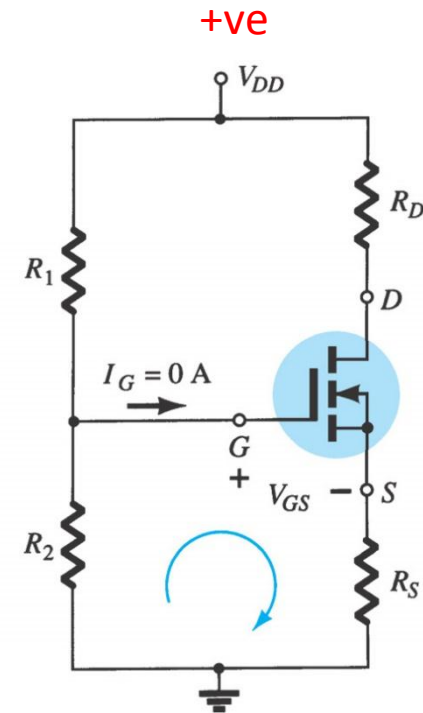


Field Effect Transistors DC biasing

Chapter 7

- Fixed Bias configuration
- Self Bias
- Voltage divider bias
- Feedback bias
- Graphical analysis
- Transfer curve
- Network equation
- Operating point



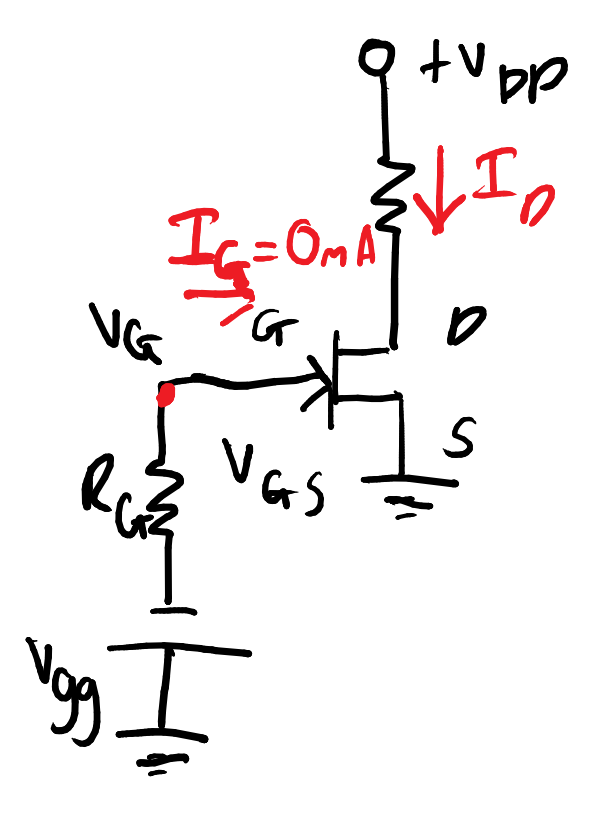
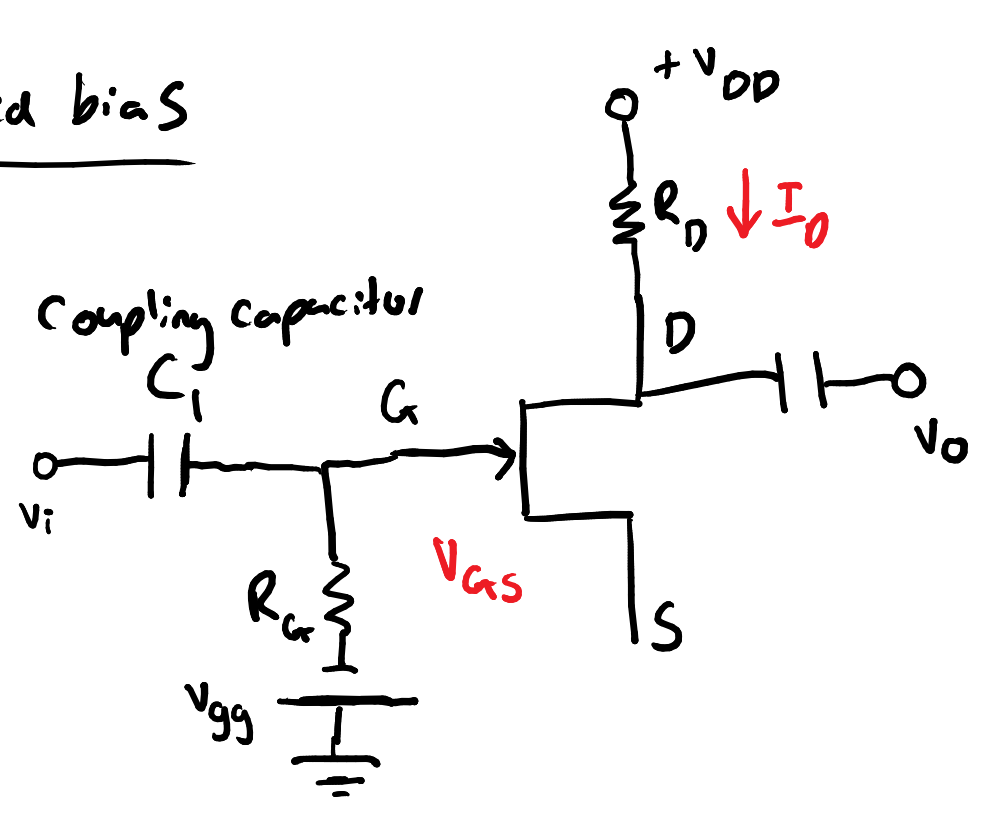
Application of DC supply (V_{DD}) to provide the required polarity and level of DC voltages for the transistors to operate in the region of interest

• DC biasing

output biasing
- transfer curve

p-channel

fixed bias



Shockley equation:

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

$$V_G = V_{GK} - I_G R_G$$

$$V_G = V_{GK}$$

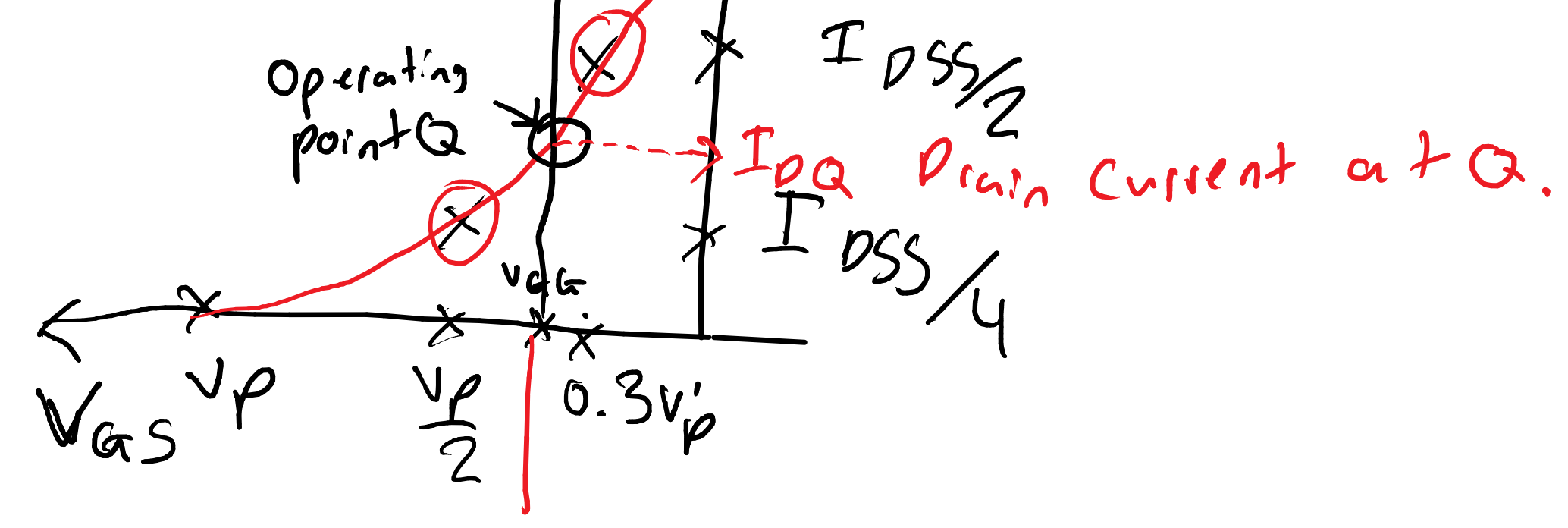
$$V_{GS} = V_G - V_S$$

$$V_{GS} = V_{GK} - 0$$

$$V_{GS} = V_{GK}$$

$$V_{GS} = V_{GK}$$

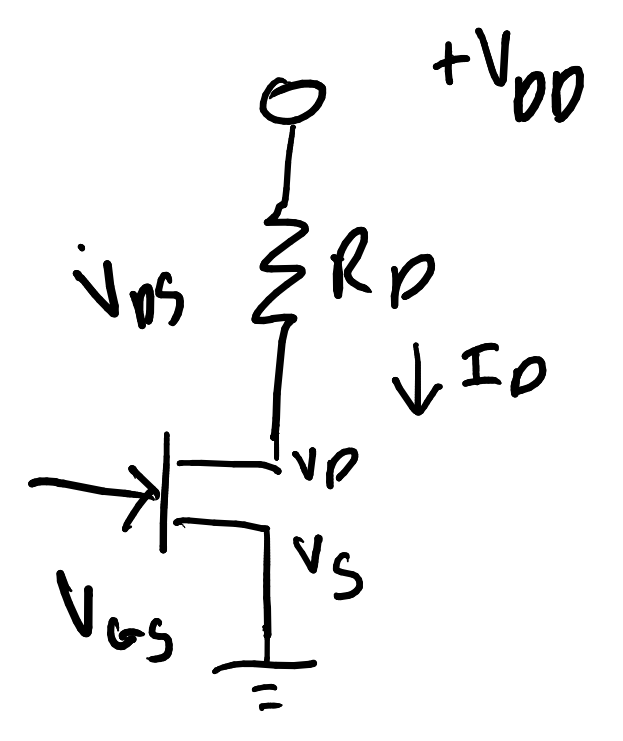
network equation



fixed bias configuration

$$V_{GSQ}$$

VGS at Q point



$$V_{DD} = I_D R_D + V_{DS}$$

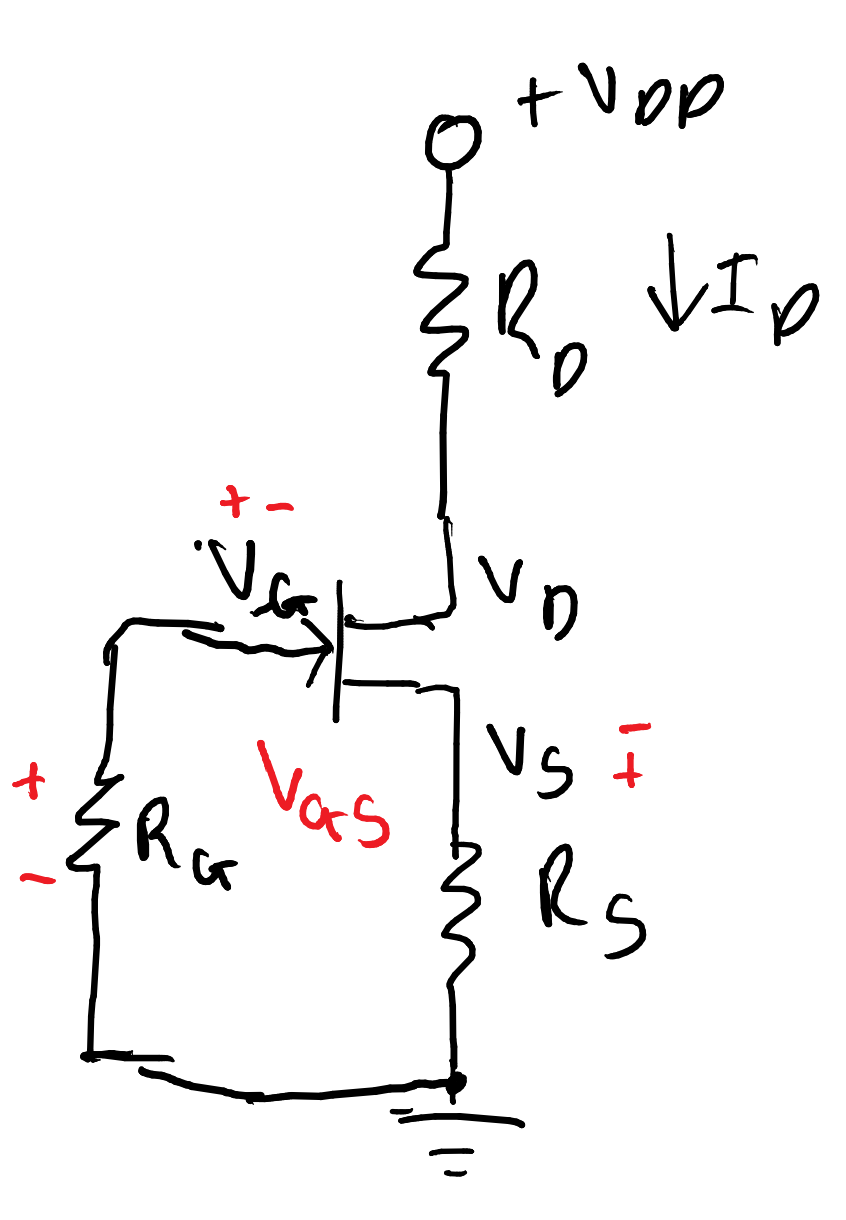
$$I_D = \frac{V_{DD} - V_{DS}}{R_D}$$

$$V_{DS} = V_{DD} - I_D R_D$$

$$V_{DS} = V_D - V_S$$

self-bias configuration

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2 \text{ Transfer curve}$$



$$V_{GS} = V_G - V_S \text{ (network eq.)}$$

$$V_G = 0, I_G = 0$$

$$V_{GS} = 0 - V_S$$

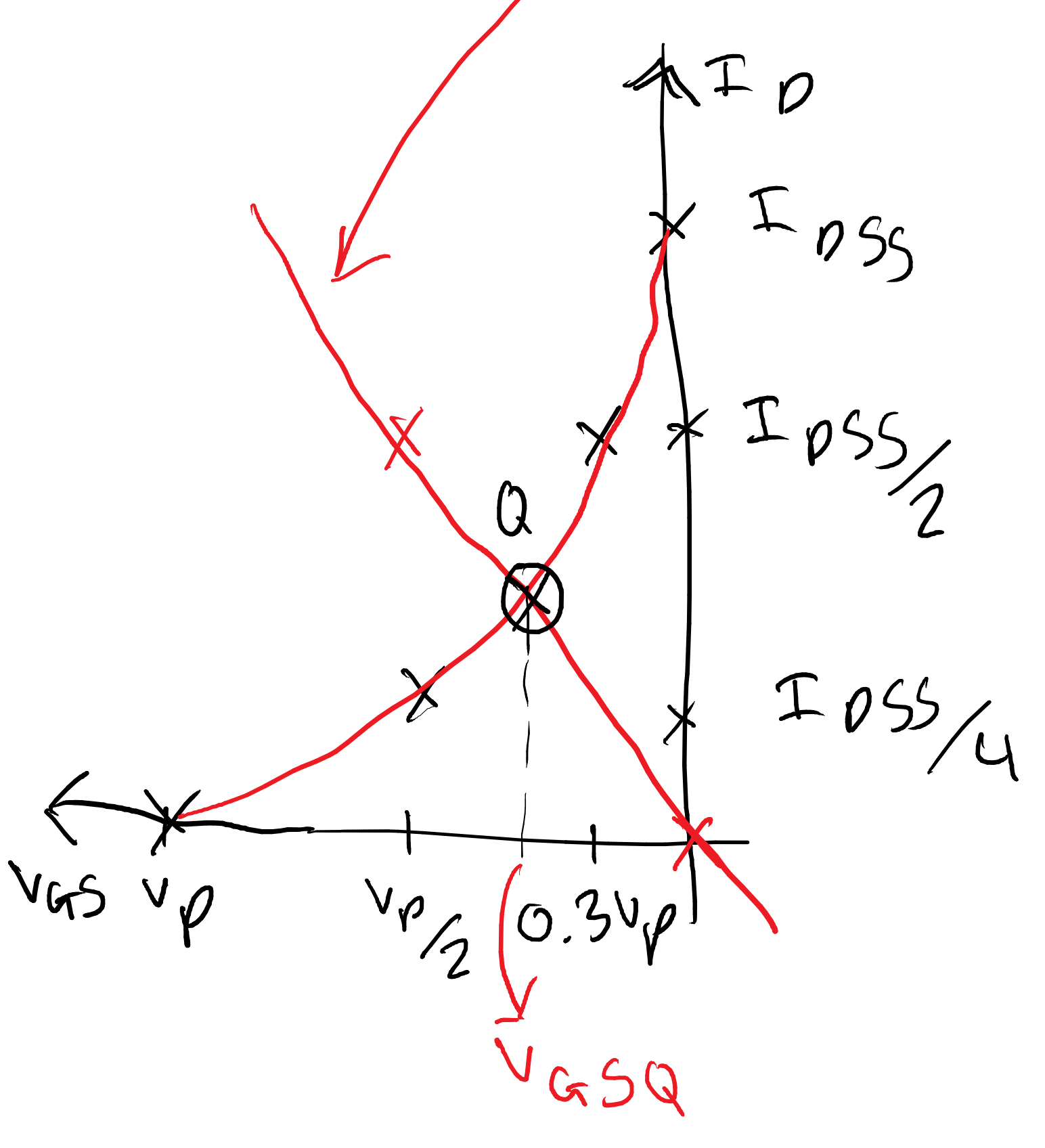
$$V_S = I_S R_S$$

$$I_S = I_D$$

$$V_S = I_D R_S$$

$$V_{GS} = -I_D R_S$$

network equation



$$\text{for } I_D = 0$$

$$V_{GS} = 0$$

$$\text{assume } I_D = \frac{I_{DSS}}{2}$$

$$V_{GS} = -\frac{I_{DSS}}{2} \times R_S$$

FET DC Biasing Circuits Analysis

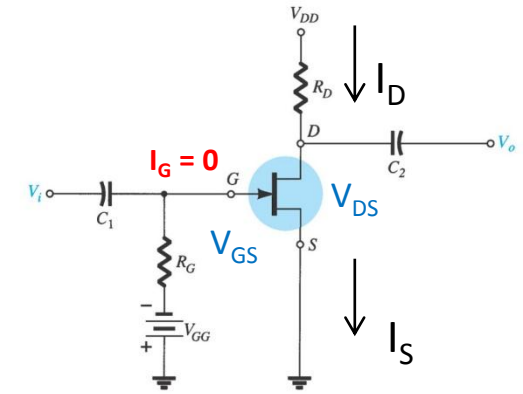
- I_D is controlled by V_{GS} **Voltage Controlled Transistor**
- In all dc analysis of FET's circuits
 $I_G = 0$ mA, gate current = 0
- $I_D = I_S$ Drain Current = Source Current
- Shockley Equation relates input voltage V_{GS} and output current I_D in JFET's and DMOS transistors:

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2 \quad \text{.....(1)}$$

- For Enhancement type MOSFET :

$$I_D = K(V_{GS} - V_T)^2 \quad \text{.....(2)}$$

- Equations 1 and 2 are applied for JFET and MOSFET devices, they don't change With biasing network configurations.
- It is the network that determine the level of current and voltage associated with the operating point Q.
- DC analysis is the solution of simultaneous equations established by the **DEVICE** and **NETWORK**.
- DC analysis can be performed by mathematical or graphical methods.

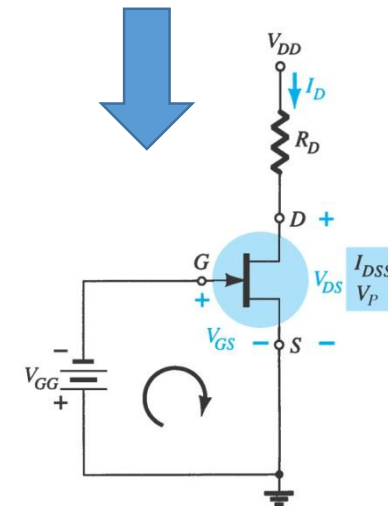
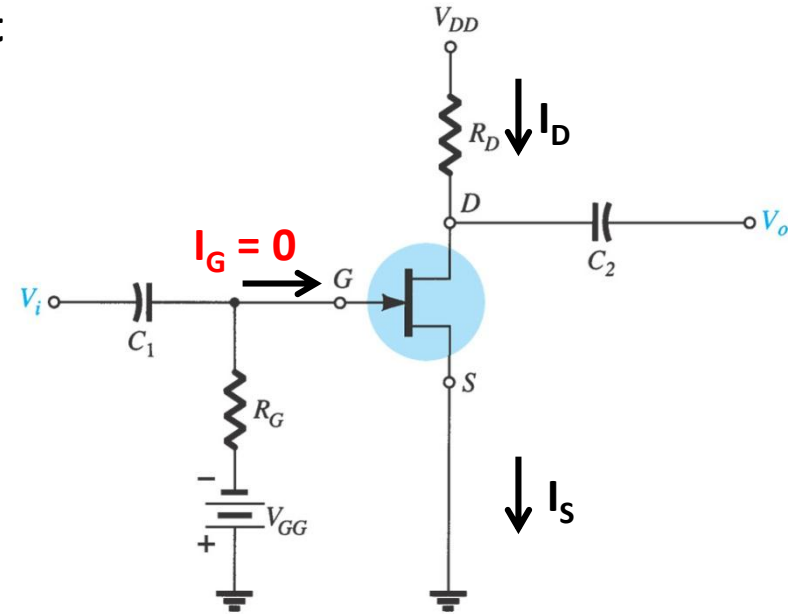


Fixed –bias configuration for JFET's

- R_G is placed to ensure that V_i appears at the input of the FET for ac applications and analysis.
- Coupling capacitors are open circuit for DC analysis and short circuit for ac analysis(and applied signals)

DC analysis and mathematical approach:

- $I_G = 0\text{mA}$ (Hence V_{GG} appears at the Gate G)
- $V_{RG} = I_G R_G = 0\text{V}$
- $-V_{GG} - V_{GS} = 0\text{V}$ (input loop)
- $V_{GS} = -V_{GG}$ (network Equation)
- Since V_{GG} is fixed supply voltage, hence the name Fixed bias configuration.
- Apply Shockley equation: $I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$
- I_{DSS} and V_P are usually obtained from the data sheet, Specified by the manufacturing company.
- V_{GS} is fixed by the V_{GG} (network equation).
- Then I_D can be calculated for the fixed bias circuit using Shockley equation.



JFET Fixed bias DC circuit

Graphical analysis(plot of Shockley equation)

1. Construct the transfer curve using Shockley equation: $I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$
2. Find the network equation for the circuit and superimpose it on the transfer curve.
 $V_{GS} = V_G - V_S = V_G$ as $V_S = 0V$ (fixed bias).

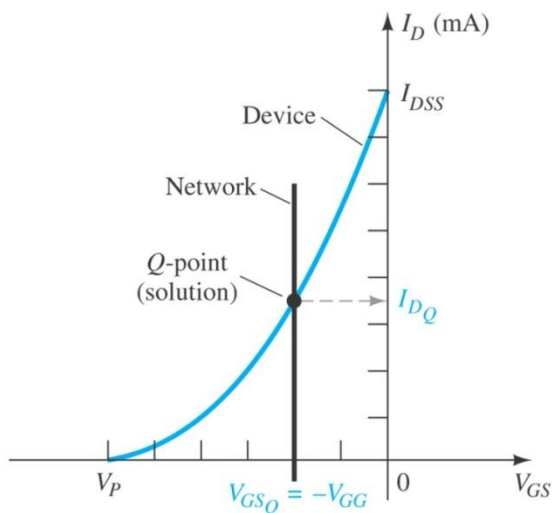
3. The point where the two curves intersect is the common solution to the two equations and it is called the Q operating point.
4. At the Q point, I_{DQ} and V_{GSQ} can be determined, e.g. $I_{DQ} = 2.6mA$, and $V_{GSQ} = -2.6V$
5. The output loop equations

$$V_{DS} = V_{DD} - I_D R_D$$

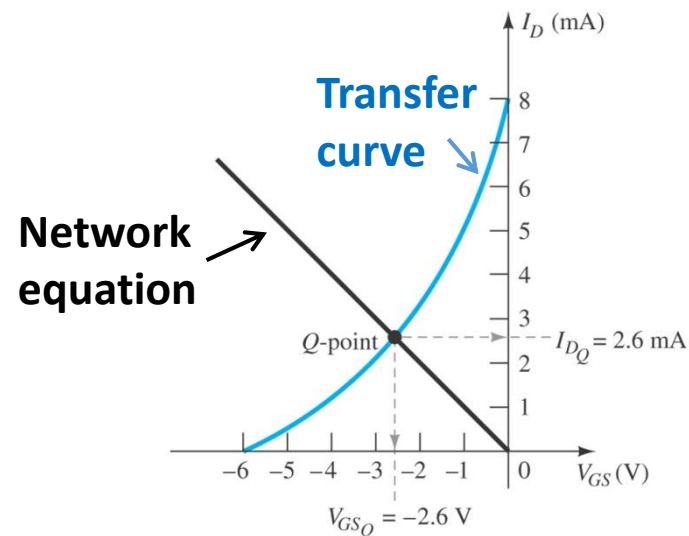
$$V_{DS} = V_D - V_S$$

$$V_D = V_{DS} + V_S \text{ for this case } V_S = 0V$$

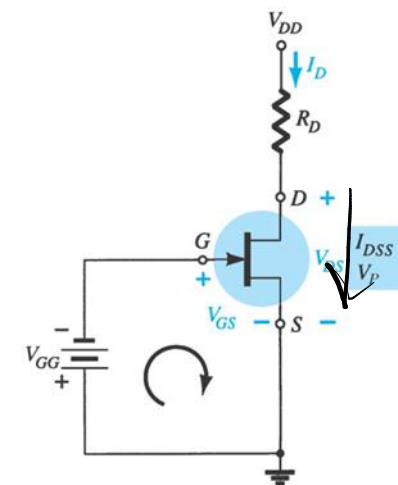
$$\text{Then } V_D = V_{DS}$$



Fixed Bias



Self Bias



Example

Find V_{GSQ} , I_{DQ} , V_{DS} , V_G and V_S for the circuit shown using mathematical and graphical method.

Mathematical method:

Network Equation

$$V_{GS} = V_G - V_S = V_G \quad \text{since } V_S = 0 \text{ (ground)}$$

$$I_G = 0 \text{ mA}$$

$$V_{GS} = V_G = -V_{GG} = -2 \text{ V} = V_{GSQ}$$

Shockley Equation

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2 = 10 \text{ mA} \left(1 - \frac{-2}{-8} \right)^2 = I_{DQ} = 5.625 \text{ mA}$$

Output loop:

$$V_{DD} = I_D R_D + V_{DS}$$

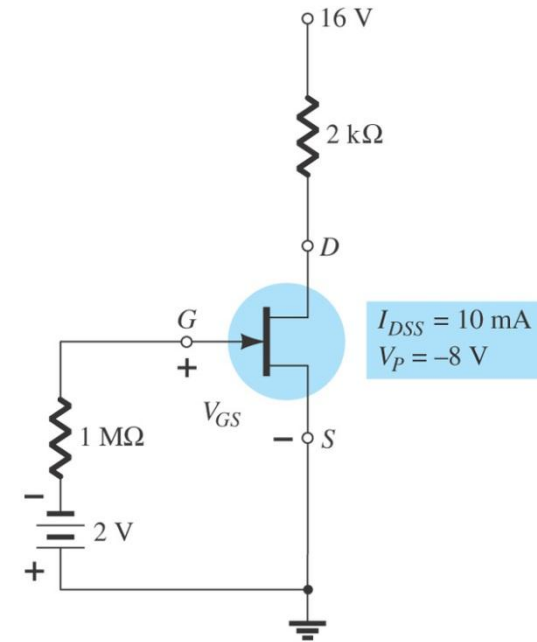
$$V_{DS} = V_D - V_S = (V_{DD} - I_D R_D) - 0 \text{ V}$$

$$V_{DS} = 16 - 5.625 \times 10^{-3} \times 2 \times 10^3 = 4.75 \text{ V}$$

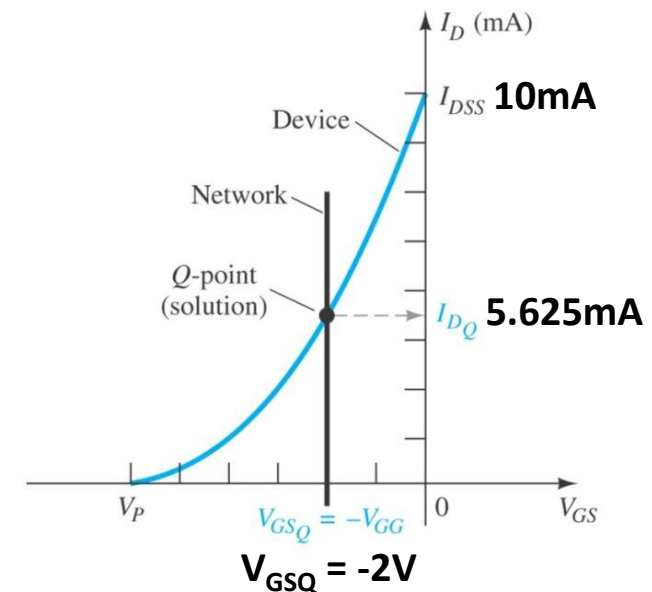
$$V_D = V_{DS} + V_S = 4.75 + 0 = 4.75 \text{ V}$$

$$V_G = V_{GS} + V_S = -2 \text{ V} + 0 = -2 \text{ V}$$

$V_S = 0 \text{ V}$ ground potential, common source configurations.



JFET fixed bias circuit



Graphical method

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$$

For $V_{GS} = 0V$, $I_D = I_{DSS} = 10mA$

For $V_{GS} = V_P$, $I_D = 0mA$

For $V_{GS} = \frac{1}{2} V_P = -4V$, $I_D = I_{DSS} / 4 = 2.5 \text{ mA}$

For $I_D = I_{DSS}/2 = 5mA$

$$V_{GS} = 0.3V_P = 0.3 \times -8V = -2.4V$$

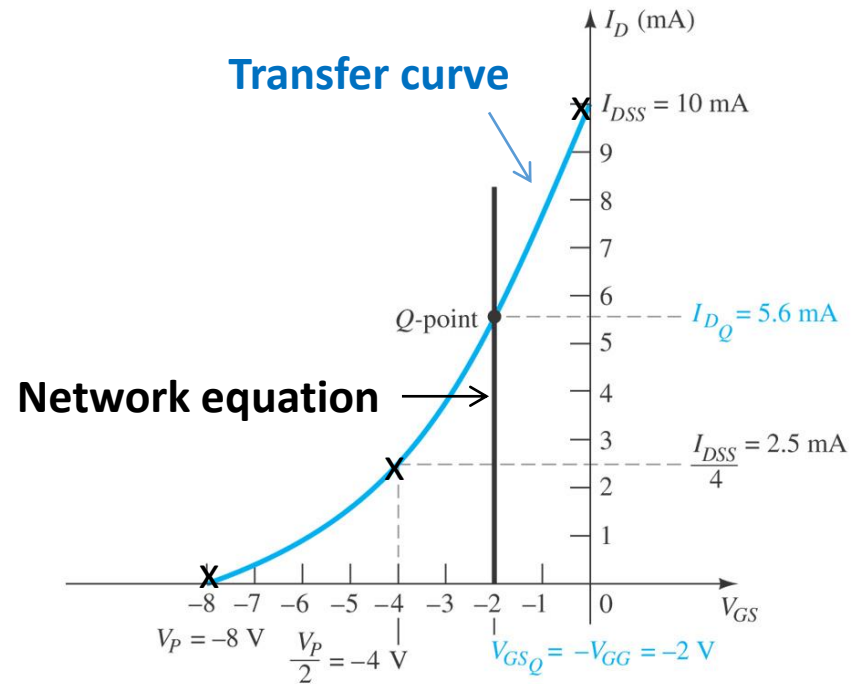
Network Equation:

$$V_{GS} = V_G - V_S = V_G - 0V$$

$$V_G = V_{GG} = -2V = V_{GSQ} \quad (\text{Fixed at } -2V)$$

Q point from the intersection of the network equation (black line) and the transfer curve (blue)

$$V_{GSQ} = -2V \text{ and } I_{DQ} = 5.6mA$$



Construction of Transfer Curve

Self- Bias Configuration

One DC supply

V_{GS} is determined by R_S

DC analysis:

$$I_G = 0\text{mA}$$

R_G can be replaced with short circuit no current flow in R_G , hence the voltage is the same on either end of R_G (ground).

$$I_D = I_S$$

$$V_{RS} = I_D R_S = V_S$$

$$V_{GS} = V_G - V_S \quad \text{but } V_G = 0\text{V}$$

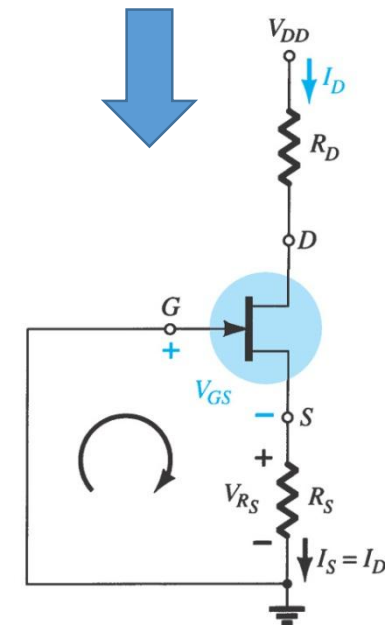
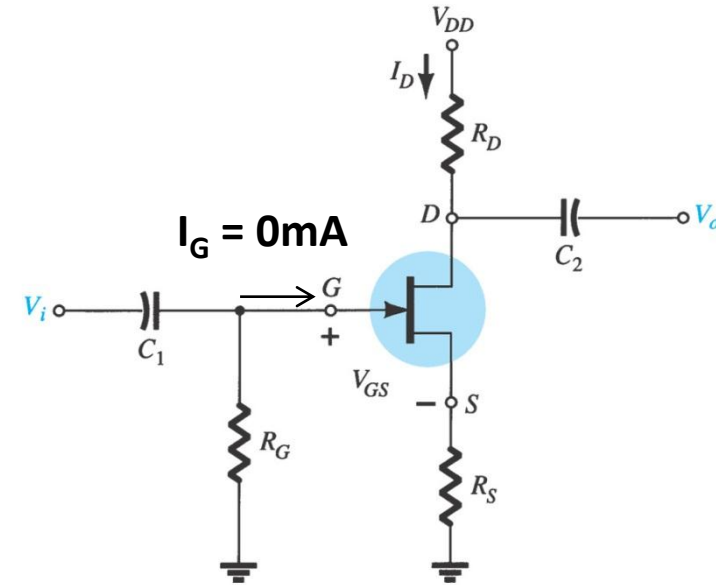
$$V_{GS} = -V_S = -I_D R_S \quad (\text{Network equation})$$

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2 \quad (\text{Transfer curve})$$

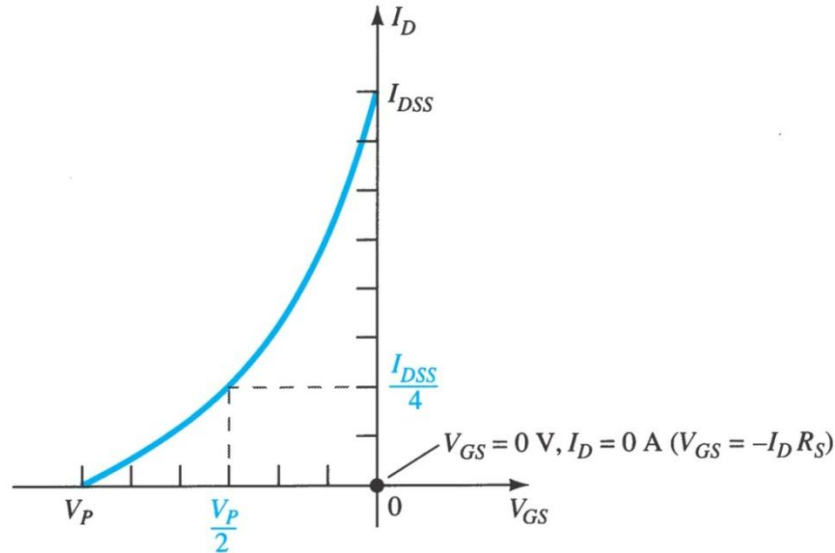
Solve Shockley equation to find I_{DQ} by substituting

$$V_{GS} = -I_D R_S$$

$$I_{DQ} = I_{DSS} \left(1 - \frac{-I_{DQ} R_S}{V_P} \right)^2$$



Graphical analysis



1. Draw the transfer curve using Shockley equation

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$$

2. Superimpose the network equation on the transfer curve;

$$V_{GS} = -I_D R_S$$

For $I_D = 0\text{ mA}$, $V_{GS} = 0\text{ V}$

1st point

For $I_D = I_{DSS}/2$

$$V_{GS} = - (I_{DSS} R_S) / 2$$

2nd point

3. From the intersection of the straight line defined by the network and transfer curve defined by Shockley equation, the operating point Q is established:

I_{DQ} and V_{GSQ} can be found.

4. From the output loop

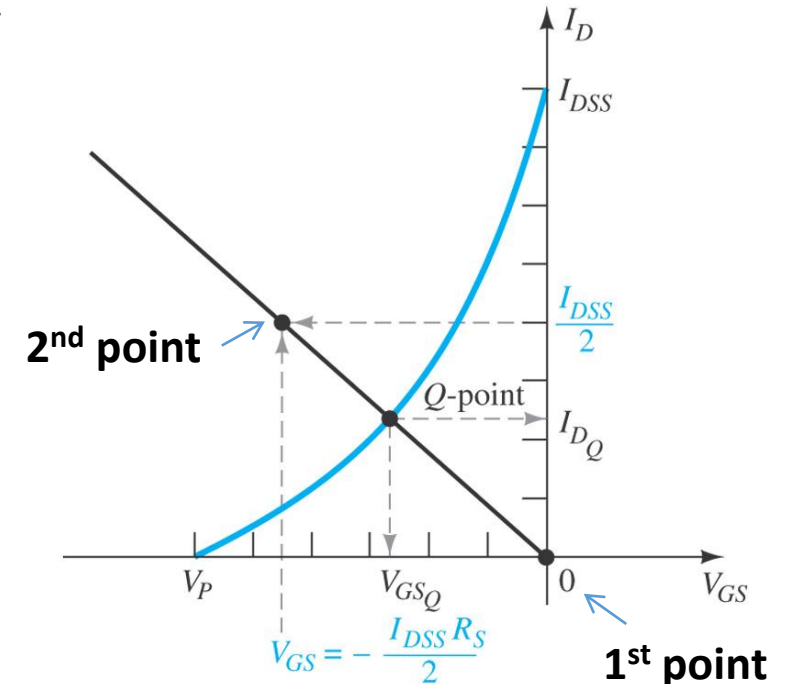
$$V_{DD} = V_{RD} + V_{DS} + V_{RS}$$

$$V_{DS} = V_{DD} - V_{RD} - V_{RS} = V_{DD} - I_D R_D - I_D R_S \quad (I_D = I_S)$$

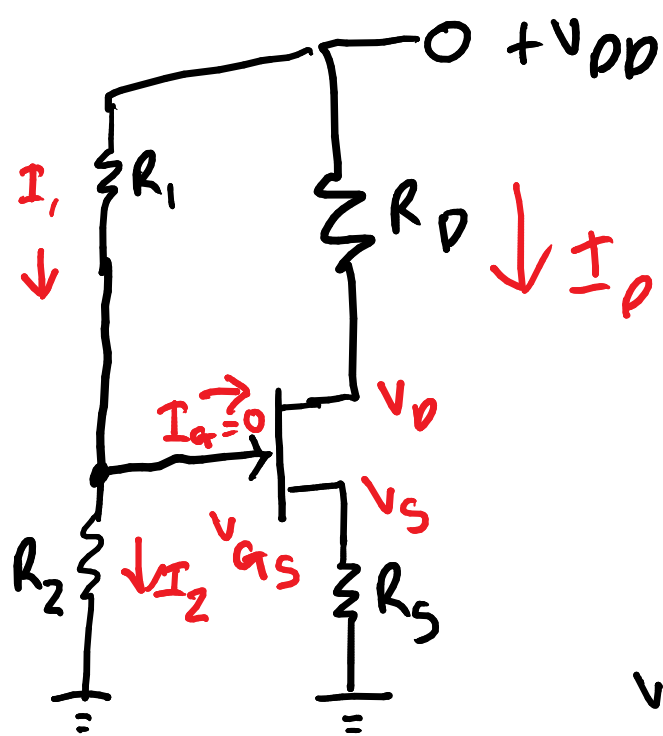
$$V_{DS} = V_{DD} - I_D (R_D + R_S)$$

$$V_S = I_D R_S, \quad V_G = 0\text{ V}$$

$$V_D = V_{DS} + V_S = V_{DD} - V_{RD}$$



Voltage Divider bias



$$V_{GS} = V_G - V_S$$

$$V_G = V_{DD} \times \frac{R_2}{R_1 + R_2}$$

$$V_S = I_D R_S$$

$$V_{GS} = V_{DD} \frac{R_2}{R_1 + R_2} - I_D R_S$$

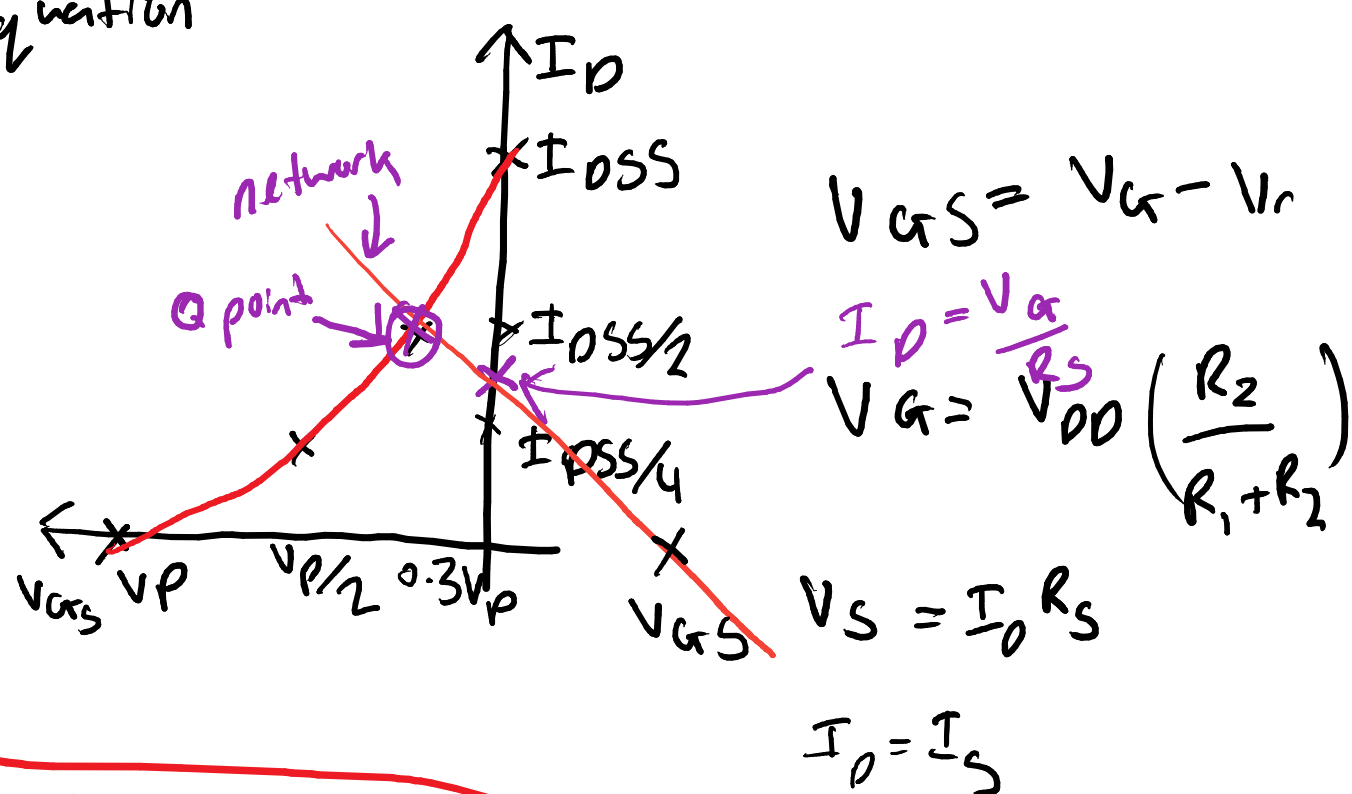
Network eq

- Operating point
- Shockley equation

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

Transfer curve

- Network equation



$$V_{GS} = V_{DD} \frac{R_2}{R_1 + R_2} - I_D R_S$$

$$V_{GS} = V_G - I_D R_S$$

for $I_D = 0$, $V_{GS} = V_G$

$$V_{GS} = 0, I_D = \frac{V_G}{R_S} *$$

$$V_{DD} = I_D R_D + V_{DS} + I_D R_S$$

$$V_{DD} = I_D (R_D + R_S) + V_{DS}$$

$$I_D = \frac{V_{DD} - V_{DS}}{R_D + R_S}$$

$$V_{DS} = V_D - I_D (R_D + R_S)$$

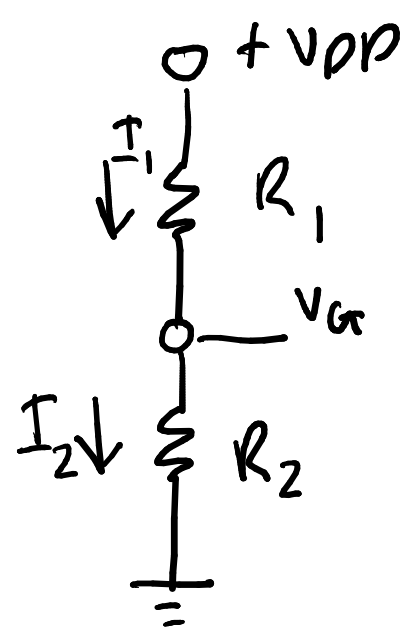
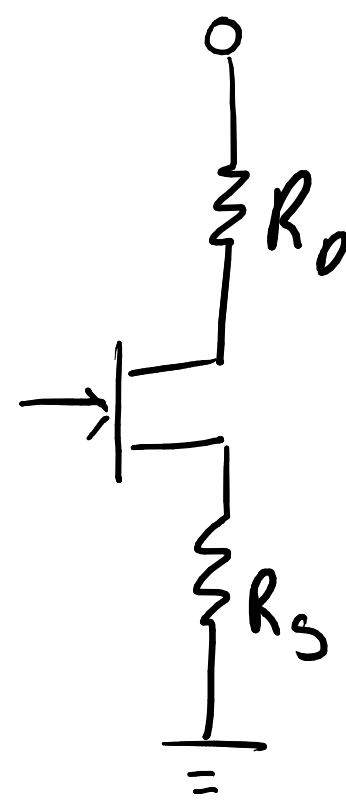
$$V_{DS} = V_D - V_S$$

$$V_D = V_{DD} - I_D R_D$$

$$V_S = I_D R_S$$

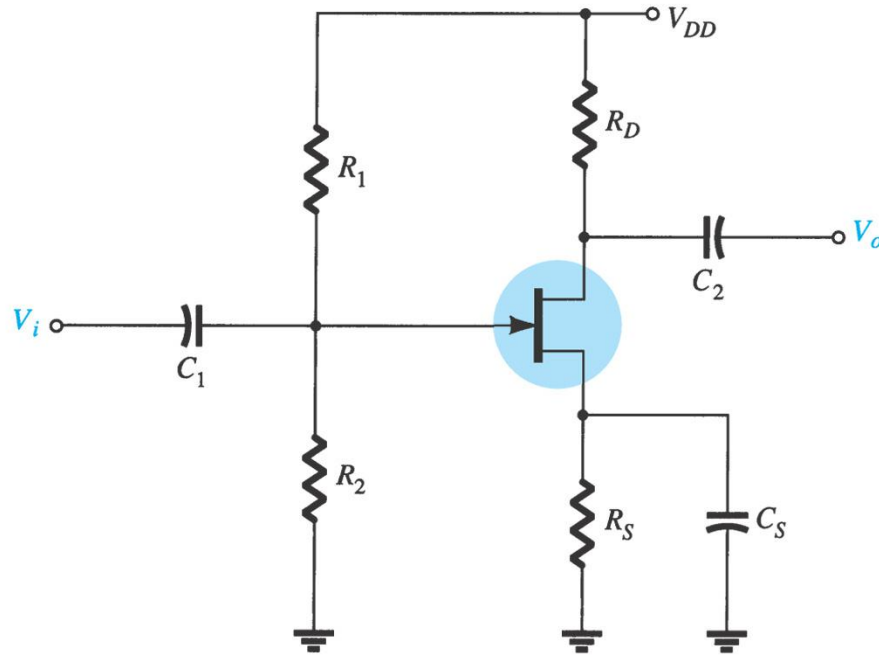
$$V_{DS} = (V_{DD} - I_D R_D)$$

$$V_{DD} = V_{DS} + I_D R_D$$



$$I_1 = I_2 = \frac{V_{DD}}{R_1 + R_2}$$

Voltage Divider Bias



$$I_G = 0\text{mA}$$

$$I_{R1} = I_{R2}$$

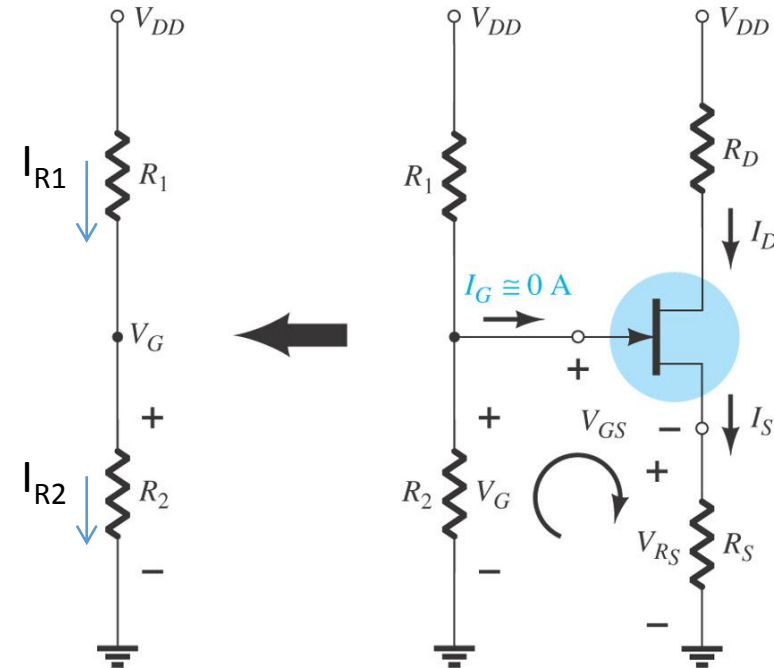
$$V_G = \frac{V_{DD} R_2}{R_2 + R_1}$$

Voltage Divider Rule

V_G is positive

$$V_{GS} = V_G - V_S$$

$$V_{GS} = V_G - I_D R_S \quad \text{Network equation}$$

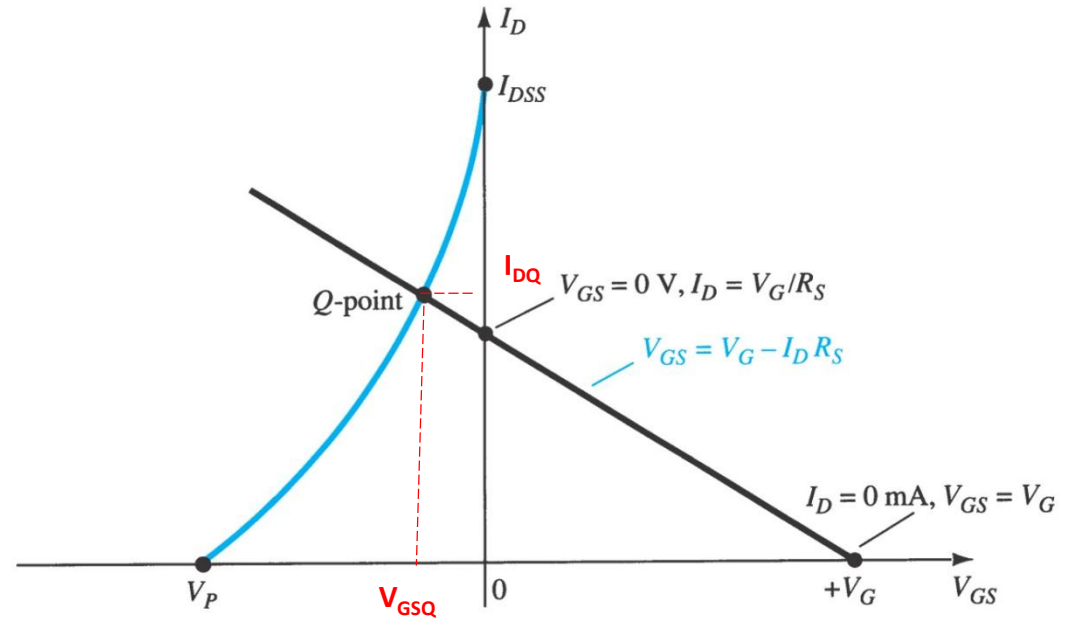


DC equivalent circuit, NO need to Thevenin's....

Transfer Curve

The operating point I_{DQ} and V_{GSQ} can be found by superimposing the *network equation* on the *transfer curve*.

1. $V_{GS} = V_G - I_D R_S$ Network Equation
2. For $I_D = 0$, $V_{GS} = V_G$ (1st point)
3. For $V_{GS} = 0V$, $I_D = V_G/R_S$ (2nd point)
4. I_{DQ} and V_{GSQ} can be found from the intersection with the transfer curve at the Q point.



Network equation and transfer curve

Output Loop:

$$V_{DS} = V_{DD} - I_D (R_D + R_S)$$

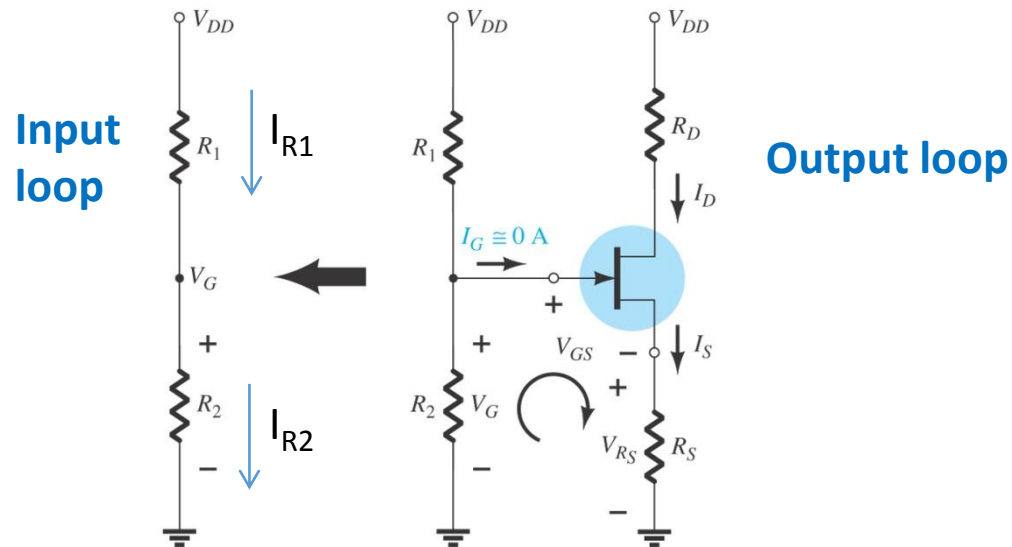
$$V_D = V_{DD} - I_D R_D$$

$$V_S = I_D R_S$$

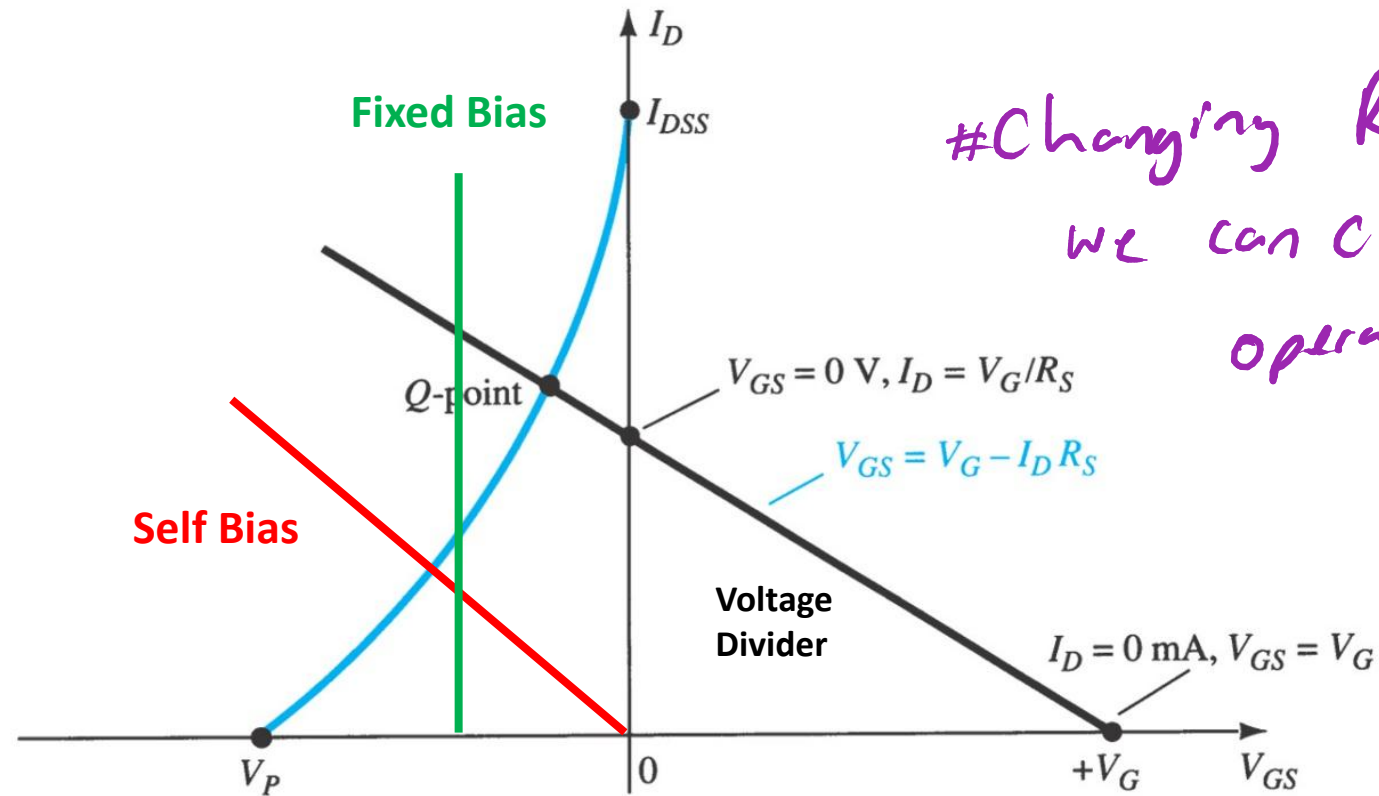
Input loop:

$$I_{R1} = I_{R2} = \frac{V_{DD}}{R_1 + R_2}$$

$$I_G = 0mA$$



Network equation and biasing configuration



#Changing R_S
we can change the
operating point.

Depletion type MOSFET biasing circuits

Same analysis as JFET

DMOSFET, n channel permit operating point with positive V_{GS} and I_D could be $> I_{DSS}$

DC analysis:

1. Draw the transfer curve using Shockley equation

For $V_{GS} = \frac{1}{2} V_P = -1.5V$

$I_D = I_{DSS}/4 = 1.5mA$

$I_D = 0$, for $V_{GS} = V_P = -3V$

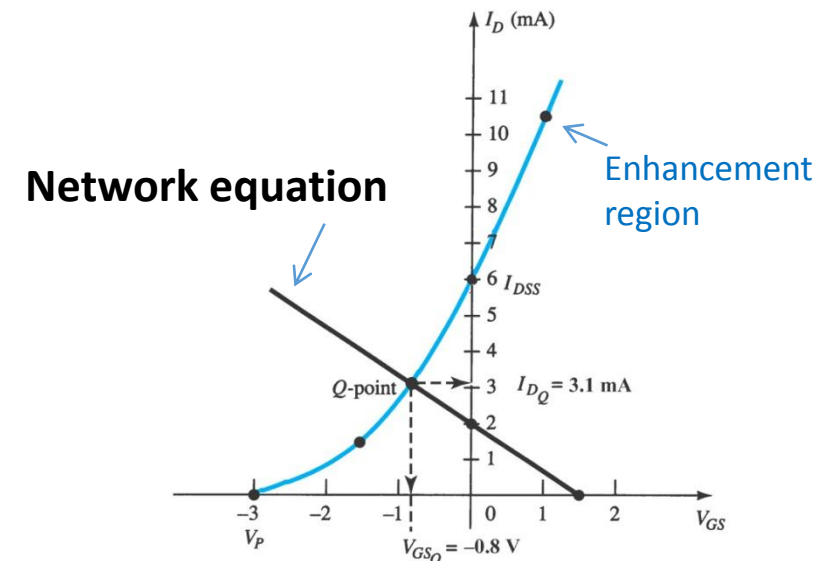
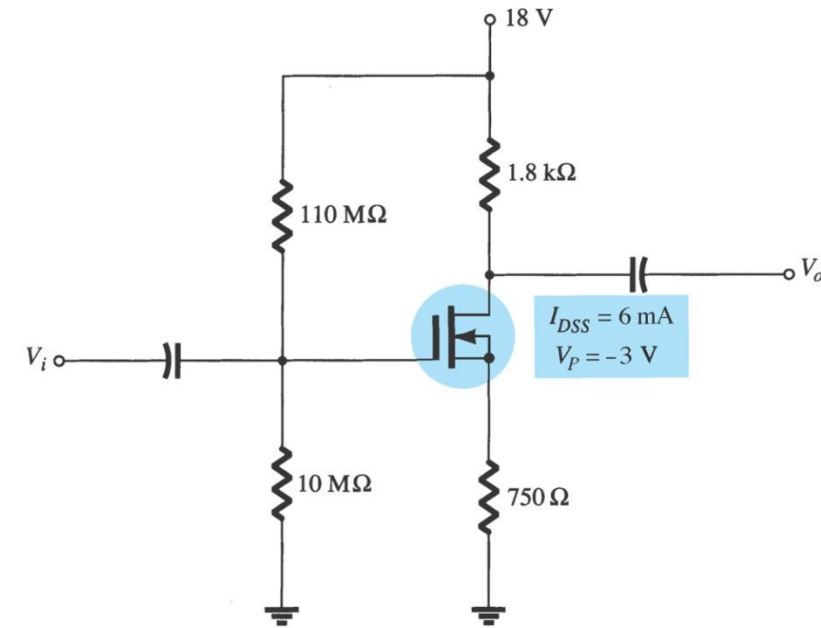
$I_D = I_{DSS}/2$, $V_{GS} = 0.3V_P = -0.9V$

$I_D = I_{DSS} = 6mA$ at $V_{GS} = 0V$

For $V_{GS} = +1V$, (enhancement region)

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$$

$$I_D = 6mA \left(1 - \frac{+1V}{-3V} \right)^2 = 10.67mA$$



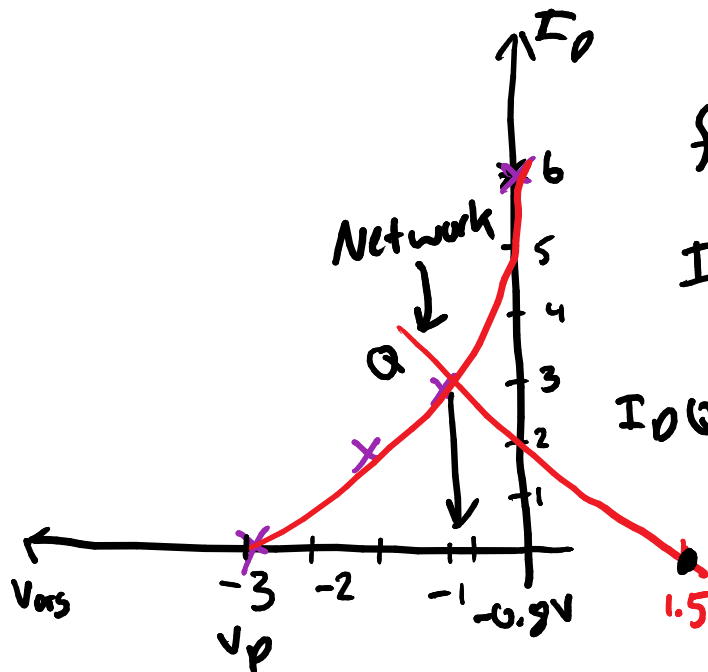
$$V_{GS} = V_G - V_S$$

$$V_G = V_{DD} \frac{R_2}{R_1 + R_2} = 19V \frac{10M}{10M + 110M}$$

$$V_G = +1.5V$$

$$V_S = I_D R_S$$

$$V_{GS} = 1.5 - I_D R_S$$



for $V_{GS} = 0$

$$I_D = \frac{1.5}{750\Omega} = 2mA$$

$$I_{DQ} = 3.1mA$$

Network equation

2. Draw the network equation

$$V_{GS} = V_G - V_S = V_G - I_D R_S$$

$$V_G = V_{DD} \frac{R_2}{R_2 + R_1} = \frac{18 \times 10M}{110M + 10M} = 1.5V$$

$$V_{GS} = 1.5 - I_D \times 750\Omega$$

Setting $I_D = 0$, $V_{GS} = V_G = 1.5V$

Setting $V_{GS} = 0$, $I_D = V_G / R_S = 1.5V / 750\Omega = 2\text{ mA}$

The intersection of the network equation with transfer curve gives the operating point:

$$I_{DQ} = 3.1\text{mA}, V_{GSQ} = 0.8V$$

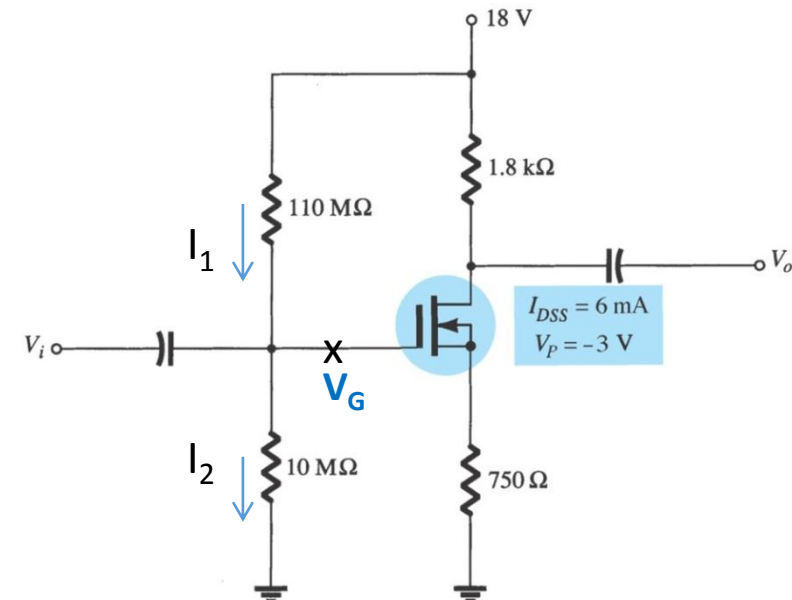
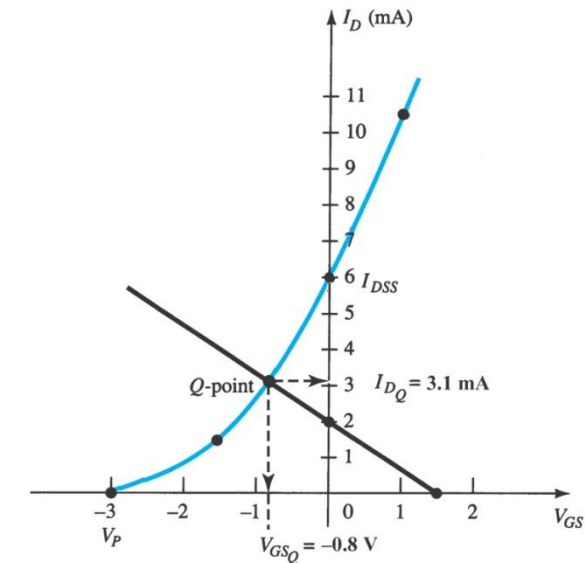
From the drain source output loop:

$$V_{DS} = V_{DD} - I_D(R_D + R_S)$$

$$V_{DS} = 18 - 3.1\text{ mA}(1.8k + 750\Omega) = 10.1\text{ V}$$

From the input loop:

$$I_1 = I_2 = \frac{18V}{110M + 10M} = 0.15\mu A$$



Enhancement type MOS biasing circuits

EMOSFET's have different transfer curve compared to JFET's and DMOSFET's

Shockley equation does not apply for EMOS.

$I_D = 0 \text{ mA}$ for $V_{GS} < V_T$

For $V_{GS} > V_T$ $I_D = k(V_{GS} - V_T)^2$

From the output characteristics

$V_{DSsat} = (V_{GS} - V_T)$

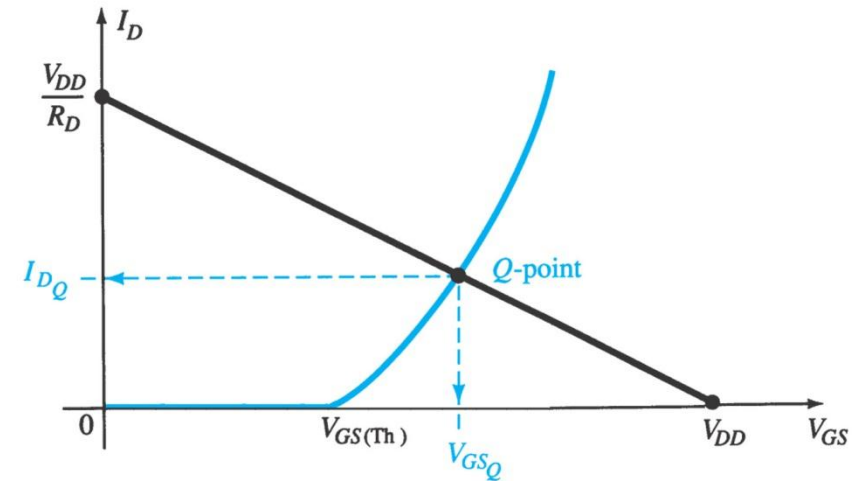
$V_{DS} > (V_{GS} - V_T)$ Saturation region

$V_{DS} < (V_{GS} - V_T)$ Ohmic Region

To draw the transfer curve V_T is provided from the data sheet, also given is $I_{D(on)}$ and $V_{GS(on)}$

Then k can be calculated from:

$$K = \frac{I_{D(on)}}{[V_{GS(on)} - V_T]^2}$$



Transfer curve(blue), load line(black) and Q point for EMOS

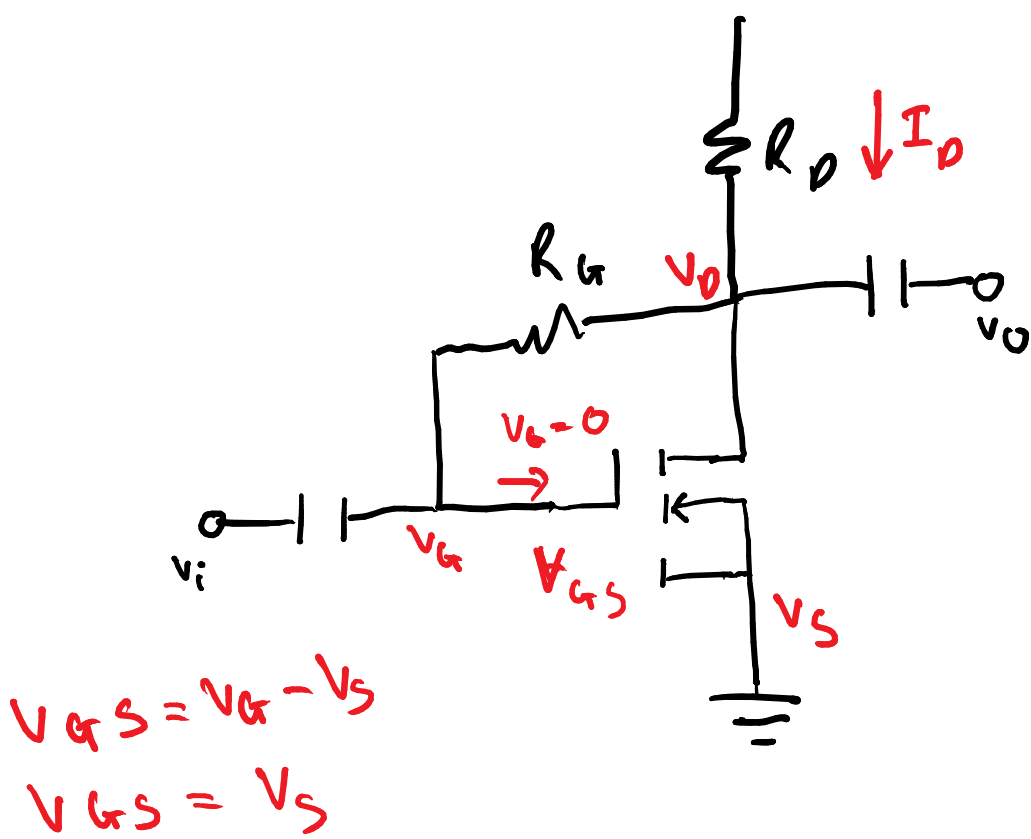
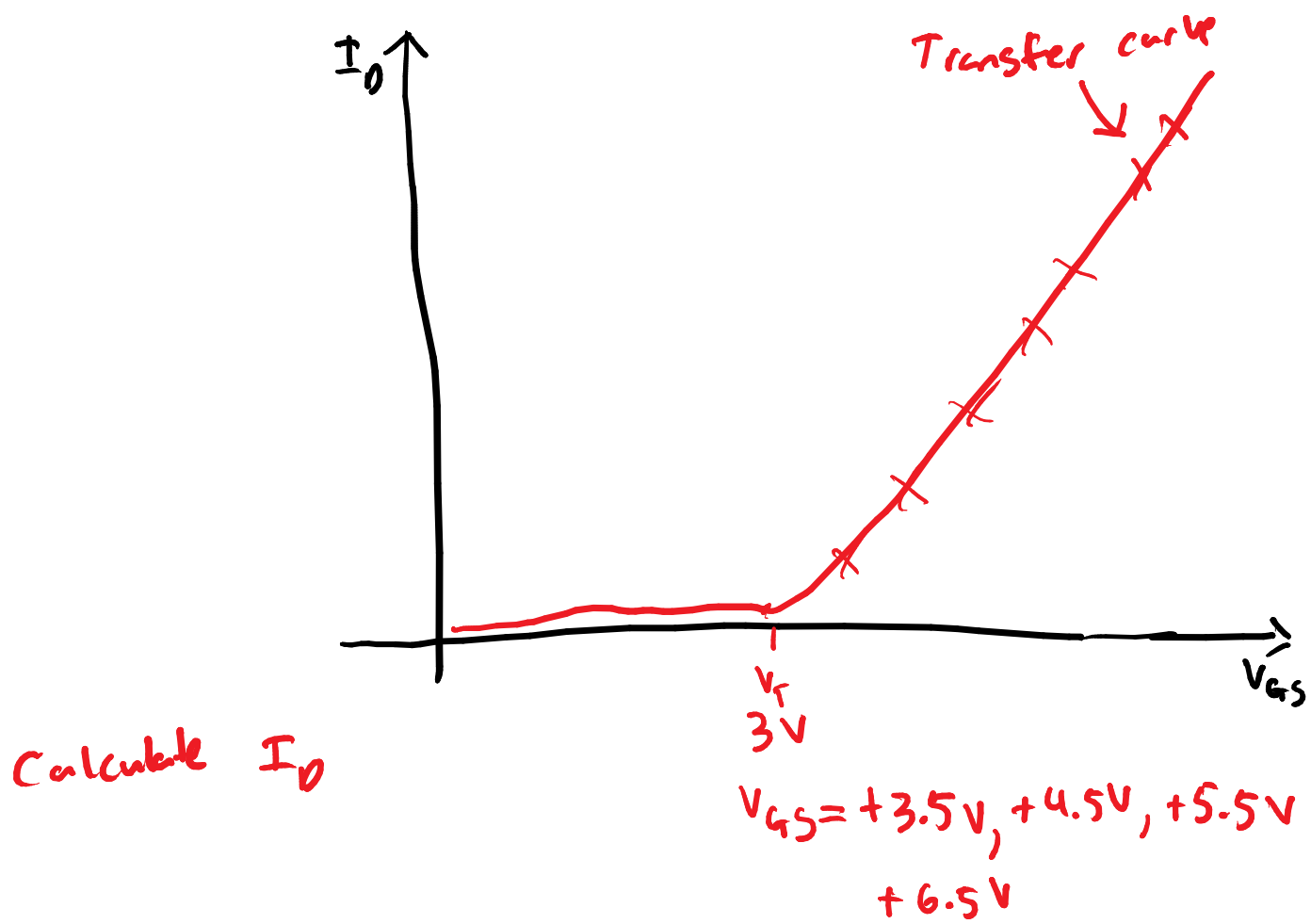
EMDSFET

Transfer curve

$$I_D = K (V_{GS} - V_T)^2$$

Both $k \in V_T$ are given by the data sheet.

for V_{GS} less than V_T , $I_D = 0$



$$V_G = V_D \text{ (no current flowing in } R_G, I_G = 0)$$

$$V_{DD} = I_D R_D + V_{DS}$$

$$V_{DS} = V_D - V_S$$

$$V_{DS} = V_D - 0$$

$$V_{DD} = I_D R_D + V_{D1}$$

$$V_{DD} = I_D R_D + V_G \quad \text{Substituting}$$

$$V_{DD} = I_D R_D + V_{GS}, \quad V_{GS} = \boxed{V_{DD} - I_D R_D}$$

network equation

$$V_{GS} = +3.5V, +4.5V, +5.5V, +6.5V$$

$$I_D = 0 \quad V_{DS} = V_{GS}$$

for $V_{GS} = 0$, $I_D = \frac{V_D n}{R_D}$

Calculate I_p

Feedback Bias for EMOS

$$I_G = 0\text{mA}$$

$$V_{RG} = 0\text{V} \quad (= I_G \cdot R_G)$$

$$V_D = V_G$$

$$V_{DS} = V_{GS} \quad (\text{no current flowing in the } 10\text{M resistor})$$

Output loop:

$$V_{DS} = V_{DD} - I_D R_D$$

$$V_{GS} = V_{DD} - I_D R_D \quad (\text{network equation})$$

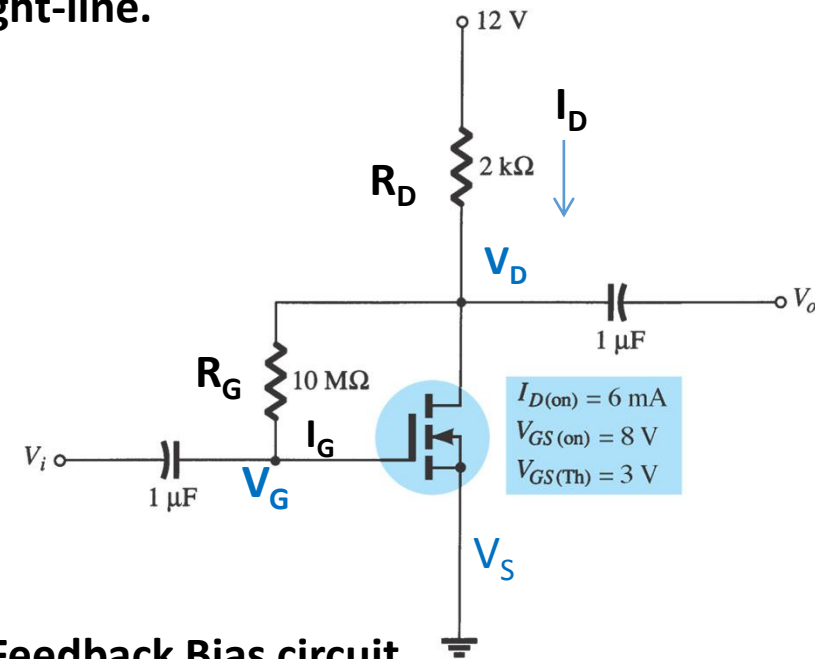
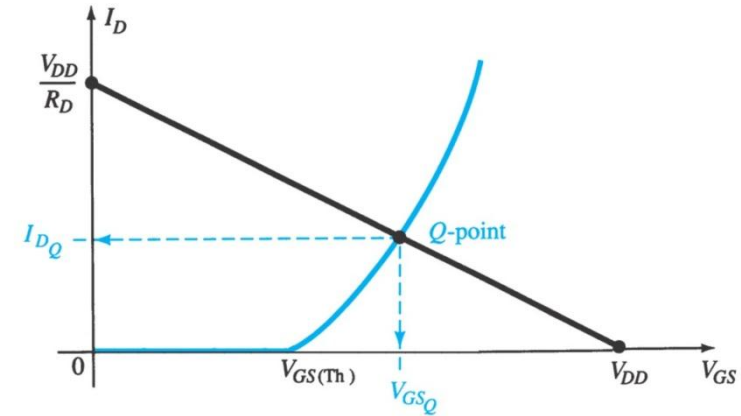
i.e. the relationship between V_{GS} and I_D is a straight-line.

Now for $I_D = 0$

$$V_{GS} = V_{DD}$$

$$\text{For } V_{GS} = 0\text{V}$$

$$I_D = \frac{V_{DD}}{R_D}$$



Feedback Bias circuit

Voltage Divider Bias

Input loop:

$I_G = 0\text{mA}$ gate is isolated

$$V_G = V_{DD} \frac{R_2}{R_2 + R_1}$$

$$V_{GS} = V_G - V_S$$

$$V_{GS} = V_G - I_D R_S$$

Network equation

$$I_D = k(V_{GS} - V_T)^2$$

Transfer curve

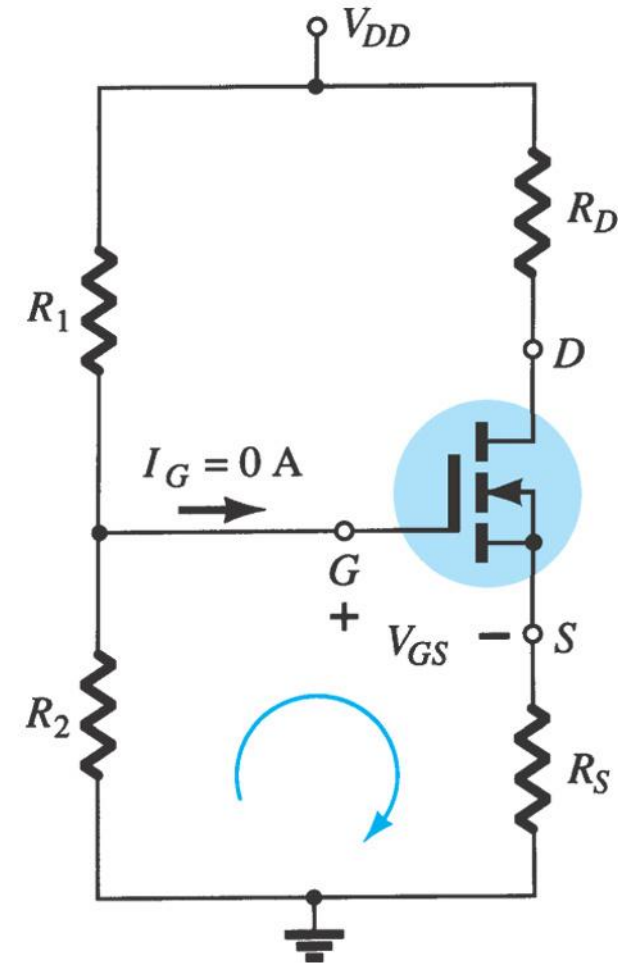
Substitute for V_{GSQ} from network equation into the transfer curve equation to find I_{DQ}

$$I_{DQ} = k \{ (V_G - I_{DQ} R_S) - V_T \}^2$$

Output loop:

$$V_{DD} - V_{RD} - V_{DS} - V_{RS} = 0$$

$$V_{DS} = V_{DD} - I_D (R_D + R_S)$$



EMOSFET biasing circuit