

Denavit Hartenberg Parameters:

Denavit Hartenberg Parameters (DH Params) is the minimal set of parameters required to create complete transformations between each joint of robot with Prismatic and Revolute joints. While there are many different ways of creating transformation between each joint frame which describe the robot, the DH Parameters provide a minimal and intuitive set parameters...

- Link **Twist:** (α_i)
- Link **Length:** (a_i)
- Link **Offset:** (d_i)
- Link **Angle** (θ_i)

These parameters have a very intuitive meaning. By agreeing to use this (DH) parameterization, we can achieve the exact same transformation of coordinate systems from the base frame to the end-effector frame, while maintaining a minimum parameterization (4 params instead of 6), which are all intuitive and easy to visualize.

The downside of this mean is that since this is merely a convention, we must follow a set of rules assigning coordinate frames to links of the robot in order to retain this parameterization.

Rules for Applying DH Parameters:

1. Actuate about the **z-axis**
 - Rotate about Z for revolute joints
 - Translate along Z for prismatic joints.
2. Axis \hat{Z}_{j-1} is **perpendicular** to, and **intersects**, \hat{X}_j
3. The y-axis is solved implicitly using Right Hand Rule and Cross-Products.
 $\hat{y}_j = \hat{z}_j \times \hat{x}_j$
- 4.

Tips for DH Parameters:

- The joint frame does not need to physically coincide with the actual joint. It only needs to align with the axis of actuation.
- The robot arm can be arranged in any configuration that suits the DH Parameters.

Forward Kinematics using DH Params:

To get the forward kinematics at a particular joint configuration \mathbf{q} , substitute the joint value into the **z-component** of the transform chain.

$$T_{j-1}^j = \begin{cases} T_{Rz}(q_j)T_z(d_j)T_x(a_j)T_{Rx}(\alpha_j), & \text{for Revolute} \\ T_{Rz}(\theta_j)T_z(q_j)T_x(a_j)T_{Rx}(\alpha_j), & \text{for Prismatic} \end{cases}$$