

Reinforcement Learning

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Reinforcement Learning In Python Course

1 Introduction

SAR:

- Start in state S_t
- Apply action A_t
- Get reward R_{t+1}

SAS:

- Start in state S_t
- Apply action A_t
- Move to state S_{t+1}

2 Return of the Multi-Armed Bandit

Explore-Exploit Strategies:

Epsilon-Greedy:

Constant exploration ratio throughout entire game. Thus, choosing to learn quickly comes at a cost in long games and vice versa.

Algorithm 1 Epsilon-Greedy Explore-Exploit Strategy

```
1: for turn do
2:   draw a random  $p \in [0,1]$ 
3:   if  $p < \epsilon$  then
4:     Explore: play some random bandit and update its predicted  $p$ 
5:   else
6:     Exploit: play the best bandit and update its predicted  $p$ 
7:   end if
8: end for
```

Efficient Mean Update:

$$\bar{X}_N = \frac{N-1}{N} \bar{X}_{N-1} + \frac{1}{N} X_N$$

Optimistic Initial Value :

By initially setting all predicted means to the upper limit, and then playing exploits-only, this strategy explores the least explored bandits first as they will have the highest predicted probabilities. We will stop exploring once the best bandit is discovered so we will not pay for unnecessary exploration late in the game.

Algorithm 2 Optimistic Initial Value Explore-Exploit Strategy

```
1: Set all initial predicted probabilities to the max possible value
2: for turn do
3:   Exploit: play the best bandit and update its predicted  $p$ 
4: end for
```

Chernoff-Hoeffding Bound:

$$P[|\bar{X} - \mu| \geq \epsilon] \leq 2(e^{-2\epsilon^2 N})$$

UCB1:

Play exploits only with respect to:

$$X_{UCB-j} = \bar{X}_j + \sqrt{2 \frac{\ln(N)}{N_j}}$$

Initially we tend to explore the least explored bandits, but as the game goes on we rely more highly on the predicted mean we have arrived at.

Thompson Sampling: