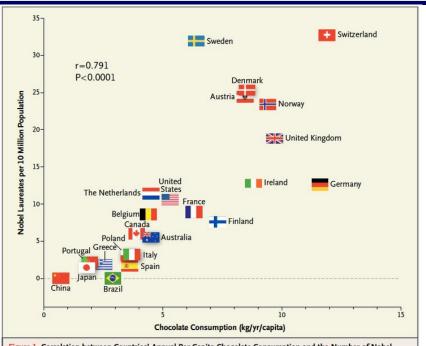
FLS 6441 - Methods III: Explanation and Causation

Week 2 - A Framework for Explanation

Jonathan Phillips

March 2019

Explanation	Causal Inference	Why Observational Data is Biased	Rest of the Course



► Why isn't correlation enough?

Rest of the Course

- Why isn't correlation enough?
 - For prediction, correlation is fine: If we know a country has chocolate consumption of 10kg/yr/capita we can reasonably predict it will have about 25 Nobel Laureates

- Why isn't correlation enough?
 - For prediction, correlation is fine: If we know a country has chocolate consumption of 10kg/yr/capita we can reasonably predict it will have about 25 Nobel Laureates
 - But for intervention, correlation does not help: forcing people to eat more chocolate does nothing on its own to produce more Nobel Laureates

- Why isn't correlation enough?
 - For prediction, correlation is fine: If we know a country has chocolate consumption of 10kg/yr/capita we can reasonably predict it will have about 25 Nobel Laureates
 - ► But for **intervention**, correlation does not help: forcing people to eat more chocolate does nothing on its own to produce more Nobel Laureates
 - ► For **explanation**, correlation also fails it is no *explanation* to say that Switzerland has the most Nobel Laureates because it has the highest chocolate consumption

► What does it mean to explain something?

Why Observational Data is Biased

Explanation

- ▶ What does it mean to explain something?
- ► To give an account of what happens, and why
 - ► The 'chain of causation'

Explanation

- What does it mean to explain something?
- ▶ To give an account of what happens, and why
 - The 'chain of causation'
- ▶ If D explains y, we are saying that the absence of D would have led to a different value of y

Why Observational Data is Biased

- ▶ What does it mean to explain something?
- ► To give an account of what happens, and why
 - ▶ The 'chain of causation'
- ► If *D* explains *y*, we are saying that the *absence* of *D* would have led to a different value of *y*
- ► There exists a 'counterfactual' possibility that did not happen

Deterministic Explanation

Why Observational Data is Biased

Explanation

Explanation

Deterministic Explanation

Sufficient conditions: Every time D happens, Y happens

Deterministic Explanation

- Sufficient conditions: Every time D happens, Y happens
- Necessary conditions: Y does not happen if D does not happen ('but for')

Deterministic Explanation

- Sufficient conditions: Every time D happens, Y happens
- Necessary conditions: Y does not happen if D does not happen ('but for')

Probabilistic Explanation

Deterministic Explanation

- Sufficient conditions: Every time D happens, Y happens
- ► Necessary conditions: Y does not happen if D does not happen ('but for')

Probabilistic Explanation

▶ If D happens, the **probability** of Y increases

Explanation

Deterministic Explanation

- Sufficient conditions: Every time D happens, Y happens
- ▶ Necessary conditions: Y does not happen if D does not happen ('but for')

Probabilistic Explanation

Why Observational Data is Biased

- ▶ If D happens, the **probability** of Y increases
- ▶ Treatment effects are a distribution, not a single value

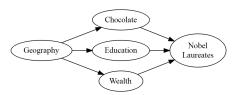
► Two perspectives on explanation:

Rest of the Course

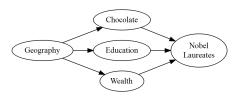
► Two perspectives on explanation:

Causes of Effects	Effects of Causes		
What caused Y?	Does D cause Y?		
Why does Switzerland have so many Nobel laureates?	Does chocolate cause more Nobel laureates?		
Backward-looking	Forward-looking		

► Two perspectives on explanation:



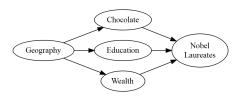
► Two perspectives on explanation:



 Identifying the source of ALL of the variation in Nobel Laureates Why Observational Data is Biased

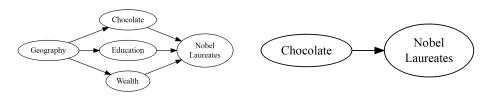
Explanation

► Two perspectives on explanation:



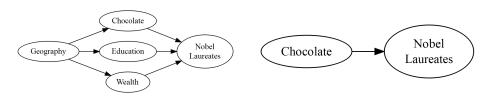
- ► Identifying the source of ALL of the variation in Nobel Laureates
- ▶ An infinite task!

► Two perspectives on explanation:



- ► Identifying the source of ALL of the variation in Nobel Laureates
- ▶ An infinite task!

► Two perspectives on explanation:

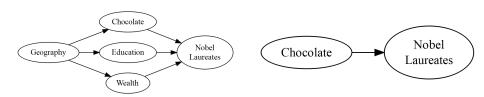


- ► Identifying the source of ALL of the variation in Nobel Laureates
- An infinite task!

► Identifying how much **ONE** variable causes variation in Nobel Laureates

Explanation

► Two perspectives on explanation:

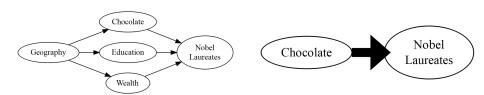


- Identifying the source of ALL of the variation in Nobel Laureates
- ► An infinite task!

- Identifying how much ONE variable causes variation in Nobel Laureates
- ► This we can do!

Rest of the Course

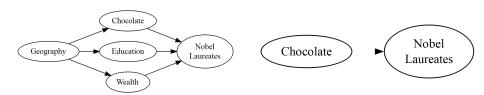
► Two perspectives on explanation:



- ► Identifying the source of ALL of the variation in Nobel Laureates
- An infinite task!

- ► Identifying how much **ONE** variable causes variation in Nobel Laureates
- ▶ This we can do!

► Two perspectives on explanation:



- ► Identifying the source of ALL of the variation in Nobel Laureates
- An infinite task!

- ► Identifying how much **ONE** variable causes variation in Nobel Laureates
- ► This we can do!

Explanation

► A focus on a single explanatory variable *D* requires a clear definition of 'Treatment'

Why Observational Data is Biased

- ► A focus on a single explanatory variable *D* requires a clear definition of 'Treatment'
- ► AND to clearly define a 'Control'

- ► A focus on a single explanatory variable *D* requires a clear definition of 'Treatment'
- AND to clearly define a 'Control'
 - What is the opposite of investing \$1bn in education?

- ► A focus on a single explanatory variable *D* requires a clear definition of 'Treatment'
- AND to clearly define a 'Control'
 - What is the opposite of investing \$1bn in education?
 - No investment, or investing it elsewhere?

Explanation

▶ A focus on a single explanatory variable *D* requires a clear definition of 'Treatment'

Why Observational Data is Biased

- AND to clearly define a 'Control'
 - What is the opposite of investing \$1bn in education?
 - No investment, or investing it elsewhere?
- Define treatment:

$$D_i = \begin{cases} 1, & \text{if treated} \\ 0, & \text{if not treated} \end{cases}$$

▶ Defining our outcome variable:

- ► Defining our outcome variable:
 - ▶ Is it the outcome we really care about? Or just what's easy to measure?

Explanation

- ▶ Defining our outcome variable:
 - ► Is it the outcome we really care about? Or just what's easy to measure?

Why Observational Data is Biased

What theory are we testing?

- Defining our outcome variable:
 - ► Is it the outcome we really care about? Or just what's easy to measure?
 - What theory are we testing?
- Tempting to look at many outcomes, but the risk of 'cherry-picking'

- ► Defining our outcome variable:
 - Is it the outcome we really care about? Or just what's easy to measure?
 - What theory are we testing?
- Tempting to look at many outcomes, but the risk of 'cherry-picking'
 - All outcomes are **probabilistic** (due to all the other factors we haven't accounted for)

- ► Defining our outcome variable:
 - Is it the outcome we really care about? Or just what's easy to measure?
 - What theory are we testing?
- Tempting to look at many outcomes, but the risk of 'cherry-picking'
 - ► All outcomes are **probabilistic** (due to all the other factors we haven't accounted for)
 - If we study 20 outcomes, on average one will show a significant effect even with no real causal effect

- ► Defining our outcome variable:
 - Is it the outcome we really care about? Or just what's easy to measure?
 - What theory are we testing?
- Tempting to look at many outcomes, but the risk of 'cherry-picking'
 - ► All outcomes are **probabilistic** (due to all the other factors we haven't accounted for)
 - If we study 20 outcomes, on average one will show a significant effect even with no real causal effect
- ► So we usually want to study a single outcome

Explanation

► What are the **units** of our analysis?

Rest of the Course

Explanation

- ► What are the **units** of our analysis?
 - ► Countries? Political Parties? Individuals?

Rest of the Course

- ► What are the **units** of our analysis?
 - Countries? Political Parties? Individuals?
 - At what level does causality operate?

- What are the units of our analysis?
 - Countries? Political Parties? Individuals?
 - At what level does causality operate?
- eg. How does the electoral system affect attitudes to redistribution?

- What are the units of our analysis?
 - Countries? Political Parties? Individuals?
 - At what level does causality operate?
- eg. How does the electoral system affect attitudes to redistribution?
 - ➤ Treatment at the national level

- What are the units of our analysis?
 - Countries? Political Parties? Individuals?
 - At what level does causality operate?
- eg. How does the electoral system affect attitudes to redistribution?
 - ▶ Treatment at the national level
 - Outcome varies at the individual level

- What are the units of our analysis?
 - Countries? Political Parties? Individuals?
 - At what level does causality operate?
- eg. How does the electoral system affect attitudes to redistribution?
 - ▶ Treatment at the national level
 - Outcome varies at the individual level
 - Measurement needed at the lowest (individual) level

- What are the units of our analysis?
 - Countries? Political Parties? Individuals?
 - At what level does causality operate?
- eg. How does the electoral system affect attitudes to redistribution?
 - ▶ Treatment at the national level
 - Outcome varies at the individual level
 - ► Measurement needed at the lowest (individual) level
 - But our analysis needs to take account of the 'clustered' treatment

- What are the units of our analysis?
 - Countries? Political Parties? Individuals?
 - At what level does causality operate?
- ▶ eg. How does the electoral system affect attitudes to redistribution?
 - Treatment at the national level
 - Outcome varies at the individual level
 - Measurement needed at the lowest (individual) level
 - But our analysis needs to take account of the 'clustered' treatment
- ▶ Units are **time-specific**: the same person 10 minutes later is a different unit

Section 2

Why Observational Data is Biased

Causal Inference

Explanation

▶ The causal effect of treatment is how each unit's outcome differs when it is treated and not treated

▶ The causal effect of treatment is how each unit's outcome differs when it is treated and not treated

Why Observational Data is Biased

▶ This means comparing the **Potential Outcomes** for unit *i*:

$$Y_{Di} = \begin{cases} Y_{1i} \text{ Potential Outcome if unit i treated} \\ Y_{0i} \text{ Potential Outcome if unit i NOT treated} \end{cases}$$

Explanation

▶ The causal effect of treatment is how each unit's outcome differs when it is treated and not treated

Why Observational Data is Biased

▶ This means comparing the **Potential Outcomes** for unit *i*:

$$Y_{Di} = \begin{cases} Y_{1i} \text{ Potential Outcome if unit i treated} \\ Y_{0i} \text{ Potential Outcome if unit i NOT treated} \end{cases}$$

▶ Individual Treatment Effect for unit *i*: $\alpha_i = Y_{1i} - Y_{0i}$

Explanation

► The causal effect of treatment is how each unit's outcome differs when it is treated and not treated

Why Observational Data is Biased

▶ This means comparing the **Potential Outcomes** for unit *i*:

$$Y_{Di} = \begin{cases} Y_{1i} \text{ GDP Growth of Brazil in 2010 if a Democracy} \\ Y_{0i} \text{ GDP Growth of Brazil in 2010 if NOT a Democracy} \end{cases}$$

▶ Individual Treatment Effect for unit i: $\alpha_i = Y_{1i} - Y_{0i}$

Explanation

► We are explicitly thinking about **counterfactuals**

- ▶ We are explicitly thinking about counterfactuals
 - What would have happened to the same unit if the treatment had not happened?

Explanation

- ► We are explicitly thinking about **counterfactuals**
 - What would have happened to the same unit if the treatment had not happened?

Why Observational Data is Biased

What would Brazil's GDP growth rate be if we lived in a dictatorship?

- ▶ We are explicitly thinking about counterfactuals
 - What would have happened to the same unit if the treatment had not happened?

- What would Brazil's GDP growth rate be if we lived in a dictatorship?
- Would World War I still have happened if Archduke Franz Ferdinand had not been assassinated in 1914?

- ▶ We are explicitly thinking about counterfactuals
 - What would have happened to the same unit if the treatment had not happened?

- What would Brazil's GDP growth rate be if we lived in a dictatorship?
- Would World War I still have happened if Archduke Franz Ferdinand had not been assassinated in 1914?
- Would Brazil have won the 2014 World Cup if Neymar had not been injured?

Explanation

- ▶ We are explicitly thinking about counterfactuals
 - What would have happened to the same unit if the treatment had not happened?

- What would Brazil's GDP growth rate be if we lived in a dictatorship?
- Would World War I still have happened if Archduke Franz Ferdinand had not been assassinated in 1914?
- Would Brazil have won the 2014 World Cup if Neymar had not been injured?



Potential Outcomes are just another Variable for each Unit

	GDP Growth if		
	Democracy	NOT Democ-	Effect
		racy	
	Y ₁	Y ₀	$Y_1 - Y_0$
Brasil	4	1	3
Argentina	7	4	3
Bolivia	2	4	-2
Colombia	7	7	0
Peru	5	4	1

► Political Science is not about explaining individual events

- ▶ Political Science is not about explaining individual events
- ▶ We ideally want general theories that apply to all our units

- ► Political Science is not about explaining individual events
- ▶ We ideally want general theories that apply to all our units

Why Observational Data is Biased

➤ To explain a systematic treatment - not a single event - we need multiple counterfactual comparisons

Explanation

- ▶ Political Science is not about explaining individual events
- ▶ We ideally want general theories that apply to all our units

- ► To explain a systematic treatment not a single event we need multiple counterfactual comparisons
- ▶ We know how democracy works in Europe; the question is what will happen if it becomes more common in the whole world?

Explanation

- ▶ Political Science is not about explaining individual events
- ▶ We ideally want general theories that apply to all our units
- ► To explain a systematic treatment not a single event we need multiple counterfactual comparisons
- ▶ We know how democracy works in Europe; the question is what will happen if it becomes more common in the whole world?

Average Treatment Effect

We want to calculate an Average Treatment Effect

Rest of the Course

Explanation

- ▶ Political Science is not about explaining individual events
- ▶ We ideally want general theories that apply to all our units

Why Observational Data is Biased

- ► To explain a systematic treatment not a single event we need multiple counterfactual comparisons
- ▶ We know how democracy works in Europe; the question is what will happen if it becomes more common in the whole world?

Average Treatment Effect

We want to calculate an Average Treatment Effect

$$ATE = E(\alpha_i) = E(Y_1 - Y_0) = E(Y_1) - E(Y_0) = \frac{\sum_i (Y_{1i} - Y_{0i})}{N}$$

Explanation

Potential Outcomes are just another Variable for each Unit

	GDP Growth if	GDP Growth if	Treatment
	Democracy	NOT Democ-	Effect
		racy	
	Y_1	Y ₀	$Y_1 - Y_0$
Brasil	4	1	3
Argentina	7	4	3
Bolivia	2	4	-2
Colombia	7	7	0
Peru	5	4	1
Average Treatment Effect	5	4	1

Explanation

▶ In reality, some units are **actually treated** (D = 1), others are actually control (D = 0)

Explanation

▶ In reality, some units are **actually treated** (D = 1), others are actually control (D=0)

Why Observational Data is Biased

Average Treatment Effect on the Treated

$$\mathsf{ATT} = \mathsf{E}(\alpha_i | D = 1) = E(Y_1 - Y_0 | D = 1) = \frac{\sum_i (Y_{1i} - Y_{0i} | D = 1)}{N_{Treated}} \quad (1)$$

Explanation

▶ In reality, some units are **actually treated** (D = 1), others are actually control (D = 0)

Why Observational Data is Biased

Average Treatment Effect on the Treated

$$ATT = E(\alpha_i | D = 1) = E(Y_1 - Y_0 | D = 1) = \frac{\sum_i (Y_{1i} - Y_{0i} | D = 1)}{N_{Treated}}$$
 (1)

Average Treatment Effect on the Untreated (Control)

ATU=E(
$$\alpha_i|D=0$$
) = $E(Y_1-Y_0|D=0)=\frac{\sum_i(Y_{1i}-Y_{0i}|D=0)}{N_{Control}}$ (2)

Explanation

▶ In reality, some units are **actually treated** (D = 1), others are actually control (D=0)

Why Observational Data is Biased

Average Treatment Effect on the Treated

$$\mathsf{ATT} = \mathsf{E}(\alpha_i | D = 1) = \mathsf{E}(Y_1 - Y_0 | D = 1) = \frac{\sum_i (Y_{1i} - Y_{0i} | D = 1)}{N_{Treated}}$$

Average Treatment Effect on the Untreated (Control)

ATU=E(
$$\alpha_i|D=0$$
) = $E(Y_1-Y_0|D=0)=\frac{\sum_i(Y_{1i}-Y_{0i}|D=0)}{N_{Control}}$

- ► The three effect estimates are usually different
 - ► The effect democracy has had in Europe is different to the effect if it were introduced in Africa

(2)

(1)

Explanation

Potential Outcomes Example

	Democracy?	GDP Growth if Democ-	GDP Growth if NOT Democ-	Treatment Effect
		racy	racy	
	Di	Y ₁	Y ₀	Y_1-Y_0
Brasil	1	4	1	3
Argentina	0	7	4	3
Bolivia	1	2	4	-2
Colombia	0	7	7	0
Peru	0	5	4	1

Explanation

Potential Outcomes Example

	Democracy?	GDP Growth if Democ- racy	GDP Growth if NOT Democ- racy	Treatment Effect
	Di	Υ ₁	Y ₀	$Y_1 - Y_0$
Brasil	1	4	1	3
Bolivia	1	2	4	-2
ATT	1	3	2.5	0.5

Potential Outcomes Example

	Democracy?	GDP Growth if Democ- racy	GDP Growth if NOT Democ- racy	Treatment Effect
	Di	Y ₁	Y ₀	$Y_1 - Y_0$
Argentina	0	7	4	3
Colombia	0	7	7	0
Peru	0	5	4	1
ATU	0	6.3	5	1.3

The Fundamental Problem of Causal Inference

► No units can receive **both** treatment and control

Explanation

The Fundamental Problem of Causal Inference

- No units can receive **both** treatment and control
- \blacktriangleright So we can never observe both Y_1 and Y_0 for the same unit

Explanation

The Fundamental Problem of Causal Inference

No units can receive **both** treatment and control

- \triangleright So we can never observe both Y_1 and Y_0 for the same unit
- ► Individual Treatment Effects are Impossible to Estimate

Explanation

The Fundamental Problem of Causal Inference

No units can receive **both** treatment and control

- \triangleright So we can never observe both Y_1 and Y_0 for the same unit
- ► Individual Treatment Effects are Impossible to Estimate

$$Y_i^{obs} = \begin{cases} Y_{1i} \text{ if } D_i = 1\\ Y_{0i} \text{ if } D_i = 0 \end{cases}$$

The Fundamental Problem of Causal Inference

No units can receive **both** treatment and control

- \triangleright So we can never observe both Y_1 and Y_0 for the same unit
- ► Individual Treatment Effects are Impossible to Estimate

$$Y_{i}^{obs} = \begin{cases} Y_{1i} \text{ if } D_{i} = 1\\ Y_{0i} \text{ if } D_{i} = 0 \end{cases}$$
$$Y_{i}^{obs} = D_{i} \cdot Y_{1i} + (1 - D_{i}) \cdot Y_{0i}$$

Explanation

Potential Outcomes Example

	Democracy?	GDP Growth if Democ-	GDP Growth if NOT Democ-	Treatment Effect
		racy	racy	
	Di	Y ₁	Y ₀	Y_1-Y_0
Brasil	1	4	1	3
Argentina	0	7	4	3
Bolivia	1	2	4	-2
Colombia	0	7	7	0
Peru	0	5	4	1

Explanation

Potential Outcomes Example

	Democracy?	GDP Growth if Democ-	GDP Growth if NOT Democ-	Treatment Effect
		racy	racy	
	Di	Y ₁	Y_0	Y_1-Y_0
Brasil	1	4	?	?
Argentina	0	?	4	?
Bolivia	1	2	?	?
Colombia	0	?	7	?
Peru	0	?	4	?

Explanation

Potential Outcomes Example

	Democracy?	if Democ-	GDP Growth if NOT Democ-	Observed GDP Growth
		racy	racy	
	Di	Y ₁	Y ₀	Y ^{obs}
Brasil	1	4	?	4
Argentina	0	?	4	4
Bolivia	1	2	?	2
Colombia	0	?	7	7
Peru	0	?	4	4

Potential Outcomes Example

	Democracy?	Observed GDP Growth
	Di	Y ^{obs}
Brasil	1	4
Argentina	0	4
Bolivia	1	2
Colombia	0	7
Peru	0	4

► Actually, nothing stops us calculating the **Average Treatment Effect**

- Actually, nothing stops us calculating the Average **Treatment Effect**
- ▶ The question is, is the ATE accurate?

Explanation

Treatment Effect

Actually, nothing stops us calculating the Average

▶ The guestion is, is the ATE accurate?

	Democracy?	GDP Growth if Democ- racy	GDP Growth if NOT Democ- racy	Treatment Effect
	Di	Υ ₁	Y ₀	$Y_1 - Y_0$
Brasil	1	4	1	3
Argentina	0	7	4	3
Bolivia	1	2	4	-2
Colombia	0	7	7	0
Peru	0	5	4	1
Average Treat- ment Effect		5	4	1

Explanation

- ► Actually, nothing stops us calculating the **Average**Treatment Effect
- ► The guestion is, is the ATE accurate?

	Democracy?		GDP Growth if NOT Democ-	Treatment Effect
		if Democ- racy	racy	Ellect
	Di	Y ₁	Y ₀	$Y_1 - Y_0$
Brasil	1	4	?	?
Argentina	0	?	4	?
Bolivia	1	2	?	?
Colombia	0	?	7	?
Peru	0	?	4	?
Average Treat- ment Effect		3	5	-2

Why Observational Data is Biased

Causal Inference

Explanation

► So what went wrong?

Explanation

- So what went wrong?
- ► The potential outcomes we observe are a biased **representation** of the potential outcomes of all the units

Explanation

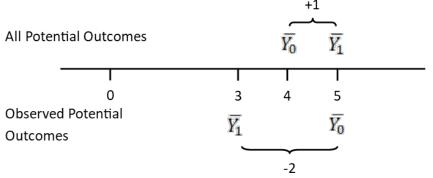
- So what went wrong?
- ► The potential outcomes we observe are a biased **representation** of the potential outcomes of all the units



Explanation

- So what went wrong?
- ► The potential outcomes we observe are a biased **representation** of the potential outcomes of all the units

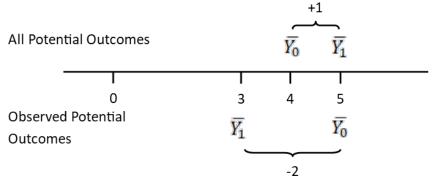
Why Observational Data is Biased



 \blacktriangleright $E(Y_1)$ values are **biased lower** in the observed data

Explanation

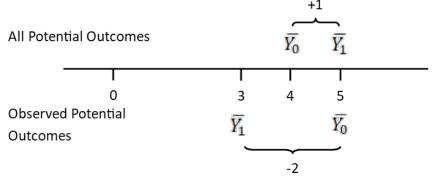
- So what went wrong?
- ► The potential outcomes we observe are a biased representation of the potential outcomes of all the units



- \blacktriangleright $E(Y_1)$ values are **biased lower** in the observed data
- \blacktriangleright $E(Y_0)$ values are **biased higher** in the observed data

► So what went wrong?

► The potential outcomes we **observe** are a **biased representation** of the potential outcomes of all the units



- \blacktriangleright $E(Y_1)$ values are **biased lower** in the observed data
- $ightharpoonup E(Y_0)$ values are **biased higher** in the observed data
- ► So $E(Y_1) E(Y_0)$ is biased

▶ The Fundamental Problem of Causal Inference means we can only discover causal relationships by comparing across units

▶ The Fundamental Problem of Causal Inference means we can only discover causal relationships by comparing across units

Why Observational Data is Biased

► Comparing treated i and control j units

Explanation

▶ The Fundamental Problem of Causal Inference means we can only discover causal relationships by comparing across units

- ► Comparing treated i and control j units
- ▶ If potential outcomes are biased in our observed data:

▶ The Fundamental Problem of Causal Inference means we can only discover causal relationships by comparing across units

- ► Comparing treated i and control j units
- ▶ If potential outcomes are biased in our observed data:
 - Our counterfactual case j does not represent what would have happened to i in the absence of treatment

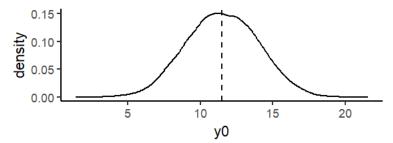
▶ The Fundamental Problem of Causal Inference means we can only discover causal relationships by comparing across units

- ► Comparing treated i and control j units
- ▶ If potential outcomes are biased in our observed data:
 - Our counterfactual case j does not represent what would have happened to i in the absence of treatment
 - Counterfactuals are not plausible

▶ The Fundamental Problem of Causal Inference means we can only discover causal relationships by comparing across units

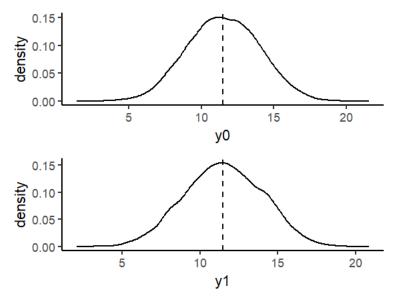
- ► Comparing treated i and control j units
- ▶ If potential outcomes are biased in our observed data:
 - Our counterfactual case j does not represent what would have happened to i in the absence of treatment
 - Counterfactuals are not plausible
 - Causal effects are biased

Explanation

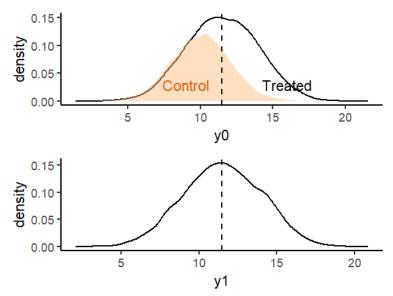


Rest of the Course

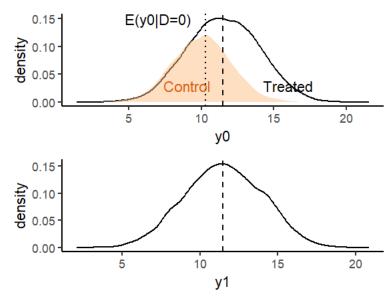
Explanation



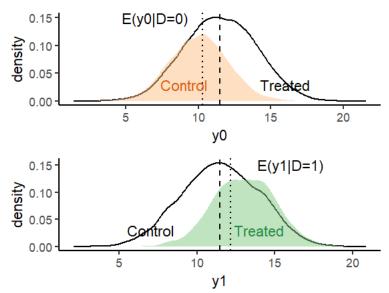
Explanation



Explanation



Explanation



► Lots of averages:

		Hypothetical outcome	
		Y0 Y1	
Actual Treatment	D = 0	$E(Y_{0i} D=0)$	$E(Y_{1i} D=0)$
	D = 1	$E(Y_{0i} D=1)$	$E(Y_{1i} D=1)$

Causal Inference

Explanation

► Lots of averages:

		Hypothetical outcome	
		Y0	Y1
Actual Treatment	D = 0	$E(Y_{0i} D=0)$	$E(Y_{1i} D=0)$
	D=1	$E(Y_{0i} D=1)$	$E(Y_{1i} D=1)$

► All our causal estimates are **averages**

Causal Inference

Explanation

- All our causal estimates are averages
 - We cannot distinguish the null hypothesis of no average effect from the sharp null hypothesis of no individual effects

Causal Inference

- All our causal estimates are averages
 - We cannot distinguish the null hypothesis of no average effect from the sharp null hypothesis of no individual effects

	No Average Effect $E(Y_1 - Y_0) = 0$	"Sharp null": No individual effects $(Y_{1i} - Y_{0i} = 0)$
Brasil	2	0
Argentina	-1	0
Bolivia	1	0
Colombia	0	0
Peru	-2	0
Average	0	0

Section 3

Explanation

▶ Why are potential outcomes biased in our data?

- ▶ Why are potential outcomes biased in our data?
 - 1. Omitted Variables

- ▶ Why are potential outcomes biased in our data?
 - 1. Omitted Variables
 - 2. Reverse Causation

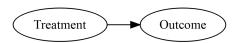
- ▶ Why are potential outcomes biased in our data?
 - 1. Omitted Variables
 - 2. Reverse Causation
 - 3. Selection Bias

- ▶ Why are potential outcomes biased in our data?
 - 1. Omitted Variables
 - 2. Reverse Causation
 - 3. Selection Bias
- In all of these cases the potential outcomes are distorted

- ▶ Why are potential outcomes biased in our data?
 - 1. Omitted Variables
 - 2. Reverse Causation
 - 3. Selection Bias
- In all of these cases the potential outcomes are distorted
- ► So basic regression is biased

Explanation

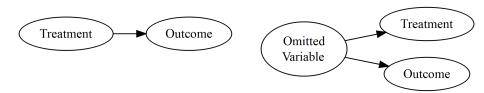
A real causal relationship:



Rest of the Course

A real causal relationship:

Being misled by omitted variable bias:



A real causal relationship:

Being misled by omitted variable bias:



▶ A third variable causes some units to have **different** values of potential outcomes, AND for those same units to be treated

A real causal relationship:

Being misled by omitted variable bias:

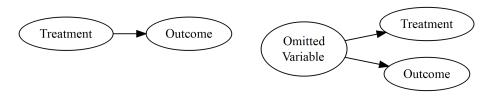


- A third variable causes some units to have different values of potential outcomes, AND for those same units to be treated
- ► So treated units have non-representative Y₁

Explanation

A real causal relationship:

Being misled by omitted variable bias:

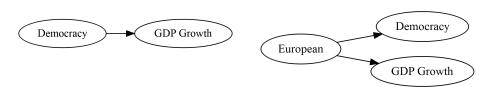


- ► A third variable causes some units to have different values of potential outcomes, AND for those same units to be treated
- ► So treated units have non-representative Y₁
- ► And control units have non-representative Y₀

Rest of the Course

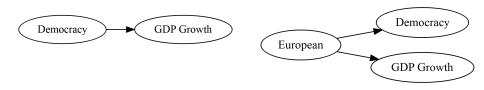
A real causal relationship:

Being misled by omitted variable bias:

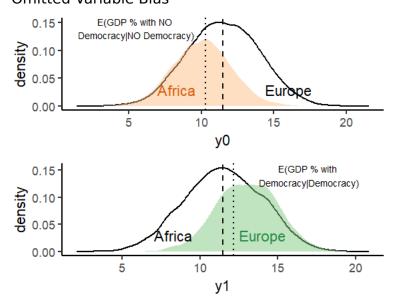


A real causal relationship:

Being misled by omitted variable bias:



 European countries faced conditions that encouraged both democracy and rapid GDP growth



Explanation

▶ Let's say that $Y_{1i} = Y_{0i} + \alpha$, where α is the real constant treatment effect

$$A\hat{T}E = E(Y_1|D=1) - E(Y_0|D=0)$$

Explanation

▶ Let's say that $Y_{1i} = Y_{0i} + \alpha$, where α is the real constant treatment effect

$$A\hat{T}E = E(Y_1|D=1) - E(Y_0|D=0)$$

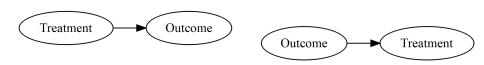
$$A\hat{T}E = \underbrace{\alpha}_{\text{Real ATE}} + \underbrace{E(Y_0|D=1) - E(Y_0|D=0)}_{\text{Bias}}$$

A real causal relationship:



A real causal relationship:

Being misled by reverse causation:

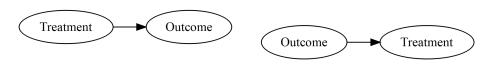


Explanation

A real causal relationship:

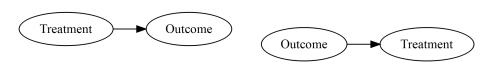
Being misled by reverse causation:

Why Observational Data is Biased



▶ D does not affect Y, but higher Y makes treatment (D) more likely

Explanation



- ► D does not affect Y, but higher Y makes treatment (D) more likely
- ► So the two variables are correlated

Rest of the Course

A real causal relationship:

Being misled by reverse causation:



A real causal relationship:

Being misled by reverse causation:



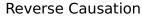
► GDP Growth encourages democratization

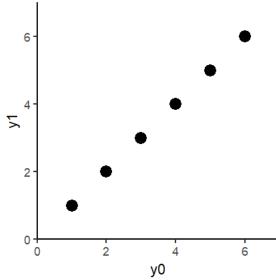
A real causal relationship:

Being misled by reverse causation:

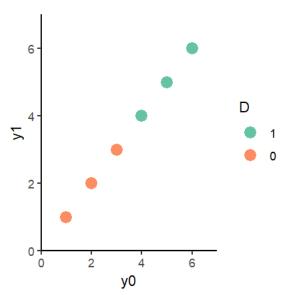


- ► GDP Growth encourages democratization
- ► So democracies are more likely to have experienced high growth rates



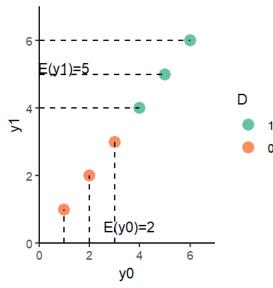


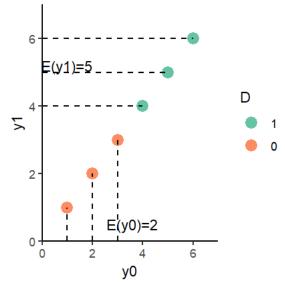
►
$$E(Y_1 - Y_0) = 0$$



Why Observational Data is Biased

Reverse Causation

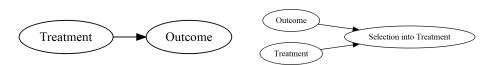




$$E(Y_1|D=1) - E(Y_0|D=0) = 5 - 2 = 3$$

A real causal relationship:

Being misled by Selection Bias:

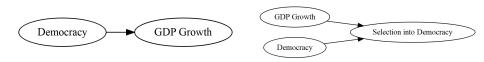


Explanation

A real causal relationship:

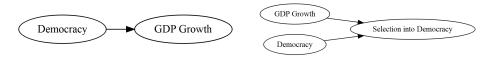
Being misled by Selection Bias:

Rest of the Course



Explanation

A real causal relationship: Being misled by Selection Bias:

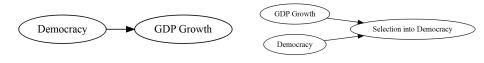


► The units which benefit most from treatment (largest $y_1 - y_0$) choose treatment

Rest of the Course

A real causal relationship:

Being misled by Selection Bias:

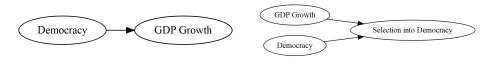


- ► The units which benefit most from treatment (largest $y_1 - y_0$) choose treatment
- \blacktriangleright We don't see any of the low y_1 's of units which avoid treatment

Selection Bias

A real causal relationship:

Being misled by Selection Bias:

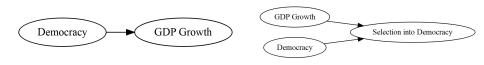


- ► The units which benefit most from treatment (largest $y_1 y_0$) choose treatment
- ▶ We don't see any of the low y₁'s of units which avoid treatment
 - Countries which can boost their GDP growth by becoming a democracy choose to democratize

Selection Bias

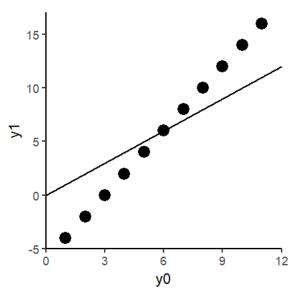
Explanation

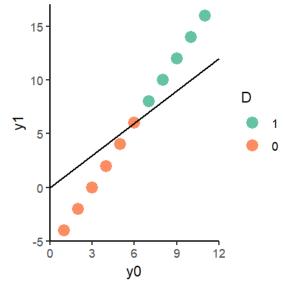
A real causal relationship: Being misled by Selection Bias:



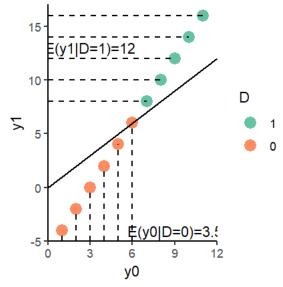
- ► The units which benefit most from treatment (largest $y_1 y_0$) choose treatment
- ▶ We don't see any of the low y₁'s of units which avoid treatment
 - Countries which can boost their GDP growth by becoming a democracy choose to democratize
 - ► Ex. Mexico? Myanmar?

Explanation





►
$$E(y_1) - E(y_0) = 0$$



$$E(y_1|D=1) - E(y_0|D=0) = 8.5$$

▶ Allow treatment effects to vary across individuals, so $Y_{1i} = Y_{0i} + \alpha_i$

Why Observational Data is Biased

Explanation

▶ Allow treatment effects to vary across individuals, so $Y_{1i} = Y_{0i} + \alpha_i$

$$\underbrace{E(Y_{i}|D=1) - E(Y_{i}|D=0)}_{\text{Observed Effect}} = \underbrace{E(Y_{1i} - Y_{0i})}_{\text{Real ATE}} + \underbrace{\frac{1}{2} \Big[E(Y_{1i}|D=1) - E(Y_{1i}|D=0) \Big]}_{\text{Imbalance on } Y_{1}} + \underbrace{\frac{1}{2} \Big[E(Y_{0i}|D=1) - E(Y_{0i}|D=0) \Big]}_{\text{Imbalance on } Y_{0}}$$
(3)

Why Observational Data is Biased

NB: For equal-sized treatment and control groups

► Allow treatment effects to vary across individuals, so $Y_{1i} = Y_{0i} + \alpha_i$

$$\underbrace{E(Y_{i}|D=1) - E(Y_{i}|D=0)}_{\text{Observed Effect}} = \underbrace{E(Y_{1i} - Y_{0i})}_{\text{Real ATE}} + \underbrace{\frac{1}{2} \Big[E(Y_{1i}|D=1) - E(Y_{1i}|D=0) \Big]}_{\text{Imbalance on } Y_{1}} + \underbrace{\frac{1}{2} \Big[E(Y_{0i}|D=1) - E(Y_{0i}|D=0) \Big]}_{\text{Imbalance on } Y_{0}}$$
(3)

NB: For equal-sized treatment and control groups

▶ In all of these cases, which units receive 'treatment' $(D_i = 1)$, and why, affect our estimate of the relationship between D and Y

- In all of these cases, which units receive 'treatment' (D_i = 1), and why, affect our estimate of the relationship between D and Y
 - ► This is the **Treatment Assignment Mechanism**

between D and Y

Explanation

- ► This is the Treatment Assignment Mechanism
- Messy treatment assignment mechanisms are why basic regression is no use for explanation

Explanation

- ▶ In all of these cases, which units receive 'treatment' $(D_i = 1)$, and why, affect our estimate of the relationship between D and Y
- This is the Treatment Assignment Mechanism
- Messy treatment assignment mechanisms are why basic regression is no use for explanation
 - ► It means our comparison control cases are really misleading

- ▶ In all of these cases, which units receive 'treatment' $(D_i = 1)$, and why, affect our estimate of the relationship between D and Y
 - This is the Treatment Assignment Mechanism
- Messy treatment assignment mechanisms are why basic regression is no use for explanation
 - It means our comparison control cases are really misleading
 - $ightharpoonup Y_0$ for North Korea is not a good guide to the Y_0 for Sweden

- ▶ In all of these cases, which units receive 'treatment' $(D_i = 1)$, and why, affect our estimate of the relationship between D and Y
 - This is the Treatment Assignment Mechanism
- Messy treatment assignment mechanisms are why basic regression is no use for explanation
 - ► It means our comparison control cases are really misleading
 - $ightharpoonup Y_0$ for North Korea is not a good guide to the Y_0 for Sweden
 - What would happen if the control units got treated?

► The comparability of treatment and control units depends on how they got to be treated

The comparability of treatment and control units depends on how they got to be treated

Treatment Assignment Mechanism

The set of factors that determine why some units have D=0and others have D=1

Explanation is more reliable where the Treatment Assignment Mechanism is Independent of Potential **Outcomes**

Outcomes

► Explanation is more reliable where the **Treatment**Assignment Mechanism is Independent of Potential

► Independent means the values of the potential outcomes give us no information about whether that unit was treated

- Explanation is more reliable where the Treatment Assignment Mechanism is Independent of Potential Outcomes
 - Independent means the values of the potential outcomes give us no information about whether that unit was treated
 - Potential outcomes are 'balanced' across control and treatment groups

- Explanation is more reliable where the Treatment
 Assignment Mechanism is Independent of Potential
 Outcomes
 - Independent means the values of the potential outcomes give us no information about whether that unit was treated
 - Potential outcomes are 'balanced' across control and treatment groups

Independence of Treatment Assignment

Treatment Assignment does NOT depend on the values of units' Potential Outcomes

- Explanation is more reliable where the Treatment Assignment Mechanism is Independent of Potential **Outcomes**
 - Independent means the values of the potential outcomes give us no information about whether that unit was treated
 - Potential outcomes are 'balanced' across control and treatment groups

Independence of Treatment Assignment

Treatment Assignment does NOT depend on the values of units' Potential Outcomes

$$(Y_1, Y_0) \perp D$$

- Explanation is more reliable where the Treatment
 Assignment Mechanism is Independent of Potential
 Outcomes
 - Independent means the values of the potential outcomes give us no information about whether that unit was treated
 - Potential outcomes are 'balanced' across control and treatment groups

Independence of Treatment Assignment

Treatment Assignment does NOT depend on the values of units' Potential Outcomes

$$(Y_1, Y_0) \perp D$$

$$Pr(D|(Y_1, Y_0)) = Pr(D)$$

- Explanation is more reliable where the Treatment Assignment Mechanism is Independent of Potential Outcomes
 - Independent means the values of the potential outcomes give us no information about whether that unit was treated
 - Potential outcomes are 'balanced' across control and treatment groups

Independence of Treatment Assignment

Treatment Assignment does NOT depend on the values of units' Potential Outcomes

$$(Y_1, Y_0) \perp D$$

 $Pr(D|(Y_1, Y_0)) = Pr(D)$
 $E(Y|D=1) = E(Y|D=0) = E(Y)$

Explanation

- ► Template to analyze a paper:
 - 1. What are the treatment and outcome variables?

Explanation

- ► Template to analyze a paper:
 - 1. What are the treatment and outcome variables?
 - 2. What are the Potential Outcomes?

- ► Template to analyze a paper:
 - 1. What are the treatment and outcome variables?
 - 2. What are the Potential Outcomes?
 - 3. What is the Fundamental Problem of Causal Inference in this case?

- Template to analyze a paper:
 - 1. What are the treatment and outcome variables?
 - 2. What are the Potential Outcomes?
 - 3. What is the Fundamental Problem of Causal Inference in this case?
 - 4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?

- Template to analyze a paper:
 - 1. What are the treatment and outcome variables?
 - 2. What are the Potential Outcomes?
 - 3. What is the Fundamental Problem of Causal Inference in this case?
 - 4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?
 - 5. What is the Treatment Assignment Mechanism?

- Template to analyze a paper:
 - 1. What are the treatment and outcome variables?
 - 2. What are the Potential Outcomes?
 - 3. What is the Fundamental Problem of Causal Inference in this case?
 - 4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?
 - 5. What is the Treatment Assignment Mechanism?
 - 6. Draw a causal diagram of the variables in the study, including the treatment assignment mechanism

► Template to analyze a paper:

- 1. What are the treatment and outcome variables?
- 2. What are the Potential Outcomes?
- 3. What is the Fundamental Problem of Causal Inference in this case?
- 4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?
- 5. What is the Treatment Assignment Mechanism?
- 6. Draw a causal diagram of the variables in the study, including the treatment assignment mechanism
- 7. Is Treatment Assignment independent of Potential Outcomes?

- ▶ Template to analyze a paper:
 - 1. What are the treatment and outcome variables?
 - 2. What are the Potential Outcomes?
 - 3. What is the Fundamental Problem of Causal Inference in this case?
 - 4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?
 - 5. What is the Treatment Assignment Mechanism?
 - 6. Draw a causal diagram of the variables in the study, including the treatment assignment mechanism
 - 7. Is Treatment Assignment independent of Potential Outcomes?
 - 8. Describe the risk of:
 - ► Omitted Variable Bias?

► Template to analyze a paper:

- 1. What are the treatment and outcome variables?
- 2. What are the Potential Outcomes?
- 3. What is the Fundamental Problem of Causal Inference in this case?
- 4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?
- 5. What is the Treatment Assignment Mechanism?
- 6. Draw a causal diagram of the variables in the study, including the treatment assignment mechanism
- 7. Is Treatment Assignment independent of Potential Outcomes?
- 8. Describe the risk of:
 - ▶ Omitted Variable Bias?
 - ▶ Reverse Causation?

- Template to analyze a paper:
 - 1. What are the treatment and outcome variables?
 - 2. What are the Potential Outcomes?
 - 3. What is the Fundamental Problem of Causal Inference in this case?
 - 4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?
 - 5. What is the Treatment Assignment Mechanism?
 - 6. Draw a causal diagram of the variables in the study, including the treatment assignment mechanism
 - 7. Is Treatment Assignment independent of Potential Outcomes?
 - Describe the risk of:
 - Omitted Variable Bias?
 - Reverse Causation?
 - Self-Selection?

DOES OIL HINDER DEMOCRACY?

By MICHAEL L. ROSS*

INTRODUCTION

DOLITICAL scientists believe that oil has some very odd properties. Many studies show that when incomes rise, governments tend to become more democratic. Yet some scholars imply there is an exception to this rule: if rising incomes can be traced to a country's oil wealth, they suggest, this democratizing effect will shrink or disappear. Does oil really have antidemocratic properties? What about other minerals and other commodities? What might explain these effects?

The claim that oil and democracy do not mix is often used by area specialists to explain why the high-income states of the Arab Middle East have not become democratic. If oil is truly at fault, this insight could help explaim—and perhaps, predict—the political problems of oil dexporters around the world, such as Niggiral, Indonesia, Venezuela, and the oil-rich states of Central Asia. If other minerals have similar properties, this effect might help account for the absence or weakness of democracy in dozens of additional states in sub-Saharan Africa, Latin America, and Southeast Asia. Yet the "oil impedes democracy" claim has received little attention outside the circle of Mideast scholars; moreover, it has not been carefully tested with regression analysis, either within or bewond the Middle East.

I use pooled time-series cross-national data from 113 states between 1971 and 1997 to explore three aspects of the oil-impedes-democracy claim. The first is the claim's validity: is it rute? Although the claim has been championed by Mideast specialists, it is difficult to test by examining only cases from the Middle East because the reion provides scholars with

Perious various of this article were presented to seniment at Princeton University, Vile University and the University of California, Los Angles, and at the September 2000 annual meeting of the American Political Science Association in Weshington, D.C. For their thoughtful comment on earter during, In amy article to Pradeer Challes for Jonat & Soyas, Centrofy Cantert, Plat Keefer, Sever Kanck, Mirina Lowi, Dilen Laur Chao, Laur Princhert, Nicobais Sambania, Jennietr Widner, Michael Workock, and these anonymous reviewers. To one special fundars to Info Norondful for the International Confession of the Confession of th

World Politics 53 (April 2001), 325-61

Explanation

► Try experimenting with the [App here](https://poliong.shinyapps.io/DAGs/)

Why Observational Data is Biased

- ► Try experimenting with the [App here](https://poliong.shinyapps.io/DAGs/)
- ► Can you create an artificial effect between *D* and *Y* even when there is no direct causal effect?

Explanation

► Try experimenting with the [App

here](https://poliong.shinyapps.io/DAGs/)

- ► Can you create an artificial effect between *D* and *Y* even when there is no direct causal effect?
- ► Under what conditions can you recover the real treatment effect?

- ▶ The rest of the course is mostly about:
 - Design-Based Solutions to the Fundamental Problem of Causal Inference: Which treatment assignment mechanisms avoid these biases and provide plausible counterfactuals

Why Observational Data is Biased

- ► The rest of the course is mostly about:
 - Design-Based Solutions to the Fundamental Problem of Causal Inference: Which treatment assignment mechanisms avoid these biases and provide plausible counterfactuals
 - ► How much can we learn with better research design?

- ▶ The rest of the course is mostly about:
 - Design-Based Solutions to the Fundamental Problem of Causal Inference: Which treatment assignment mechanisms avoid these biases and provide plausible counterfactuals
 - How much can we learn with better research design?
 - Model-Based Solutions: Not so much.

Explanation

		Independence of Treatment Assignment	Researcher Controls Treatment Assignment?
Controlled Experi- ments	Field Experiments	✓	✓
	Survey and Lab Experiments	✓	✓
liicites			
Natural Ex- periments	Randomized Natural Experiments	√	
	Instrumental Variables	√	
	Discontinuities	✓	
Observational Studies	Difference-in-Differences		
	Controlling for Confounding		
	Matching		
	Comparative Cases and Process Tracing		

Why Observational Data is Biased