

1.  $\frac{1}{2}$  point for right answer,  $-\frac{1}{2}$  point for wrong answer

- a) every non-greedy action is chosen with probability  $\frac{\epsilon}{n}$ , where  $n$  is number of actions
- b) each action is at least picked with probability  $\frac{\epsilon}{n}$
- c) Q-Learning has a maximization bias problem
- d) Q-Learning is on-policy learning
- e) episodic tasks can be transformed to non episodic tasks
- f) TD-learning can learn before episode terminates
- g) Inverse RL tries to learn the transition function
- h) Value function of Sarsa converges to optimal value function if all state-action pairs are infinitely often visited
- i) Value iteration converges after one step for any MDP if  $\gamma=1$
- j) Monte Carlo is non-applicable on non-episodic tasks

## 2. Bandits

a) 3 actions,  $p(a_1) = 0.6$ ,  $p(a_2) = p(a_3) = 0.2$

Find Action Function for  $Q(a_1)$ ,  $Q(a_2)$  and for  $\epsilon$

b) For arbitrary distribution  $p_1, p_2, p_3$ , can  $\epsilon$  and  $Q$ -Functions be represented?

Give a proof or a counter example

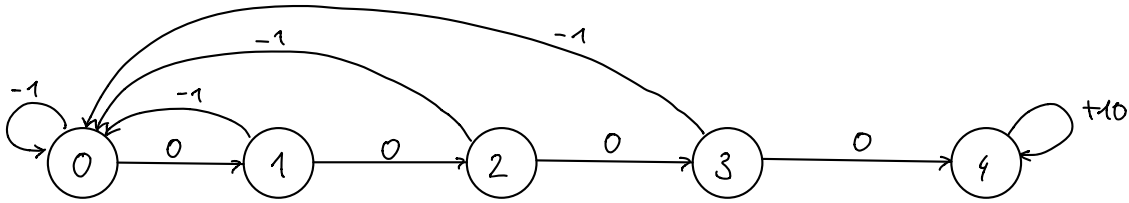
### 3. Backup diagrams

Give the backup diagrams for Q-Learning, Sarsa and Monte Carlo

#### 4. Value iteration

- a) Give the recursive relationship of  $v_{\pi}$
- b) Express  $q_{\pi}$  in terms of  $v_{\pi}$
- c) Prove the Contraction Theorem (Bellman Operator given)

5. Markov decision process



a) What is the optimal policy

b) Calculate value iteration for  $V_1, V_2$  for all states

c) Calculate optimal value function  $V^*$  for all states

Hint :  $\sum_{i=0}^{\infty} \alpha^i = \frac{1}{1-\alpha}$  ,  $|\alpha| < 1$

## 6. Policy improvement

- a)  $\mu$  is probabilistic policy, that is greedy wrt  $v_\pi$   
 $\pi$  is a deterministic policy

Prove that  $v_\mu(s) \geq v_\pi(s)$  for all  $s$

- b) If  $v_\mu(s) = v_\pi(s)$  for all  $s$ , show that  $\mu$  is the optimal policy

## 7. Monte Carlo

a) Give the update rule for first visit MC

7	8	9
4	5	6
1	2	3

3 episodes given as table with rewards

- ep1:  $s=3, r=2$
- ep2:  $s=3, r=2$
- ep3:  $s=4, r=1, s=3, r=3$

b) Calculate the value function for all states for first visit and for every visit

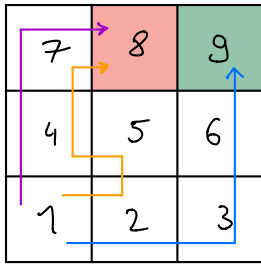
c) Episodes are done with a policy that chooses each action with probability 0.25.

Now we want to learn a target policy with  $\pi(\downarrow|s) = 0.5 = \pi(\rightarrow|s) \forall s$

Perform ordinary importance sampling and provide a value function.

## 8. Sarsa

a) Provide the update rule for Sarsa



b) Calculate the relevant Q-Functions for states and actions after each episode

$$c) Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha (R_{t+1} + \gamma \sum_a \pi(a|S_{t+1}) Q(S_{t+1}, a) - Q(S_t, A_t))$$

Explain if this update rule is on-policy or off-policy

d) Give the value function for Linear function approximation and explain

$$e) \underline{\omega}^T = [1, -1, 2, 1]$$

features consist of x-position and y-position of field, i.e. 1 has (1, 1), 8 has (2, 3)

and actions encoded as:  $\rightarrow$  is  $[1, 0]$ ,  $\downarrow$  is  $[0, -1]$ ,  $\uparrow$  is  $[0, 1]$  and  $\leftarrow$  is  $[-1, 0]$

features:  $[x\text{-position}, y\text{-position}, \text{action}]$

Calculate  $q(1, \uparrow)$ ,  $q(5, \uparrow)$ ,  $q(5, \rightarrow)$ ,  $q(6, \downarrow)$

f) Discuss if this choice of features is a good representation.



## 9. Policy gradient

Trajectory  $\tau = (S_0, A_0, R_1, S_1, A_1, R_2, \dots, S_T)$

- a) Give  $\nabla_{\theta} \log p(\tau|\theta)$ . Start with the likelihood of the probability
- b) Give a formula for  $\nabla_{\theta} \mathbb{E}[G_0]$
- c) Two actions are given  $a_0$  and  $a_1$ . Give a simple parametrization for  $\pi(a_0|s; \theta)$  and  $\pi(a_1|s; \theta)$  with features  $\phi(s)$