

Tutorial #13

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Deep Q-learning

- Recall the Bellman equations for

(i) Value function:

$$V(s) = \max_{a \in \mathcal{A}} \mathbb{E} \left[r(a, s, s') + \gamma V(s') \right]$$

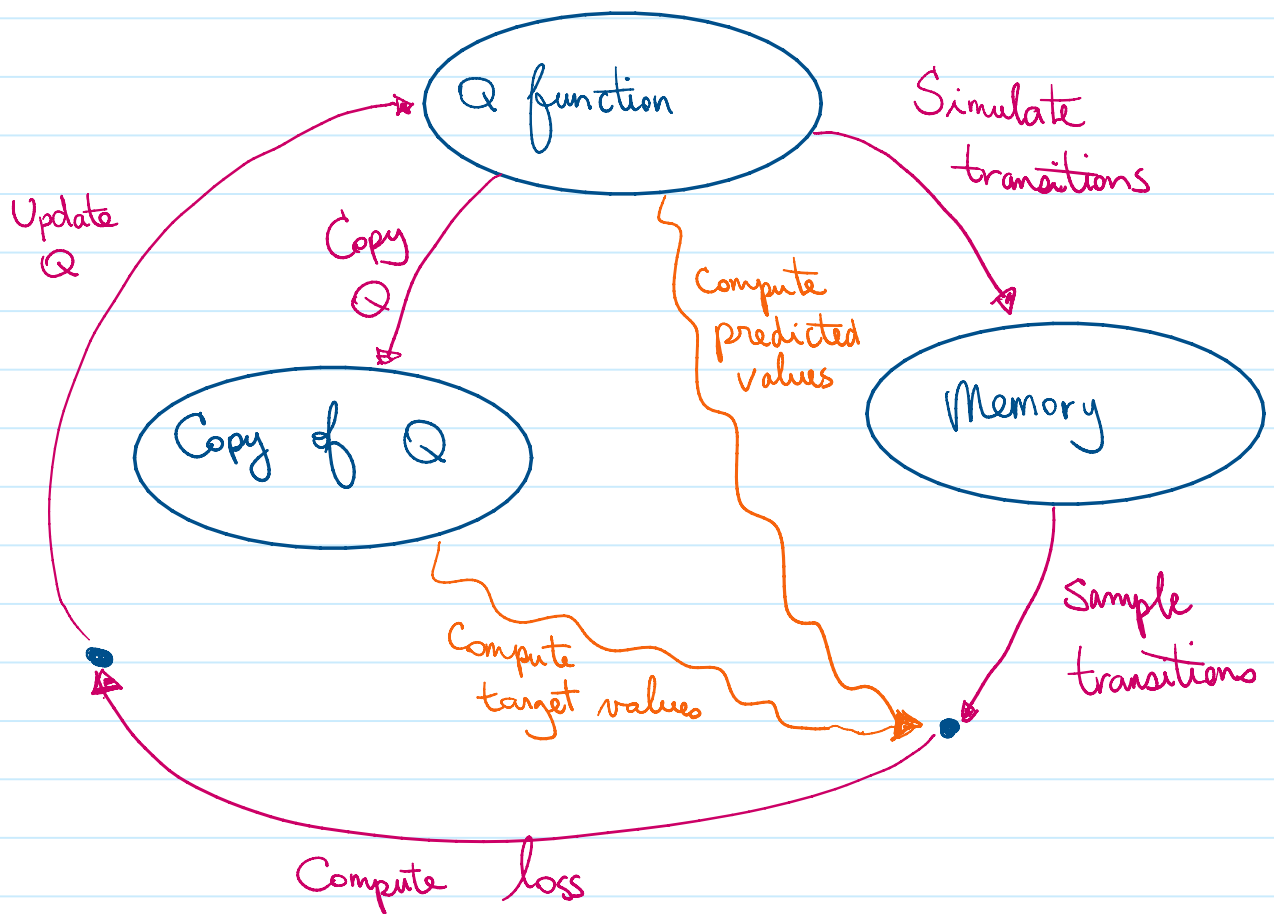
(ii) Q function:

$$Q(s, a) = \mathbb{E} \left[r(a, s, s') + \gamma V(s') \right]$$

$$= \mathbb{E} \left[r(a, s, s') + \gamma \max_{a' \in \mathcal{A}'} Q(s', a') \right].$$

- We want to use the Q-function (as a neural network) to find the best policy.

Representation of the algorithm



More details on deep Q-learning

- Q function (main and target networks):

ANN with state dimension as inputs and number of actions as outputs, to give

$$Q(s, a^{(1)}), Q(s, a^{(2)}), \dots, Q(s, a^{(|A|)}).$$

- Memory : a replay buffer with a fixed size to store & sample transitions (S_t, a_t, R_t, S_{t+1})
- Simulate transitions :
 - ϵ -greedy policy, where we select the best action (with respect to the Q function) with probability $1-\epsilon$, and a random action with probability ϵ . It allows exploration & exploitation.
- Predicted Q value : $Q(S_t, a_t)$
- Target Q value : $R_t + \gamma \max_{a' \in A} Q(S_{t+1}, a')$
- Update loss : Mean squared error between the predicted and target values.
- Other implementation details :
 - frequency of the copy of Q as the target network.
 - decay the ϵ in the ϵ -greedy.
 - mini-batch size when sampling transitions from the memory.
 - select only valid actions.