Database Assignment #1

Top-k Query Processing

PPT source - Sanjay Kulhari

Objects, Attributes and Scores

- Each object X_i has m scores $(r_{i1}, r_{i2}, \ldots, r_{im})$, one for each of m attributes.
- Objects are listed, for each attribute sorted by score.
- Each object is assigned an overall score by combining the attribute score using aggregate function or combining rule.
- Aim: Determine k objects with the highest overall score.

	R_1	R_2	R_3
X_1	1	0.3	0.2
X_2	0.8	0.8	0
X_3	0.5	0.7	0.6
X_4	0.3	0.2	0.8
X_5	0.1	0.1	0.1

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Querying Fuzzy Data - Example

- **Given the following relational structure**

	R_1	R_2	R_3
X_1	1	0.3	0.2
X_2	0.8	0.8	0
X_3	0.5	0.7	0.6
X_4	0.3	0.2	0.8
X_5	0.1	0.1	0.1

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

- **Query: Select top-2 for the sum aggregate function**
  Monotonicity property: An aggregation function t is monotone
  - if $t(x_1, \ldots, x_m) \leq t(x'_1, \ldots, x'_m)$ whenever $x_i \leq x'_i$ for every i.

Naïve Algorithm

- **1. Compute overall score for every object by looking into each sorted list.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Naïve Algorithm

- **1. Compute overall score for every object by looking into each sorted list.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

X_1	1.5

Naïve Algorithm

- **1. Compute overall score for every object by looking into each sorted list.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

X_1	1.5
X_2	1.6

Naïve Algorithm

- **1. Compute overall score for every object by looking into each sorted list.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

X_1	1.5
X_2	1.6
X_3	1.8

Naïve Algorithm

- **1. Compute overall score for every object by looking into each sorted list.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

X_1	1.5
X_2	1.6
X_3	1.8
X_4	1.3

Naïve Algorithm

- **1. Compute overall score for every object by looking into each sorted list.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

X_1	1.5
X_2	1.6
X_3	1.8
X_4	1.3
X_5	0.3

Naïve Algorithm

- **2. Return *k* objects with the highest overall score.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

X_3	1.8
X_2	1.6
X_1	1.5
X_4	1.3
X_5	0.3

Return top-2 objects

Fagin's Algorithm

Fagin's Algorithm

- **1. Sequentially access all the sorted lists in parallel until there are k objects that have been seen in all lists.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Fagin's Algorithm

- **1. Sequentially access all the sorted lists in parallel until there are k objects that have been seen in all lists.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Fagin's Algorithm

- **1. Sequentially access all the sorted lists in parallel until there are k objects that have been seen in all lists.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Fagin's Algorithm

- **1. Sequentially access all the sorted lists in parallel until there are k objects that have been seen in all lists.**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Since $k = 2$, and X_1 and X_3 have been seen in all the 3 lists

Fagin's Algorithm

- **2. Perform random accesses to obtain the scores of all seen objects**

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Fagin's Algorithm

- 3. Compute score for all objects and return the top-k

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

X_3	1.8
X_2	1.6
X_1	1.5
X_4	1.3

Return top-2 objects

Threshold Algorithm

Threshold Algorithm

- 1. Access the elements sequentially

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

Threshold Algorithm

- **At each sequential access**
  - (a) Set the threshold t to be the aggregate of the scores seen in this access.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

t = 2.6

Threshold Algorithm

- **At each sequential access**
  - (b) Do random accesses and compute the scores of the seen objects.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

t = 2.6

X_1	1.5
X_2	1.6
X_4	1.3

Threshold Algorithm

- **At each sequential access**
  - (c) Maintain a list of top-k objects seen so far

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

t = 2.6

X_2	1.6
X_1	1.5

Threshold Algorithm

- **At each sequential access**
  - (d) Stop, when the scores of the top-k are greater or equal to the threshold.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

t = 2.1

X_3	1.8
X_2	1.6

Threshold Algorithm

- **At each sequential access**
  - (d) Stop, when the scores of the top-k are greater or equal to the threshold.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

t = 1

X_3	1.8
X_2	1.6

Threshold Algorithm

- 2. Return the top-k seen so far

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

t = 1

Return the objects

X_3	1.8
X_2	1.6

No Random Access Algorithm

No Random Access Algorithm

- 1. Access sequentially all lists in parallel until there are k objects for which the lower bound is higher than the upper bound of all other objects.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

	LB	UB
X_1	1	2.6
X_2	.8	2.6
X_4	.8	2.6

No Random Access Algorithm

- 1. Access sequentially all lists in parallel until there are k objects for which the lower bound is higher than the upper bound of all other objects.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

	LB	UB
X_2	1.6	2.2
X_3	1.3	2.1
X_1	1	2.3
X_4	0.8	2.3

No Random Access Algorithm

- 1. Access sequentially all lists in parallel until there are k objects for which the lower bound is higher than the upper bound of all other objects.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

	LB	UB
X_3	1.8	1.8
X_2	1.6	1.8
X_1	1.5	1.5
X_4	0.8	1.6

No Random Access Algorithm

- 2. Return top-k objects for which the lower bound is higher than the upper bound of all other objects.

	R_1
X_1	1
X_2	0.8
X_3	0.5
X_4	0.3
X_5	0.1

	R_2
X_2	0.8
X_3	0.7
X_1	0.3
X_4	0.2
X_5	0.1

	R_3
X_4	0.8
X_3	0.6
X_1	0.2
X_5	0.1
X_2	0

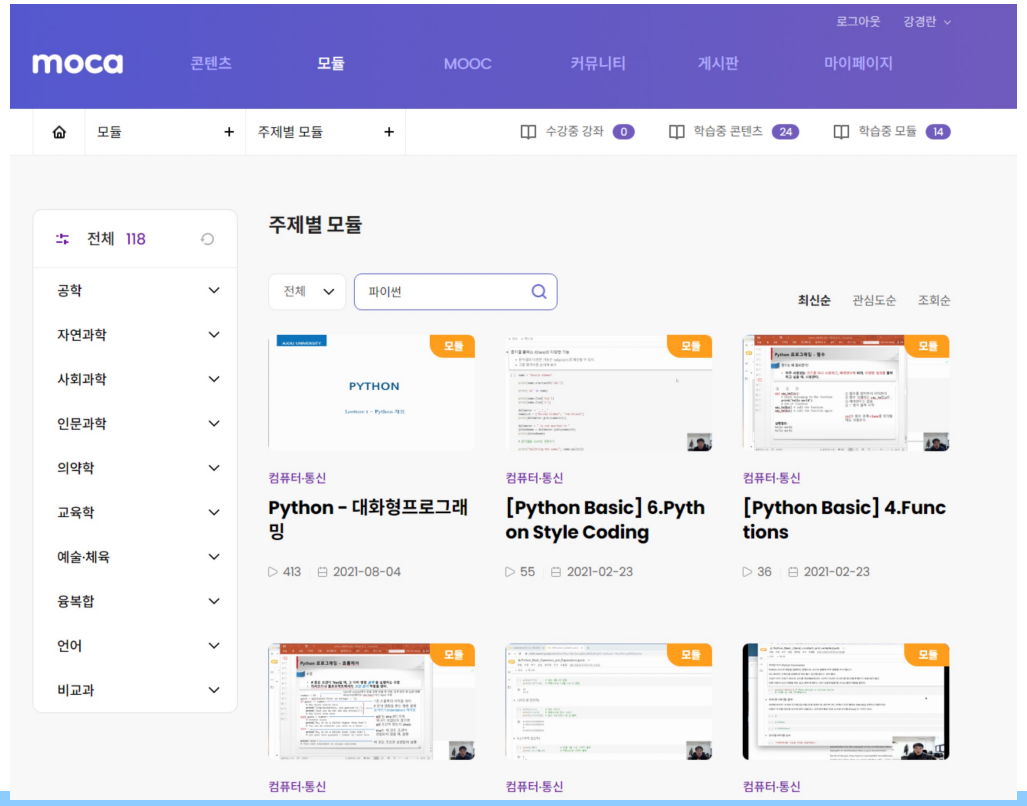
	LB	UB
X_3	1.8	1.8
X_2	1.6	1.8
X_1	1.5	1.5
X_4	0.8	1.6

Return top-2 objects

Tips for Assignment #2

Python

- https://moca.ajou.ac.kr
- 신승훈 교수님 & 최재영 교수님의 python 강의 동영상



Structure

- **202312345**
  - **compare_alg.py**
  - sorted_score_0.txt
  - …
  - sorted_score_9.txt
  - **topk.py**

Raw Data File (sorted_score_0.txt)

```
id_4268 99.99
id_1494 99.98
id_3640 99.95
id_8139 99.94
id_8484 99.93
id_9715 99.93
id_1544 99.91
id_5128 99.91
id_4337 99.9
id_5227 99.89
id_2302 99.88
id_4321 99.88
id_1739 99.87
id_2272 99.87
id_8232 99.86
id_9120 99.84
id_2575 99.8
id_4863 99.8
id_6839 99.79
```

compare_alg.py

```python
from collections import defaultdict

# D-dimensional sorted lists of pair(user_id, score)
def read_sorted_files(num_dim):
    list_sorted_entities = []
    uid2dim2value = defaultdict(dict)
    for dim in range(num_dim):
        sorted_entities = []
        with open("sorted_score_{}.txt".format(dim), "r", encoding="utf-8") as f:
            for line in f:
                words = line.strip().split("\t")
                if len(words) != 2:
                    continue
                uid = words[0]
                score = float(words[1])
                sorted_entities.append((uid,score))
                uid2dim2value[uid][dim] = score
        list_sorted_entities.append(sorted_entities)

    return list_sorted_entities, uid2dim2value
```

compare_alg.py

```
32  # you can use print_head method to understand "list_sorted_entities" variable
33  def print_head(list_sorted_entities):
34      print("shape of list_sorted_entities")
35      for dim in range(len(list_sorted_entities)):
36          print("Dim: {}".format(dim))
37          line = "\t"
38          for e in list_sorted_entities[dim][:3]:
39              line += "{}, ".format(e)
40          line += " ... "
41          print(line)
42      print("-----------------")
```

compare_alg.py

```python
def compare_algorithms(num_dim, top_k, list_sorted_entities_all, uid2dim2value):
    list_sorted_entities = list_sorted_entities_all[:num_dim]
    #print_head(list_sorted_entities)
    myTopk = topk.Algo(list_sorted_entities, uid2dim2value)

    uids_Naive, cnt_Naive = myTopk.Naive(num_dim, top_k)
    uids_Fagin, cnt_Fagin = myTopk.Fagin(num_dim, top_k)
    uids_TA, cnt_TA = myTopk.TA(num_dim, top_k)
    uids_NRA, cnt_NRA = myTopk.NRA(num_dim, top_k)

    print("Dim: {}, Top-K: {}".format(num_dim, top_k))
    if compare_results(uids_Naive, uids_Fagin) == False:
        print("!!Error in Fagin")
    if compare_results(uids_Naive, uids_TA) == False:
        print("!!Error in TA")
    if compare_results(uids_Naive, uids_NRA) == False:
        print("!!Error in NRA")

    print("\tNaive:\t{}".format(cnt_Naive))
    print("\tFagin:\t{}".format(cnt_Fagin))
    print("\tTA:\t{}".format(cnt_TA))
    print("\tNRA:\t{}".format(cnt_NRA))

if __name__ == "__main__":
    list_sorted_entities_all, uid2dim2value = read_sorted_files(10)
    compare_algorithms(2, 3, list_sorted_entities_all, uid2dim2value)
    compare_algorithms(3, 3, list_sorted_entities_all, uid2dim2value)
    compare_algorithms(5, 10, list_sorted_entities_all, uid2dim2value)
```

topk.py

```
1. Replace folder name "202312345" with your student !!
   !!WARNING!! you will get 0 score,
   if your folder name is "202312345"
2. Implement Fagin method
3. Implement TA method
4. Implement NRA method
```

topk.py

```
 9  Input: num_dim, top_k
10      num_dim: Number of dimension
11      top_k: Variable k in top-'k' query
12  Output: uids_result, cnt_access
13      uid_result: Result of top-k uids of the scores.
14                  The summation function is used
15                  for the score function.
16
17                  i.e., num_dim = 4, k = 2
18                  ---------------------------
19                   uid    D0   D1    D2    D3
20                  ---------------------------
21                  "001"    1    1     1     1
22                  "002"    2    2     2     2
23                  "003"    3    3     3     3
24                  "004"    5    5     5     5
25                  ---------------------------
26
27                  score("001") = 1 + 1 + 1 + 1 = 4
28                  score("002") = 2 + 2 + 2 + 2 = 8
29                  score("003") = 3 + 3 + 3 + 3 = 12  --> top-2
30                  score("004") = 4 + 4 + 4 + 4 = 16  --> top-1
31
32                  uids_result: ["004", "003"]
```

topk.py [get_score]

```
39  from collections import defaultdict
40  from typing import Tuple
41
42  def get_score(list_values) -> float:
43      result = 0.0
44      for v in list_values:
45          result += v
46      return result
```

topk.py [random_access]

```
48  class Algo():
49      def __init__(self, list_sorted_entities, uid2dim2value):
50          self.list_sorted_entities = list_sorted_entities
51
52          '''
53          variable for random access,
54          but please do not use this variable directly.
55          If you want to get the value of the entity,
56          use method 'random_access(uid, dim)'
57          '''
58          self.__uid2dim2value__ = uid2dim2value
59
60      def random_access(cls, uid, dim) -> float:
61          return cls.__uid2dim2value__[uid][dim]
```

topk.py [Naive: gift]

```python
    def Naive(cls, num_dim, top_k) -> Tuple[list, int]:
        uids_result = []
        cnt_access = 0

        # read all values from the sorted lists
        uid2dim2value = defaultdict(dict)
        for dim in range(num_dim):
            for uid,value in cls.list_sorted_entities[dim]:
                uid2dim2value[uid][dim] = value
                cnt_access += 1

        # compute the score and sort it
        uid2score = defaultdict(float)
        for uid, dim2value in uid2dim2value.items():
            list_values = []
            for dim in range(num_dim):
                list_values.append(dim2value[dim])
            score = get_score(list_values)
            uid2score[uid] = score

        sorted_uid2score = sorted(uid2score.items(), key = lambda x : -x[1])

        # get the top-k results
        for i in range(top_k):
            uids_result.append(sorted_uid2score[i][0])

        return uids_result, cnt_access
```

topk.py [To Do]

```python
    # Please use random_access(uid, dim) for random access
    def Fagin(cls, num_dim, top_k) -> Tuple[list, int]:
        uids_result = []
        cnt_access = 0

        return uids_result, cnt_access

    # Please use random_access(uid, dim) for random access
    def TA(cls, num_dim, top_k) -> Tuple[list, int]:
        uids_result = []
        cnt_access = 0

        return uids_result, cnt_access

    # You cannot use random access in this method
    def NRA(cls, num_dim, top_k) -> Tuple[list, int]:
        uids_result = []
        cnt_access = 0

        return uids_result, cnt_access
```