}(x - \frac{\pi}{6})}{2} + \frac{1}{2}$ |
| 30. | x + 9 | -10 | -1 | 1 | 1 | y = x + 9 |
| 31. | $\cos(x)$ | $\frac{\pi}{2}$ | 0 | $-\sin(x)$ | -1 | $y = -x + \frac{\pi}{2}$ |
| 32. | $\frac{1}{x+3}$ | -4 | -1 | $-\frac{1}{(x+3)^2}$ | -1 | y = -x - 5 |
| 33. | $(x+6)^2$ | -5 | 1 | 2x + 12 | 2 | y = 2x + 11 |
| 34. | $-7\tan(x)$ | $\frac{\pi}{3}$ | $-7\sqrt{3}$ | $-7\sec^2(x)$ | -28 | $y = -28x - 7\sqrt{3} + \frac{28\pi}{3}$ |
| 35. | $2\cos(x)$ | $\frac{\pi}{2}$ | 0 | $-2\sin(x)$ | -2 | $y = \pi - 2x$ |
| 36. | $-7\tan(x)$ | $-\frac{\pi}{6}$ | $\frac{7\sqrt{3}}{3}$ | $-7\sec^2(x)$ | $-\frac{28}{3}$ | $y = -\frac{28x}{3} - \frac{14\pi}{9} + \frac{7\sqrt{3}}{3}$ |
| 37. | $(x+2)^2$ | -3 | 1 | 2x + 4 | -2 | y = -2x - 5 |
| 38. | $2\cos(x)$ | $-\frac{\pi}{6}$ | $\sqrt{3}$ | $-2\sin(x)$ | 1 | $y = x + \frac{\pi}{6} + \sqrt{3}$ |
| 39. | x-2 | 3 | 1 | 1 | 1 | y = x - 2 |
| 40. | $\frac{1}{x+8}$ | -9 | -1 | $-\frac{1}{(x+8)^2}$ | -1 | y = -x - 10 |

| n. | f(x) | x_1 | y_1 | f'(x) | m | tangent line |
|-----|---------------------|------------------|-----------------------|----------------------|-----------------------|---|
| 41. | $(x-7)^2$ | 6 | 1 | 2x - 14 | -2 | y = 13 - 2x |
| 42. | $5\tan(x)$ | $-\frac{\pi}{3}$ | $-5\sqrt{3}$ | $5\sec^2(x)$ | 20 | $y = 20x - 5\sqrt{3} + \frac{20\pi}{3}$ |
| 43. | $\frac{1}{(x+1)^2}$ | -2 | 1 | $-\frac{2}{(x+1)^3}$ | 2 | y = 2x + 5 |
| 44. | $\sin(x)$ | $-\frac{\pi}{2}$ | -1 | $\cos(x)$ | 0 | y = -1 |
| 45. | $\sin(x)$ | $\frac{2\pi}{3}$ | $\frac{\sqrt{3}}{2}$ | $\cos(x)$ | $-\frac{1}{2}$ | $y = -\frac{x}{2} + \frac{\sqrt{3}}{2} + \frac{\pi}{3}$ |
| 46. | $-\cos(x)$ | $\frac{\pi}{4}$ | $-\frac{\sqrt{2}}{2}$ | $\sin(x)$ | $\frac{\sqrt{2}}{2}$ | $y = \frac{\sqrt{2}(x - \frac{\pi}{4})}{2} - \frac{\sqrt{2}}{2}$ |
| 47. | $\frac{1}{x+6}$ | -5 | 1 | $-\frac{1}{(x+6)^2}$ | -1 | y = -x - 4 |
| 48. | $(x+8)^2$ | -6 | 4 | 2x + 16 | 4 | y = 4x + 28 |
| 49. | $(x-2)^2$ | 3 | 1 | 2x-4 | 2 | y = 2x - 5 |
| 50. | $-2\cos(x)$ | 0 | -2 | $2\sin(x)$ | 0 | y = -2 |
| 51. | $-4\tan(x)$ | $\frac{\pi}{3}$ | $-4\sqrt{3}$ | $-4\sec^2(x)$ | -16 | $y = -16x - 4\sqrt{3} + \frac{16\pi}{3}$ |
| 52. | $-\sin(x)$ | 2π | 0 | $-\cos(x)$ | -1 | $y = -x + 2\pi$ |
| 53. | $\sin(x)$ | $\frac{\pi}{6}$ | $\frac{1}{2}$ | $\cos(x)$ | $\frac{\sqrt{3}}{2}$ | $y = \frac{\sqrt{3}(x - \frac{\pi}{6})}{2} + \frac{1}{2}$ |
| 54. | $\frac{1}{x-4}$ | 6 | $\frac{1}{2}$ | $-\frac{1}{(x-4)^2}$ | $-\frac{1}{4}$ | $y = 2 - \frac{x}{4}$ |
| 55. | $-\cos(x)$ | $-\frac{\pi}{4}$ | $-\frac{\sqrt{2}}{2}$ | $\sin(x)$ | $-\frac{\sqrt{2}}{2}$ | $y = -\frac{\sqrt{2}(x + \frac{\pi}{4})}{2} - \frac{\sqrt{2}}{2}$ |
| 56. | x-5 | 6 | 1 | 1 | 1 | y = x - 5 |
| 57. | $-2\cos(x)$ | π | 2 | $2\sin(x)$ | 0 | <i>y</i> = 2 |
| 58. | $\sin(x)$ | $\frac{2\pi}{3}$ | $\frac{\sqrt{3}}{2}$ | $\cos(x)$ | $-\frac{1}{2}$ | $y = -\frac{x}{2} + \frac{\sqrt{3}}{2} + \frac{\pi}{3}$ |
| 59. | $2\cos(x)$ | $\frac{\pi}{3}$ | 1 | $-2\sin(x)$ | $-\sqrt{3}$ | $y = -\sqrt{3}\left(x - \frac{\pi}{3}\right) + 1$ |
| 60. | x-7 | 8 | 1 | 1 | 1 | y = x - 7 |

| n. | f(x) | x_1 | y_1 | f'(x) | m | tangent line |
|-----|---------------------|-------------------|-----------------------|-----------------------|-----------------------|--|
| 61. | $\frac{1}{x-2}$ | 3 | 1 | $-\frac{1}{(x-2)^2}$ | -1 | y = 4 - x |
| 62. | $\frac{1}{x+9}$ | -8 | 1 | $-\frac{1}{(x+9)^2}$ | -1 | y = -x - 7 |
| 63. | $\cos(x)$ | $\frac{\pi}{3}$ | $\frac{1}{2}$ | $-\sin(x)$ | $-\frac{\sqrt{3}}{2}$ | $y = -\frac{\sqrt{3}(x - \frac{\pi}{3})}{2} + \frac{1}{2}$ |
| 64. | $-2\sin(x)$ | $\frac{\pi}{6}$ | -1 | $-2\cos(x)$ | $-\sqrt{3}$ | $y = -\sqrt{3}\left(x - \frac{\pi}{6}\right) - 1$ |
| 65. | $\frac{1}{x-1}$ | 3 | $\frac{1}{2}$ | $-\frac{1}{(x-1)^2}$ | $-\frac{1}{4}$ | $y = \frac{5}{4} - \frac{x}{4}$ |
| 66. | $-\sin(x)$ | $\frac{2\pi}{3}$ | $-\frac{\sqrt{3}}{2}$ | $-\cos(x)$ | $\frac{1}{2}$ | $y = \frac{x}{2} - \frac{\pi}{3} - \frac{\sqrt{3}}{2}$ |
| 67. | $-2\cos(x)$ | 2π | -2 | $2\sin\left(x\right)$ | 0 | y = -2 |
| 68. | $-2\cos(x)$ | $\frac{\pi}{4}$ | $-\sqrt{2}$ | $2\sin(x)$ | $\sqrt{2}$ | $y = \sqrt{2}\left(x - \frac{\pi}{4}\right) - \sqrt{2}$ |
| 69. | $-3\tan(x)$ | $-\frac{2\pi}{3}$ | $-3\sqrt{3}$ | $-3\sec^2(x)$ | -12 | $y = -12x - 8\pi - 3\sqrt{3}$ |
| 70. | $\sin(x)$ | $-\frac{\pi}{2}$ | -1 | $\cos(x)$ | 0 | y = -1 |
| 71. | $\sin(x)$ | $\frac{3\pi}{4}$ | $\frac{\sqrt{2}}{2}$ | $\cos(x)$ | $-\frac{\sqrt{2}}{2}$ | $y = -\frac{\sqrt{2}(x - \frac{3\pi}{4})}{2} + \frac{\sqrt{2}}{2}$ |
| 72. | $(x-9)^2$ | 8 | 1 | 2x - 18 | -2 | y = 17 - 2x |
| 73. | $\sin(x)$ | $-\frac{\pi}{6}$ | $-\frac{1}{2}$ | $\cos(x)$ | $\frac{\sqrt{3}}{2}$ | $y = \frac{\sqrt{3}(x + \frac{\pi}{6})}{2} - \frac{1}{2}$ |
| 74. | x + 7 | -5 | 2 | 1 | 1 | y = x + 7 |
| 75. | x-4 | 6 | 2 | 1 | 1 | y = x - 4 |
| 76. | $\sin(x)$ | $-\frac{\pi}{2}$ | -1 | $\cos(x)$ | 0 | y = -1 |
| 77. | $-\sin(x)$ | $-\frac{\pi}{6}$ | $\frac{1}{2}$ | $-\cos(x)$ | $-\frac{\sqrt{3}}{2}$ | $y = -\frac{\sqrt{3}(x + \frac{\pi}{6})}{2} + \frac{1}{2}$ |
| 78. | $\frac{1}{(x-1)^2}$ | 2 | 1 | $-\frac{2}{(x-1)^3}$ | -2 | y = 5 - 2x |
| 79. | $\frac{1}{x-10}$ | 12 | $\frac{1}{2}$ | $-\frac{1}{(x-10)^2}$ | $-\frac{1}{4}$ | $y = \frac{7}{2} - \frac{x}{4}$ |
| 80. | $2\cos(x)$ | $-\frac{\pi}{6}$ | $\sqrt{3}$ | $-2\sin(x)$ | 1 | $y = x + \frac{\pi}{6} + \sqrt{3}$ |

| n. | f(x) | x_1 | y_1 | f'(x) | m | tangent line |
|------|---------------------|------------------|----------------------|----------------------|----------------------|---|
| 81. | $2\tan(x)$ | $\frac{2\pi}{3}$ | $-2\sqrt{3}$ | $2\sec^2(x)$ | 8 | $y = 8x - \frac{16\pi}{3} - 2\sqrt{3}$ |
| 82. | $-8\tan(x)$ | 0 | 0 | $-8\sec^2(x)$ | -8 | y = -8x |
| 83. | $2\sin(x)$ | $\frac{3\pi}{4}$ | $\sqrt{2}$ | $2\cos(x)$ | $-\sqrt{2}$ | $y = -\sqrt{2}\left(x - \frac{3\pi}{4}\right) + \sqrt{2}$ |
| 84. | $(x+8)^2$ | -9 | 1 | 2x + 16 | -2 | y = -2x - 17 |
| 85. | $-2\sin(x)$ | $-\frac{\pi}{6}$ | 1 | $-2\cos(x)$ | $-\sqrt{3}$ | $y = -\sqrt{3}\left(x + \frac{\pi}{6}\right) + 1$ |
| 86. | $6\tan(x)$ | π | 0 | $6\sec^2(x)$ | 6 | $y = 6x - 6\pi$ |
| 87. | x + 8 | -7 | 1 | 1 | 1 | y = x + 8 |
| 88. | $2\cos(x)$ | π | -2 | $-2\sin(x)$ | 0 | y = -2 |
| 89. | $\frac{1}{x+7}$ | -6 | 1 | $-\frac{1}{(x+7)^2}$ | -1 | y = -x - 5 |
| 90. | $\cos(x)$ | $-\pi$ | -1 | $-\sin(x)$ | 0 | y = -1 |
| 91. | $-2\cos(x)$ | 2π | -2 | $2\sin(x)$ | 0 | y = -2 |
| 92. | $\frac{1}{(x+6)^2}$ | -7 | 1 | $-\frac{2}{(x+6)^3}$ | 2 | y = 2x + 15 |
| 93. | $7\tan(x)$ | -2π | 0 | $7\sec^2(x)$ | 7 | $y = 7x + 14\pi$ |
| 94. | $\frac{1}{(x-4)^2}$ | 5 | 1 | $-\frac{2}{(x-4)^3}$ | -2 | y = 11 - 2x |
| 95. | $\cos(x)$ | $-\frac{\pi}{4}$ | $\frac{\sqrt{2}}{2}$ | $-\sin(x)$ | $\frac{\sqrt{2}}{2}$ | $y = \frac{\sqrt{2}\left(x + \frac{\pi}{4}\right)}{2} + \frac{\sqrt{2}}{2}$ |
| 96. | $3\tan(x)$ | $\frac{2\pi}{3}$ | $-3\sqrt{3}$ | $3\sec^2(x)$ | 12 | $y = 12x - 8\pi - 3\sqrt{3}$ |
| 97. | $\frac{1}{x-4}$ | 3 | -1 | $-\frac{1}{(x-4)^2}$ | -1 | y = 2 - x |
| 98. | $2\cos(x)$ | $\frac{\pi}{2}$ | 0 | $-2\sin(x)$ | -2 | $y = \pi - 2x$ |
| 99. | $2\sin(x)$ | $\frac{3\pi}{4}$ | $\sqrt{2}$ | $2\cos(x)$ | $-\sqrt{2}$ | $y = -\sqrt{2}\left(x - \frac{3\pi}{4}\right) + \sqrt{2}$ |
| 100. | $2\cos(x)$ | $-\frac{\pi}{3}$ | 1 | $-2\sin(x)$ | $\sqrt{3}$ | $y = \sqrt{3}\left(x + \frac{\pi}{3}\right) + 1$ |

| n. | f(x) | x_1 | y_1 | f'(x) | m | tangent line |
|------|-------------|------------------|--------------|---------------|------------|--|
| 101. | $2\cos(x)$ | $-\frac{\pi}{3}$ | 1 | $-2\sin(x)$ | $\sqrt{3}$ | $y = \sqrt{3}\left(x + \frac{\pi}{3}\right) + 1$ |
| 102. | x-2 | 1 | -1 | 1 | 1 | y = x - 2 |
| 103. | $\sin(x)$ | π | 0 | $\cos(x)$ | -1 | $y = \pi - x$ |
| 104. | $-6\tan(x)$ | $\frac{\pi}{6}$ | $-2\sqrt{3}$ | $-6\sec^2(x)$ | -8 | $y = -8x - 2\sqrt{3} + \frac{4\pi}{3}$ |