

for the first sample \Rightarrow

$$x^{(1)} = [x_0^{(1)}, x_1^{(1)}, x_2^{(1)}] = [1, 5.1, 3.5]$$

$$w = [w_0, w_1, w_2] = [0.2, 0.3, -0.5]$$

$$\eta = 0.1 \text{ [Learning rate]}$$

$$\phi(z) = \phi(w_0 x_0 + w_1 x_1 + w_2 x_2)$$

$$\hat{y} = \phi(0.2 \times 1 + 0.3 \times 5.1 + (-0.5) \times (3.5))$$

$$\phi(0.2 + 1.53 - 1.75)$$

$$\phi(1.73 - 1.75)$$

$$-0.02$$

for the second sample \Rightarrow

$$x^{(2)} = [x_0^{(2)}, x_1^{(2)}, x_2^{(2)}] = [1, 4.9, 3.0]$$

$$w = [w_0, w_1, w_2] = [0.2, 0.3, -0.5]$$

$$\eta = 0.1 \text{ [Learning rate]}$$

$$\hat{y} = \phi(\omega_0 x_2^{(2)} + \omega_1 x_1^{(2)} + \omega_2 x_2^{(2)})$$

$$\phi(0.2 \times 1 + 0.3 \times 4.9 + (-0.5) \times 3.0)$$

$$\phi(0.2 + 1.47 + (-1.5))$$

$$\hat{y} = 0.17$$

Weight updates in the first iteration over the two samples

$$\Delta \omega_0 = \eta \sum_{i=1} (y^{(i)} - \phi(z^{(i)})) x_0^{(i)}$$

$$0.1 \times [y^{(1)} - \phi(z^{(1)}) \times x_0^{(1)} + (y^{(2)} - \phi(z^{(2)})) \times x_0^{(2)}]$$

$$0.1 \times [1 - (-0.02) \times 1 + (1 - 0.17) \times 1]$$

$$0.1 \times [1.02 + 0.83]$$

$$\Delta \omega_0 = 0.185$$

$$\Delta \omega_1 = \eta \sum_{i=1} (y^{(i)} - \phi(z^{(i)})) x_1^{(i)}$$

$$0.1 \times [1 - (-0.02) \times 5.1 + (1 - 0.17) \times 4.9]$$

$$0.1 \times [5.202 + 4.067]$$

$$\Delta \omega_1 = 9.269 \times 0.1 = 0.9269$$

$$\Delta w_2 = \eta \sum_{i=1}^n (y^{(i)} - \phi(z^{(i)})) x_2^{(i)}$$

$$0.1 \times [(y^1 - \phi(z^1)) x_2^1 + (y^2 - \phi(z^2)) x_2^2]$$

$$0.1 \times [(1 - (-0.02)) 3.5 + (1 - 0.17) \times 3.0]$$

$$0.1 \times [3.57 + 2.49]$$

$$\Delta w_2 = 6.06 \times 0.1 \Rightarrow 0.606$$

Therefore, by adding the update to the current weight and they become

$$[0.2 + 0.185, 0.3 + 0.9269, -0.5 + 0.606]$$

$$[0.385, 1.2269, 0.106]$$