Literature Review on Related Work

[1] (review, compare to other works...)

Papers Involving Stochastic Dynamics

[2]

Papers Involving Deterministic Dynamics

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[3] [4] (Cucker-Smale) [5] [6] [7] [8] (Cucker-Smale)
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Theoretical Papers

- [2] (existence of our type of optimal controls)
- [9] (optimality conditions, convergence to mean field)
- [10] (well posedness of the mean field equation and the microscopic model, large time behaviour and consensus formation)
- [11] (existence and regularity of the solution of the OCP, well posedness of forward problem)
- [5] (convergence of microscopic to macroscopic OCP, gamma limit)
- [6] (compare to above)
- [7] (existence and consistency of mean field OCP, gamma convergence)
- [8] (well posedness of the constrained Cucker-Smale equation)
- [12] (some convergence results)

Numerical Papers

- [2] (Chang Cooper, Finite Volumes, finite differences, Monte Carlo,...),
- [3] (Compass search method, fmincon)
- [13] (steady state fokker planck only)
- [4] (comparing two control approaches, stochastic approximation of interaction, iterative solving with transport and interactions step)
- [14] (strang splitting scheme, semi Lagrangian, finite volume)
- [15] (compare to [14], this one is older!)
- [10] (implicit finite difference for inverse distribution)
- [12] (Galerkin scheme, split transport and diffusion, iterative)

Leader-Follower Interaction

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[3] [16] (compare to [13]) [14]
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Relevant Boundary Conditions

[2] (no flux) [10] (no flux) [11] (periodic boundary data)

Control Types

- [2] (flow control)
- [3] (minimizing total mass of followers)
- [13] (control via interaction term)
- [4] (control function vs control region, sparse control, flocking)
- [16](embedded in microscopic interactions)
- [9] (through interaction term)
- [14] (control from external agents)
- [15] (control from external agents)
- [11] (flow control)
- [5] (flow control)
- [6] (external agents, sparse)
- [7] (flow control)
- [8] (flow control)

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