

Name:

Student ID:

Pre-tutorial 7 Questions (to be attempted before class on July 26th, 2019)

Chapter 10, Ex 33: Phasors

Assuming the passive sign convention and an operating frequency of 314 rad/s, calculate the phasor voltage \bar{V} which appears across each of the following when driven by the phasor current $\bar{I} = 10 \angle 0^\circ$ mA.

a) A 2Ω resistor.

$$\begin{aligned}\bar{V}_R &= \bar{I} R \\ &= 10 \times 10^{-3} \angle 0^\circ \times 2 \\ &= 20 \angle 0^\circ \text{ mV}\end{aligned}$$

b) A 1 F capacitor.

$$\begin{aligned}\bar{V}_C &= \frac{1}{C} \int \bar{I} dt \\ &= \frac{1}{j\omega C} \bar{I} \\ &= \frac{1}{314 \angle 90^\circ} \cdot 10 \times 10^{-3} \angle 0^\circ \\ &= 0.03 \angle -90^\circ \text{ mV}\end{aligned}$$

c) A 1 H inductor.

$$\begin{aligned}\bar{V}_L &= L d\bar{I}/dt \\ &= j\omega L \bar{I} \\ &= 314 \times 1 \angle 90^\circ \times 10 \times 10^{-3} \angle 0^\circ \\ &= 3.14 \angle 90^\circ \text{ V}\end{aligned}$$

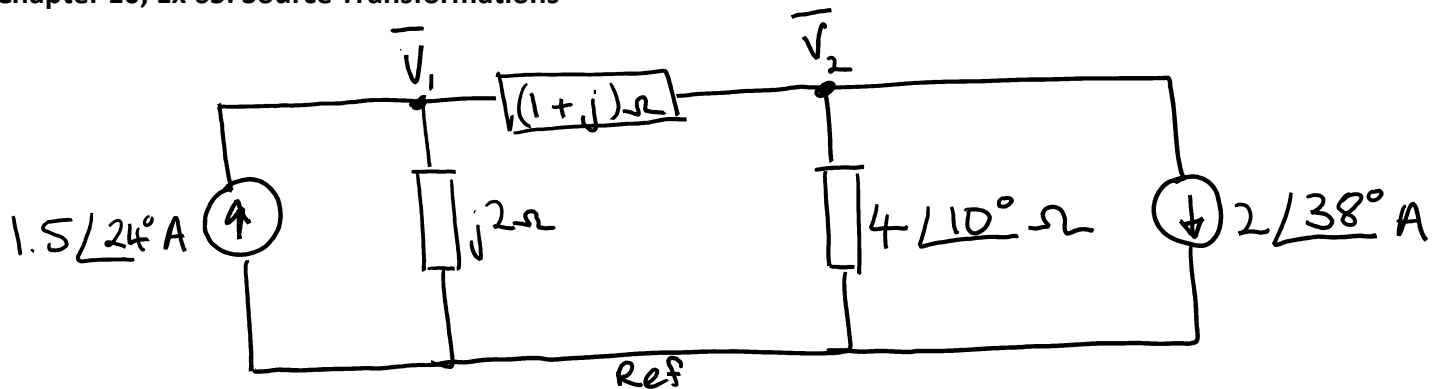
d) A 2Ω resistor in series with a 1 F capacitor.

$$\begin{aligned}\bar{V}_{RC} &= \bar{V}_R + \bar{V}_C \\ &= (20 \angle 0^\circ + 0.03 \angle -90^\circ) \times 10^{-3} \\ &= (20 - j0.03) \times 10^{-3} \\ &= 20 \angle -0.09^\circ \text{ mV}\end{aligned}$$

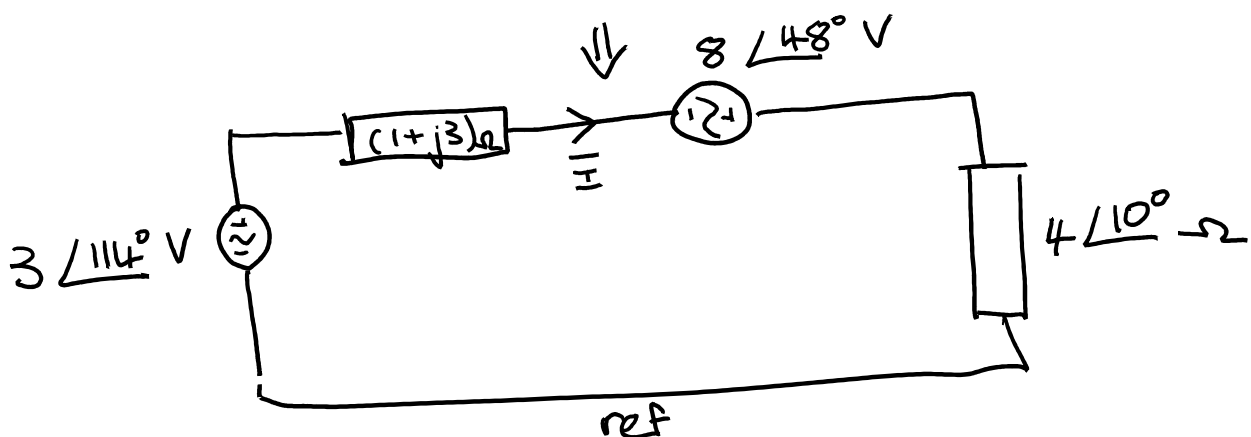
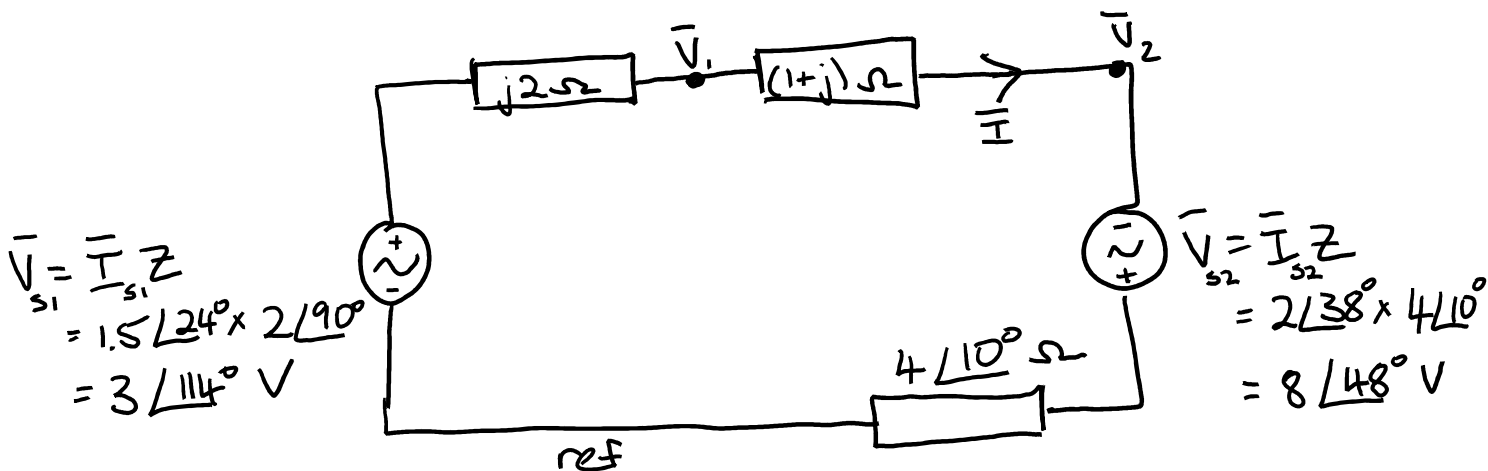
e) A $2\ \Omega$ resistor in series with a $1\ \text{H}$ inductor.

$$\begin{aligned}\bar{V}_{RL} &= \bar{V}_R + \bar{V}_L \\ &= 20 \times 10^{-3} \angle 0^\circ + 3.14 \angle 90^\circ \\ &= 20 \times 10^{-3} + j 3.14 \\ &= 3.14 \angle 89.6^\circ \text{ V}\end{aligned}$$

Chapter 10, Ex 65: Source Transformations



For the circuit above, perform a source transformation on each source, simplify the resulting circuit as much as possible, and calculate the current flowing through the $(1+j)\ \Omega$ impedance.

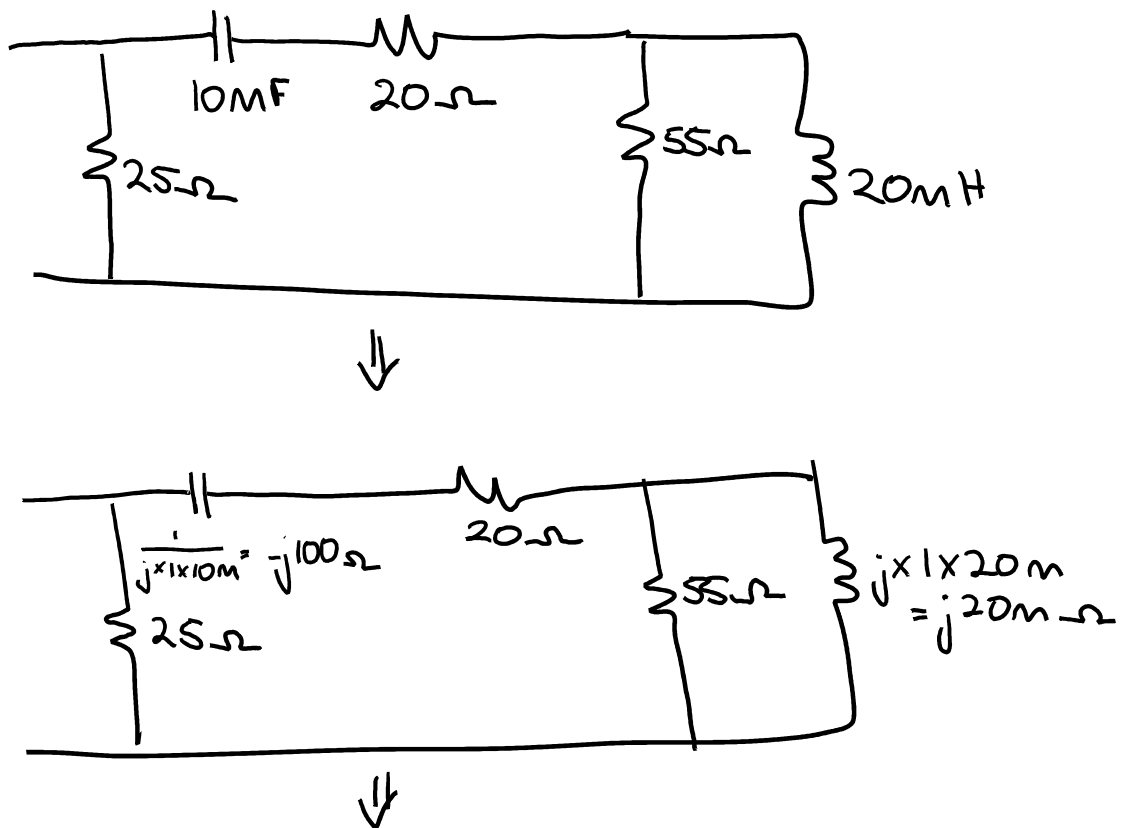


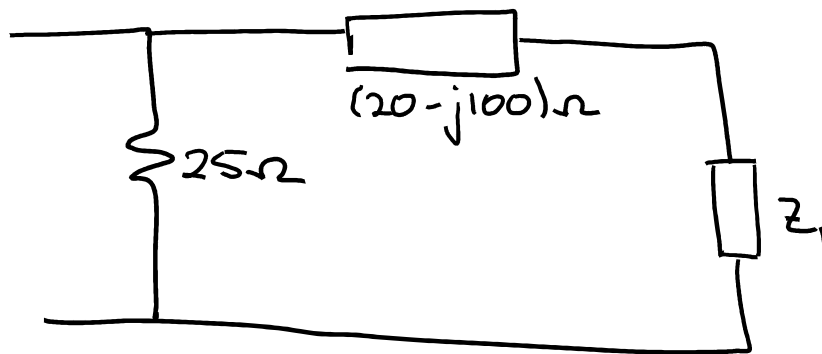
$$\begin{aligned}
 -3 \angle 114^\circ + \bar{I}(1+j3) - 8 \angle 48^\circ + \bar{I}(4 \angle 110^\circ) &= 0 \\
 \bar{I}(1+j3+4 \angle 110^\circ) &= 3 \angle 114^\circ + 8 \angle 48^\circ \\
 \bar{I}(1+j3+3.94+j0.69) &= -1.22+j2.74+5.35+j5.95 \\
 \bar{I}(4.94+j3.69) &= 4.13+j8.69 \\
 \bar{I} &= \frac{9.62 \angle 64.6^\circ}{6.17 \angle 36.8^\circ} \\
 &= 1.56 \angle 27.8^\circ \text{ A}
 \end{aligned}$$

At Tutorial 7 – Marked Question (26th July 2019)

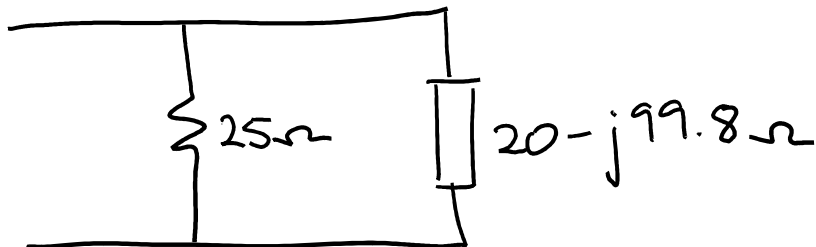
Chapter 10, Ex 40a: Impedance and Admittance

Consider the network below, and determine the equivalent impedance seen looking into the open terminals if $\omega = 1 \text{ rad/s}$.

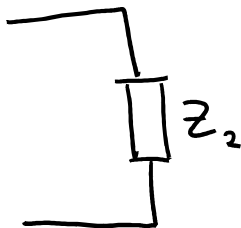




$$\begin{aligned}
 Z_1 &= \frac{55 \times 20 \angle 90^\circ}{55 + j20} \\
 &= \frac{1.1 \angle 90^\circ}{55 \angle 10.02^\circ} \\
 &= 0.02 \angle 89.98^\circ \Omega = 7.27 \times 10^{-6} + j0.02 \Omega
 \end{aligned}$$



↓



$$\begin{aligned}
 Z_2 &= \frac{(20 - j99.98)25}{20 - j99.98 + 25} \\
 &= \frac{500 - j2,499.5}{45 - j99.98} \\
 &= \frac{2549 \angle -78.69^\circ}{109.6 \angle -65.77^\circ} \\
 &= 23.26 \angle -12.92^\circ \Omega
 \end{aligned}$$

At Tutorial 7 – Unmarked Questions (26th July 2019)

Chapter 10, Ex 28: Phasors

The following complex voltages are written in a combination of rectangular and polar form. Rewrite each, using conventional phasor notation (i.e. a magnitude and angle):

a) $\frac{2-j}{5\angle 45^\circ} \text{ V}$

$$\frac{2-j}{5\angle 45^\circ} = \frac{2.24 \angle -26.6^\circ}{5 \angle 45^\circ} \\ = 0.45 \angle -71.6^\circ \text{ V}$$

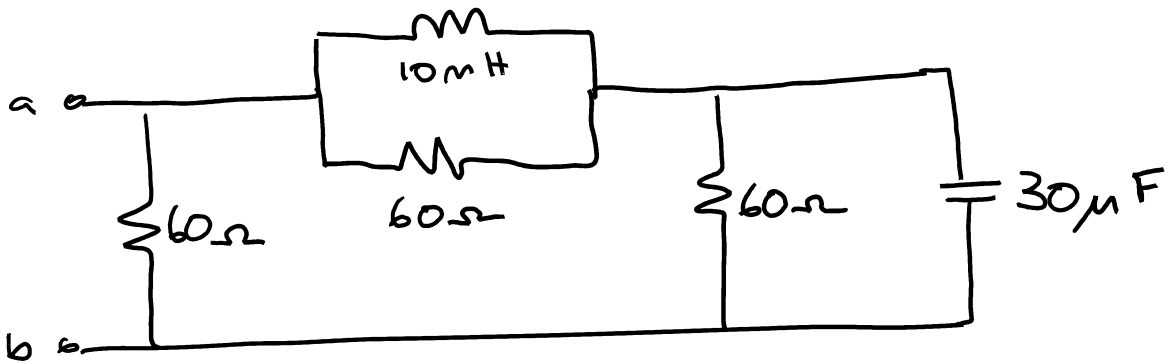
b) $\frac{6\angle 20^\circ}{1000} - j \text{ V}$

$$\frac{6\angle 20^\circ}{1000} - j = 6 \times 10^{-3} \angle 20^\circ - j \\ = 5.64 \times 10^{-3} + j 2.05 \times 10^{-3} - j \\ = 5.64 \times 10^{-3} - j 0.998 \\ = 0.998 \angle -89.7^\circ \text{ V}$$

c) $(j)(52.5\angle -90^\circ) \text{ V}$

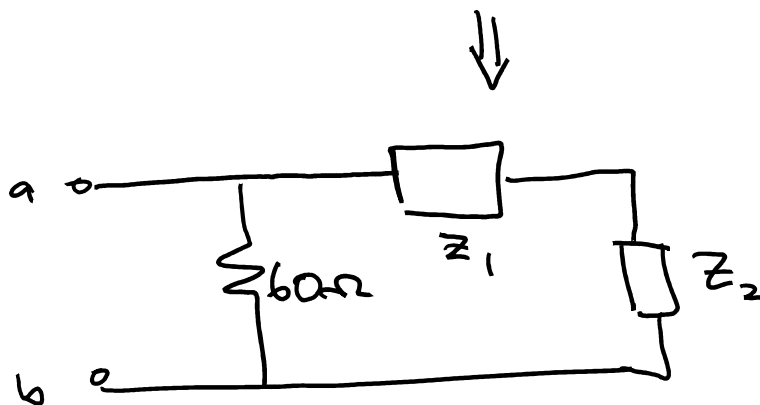
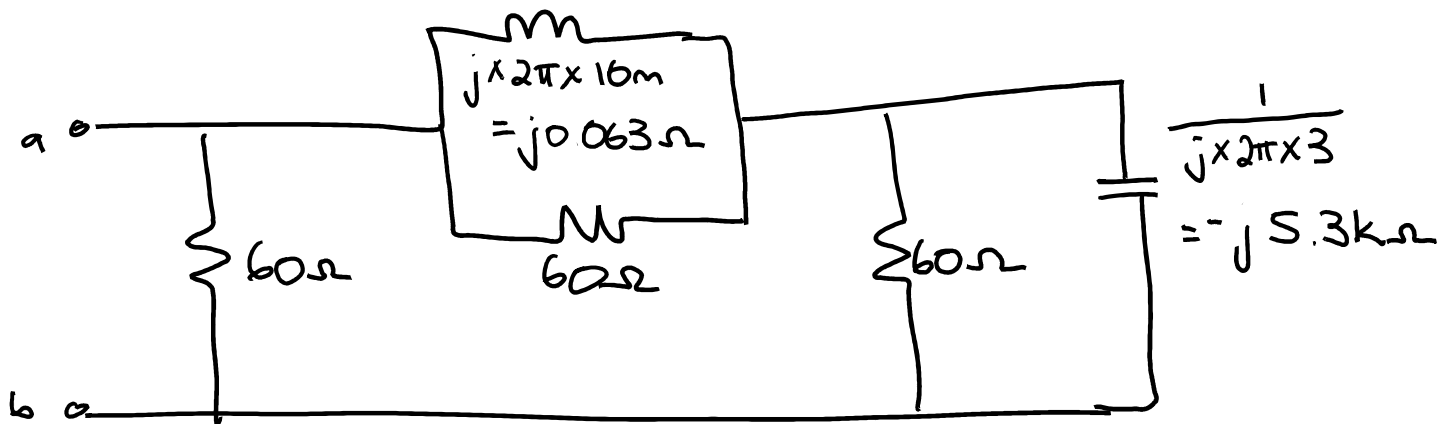
$$(j)(52.5\angle -90^\circ) = \angle 90^\circ \times 52.5\angle -90^\circ \\ = 52.5 \angle 0^\circ \text{ V}$$

Chapter 10, Ex 43a: Impedance and Admittance



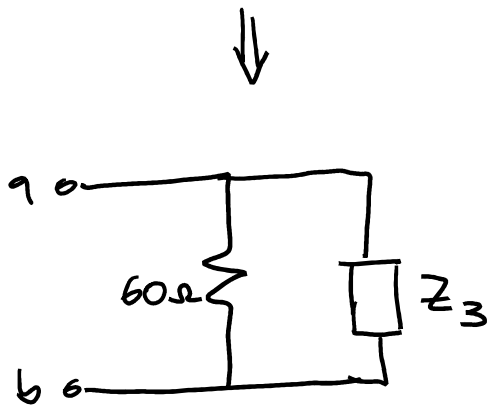
Calculate the equivalent impedance seen at the open terminals of the network shown above if f is equal to 1 Hz.

$$f = 1 \text{ Hz}, \quad \omega = 2\pi f \\ = 2\pi \text{ rad/s}$$

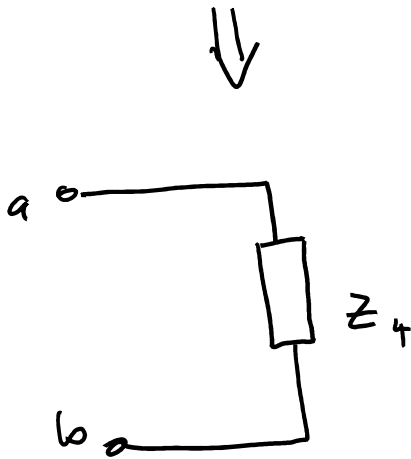


$$Z_1 = \frac{j0.063 \times 60}{j0.063 + 60} \\ = \frac{3.78 \angle 90^\circ}{60 \angle 0.06^\circ} \\ = 0.063 \angle 89.9^\circ \Omega$$

$$Z_2 = \frac{60 \times -j5.3k}{60 - j5.3k} \\ = \frac{318k \angle -90^\circ}{5.3k \angle -89.4^\circ} = 60 \angle -0.6^\circ \Omega$$

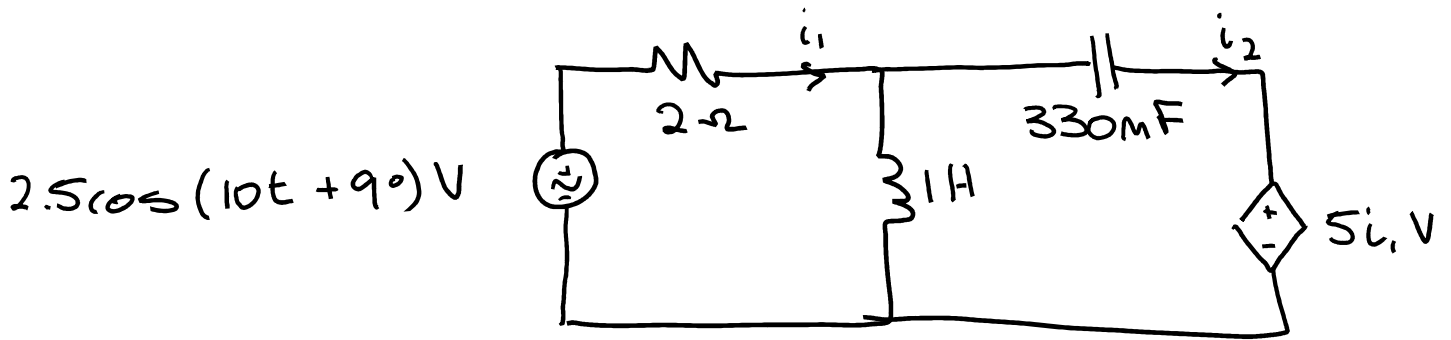


$$\begin{aligned}
 Z_3 &= 60 \angle -0.6^\circ + 0.063 \angle 89.94^\circ \\
 &= 60 - j0.63 + 65.9 \mu + j0.063 \\
 &= 60 - j0.567 \\
 &= 60 \angle -0.54^\circ \Omega
 \end{aligned}$$

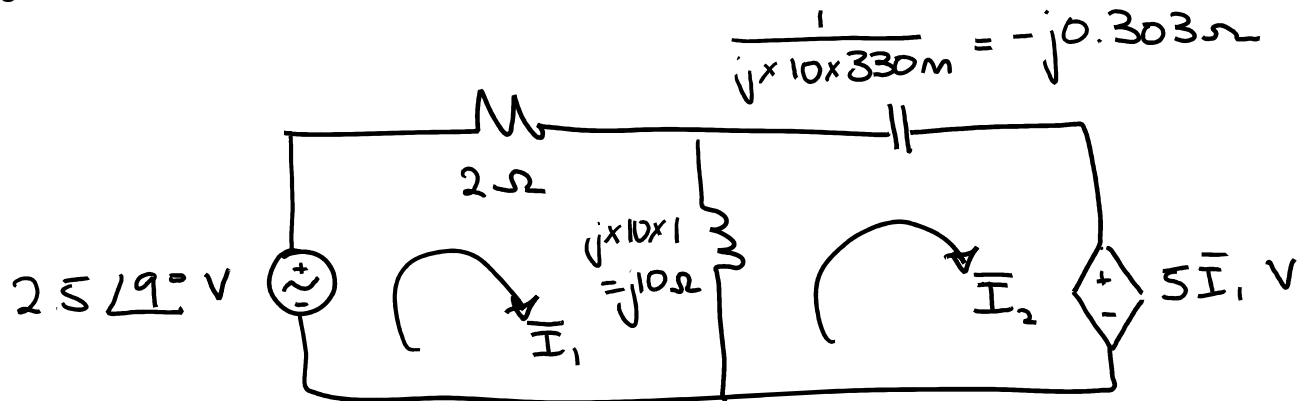


$$\begin{aligned}
 Z_4 &= \frac{60 \angle -0.54^\circ \times 60}{60 + 60 - j0.567} \\
 &= \frac{3600 \angle -0.54^\circ}{120 - j0.567} \\
 &= \frac{3600 \angle -0.54^\circ}{120 \angle -0.27^\circ} \\
 &= 30 \angle -0.27^\circ \Omega
 \end{aligned}$$

Chapter 10, Ex 52: Nodal and Mesh Analysis



Employ phasor analysis techniques to obtain expressions for the two mesh currents i_1 and i_2 as shown in the figure above.



Mesh 1

$$-2.5 \angle 9^\circ + 2\bar{I}_1 + j10(\bar{I}_1 - \bar{I}_2) = 0$$

$$(2 + j10)\bar{I}_1 - j10\bar{I}_2 = 2.5 \angle 9^\circ \quad (1)$$

Mesh 2

$$j10(\bar{I}_2 - \bar{I}_1) - j0.303\bar{I}_2 + 5\bar{I}_1 = 0$$

$$(5 - j10)\bar{I}_1 + j9.697\bar{I}_2 = 0$$

$$j9.697\bar{I}_2 = (-5 + j10)\bar{I}_1$$

$$\bar{I}_2 = \frac{(-5 + j10)\bar{I}_1}{j9.697}$$

$$= -j0.103(-5 + j10)\bar{I}_1$$

$$= (j0.516 + 1.03)\bar{I}_1 \quad (2)$$

(2) into (1):

$$(2+j10)\bar{I}_1 - j10(1.03+j0.516)\bar{I}_1 = 2.5 \angle 9^\circ$$

$$(2+j10)\bar{I}_1 + (-j10.3 + 5.16)\bar{I}_1 = 2.5 \angle 9^\circ$$

$$(7.16 - j0.3)\bar{I}_1 = 2.5 \angle 9^\circ$$

$$\bar{I}_1 = \frac{2.5 \angle 9^\circ}{7.16 - j0.3}$$

$$= \frac{2.5 \angle 9^\circ}{7.17 \angle -2.4^\circ}$$

$$= 0.35 \angle 11.4^\circ \text{ A}$$

$$\bar{I}_2 = (j0.516 + 1.03)\bar{I}_1$$

$$= 1.15 \angle 26.7^\circ \times 0.35 \angle 11.4^\circ$$

$$= 0.40 \angle 38.1^\circ \text{ A}$$

$$i_1 = 0.35 \cos(10t + 11.4^\circ) \text{ A}$$

$$i_2 = 0.40 \cos(10t + 38.1^\circ) \text{ A}$$