

MATH 22AL

LAB # 10

8 Sum, Difference and Product of Complex Numbers

If $c_1 = a_1 + ib_1$ and $c_2 = a_2 + ib_2$ then the **sum** of c_1 and c_2 is

$$c_1 + c_2 = (a_1 + a_2) + i(b_1 + b_2)$$

and their **difference** is

$$c_1 - c_2 = (a_1 - a_2) + i(b_1 - b_2)$$

.

The **product** of $c_1 = a_1 + ib_1$ and $c_2 = a_2 + ib_2$ in Rectangular coordinates is given by

$$c_1 c_2 = (a_1 + ib_1)(a_2 + ib_2) = (a_1 a_2 - b_1 b_2) + i(a_1 b_2 + a_2 b_1)$$

The **product** of $c_1 = r_1(\cos \theta_1 + i \sin \theta)$ and $c_2 = r_2(\cos \theta_2 + i \sin \theta_2)$ in Polar coordinates is given by

$$c_1 c_2 = r_1 r_2 [\cos(\theta_1 + \theta_2) + i \sin(\theta_1 + \theta_2)]$$

type	$c10 = -1 - i$	
type	$c11 = 7 + 2i$	
type	$c12 = 3 - i$	

type	$z_1 = c10 + c11$	
type	$z_2 = c10 - c11$	
type	$z_3 = c10 * c11$	

type	$\text{imag}(c11)$	
type	$\text{real}(c11)$	

Exercise 3: Let $c16 = 3cis(0.7)$ and $c17 = 2cis(1.2)$ (recall that the angles are in radians) :

- Find a complex number $z16 = rcis(\theta)$ such that $(z16)(c16) = 1cis(0)$
- Find a complex number $z17 = rcis(\theta)$ such that $(z17)(c17) = 1cis(0)$
- Find a complex number $z18 = rcis(\theta)$ such that $(z18)(rcis(\theta)) = 1cis(0)$