

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$0.1\tilde{g}(t)$	$\mathcal{E}_{\vec{w}_{uc}}$	$1,000\,0 \cdot 10^{-1}$	$1,000\,0 \cdot 10^{-1}$	$1,000\,0 \cdot 10^{-1}$	$1,000\,0 \cdot 10^{-1}$
	$\mathcal{E}_{\vec{w}_c}$	$5,377\,0 \cdot 10^{-5}$	$5,234\,0 \cdot 10^{-5}$	$5,220\,1 \cdot 10^{-5}$	$5,220\,3 \cdot 10^{-5}$
	\mathcal{E}_ρ	$1,139\,6 \cdot 10^{-5}$	$7,859\,7 \cdot 10^{-5}$	$7,859\,5 \cdot 10^{-5}$	$7,859\,7 \cdot 10^{-5}$
	\mathcal{E}_q	$2,785\,4 \cdot 10^{-5}$	$2,783\,6 \cdot 10^{-4}$	$5,704\,3 \cdot 10^{-4}$	$5,704\,5 \cdot 10^{-4}$
$0.5\tilde{g}(t)$	$\mathcal{E}_{\vec{w}_{uc}}$	$5,000\,0 \cdot 10^{-1}$	$5,000\,0 \cdot 10^{-1}$	$5,000\,0 \cdot 10^{-1}$	$5,000\,0 \cdot 10^{-1}$
	$\mathcal{E}_{\vec{w}_c}$	$2,197\,0 \cdot 10^{-4}$	$2,174\,7 \cdot 10^{-4}$	$2,173\,5 \cdot 10^{-4}$	$2,173\,5 \cdot 10^{-4}$
	\mathcal{E}_ρ	$2,425\,6 \cdot 10^{-5}$	$2,287\,8 \cdot 10^{-4}$	$2,287\,8 \cdot 10^{-4}$	$2,287\,9 \cdot 10^{-4}$
	\mathcal{E}_q	$3,324\,7 \cdot 10^{-5}$	$3,322\,7 \cdot 10^{-4}$	$6,808\,8 \cdot 10^{-4}$	$6,809\,0 \cdot 10^{-4}$
$0.1\tilde{h}(x)$	$\mathcal{E}_{\vec{w}_{uc}}$	$8,556\,8 \cdot 10^{-2}$	$8,556\,8 \cdot 10^{-2}$	$8,556\,8 \cdot 10^{-2}$	$8,556\,8 \cdot 10^{-2}$
	$\mathcal{E}_{\vec{w}_c}$	$5,370\,0 \cdot 10^{-5}$	$5,225\,0 \cdot 10^{-5}$	$5,210\,0 \cdot 10^{-5}$	$5,210\,3 \cdot 10^{-5}$
	\mathcal{E}_ρ	$1,170\,4 \cdot 10^{-5}$	$7,797\,3 \cdot 10^{-5}$	$7,796\,9 \cdot 10^{-5}$	$7,796\,8 \cdot 10^{-5}$
	\mathcal{E}_q	$2,642\,6 \cdot 10^{-5}$	$2,638\,7 \cdot 10^{-4}$	$5,698\,2 \cdot 10^{-4}$	$5,698\,4 \cdot 10^{-4}$
$0.5\tilde{h}(x)$	$\mathcal{E}_{\vec{w}_{uc}}$	$4,278\,4 \cdot 10^{-1}$	$4,278\,4 \cdot 10^{-1}$	$4,278\,4 \cdot 10^{-1}$	$4,278\,4 \cdot 10^{-1}$
	$\mathcal{E}_{\vec{w}_c}$	$2,120\,3 \cdot 10^{-4}$	$2,098\,2 \cdot 10^{-4}$	$2,096\,7 \cdot 10^{-4}$	$2,096\,8 \cdot 10^{-4}$
	\mathcal{E}_ρ	$2,256\,5 \cdot 10^{-5}$	$2,127\,5 \cdot 10^{-4}$	$2,127\,4 \cdot 10^{-4}$	$2,127\,5 \cdot 10^{-4}$
	\mathcal{E}_q	$3,022\,5 \cdot 10^{-5}$	$3,021\,9 \cdot 10^{-4}$	$6,192\,0 \cdot 10^{-4}$	$6,192\,3 \cdot 10^{-4}$

Table 1: Test Problem 2: Error measures for \vec{w}_{uc} , \vec{w}_c , ρ , and q , for four perturbation strategies for \vec{w} , and a range of β .

testdocument for random tests

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$N = 20, n = 10$	\mathcal{E}_ρ	$1,992\,3 \cdot 10^{-7}$	$1,599\,3 \cdot 10^{-6}$	$1,607\,0 \cdot 10^{-6}$	$1,607\,0 \cdot 10^{-6}$
	\mathcal{E}_q	$1,724\,7 \cdot 10^{-7}$	$2,958\,1 \cdot 10^{-6}$	$6,170\,9 \cdot 10^{-6}$	$6,175\,0 \cdot 10^{-6}$
	$\mathcal{E}_{\vec{w}}$	$1,244\,4 \cdot 10^{-6}$	$1,271\,9 \cdot 10^{-6}$	$1,250\,1 \cdot 10^{-6}$	$1,259\,5 \cdot 10^{-6}$
$N = 30, n = 20$	\mathcal{E}_ρ	$1,248\,7 \cdot 10^{-7}$	$5,374\,4 \cdot 10^{-8}$	$2,926\,8 \cdot 10^{-8}$	$2,926\,8 \cdot 10^{-8}$
	\mathcal{E}_q	$1,056\,4 \cdot 10^{-7}$	$1,950\,2 \cdot 10^{-8}$	$1,143\,1 \cdot 10^{-7}$	$1,102\,1 \cdot 10^{-7}$
	$\mathcal{E}_{\vec{w}}$	$1,034\,9 \cdot 10^{-5}$	$7,822\,7 \cdot 10^{-8}$	$9,704\,2 \cdot 10^{-8}$	$3,061\,3 \cdot 10^{-8}$
$N = 40, n = 30$	\mathcal{E}_ρ	$1,252\,3 \cdot 10^{-7}$	$5,421\,1 \cdot 10^{-8}$	$2,937\,4 \cdot 10^{-8}$	$2,937\,4 \cdot 10^{-8}$
	\mathcal{E}_q	$1,015\,8 \cdot 10^{-7}$	$2,349\,8 \cdot 10^{-8}$	$1,134\,6 \cdot 10^{-7}$	$1,165\,1 \cdot 10^{-7}$
	$\mathcal{E}_{\vec{w}}$	$9,823\,9 \cdot 10^{-6}$	$1,195\,0 \cdot 10^{-7}$	$1,014\,8 \cdot 10^{-7}$	$1,846\,3 \cdot 10^{-8}$

Table 2: Test Problem 2: Error measures for state ρ , adjoint q , and control \vec{w} , for a range of N , n , and β .

		Fixed Point	<code>fsolve</code>	Difference
$\kappa = -1$	\mathcal{J}_{uc}	0,043 8	0,043 8	
	\mathcal{J}_c	0,001 1	0,001 1	
	Iter (funcEval)	670 (670)	38 (31 959)	
	Time taken (s)	$2,493\,9 \cdot 10^2$	$9,154\,6 \cdot 10^3$	
	$\mathcal{E}_{\rho_{Diff}}$			$1,134\,8 \cdot 10^{-3}$
	$\mathcal{E}_{q_{Diff}}$			$7,274\,2 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w}_{Diff}}$			$7,672\,5 \cdot 10^{-2}$
$\kappa = 1$	\mathcal{J}_{uc}	0,043 4	0,043 4	
	\mathcal{J}_c	0,002 0	0,002 0	
	Iter (funcEval)	654 (654)	38 (34 239)	
	Time taken (s)	$3,379\,4 \cdot 10^2$	$1,016\,7 \cdot 10^4$	
	$\mathcal{E}_{\rho_{Diff}}$			$3,061\,0 \cdot 10^{-4}$
	$\mathcal{E}_{q_{Diff}}$			$4,870\,1 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w}_{Diff}}$			$8,905\,6 \cdot 10^{-3}$

Table 3: Comparison of the outputs of the fixed point method, with those obtained using `fsolve`.

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$\kappa = -1$	\mathcal{J}_{uc}	0,043 8	0,043 8	0,043 8	0,043 8
	\mathcal{J}_c	0,001 1	0,026 7	0,043 5	0,043 8
	Iter	670	650	449	1
$\kappa = 0$	\mathcal{J}_{uc}	0,041 7	0,041 7	0,041 7	0,041 7
	\mathcal{J}_c	0,001 4	0,028 3	0,041 5	0,041 7
	Iter	665	656	434	1
$\kappa = 1$	\mathcal{J}_{uc}	0,043 4	0,043 4	0,043 4	0,043 4
	\mathcal{J}_c	0,002 0	0,032 2	0,043 2	0,043 4
	Iter	654	682	422	1

Table 4: Example 1: Cost \mathcal{J}_{uc} of applying no control (i.e., $\vec{w} = \vec{0}$), optimal control cost \mathcal{J}_c , and number of iterations (PDE solves) **Iter** required, for a range of values of the interaction strength κ and regularization parameter β .

		Fixed Point	fsolve	Difference
$\kappa = -1$	\mathcal{J}_{uc}	0,043 8	0,043 8	
	\mathcal{J}_c	0,001 1	0,001 1	
	Iter (funcEval)	670 (670)	38 (31 959)	
	Time taken (s)	$2,493\,9 \cdot 10^2$	$9,154\,6 \cdot 10^3$	
	$\mathcal{E}_{\rho Diff}$			$1,134\,8 \cdot 10^{-3}$
	$\mathcal{E}_{q Diff}$			$7,274\,2 \cdot 10^{-5}$
$\kappa = 1$	$\mathcal{E}_{\vec{w} Diff}$			$7,672\,5 \cdot 10^{-2}$
	\mathcal{J}_{uc}	0,043 4	0,043 4	
	\mathcal{J}_c	0,002 0	0,002 0	
	Iter (funcEval)	654 (654)	38 (34 239)	
	Time taken (s)	$3,379\,4 \cdot 10^2$	$1,016\,7 \cdot 10^4$	
	$\mathcal{E}_{\rho Diff}$			$3,061\,0 \cdot 10^{-4}$
	$\mathcal{E}_{q Diff}$			$4,870\,1 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w} Diff}$			$8,905\,6 \cdot 10^{-3}$

Table 5: Comparison of the outputs of the fixed point method, with those obtained using **fsolve**.

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$N = 20, n = 10$	\mathcal{E}_ρ	$1,545\,9 \cdot 10^{-8}$	$1,544\,2 \cdot 10^{-8}$	$1,544\,2 \cdot 10^{-8}$	$1,544\,2 \cdot 10^{-8}$
	\mathcal{E}_q	$2,171\,5 \cdot 10^{-8}$	$2,171\,4 \cdot 10^{-8}$	$2,171\,4 \cdot 10^{-8}$	$2,171\,4 \cdot 10^{-8}$
	$\mathcal{E}_{\vec{w}}$	$3,432\,1 \cdot 10^{-8}$	$2,883\,6 \cdot 10^{-8}$	$2,664\,5 \cdot 10^{-9}$	$2,664\,5 \cdot 10^{-11}$
$N = 30, n = 20$	\mathcal{E}_ρ	$1,444\,8 \cdot 10^{-8}$	$1,444\,8 \cdot 10^{-8}$	$1,444\,8 \cdot 10^{-8}$	$1,444\,8 \cdot 10^{-8}$
	\mathcal{E}_q	$1,651\,8 \cdot 10^{-8}$	$1,651\,8 \cdot 10^{-8}$	$1,651\,8 \cdot 10^{-8}$	$1,651\,8 \cdot 10^{-8}$
	$\mathcal{E}_{\vec{w}}$	$4,742\,2 \cdot 10^{-8}$	$2,641\,0 \cdot 10^{-8}$	$1,651\,9 \cdot 10^{-9}$	$1,651\,9 \cdot 10^{-11}$
$N = 40, n = 30$	\mathcal{E}_ρ	$9,952\,8 \cdot 10^{-9}$	$1,303\,6 \cdot 10^{-8}$	$1,325\,4 \cdot 10^{-8}$	$1,325\,4 \cdot 10^{-8}$
	\mathcal{E}_q	$1,291\,1 \cdot 10^{-8}$	$1,426\,8 \cdot 10^{-8}$	$1,437\,5 \cdot 10^{-8}$	$1,437\,5 \cdot 10^{-8}$
	$\mathcal{E}_{\vec{w}}$	$3,641\,9 \cdot 10^{-8}$	$3,417\,2 \cdot 10^{-8}$	$1,457\,7 \cdot 10^{-9}$	$1,457\,7 \cdot 10^{-11}$

Table 6: Test Problem 5: Error measures for state ρ , adjoint q , and control \vec{w} , for a range of N , n , and β .

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$N = 20, n = 10$	\mathcal{E}_ρ	$1,992\,3 \cdot 10^{-7}$	$1,599\,3 \cdot 10^{-6}$	$1,607\,0 \cdot 10^{-6}$	$1,607\,0 \cdot 10^{-6}$
	\mathcal{E}_q	$1,724\,7 \cdot 10^{-7}$	$2,958\,1 \cdot 10^{-6}$	$6,170\,9 \cdot 10^{-6}$	$6,175\,0 \cdot 10^{-6}$
	$\mathcal{E}_{\vec{w}}$	$1,244\,4 \cdot 10^{-6}$	$1,271\,9 \cdot 10^{-6}$	$1,250\,1 \cdot 10^{-6}$	$1,259\,5 \cdot 10^{-6}$
$N = 30, n = 20$	\mathcal{E}_ρ	$1,248\,7 \cdot 10^{-7}$	$5,374\,4 \cdot 10^{-8}$	$2,926\,8 \cdot 10^{-8}$	$2,926\,8 \cdot 10^{-8}$
	\mathcal{E}_q	$1,056\,4 \cdot 10^{-7}$	$1,950\,2 \cdot 10^{-8}$	$1,143\,1 \cdot 10^{-7}$	$1,102\,1 \cdot 10^{-7}$
	$\mathcal{E}_{\vec{w}}$	$1,034\,9 \cdot 10^{-5}$	$7,822\,7 \cdot 10^{-8}$	$9,704\,2 \cdot 10^{-8}$	$3,061\,3 \cdot 10^{-8}$
$N = 40, n = 30$	\mathcal{E}_ρ	$1,252\,3 \cdot 10^{-7}$	$5,421\,1 \cdot 10^{-8}$	$2,937\,4 \cdot 10^{-8}$	$2,937\,4 \cdot 10^{-8}$
	\mathcal{E}_q	$1,015\,8 \cdot 10^{-7}$	$2,349\,8 \cdot 10^{-8}$	$1,134\,6 \cdot 10^{-7}$	$1,165\,1 \cdot 10^{-7}$
	$\mathcal{E}_{\vec{w}}$	$9,823\,9 \cdot 10^{-6}$	$1,195\,0 \cdot 10^{-7}$	$1,014\,8 \cdot 10^{-7}$	$1,846\,3 \cdot 10^{-8}$

Table 7: Test Problem 2: Error measures for state ρ , adjoint q , and control \vec{w} , for a range of N , n , and β .

		Fixed Point	fsolve	Difference
$\kappa = -1$	\mathcal{J}_{uc}	0,043 8	0,043 8	
	\mathcal{J}_c	0,001 1	0,001 1	
	Iter (funcEval)	670 (670)	38 (31 959)	
	Time taken (s)	$2,493\,9 \cdot 10^{+2}$	$9,154\,6 \cdot 10^{+3}$	
	$\mathcal{E}_{\rho Diff}$			$1,134\,8 \cdot 10^{-3}$
	$\mathcal{E}_{q Diff}$			$7,274\,2 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w} Diff}$			$7,672\,5 \cdot 10^{-2}$
$\kappa = 1$	\mathcal{J}_{uc}	0,043 4	0,043 4	
	\mathcal{J}_c	0,002 0	0,002 0	
	Iter (funcEval)	654 (654)	38 (34 239)	
	Time taken (s)	$3,379\,4 \cdot 10^{+2}$	$1,016\,7 \cdot 10^{+4}$	
	$\mathcal{E}_{\rho Diff}$			$3,061\,0 \cdot 10^{-4}$
	$\mathcal{E}_{q Diff}$			$4,870\,1 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w} Diff}$			$8,905\,6 \cdot 10^{-3}$

Table 8: Comparison of the outputs of the fixed point method, with those obtained using **fsolve**.

		Fixed Point	fsolve	Difference
$\kappa = -1$	\mathcal{J}_{uc}	0,043 8	0,043 8	
	\mathcal{J}_c	0,001 1	0,001 1	
	Iter	670	38 (31 959)	
	Time taken (s)	$2,493\,9 \cdot 10^{+2}$	$9,154\,6 \cdot 10^{+3}$	
	$\mathcal{E}_{\rho Diff}$			0,001 1
	$\mathcal{E}_{q Diff}$			0,000 1
	$\mathcal{E}_{\vec{w} Diff}$			0,076 7
$\kappa = 1$	\mathcal{J}_{uc}	0,043 4	0,043 4	
	\mathcal{J}_c	0,002 0	0,002 0	
	Iter	654	38 (34 239)	
	Time taken (s)	$3,379\,4 \cdot 10^{+2}$	$1,016\,7 \cdot 10^{+4}$	
	$\mathcal{E}_{\rho Diff}$			0,000 3
	$\mathcal{E}_{q Diff}$			0,000 0
	$\mathcal{E}_{\vec{w} Diff}$			0,008 9

Table 9: Comparison of the outputs of the fixed point method, with those obtained using **fsolve**.

		Fixed Point	fsolve	Difference
$\kappa = -1$	\mathcal{J}_{uc}	0,043 8	0,043 8	
	\mathcal{J}_c	0,001 1	0,001 1	
	Iter	670	38 (31 959)	
	Time taken (s)	$2,493\,9 \cdot 10^{+2}$	$9,154\,6 \cdot 10^{+3}$	
	$\mathcal{E}_{\rho Diff}$			$1,134\,8 \cdot 10^{-3}$
	$\mathcal{E}_{q Diff}$			$7,274\,2 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w} Diff}$			$7,672\,5 \cdot 10^{-2}$
$\kappa = 1$	\mathcal{J}_{uc}	0,043 4	0,043 4	
	\mathcal{J}_c	0,002 0	0,002 0	
	Iter	654	38 (34 239)	
	Time taken (s)	$3,379\,4 \cdot 10^{+2}$	$1,016\,7 \cdot 10^{+4}$	
	$\mathcal{E}_{\rho Diff}$			$3,061\,0 \cdot 10^{-4}$
	$\mathcal{E}_{q Diff}$			$4,870\,1 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w} Diff}$			$8,905\,6 \cdot 10^{-3}$

Table 10: Comparison of the outputs of the fixed point method, with those obtained using **fsolve**.

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$\kappa = -1$	\mathcal{J}_{uc}	0,043 8	0,043 8	0,043 8	0,043 8
	\mathcal{J}_c	0,001 1	0,026 7	0,043 5	0,043 8
	Iter	670	650	449	1
$\kappa = 0$	\mathcal{J}_{uc}	0,041 7	0,041 7	0,041 7	0,041 7
	\mathcal{J}_c	0,001 4	0,028 3	0,041 5	0,041 7
	Iter	665	656	434	1
$\kappa = 1$	\mathcal{J}_{uc}	0,043 4	0,043 4	0,043 4	0,043 4
	\mathcal{J}_c	0,002 0	0,032 2	0,043 2	0,043 4
	Iter	654	682	422	1

Table 11: Example 1: Cost \mathcal{J}_{uc} of applying no control (i.e., $\vec{w} = \vec{0}$), optimal control cost \mathcal{J}_c , and number of iterations (PDE solves) **Iter** required, for a range of values of the interaction strength κ and regularization parameter β .

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$\kappa = -1$	\mathcal{J}_{uc}	0,043 75	0,043 75	0,043 75	0,043 75
	\mathcal{J}_c	0,001 086	0,026 68	0,043 48	0,043 75
	Iter	670	650	449	1
$\kappa = 0$	\mathcal{J}_{uc}	0,041 67	0,041 67	0,041 67	0,041 67
	\mathcal{J}_c	0,001 447	0,028 27	0,041 47	0,041 67
	Iter	665	656	434	1
$\kappa = 1$	\mathcal{J}_{uc}	0,043 36	0,043 36	0,043 36	0,043 36
	\mathcal{J}_c	0,002 03	0,032 23	0,043 21	0,043 37
	Iter	654	682	422	1

Table 12: Example 1: Cost \mathcal{J}_{uc} of applying no control (i.e., $\vec{w} = \vec{0}$), optimal control cost \mathcal{J}_c , and number of iterations (PDE solves) **Iter** required, for a range of values of the interaction strength κ and regularization parameter β .

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$N = 20, n = 10$	\mathcal{E}_ρ	$3,831\,7 \cdot 10^{-8}$	$1,906\,9 \cdot 10^{-8}$	$1,379\,6 \cdot 10^{-8}$	$1,355\,3 \cdot 10^{-8}$
	\mathcal{E}_q	$2,538\,0 \cdot 10^{-8}$	$2,367\,2 \cdot 10^{-8}$	$4,646\,4 \cdot 10^{-8}$	$4,399\,0 \cdot 10^{-8}$
	$\mathcal{E}_{\vec{w}}$	$4,119\,1 \cdot 10^{-6}$	$1,337\,7 \cdot 10^{-7}$	$4,177\,1 \cdot 10^{-8}$	$3,921\,3 \cdot 10^{-8}$
$N = 30, n = 20$	\mathcal{E}_ρ	$3,920\,6 \cdot 10^{-8}$	$1,902\,3 \cdot 10^{-8}$	$1,401\,9 \cdot 10^{-8}$	$1,386\,3 \cdot 10^{-8}$
	\mathcal{E}_q	$3,933\,7 \cdot 10^{-8}$	$1,943\,6 \cdot 10^{-8}$	$1,335\,5 \cdot 10^{-8}$	$2,332\,7 \cdot 10^{-8}$
	$\mathcal{E}_{\vec{w}}$	$6,464\,1 \cdot 10^{-6}$	$1,782\,3 \cdot 10^{-7}$	$2,025\,6 \cdot 10^{-8}$	$1,986\,6 \cdot 10^{-8}$
$N = 40, n = 30$	\mathcal{E}_ρ	$3,806\,9 \cdot 10^{-8}$	$1,908\,5 \cdot 10^{-8}$	$1,484\,4 \cdot 10^{-8}$	$1,470\,0 \cdot 10^{-8}$
	\mathcal{E}_q	$3,639\,8 \cdot 10^{-8}$	$1,981\,3 \cdot 10^{-8}$	$1,527\,5 \cdot 10^{-8}$	$2,845\,2 \cdot 10^{-8}$
	$\mathcal{E}_{\vec{w}}$	$5,951\,0 \cdot 10^{-6}$	$2,153\,1 \cdot 10^{-7}$	$2,313\,9 \cdot 10^{-8}$	$2,582\,0 \cdot 10^{-8}$

Table 13: Test Problem 1: Error measures for state ρ , adjoint q , and control \vec{w} , for a range of N , n , and β .

		Fixed Point	<code>fsolve</code>	Difference
$\kappa = -1$	\mathcal{J}_{FW}	$4,375\,1 \cdot 10^{-2}$	$4,375\,1 \cdot 10^{-2}$	
	\mathcal{J}_{Opt}	$1,085\,6 \cdot 10^{-3}$	$1,085\,7 \cdot 10^{-3}$	
	Iter	670	38	
	Time taken (s)	$2,493\,9 \cdot 10^{+2}$	$9,154\,6 \cdot 10^{+3}$	
	$\mathcal{E}_{\rho Diff}$			$1,134\,8 \cdot 10^{-3}$
	$\mathcal{E}_{q Diff}$			$7,274\,2 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w} Diff}$			$7,672\,5 \cdot 10^{-2}$
$\kappa = 1$	\mathcal{J}_{FW}	$4,336\,5 \cdot 10^{-2}$	$4,336\,5 \cdot 10^{-2}$	
	\mathcal{J}_{Opt}	$2,029\,9 \cdot 10^{-3}$	$2,030\,0 \cdot 10^{-3}$	
	Iter	654	38	
	Time taken (s)	$3,379\,4 \cdot 10^{+2}$	$1,016\,7 \cdot 10^{+4}$	
	$\mathcal{E}_{\rho Diff}$			$3,061\,0 \cdot 10^{-4}$
	$\mathcal{E}_{q Diff}$			$4,870\,1 \cdot 10^{-5}$
	$\mathcal{E}_{\vec{w} Diff}$			$8,905\,6 \cdot 10^{-3}$

Table 14: Comparison of the outputs of the fixed point method, with those obtained using `fsolve`.

		$\beta = 10^{-3}$	$\beta = 10^{-1}$	$\beta = 10^1$	$\beta = 10^3$
$0.1\tilde{g}(t)$	$\mathcal{E}_{\vec{w}_{uc}}$	$1,000\,0 \cdot 10^{-1}$	$1,000\,0 \cdot 10^{-1}$	$1,000\,0 \cdot 10^{-1}$	$1,000\,0 \cdot 10^{-1}$
	$\mathcal{E}_{\vec{w}_c}$	$5,377\,0 \cdot 10^{-5}$	$5,234\,0 \cdot 10^{-5}$	$5,220\,1 \cdot 10^{-5}$	$5,220\,3 \cdot 10^{-5}$
	\mathcal{E}_ρ	$1,139\,6 \cdot 10^{-5}$	$7,859\,7 \cdot 10^{-5}$	$7,859\,5 \cdot 10^{-5}$	$7,859\,7 \cdot 10^{-5}$
	\mathcal{E}_q	$2,785\,4 \cdot 10^{-5}$	$2,783\,6 \cdot 10^{-4}$	$5,704\,3 \cdot 10^{-4}$	$5,704\,5 \cdot 10^{-4}$
$0.5\tilde{g}(t)$	$\mathcal{E}_{\vec{w}_{uc}}$	$5,000\,0 \cdot 10^{-1}$	$5,000\,0 \cdot 10^{-1}$	$5,000\,0 \cdot 10^{-1}$	$5,000\,0 \cdot 10^{-1}$
	$\mathcal{E}_{\vec{w}_c}$	$2,197\,0 \cdot 10^{-4}$	$2,174\,7 \cdot 10^{-4}$	$2,173\,5 \cdot 10^{-4}$	$2,173\,5 \cdot 10^{-4}$
	\mathcal{E}_ρ	$2,425\,6 \cdot 10^{-5}$	$2,287\,8 \cdot 10^{-4}$	$2,287\,8 \cdot 10^{-4}$	$2,287\,9 \cdot 10^{-4}$
	\mathcal{E}_q	$3,324\,7 \cdot 10^{-5}$	$3,322\,7 \cdot 10^{-4}$	$6,808\,8 \cdot 10^{-4}$	$6,809\,0 \cdot 10^{-4}$
$0.1\tilde{h}(x)$	$\mathcal{E}_{\vec{w}_{uc}}$	$8,556\,8 \cdot 10^{-2}$	$8,556\,8 \cdot 10^{-2}$	$8,556\,8 \cdot 10^{-2}$	$8,556\,8 \cdot 10^{-2}$
	$\mathcal{E}_{\vec{w}_c}$	$5,370\,0 \cdot 10^{-5}$	$5,225\,0 \cdot 10^{-5}$	$5,210\,0 \cdot 10^{-5}$	$5,210\,3 \cdot 10^{-5}$
	\mathcal{E}_ρ	$1,170\,4 \cdot 10^{-5}$	$7,797\,3 \cdot 10^{-5}$	$7,796\,9 \cdot 10^{-5}$	$7,796\,8 \cdot 10^{-5}$
	\mathcal{E}_q	$2,642\,6 \cdot 10^{-5}$	$2,638\,7 \cdot 10^{-4}$	$5,698\,2 \cdot 10^{-4}$	$5,698\,4 \cdot 10^{-4}$
$0.5\tilde{h}(x)$	$\mathcal{E}_{\vec{w}_{uc}}$	$4,278\,4 \cdot 10^{-1}$	$4,278\,4 \cdot 10^{-1}$	$4,278\,4 \cdot 10^{-1}$	$4,278\,4 \cdot 10^{-1}$
	$\mathcal{E}_{\vec{w}_c}$	$2,120\,3 \cdot 10^{-4}$	$2,098\,2 \cdot 10^{-4}$	$2,096\,7 \cdot 10^{-4}$	$2,096\,8 \cdot 10^{-4}$
	\mathcal{E}_ρ	$2,256\,5 \cdot 10^{-5}$	$2,127\,5 \cdot 10^{-4}$	$2,127\,4 \cdot 10^{-4}$	$2,127\,5 \cdot 10^{-4}$
	\mathcal{E}_q	$3,022\,5 \cdot 10^{-5}$	$3,021\,9 \cdot 10^{-4}$	$6,192\,0 \cdot 10^{-4}$	$6,192\,3 \cdot 10^{-4}$

Table 15: Test Problem 2: Error measures for \vec{w}_{uc} , \vec{w}_c , ρ , and q , for four perturbation strategies for \vec{w} , and a range of β .