

Start Typing in MATLAB

16 Exercise 3

3.1) Enter the matrix $A2 = \begin{bmatrix} 1 & 0 & 2 & 3 \\ 4 & -1 & 0 & 2 \\ 0 & -1 & -8 & -10 \end{bmatrix}$

Find a basis for $\text{null}(A2)$, you may use the ones from the previous section or compute it again. Call these vectors $N1$ and $N2$.

Recall that any linear combination of the basis vectors will be in the subspace.

That means $k1 * N1 + k2 * N2$ should be in the null-space of $A2$ no matter what $k1$ and $k2$ are. so $A2(k1 * N1 + k2 * N2) = 0$.

We can demonstrate this with the following commands:

for $i = 1:10$, $k1 = \text{round}(10 * \text{rand}(1))$; $k2 = -\text{round}(10 * \text{rand}(1))$;

$V(:,i) = k1 * N1 + k2 * N2$;

$AV(:,i) = A2 * V(:,i)$;

end

Explanation: The `rand` function gives numbers between zero and 1 so multiplying by 10 and rounding off gives integers between zero and 10. Thus $k1$ and $k2$ are randomly chosen numbers.

Each column of the matrix V is a vector which is a linear combination of our basis vectors $N1$ and $N2$. The corresponding column in AV is the vector $A2 * (\text{that column of } V)$.

Claim AV should be a matrix of zeros.

Type	$A2V = AV$
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to check what the loop did.

Wow! It works! All of the columns of V are in the null-space of $A2$!

3.2) Which of the following vectors are in the null-space of $A2$? (you need to enter these vectors in MATLAB as matrices, column vectors).

- $v1 = (5, -35, 81, 2)$
- $v2 = (38, 104, 17, -24)$
- $v3 = (-9, -26, -3, 5)$
- $v4 = (1, 0, 1, 1)$

Use MATLAB, then type the following and enter your answer in the following format:

If you decided $v1$ is in the null-space of $A2$ type :

type	<code>% A2v1= is in null(A2)</code>
otherwise type	<code>% A2v1= is NOT in null(A2)</code>