Making Causal Critiques Day 2 - Fundamental Critiques

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- Proportional Representation electoral systems have more parties
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- ► Development helps democracies endure
- ...And that's about it

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- ► Many investigate **specific** events, not generalizable variables

Causal Inference Observational Data 3 Critiques Introduction

What do political scientists **know**?

knowledge about what explains political processes Many add descriptive knowledge

▶ Thousands of books and papers have *not* generated any

- Many investigate specific events, not generalizable variables
- Many highlight correlations between variables

► Why aren't case studies enough?

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- And detailed case studies can help us identify plausible hypotheses
- ▶ But the only way to *confirm* the hypothesis is to verify that:
 - In other cases, the presence of the condition also produces the same outcome (if not, the explanation is not sufficient)
 - 2. The absence of the condition does not produce the same outcome (if not, the explanation is not necessary)

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- ► For example, we could look at India and conclude large Asian countries produce successful democracies
 - ► But...China
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- Only by looking at other cases, particularly 'control' cases (small non-Asian countries) can we understand if this explanation is plausible

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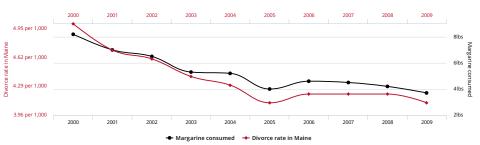
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 - ► By chance...
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 - ightharpoonup But we cannot conclude that there is a causal effect of x on y
- More data will not help
- ► The problem is the type of data; it does not allow us to answer causal question

Divorce rate in Maine

correlates with

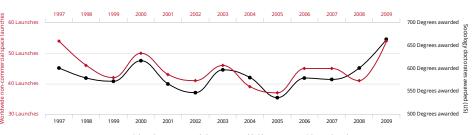
Per capita consumption of margarine



Worldwide non-commercial space launches

correlates with

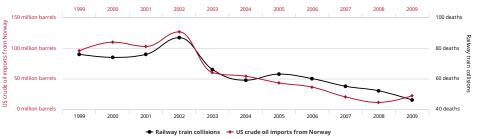
Sociology doctorates awarded (US)



US crude oil imports from Norway

correlates with

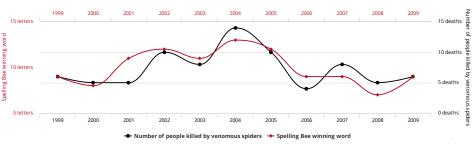
Drivers killed in collision with railway train



Letters in Winning Word of Scripps National Spelling Bee

correlates with

Number of people killed by venomous spiders



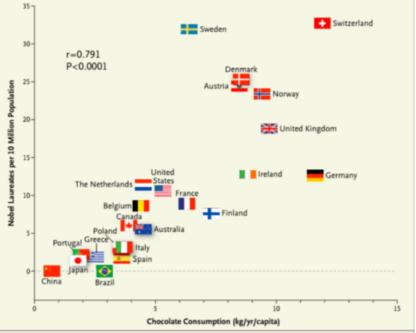


Figure 1. Correlation between Countries' Annual Per Capita Chocolate Consumption and the Number of Nobel Laureates per 10 Million Population.

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 - For prediction, correlation is fine: If we know a country has income of US\$50,000 per capita we can confidently predict it is perceived as being less corrupt
 - But for intervention, correlation does not help: investing to boost the economy does nothing on its own to reduce corruption
- ► So if we want to provide policy-relevant advice, we need to know more than just correlation

- ► Why isn't correlation enough?
 - ► For explanation, correlation also fails it is no explanation to say that you are a student because you are in your 20's
 - Explanation means identifying the direct and 'local' causal effects

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 Introduction
 Causal Inference
 Observational Data
 3 Critiques

- Why isn't correlation enough?
 - People are **strategic**, so their behaviour changes
- ► The Lucas Critique: Relationships fall apart when we intervene with policy
 - The data shows no-one lies on their tax forms
 - So let's abandon tax checks; the government wants to save money
 - But reducing checks reduces the chances of getting caught
 - Citizens start to lie on their tax forms
- ► That means we need to understand what *causes* people to lie on tax forms, so we can better understand their behaviour

► To accumulate knowledge, we have to ask specific types of questions:

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Causes of Effects	Effects of Causes
What caused Y?	Does X cause Y?
Why did the United States grow faster than Bolivia in the twentieth century?	Did the more permanent colonial settlement of the United States compared to Bolivia affect their subsequent growth rates?

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- ► A focus on a single explanatory variable *D* requires us to clearly define this 'treatment'
- ► AND to clearly define a control
 - What is the opposite of investing \$1bn in education?
 - No investment, or investing it elsewhere?
- ► Define treatment:

$$D_i = \begin{cases} 1, & \text{if treated} \\ 0, & \text{if not treated} \end{cases}$$

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 - Can we measure our outcome of interest?
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 - Tempting to look at many outcomes, but the risk of cherry-picking
 - All outcomes are probabilistic
 - If we study 20 outcomes, on average one will show a significant effect even with no real causal effect

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- eg. how a proportional representation electoral system affects investment in education
 - ► The **treatment** is a change to a PR electoral system (vs FPTP)
 - ► The **outcome** is the level of (public?) investment in education

► So we need a precise framework to analyze causation

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- ► The causal effect of treatment is how the unit's outcome differs when it is treated and not treated

- ► So we need a precise framework to analyze causation
- ► The causal effect of treatment is how the unit's outcome differs when it is treated and not treated
- ► These are the **potential outcomes** for unit *i*:

$$Y_{Di} = \begin{cases} Y_{1i} \text{ Potential Outcome if unit i treated} \\ Y_{0i} \text{ Potential Outcome if unit i not treated} \end{cases}$$

► Treatment Effect = $Y_{1i} - Y_{0i}$

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 - Would World War I still have happened if Archduke Franz Ferdinand had not been assassinated in 1914?
 - Would people have voted for Brexit if the campaign had been better regulated?
 - Would Brazil have won the 2014 World Cup if Neymar had not been injured?
- ► To explain a class of events not a single event we need multiple counterfactual comparisons

Potential Outcomes Example

	Investment in Education if PR system	Investment in Educa- tion if FPTP system	
	Y ₁	Y ₀	Treatment Effect
Brasil	8	4	4
Argentina	10	7	3
Bolivia	2	4	-2
Colombia	11	11	0
Peru	6	2	4

► The Fundamental Problem of Causal Inference

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 - ▶ No units can receive both treatment and control

- ► The Fundamental Problem of Causal Inference
 - No units can receive **both** treatment and control
 - So we can never observe both Y₁ and Y₀ for the same unit

Potential Outcomes Example

	PR Sys- tem?	Investment in Education if PR system	Investment in Education if FPTP system	
	Di	Y ₁	Y ₀	Treatment Effect
Brasil	1	8	?	?
Argentina	1	10	?	?
Bolivia	0	?	4	?
Colombia	0	?	11	?
Peru	0	?	2	?

► We can't even look at the change in countries that switch to a PR system

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 - ▶ What if all countries had started to invest more in education at the same time, for different reasons?

- We can't even look at the change in countries that switch to a PR system
 - What if all countries had started to invest more in education at the same time, for different reasons?
 - The potential outcome for Country X in time 1 is different to at time 2

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 - ► This is **impossible** to know
 - We can only estimate the effect by comparing across units in some way
 - ► That is why we are doing causal **inference**, not causal proof

► Which comparisons to make?

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- Which comparisons to make?
- Control units can never be perfect substitutes
- Causal Inference is all about identifying a plausible counterfactual
 - Plausible means that the potential outcomes of the control unit are likely to be the same as those of the treated unit

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 - On the Treatment Assignment Mechanism
- ► If we 'treated' an outlier like the Galapagos Islands, could we find a comparable control unit?
- ► Comparisons are easier where the **Treatment Assignment Mechanism is independent of potential outcomes**
 - This makes it more likely that potential outcomes are 'balanced' and comparable

► Types of Research Design:

Add caption

	creatment assignment	ate com outcome Indepen
Controlled Experiments	Yes	Yes
Natural Experiments	No	Yes
Observable Studies	No	No

Researcher controls the treatment assignment

Treatme

mechan

► Observational Studies

- Observational Studies
 - Household surveys
 - Simple regression on secondary data
 - ► Interviews of a random sample

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- We do not know what the treatment assignment mechanism was
 - Which units were treated and why?
- Treatment assignment is unlikely to create comparable potential outcomes
 - Which units might be appropriate counterfactuals?

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Calculating Treatment Effects

	D	<i>Y</i> ₁	<i>Y</i> ₀	Yi	Real Effect, $Y_1 - Y_0$
Α	1	7	4	7	3
В	0	9	5	5	4
С	0	4	4	4	0
D	1	4	3	4	1

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$E(Y_1) =$		6			
$E(Y_0) =$			4		

$$\rightarrow$$
 ATE = $E(Y_1 - Y_0) = 8/4 = 2$

$$\rightarrow$$
 ATE = $E(Y_1) - E(Y_0) = 6 - 4 = 2$

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$E(Y_1) =$		5.5			
$E(Y_0) =$			4.5		

▶ If we use the control units as counterfactuals...

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- Average Treatment Effect:

$$ATE = E(Y_1) - E(Y_0) \tag{1}$$

$$=$$
 5.5 $-$ 4.5 (2)

Observational Data

$$= 1 (3)$$

Half the true treatment effect

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- ► Why?

3 Critiques

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- ► Half the true treatment effect
- ► Why?
 - ► The units that got treated had lower Y₁
 - ► The units that were controls had higher Y₀
 - ► The 'stand-in' counterfactuals were wrong

► The bias in units' potential outcomes depends on which units get treated and which ones don't

Problems with Observational Data

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Problems with Observational Data

- ► The bias in units' potential outcomes depends on which units get treated and which ones don't
- ► In observational studies, we have very little protection against causal critiques
 - 1. Omitted variable bias (confounding)
 - 2. Selection bias
 - 3. Reverse Causation

► Wealthier countries are more likely to be democracies

- Wealthier countries are more likely to be democracies
 - ► But wealthier countries are more likely to be European

- Wealthier countries are more likely to be democracies
 - But wealthier countries are more likely to be European
 - And democracies are more likely to be European

- Wealthier countries are more likely to be democracies
 - But wealthier countries are more likely to be European
 - And democracies are more likely to be European
- ► Maybe the correlation just reflects the fact that European countries are 'different'?

```
## Error in create_graph() %>%
add_global_graph_attrs("graph", "rankdir", : could
not find function "%>%"
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► Imagine a treatment assignment mechanism where all women get treated

Treatment Assignment by Covariate

	Χ	D	Y ₁	Y ₀	Yi	Real Effect
Α	Man	0	7	4	4	3
В	Man	0	9	5	5	4
С	Woman	1	4	4	4	0
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$E(Y_0) =$				4.5		

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$E(Y_0) =$				4.5		

- \blacktriangleright ATE = 4 4.5 = -0.5
- ▶ This is **confounding** or an **omitted variable** another variable affects both treatment and potential outcomes 33/48

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 - But wealthy autocracies and poor democracies do not like to report data

Self-Selecion Bias

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Self-Selecion Bias

- Wealthier countries are more likely to be democracies
 - But wealthy autocracies and poor democracies do not like to report data
 - So we cannot compare them
 - Only wealthy democracies 'self-select' into our sample

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$E(Y_1) =$		8			
$E(Y_0) =$			3.5		

► Imagine a treatment assignment mechanism where people get to *choose* their treatment

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- \rightarrow ATE = 8 3.5 = 4.5
- ► This is **self-selection bias** treatment is affected by potential outcomes

► We can identify the source of these biases in potential outcomes:

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$$\underbrace{E(Y_i|D=1) - E(Y_i|D=0)}_{\text{Observed Effect}} \quad (4)$$

▶ We can identify the source of these biases in potential outcomes:

$$\underbrace{E(Y_{i}|D=1) - E(Y_{i}|D=0)}_{\text{Observed Effect}} = \underbrace{E(Y_{1i} - Y_{0i})}_{\text{Real ATE}} + \underbrace{\frac{1}{2} \Big[E(Y_{1i}|D=1) - E(Y_{1i}|D=0) \Big]}_{\text{Imbalance on } Y_{1}} + \underbrace{\frac{1}{2} \Big[E(Y_{0i}|D=1) - E(Y_{0i}|D=0) \Big]}_{\text{Imbalance on } Y_{0}}$$
(5)

NB: For equal-sized treatment and control groups

Disaggregating the Self-Selection Bias:

$$\frac{(7+9-4-3)}{2} = \frac{(7+9+4+4-4-5-4-3)}{4} + \frac{1}{2} \left[\frac{(7+9)}{2} - \frac{(4+4)}{2} \right] + \frac{1}{2} \left[\frac{(4+5)}{2} - \frac{(4+3)}{2} \right] + \frac{1}{2} \left[\frac{(4+5)}{2} - \frac{(4+3)}{2} \right]$$

$$4.5 = 2 + 2 + \frac{1}{2} \quad (6)$$

► Depending on the treatment assignment mechanism we get a range of Average Treatment Effects:

Comparing Average Treatment Effects

Treated Units	ATE
Real Effect for all units	2
A & D	1
Omitted Variable Bias (Women)	-0.5
Self-selection	4.5

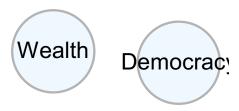
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 - But does wealth create democracy?
 - Or democracy create wealth?
- We cannot tell from the correlation alone
- Both may be true







▶ Where treatment has no effect

Treatment Assignment by Covariate

	D	<i>Y</i> ₁	Y_0	Yi	Real Effect
Α	0	7	7	7	0
В	0	9	9	9	0
С	1	4	4	4	0
D	1	4	4	4	0

▶ Where treatment has no effect

Treatment Assignment by Covariate

	D	Y ₁	<i>Y</i> ₀	Yi	Real Effect
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$E(Y_1) =$		4			
$E(Y_0) =$			4		

Reverse Causation

▶ Where treatment has no effect

Treatment Assignment by Covariate

	D	Y ₁	<i>Y</i> ₀	Yi	Real Effect
Α	0	7	7	7	0
В	0	9	9	9	0
С	1	4	4	4	0
D	1	4	4	4	0
$E(Y_1) =$		4			
$E(Y_0) =$			4		

- \blacktriangleright ATE = 4 4 = 0. There is no effect.
- ► The (negative) correlation between *D* and *Y* is because *Y* causes *D*

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 - Label this number Y₀.

- ► Does fruit make you happier?
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 - ▶ Label this number Y₁.
 - Then write down a second number between 0 and 10 representing how happy you would be if I did NOT give you an apple now.
 - ► Label this number *Y*₀.
- ► These are your **potential outcomes**.

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- Now we will consider how estimates of the average effect of fruit on happiness vary depending on how treatment (apples) are assigned.
 - 1. All the female participants are given an apple.
 - 2. The tallest half are given an apple.
 - 3. You are free to choose yourself to take an apple or not.
 - 4. Apples are distributed randomly