# Making Causal Critiques Day 2 - Fundamental Critiques

Jonathan Phillips

January 23, 2019

- Door-to-door political campaigning works
- Proportional Representation electoral systems have more parties
- Democracies do not go to war with each other
- Development helps democracies endure
- ...And that's about it

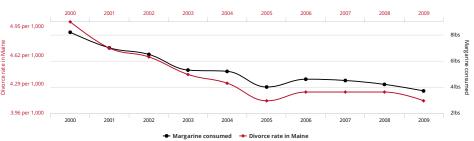
- Thousands of books and papers have not generated any causal knowledge
  - Many add descriptive knowledge
  - Many investigate specific events, not generalizable variables
  - Many highlight correlations between variables

- Correlation is not causation
  - If we look hard enough we can always find correlations
  - By chance...
  - Due to complex social patterns...
  - ▶ But we cannot conclude that there is a causal effect of x on y
- ► More data will not help
- The problem is the type of data; it does not allow us to answer causal question

#### Divorce rate in Maine

correlates with

### Per capita consumption of margarine

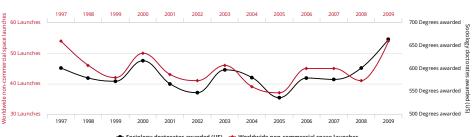


tylervigen.com

#### Worldwide non-commercial space launches

correlates with

#### Sociology doctorates awarded (US)

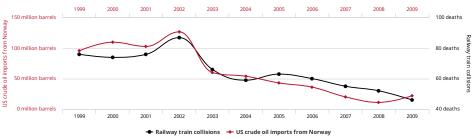


◆ Sociology doctorates awarded (US) ◆ Worldwide non-commercial space launches

#### US crude oil imports from Norway

correlates with

#### Drivers killed in collision with railway train

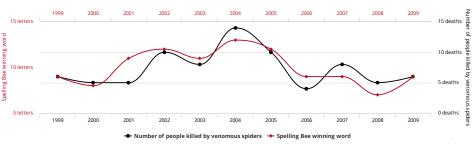


tylervigen.com

#### Letters in Winning Word of Scripps National Spelling Bee

correlates with

#### Number of people killed by venomous spiders



tylervigen.com

- Why isn't correlation enough?
  - For prediction correlation is fine: If we know a country has income of US\$50,000 per capita we can confidently predict it is perceived as being less corrupt
  - But for intervention, correlation does not help: investing to boost the economy does nothing on its own to reduce corruption

- Why isn't correlation enough?
- ► The Lucas Critique: Relationships fall apart when we intervene with policy
  - ► The data shows no-one lies on their tax forms
  - So let's abandon tax checks; the government wants to save money
  - But reducing checks reduces the chances of getting caught
  - Citizens start to lie on their tax forms
- ► That means we need to understand what *causes* people to lie on tax forms, so we can better understand their behaviour

► To accumulate knowledge, we have to ask specific types of questions:

Causes of Effects	Effects of Causes
What caused Y?	Does X cause Y?"
Why did the United States grow faster than Bolivia in the twentieth century?	Did the more permanent colonial settlement of the United States compared to Bolivia affect their subsequent growth rates?

- ► A focus on a single explanatory variable X requires us to clearly define this 'treatment'
- ► AND to clearly define a control
  - What is the opposite of investing \$1bn in education?
  - No investment, or investing it elsewhere?
- ▶ Define treatment:

$$D_i = \begin{cases} 1, & \text{if treated} \\ 0, & \text{if not treated} \end{cases}$$

- Defining our outcome is also crucial:
  - Can we measure our outcome of interest?
  - Is that outcome the end of the causal chain?
  - Tempting to look at many outcomes, but the risk of cherry-picking
    - All outcomes are probabilistic
    - If we study 20 outcomes, on average one will show a significant effect even with no real causal effect

- We want to know how some variable affects another variable
- eg. how a proportional representation electoral system affects investment in education
  - ► The **treatment** is a change to a PR electoral system (vs FPTP)
  - ► The **outcome** is the level of (public?) investment in education

- ► So we need a precise framework to analyze causation
- ► The causal effect of treatment is how the unit's outcome differs when it is treated and not treated
- ► These are the **potential outcomes** for unit *i*:

$$Y_{Di} = \begin{cases} Y_{1i} \text{ Potential Outcome if unit i treated} \\ Y_{0i} \text{ Potential Outcome if unit i not treated} \end{cases}$$

► Treatment Effect =  $Y_{1i} - Y_{0i}$ 

## Potential Outcomes Example

	Investment in Education if PR system	Investment in Educa- tion if FPTP system	
	Y <sub>1</sub>	Y <sub>0</sub>	Treatment Effect
Brasil	8	4	4
Argentina	10	7	3
Bolivia	2	4	-2
Colombia	11	11	0
Peru	6	2	4

- ► The Fundamental Problem of Causal Inference
  - No units can receive both treatment and control
  - ▶ So we can never observe both  $Y_1$  and  $Y_0$  for the same unit

## Potential Outcomes Example

	PR Sys- tem?	Investment in Education if PR system	Investment in Education if FPTP system	
	Di	Y <sub>1</sub>	Y <sub>0</sub>	Treatment Effect
Brasil	1	8	?	?
Argentina	1	10	?	?
Bolivia	0	?	4	?
Colombia	0	?	11	?
Peru	0	?	2	?

- We can't even look at the change in countries that switch to a PR system
  - What if all countries had started to invest more in education at the same time, for different reasons?
  - ► The potential outcome for Country X in time 1 is different to at time 2

- ➤ So we need to consider the counterfactual what would have happened if the country had not switched to a PR system?
  - ► This is **impossible** to know
  - We can only estimate the effect by comparing across units in some way
  - That is why we are doing causal inference, not causal proof

- Which comparisons to make?
- Control units can never be perfect substitutes
- Causal Inference is all about identifying a plausible counterfactual
  - Plausible means that the potential outcomes of the control unit are likely to be the same as those of the treated unit

- ► The comparability of treatment and control units depends on how they got to be treated
  - On the Treatment Assignment Mechanism
- ► If we 'treated' an outlier like the Galapagos Islands, could we find a comparable control unit?
- ► Comparisons are easier where the **Treatment Assignment Mechanism is independent of potential outcomes** 
  - This makes it more likely that potential outcomes are 'balanced' and comparable

► Types of Research Design:

## Add caption

	Researcher controls the treatment assignment	Treatme mechan ate com outcome
Controlled Experiments	Yes	Yes
Natural Experiments	No	Yes
Observable Studies	No	No

- ▶ Observational Studies
  - Household surveys
  - Simple regression on secondary data
  - ► Interviews of a random sample

- We do not know what the treatment assignment mechanism was
  - Which units were treated and why?
- Treatment assignment is unlikely to create comparable potential outcomes
  - Which units might be appropriate counterfactuals?

 With complete information on potential outcomes, calculating treatment effects is trivial

D	$Y_1$	$Y_0$	Yi	Real Effect, $Y_1 - Y_0$
1	7	4	7	3
0	9	5	5	4
0	4	4	4	0
1	4	3	4	1
	D 1 0 1 1	D Y <sub>1</sub> 1 7 0 9 0 4 1 4	D     Y1     Y0       1     7     4       0     9     5       0     4     4       1     4     3	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

 With complete information on potential outcomes, calculating treatment effects is trivial

	D	<i>Y</i> <sub>1</sub>	<i>Y</i> <sub>0</sub>	Yi	Real Effect, $Y_1 - Y_0$
Α	1	7	4	7	3
В	0	9	5	5	4
С	0	4	4	4	0
D	1	4	3	4	1
$E(Y_1) =$		6			
$E(Y_0) =$			4		

$$\rightarrow$$
 ATE =  $E(Y_1 - Y_0) = 8/4 = 2$ 

$$\rightarrow$$
 ATE =  $E(Y_1) - E(Y_0) = 6 - 4 = 2$ 

► From observed outcomes can we calculate an Average Treatment Effect?

	D	<i>Y</i> <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect, $Y_1 - Y_0$
Α	1	7	?	7	?
В	0	?	5	5	?
С	0	?	4	4	?
D	1	4	?	4	?

► From observed outcomes can we calculate an Average Treatment Effect?

	D	Y <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect, $Y_1 - Y_0$
Α	1	7	?	7	?
В	0	?	5	5	?
С	0	?	4	4	?
D	1	4	?	4	?
$E(Y_1) =$		5.5			
$E(Y_0) =$			4.5		

- ▶ If we use the control units as counterfactuals...
- ► Average Treatment Effect:

$$ATE = E(Y_1) - E(Y_0) \tag{1}$$

$$= 5.5 - 4.5 \tag{2}$$

$$= 1 (3)$$

► Half the true treatment effect

- If we use the control units as counterfactuals...
- Average Treatment Effect:

$$ATE = E(Y_1) - E(Y_0) \tag{1}$$

$$= 5.5 - 4.5 \tag{2}$$

$$= 1 \tag{3}$$

- ► Half the true treatment effect
- ► Why?

- If we use the control units as counterfactuals...
- Average Treatment Effect:

$$ATE = E(Y_1) - E(Y_0) \tag{1}$$

$$= 5.5 - 4.5 \tag{2}$$

- ▶ Half the true treatment effect
- ► Why?
  - ► The units that got treated had lower Y<sub>1</sub>
  - ► The units that were controls had higher Y<sub>0</sub>

- If we use the control units as counterfactuals...
- Average Treatment Effect:

$$ATE = E(Y_1) - E(Y_0) \tag{1}$$

$$= 5.5 - 4.5 \tag{2}$$

$$= 1 (3)$$

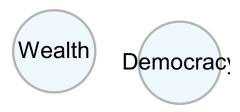
- ► Half the true treatment effect
- ► Why?
  - The units that got treated had lower Y<sub>1</sub>
  - The units that were controls had higher Y<sub>0</sub>
  - ► The 'stand-in' counterfactuals were wrong

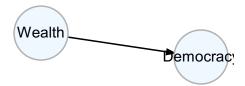
- ► The bias in units' potential outcomes depends on which units get treated and which ones don't
- In observational studies, we have very little protection against causal critiques
  - 1. Reverse Causation
  - 2. Omitted variable bias (confounding)
  - 3. Selection bias

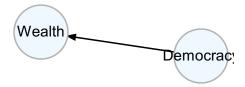
#### **Reverse Causation**

- Wealthier countries are more likely to be democracies
  - But does wealth create democracy?
  - Or democracy create wealth?
- ▶ We cannot tell from the correlation alone
- Both may be true

## **Reverse Causation**







▶ Where treatment has no effect

Treatment Assignment by Covariate

	D	<i>Y</i> <sub>1</sub>	<i>Y</i> <sub>0</sub>	Yi	Real Effect
Α	0	7	7	7	0
В	0	9	9	9	0
С	1	4	4	4	0
D	1	4	4	4	0

▶ Where treatment has no effect

# Treatment Assignment by Covariate

	D	<i>Y</i> <sub>1</sub>	<i>Y</i> <sub>0</sub>	Yi	Real Effect
А	0	7	7	7	0
В	0	9	9	9	0
С	1	4	4	4	0
D	1	4	4	4	0
$E(Y_1) =$		4			
$E(Y_0) =$			4		

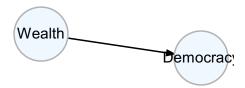
▶ Where treatment has no effect

# Treatment Assignment by Covariate

	D	Y <sub>1</sub>	<i>Y</i> <sub>0</sub>	Yi	Real Effect
Α	0	7	7	7	0
В	0	9	9	9	0
С	1	4	4	4	0
D	1	4	4	4	0
$E(Y_1) =$		4			
$E(Y_0) =$			4		

- $\blacktriangleright$  ATE = 4 4 = 0. There is no effect.
- ► The (negative) correlation between D and Y is because Y causes D

- Wealthier countries are more likely to be democracies
  - But wealthier countries are more likely to be European
  - And democracies are more likely to be European
- ► Maybe the correlation just reflects the fact that European countries are 'different'?





► Imagine a treatment assignment mechanism where all women get treated

Treatment Assignment by Covariate

	Χ	D	Y <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect
Α	Man	0	7	4	4	3
В	Man	0	9	5	5	4
С	Woman	1	4	4	4	0
D	Woman	1	4	3	4	1

► Imagine a treatment assignment mechanism where all women get treated

Treatment Assignment by Covariate

	Х	D	<i>Y</i> <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect
Α	Man	0	7	4	4	3
В	Man	0	9	5	5	4
С	Woman	1	4	4	4	0
D	Woman	1	4	3	4	1
$E(Y_1) =$			4			
$E(Y_0) =$				4.5		

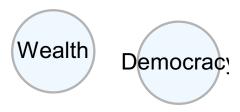
▶ Imagine a treatment assignment mechanism where all women get treated

Treatment Assignment by Covariate

	Х	D	<i>Y</i> <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect
Α	Man	0	7	4	4	3
В	Man	0	9	5	5	4
С	Woman	1	4	4	4	0
D	Woman	1	4	3	4	1
$E(Y_1) =$			4			
$E(Y_0) =$				4.5		

- $\blacktriangleright$  ATE = 4 4.5 = -0.5
- ▶ This is **confounding** or an **omitted variable** another variable affects both treatment and potential outcomes 34/42

- Wealthier countries are more likely to be democracies
  - But wealthy autocracies and poor democracies do not like to report data
  - ► So we cannot compare them
  - Only wealthy democracies 'self-select' into our sample





► Imagine a treatment assignment mechanism where people get to *choose* their treatment

Treatment Assignment by Self-Selection

	D	<i>Y</i> <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect
Α	1	7	4	7	3
В	1	9	5	9	4
С	0	4	4	4	0
D	0	4	3	3	1

► Imagine a treatment assignment mechanism where people get to *choose* their treatment

Treatment Assignment by Self-Selection

	D	<i>Y</i> <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect
Α	1	7	4	7	3
В	1	9	5	9	4
С	0	4	4	4	0
D	0	4	3	3	1
$E(Y_1) =$		8			
$E(Y_0) =$			3.5		

 Imagine a treatment assignment mechanism where people get to choose their treatment

# Treatment Assignment by Self-Selection

	D	<i>Y</i> <sub>1</sub>	Y <sub>0</sub>	Yi	Real Effect
Α	1	7	4	7	3
В	1	9	5	9	4
С	0	4	4	4	0
D	0	4	3	3	1
$E(Y_1) =$		8			
$E(Y_0) =$			3.5		

- $\rightarrow$  ATE = 8 3.5 = 4.5
- ► This is **self-selection bias** treatment is affected by potential outcomes

► Depending on the treatment assignment mechanism we get a range of Average Treatment Effects:

# Comparing Average Treatment Effects

Treated Units	ATE
Real Effect for all units	2
A & D	1
Women	-0.5
Self-selection	4.5

We can identify the source of these biases in potential outcomes:

We can identify the source of these biases in potential outcomes:

$$\underbrace{E(Y_i|D=1) - E(Y_i|D=0)}_{\text{Observed Effect}} \quad (4)$$

► We can identify the source of these biases in potential outcomes:

$$\underbrace{\frac{E(Y_i|D=1)-E(Y_i|D=0)}{\text{Observed Effect}}}_{\text{Observed Effect}} = \underbrace{\frac{E(Y_{1i}-Y_{0i})}{\text{Real ATE}}}_{\text{Real ATE}} + \underbrace{\frac{1}{2}\Big[E(Y_{1i}|D=1)-E(Y_{1i}|D=0)\Big]}_{\text{Imbalance on } Y_1} + \underbrace{\frac{1}{2}\Big[E(Y_{0i}|D=1)-E(Y_{0i}|D=0)\Big]}_{\text{Imbalance on } Y_0}$$
(5)

NB: For equal-sized treatment and control groups

► Disaggregating the Self-Selection Bias:

$$\frac{(7+9-4-3)}{2} = \frac{(7+9+4+4-4-5-4-3)}{4} + \frac{1}{2} \left[ \frac{(7+9)}{2} - \frac{(4+4)}{2} \right] + \frac{1}{2} \left[ \frac{(4+5)}{2} - \frac{(4+3)}{2} \right] + \frac{1}{2} \left[ \frac{(4+5)}{2} - \frac{(4+3)}{2} \right]$$

$$4.5 = 2 + 2 + \frac{1}{2} \quad (6)$$