FLS 6441 - Methods III: Explanation and Causation

Week 6 - Instrumental Variables

Jonathan Phillips

April 2020

Section 1

► What can we do when the treatment assignment mechanism is not 'as-if' random?

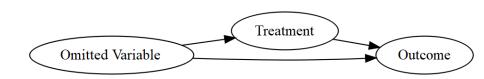
- ► What can we do when the treatment assignment mechanism is not 'as-if' random?
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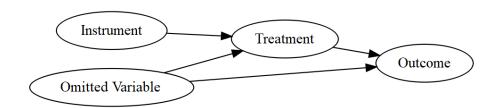
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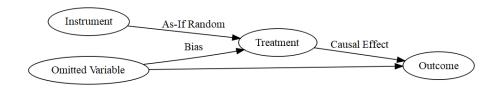
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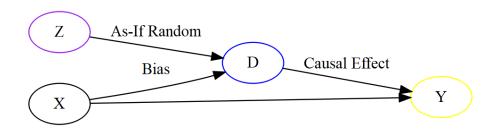
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 - ► I.e. Independent of potential outcomes
 - ► Even if other variables linked to potential outcomes **also** affect treatment









- Example Instruments:
 - ► Rainfall for conflict
 - Gender of first two children for effect of having a third child
 - ▶ Distance from the coast for exposure to slave trade

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- ► Theory and qualitative evidence needed

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Instrumental Variables

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 - 4. **2-Stage Least Squares:** Two linear regressions: correct coefficient, wrong p-value: $D_i \sim Z_i$, then $Y_i \sim \hat{D_i}$
 - 5. **Reduced-Form Regression:** Estimate of the Instrument on the Outcome, *ignoring treatment*: $Y_i \sim Z_i$

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- ► First-Stage Regression:

```
Growth_i = 0.12 - 0.1*Rainfall_i + \epsilon_i
```

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- ► First-Stage Regression: $Growth_i = 0.12 - 0.1*Rainfall_i + \epsilon_i$
- ► Fitted values from First-Stage Regression: $Growth_i = 0.12 0.1*0.5 + \epsilon_i$

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- ► Fitted values from First-Stage Regression: Growth = 0.07, 0.02, 0.06, 0.12, 0.03...

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- ► Second-Stage Regression: $Conflict_i = \alpha + \beta_2 Growth_i + \epsilon_i$

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- ► Our instrument for treatment: Low Rainfall
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- ► Fitted values from First-Stage Regression: Conflict_i = 0.07, 0.02, 0.06, 0.12, 0.03...
- ► Second-Stage Regression: $Conflict_i = 1.2 0.04*Growth_i + \epsilon_i$

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The Average Treatment Effect among the subset of units who are treated because of the instrument:

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Remember, these 'Local' units might be very rare and unusual so our estimate might be very difficult to generalize

Non-Compliance in Experiments

Section 2

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- ► Can we find a natural experiment?

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- ► They need an Instrumental Variable that:
 - 1. First Stage: Predicts Institutions
 - Exclusion Restriction: Only affects growth through institutions
- ► They make the *argument* that Settler (soldier) mortality rates are an appropriate instrument for institutions

Population:

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- ► **Population:** Ex-colonies
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- **►** Treatment:

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➤ **Treatment:** 'Settler' Institutions in ex-colonies (measured by 'risk of expropriation' index 1985-95)

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- ➤ **Treatment:** 'Settler' Institutions in ex-colonies (measured by 'risk of expropriation' index 1985-95)
- ► Control: 'Extractive' institutions
- ▶ Outcome:

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► Instrument: Settler (soldier) mortality rates

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- ► Supporting Evidence:
- "Mortality rates faced by the settlers more than 100 years ago explains over 25 percent of the variation in current institutions."

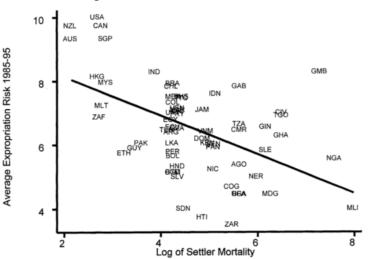


FIGURE 3. FIRST-STAGE RELATIONSHIP BETWEEN SETTLER MORTALITY AND EXPROPRIATION RISK

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 - Mortality rates for locals are low and don't affect human capital or growth directly, due to local immunity
 - Control for other possible correlated variables geography, climate, etc.

- Methodology:
 - ► Institutions_i = $\alpha + \beta_0$ Settler_Mortality_i + ϵ_i
 - ► $Growth_i = \alpha + \beta_1 Institutions_i + \epsilon_i$

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Average protection against

"Other" continent dummy

Log European settler mortality

"Other" continent dummy

expropriation risk 1985-1995

Base

sample

(1)

0.94

(0.16)

-0.61

(0.13)

0.27

ables	Instrumenting for Institutions oooooooo•o

Base

sample

(2)

1.00

(0.22)

(1.34)

-0.65

-0.51

(0.14)

2.00

(1.34)

0.30

Base sample

without

Neo-Europes

(3)

1.28

(0.36)

-0.39

(0.13)

0.13

ns	Non-Compliance in Experiments

Base sample

without

Neo-Europes

(4)

1.21

(0.35)

0.94

(1.46)

Panel A: Two-Stage Least Squares

Panel B: First Stage for Average Protection Against Expropriation Risk in 1985-1995

-0.39

-0.11

(0.14)

(1.50)

0.13

Base

sample

without

Africa

(5)

0.58

(0.10)

-1.20

(0.22)

0.47

Base

sample

without

Africa

(6)

0.58

(0.12)

0.04

(0.84)

-1.10

(0.24)

0.99

(1.43)

0.47

Base

sample,

depender

variable

log outpi

per work

(9)

0.98

(0.17)

-0.63

26/3.58

(0.13)

Base

sample

with

continent

dummies

(7)

0.98

(0.30)

-0.92(0.40)

-0.46

(0.36)

(0.85)

-0.94

-0.43

(0.17)

0.33

(0.49)

(0.41)

1.24

(0.84)

0.30

-0.27

Base

sample

with

continent

dummies

(8)

1.10

(0.46)

-1.20

(1.8)

-1.10

-0.44

-0.99

(1.0)

-0.34

(0.18)

2.00

(1.40)

0.47

(0.50)

(0.41)

(0.84)

0.33

1.1

-0.26

(0.52)

(0.42)

Instrumenting for Institutions

Latitude

Latitude

 R^2

Asia dummy

Africa dummy

Asia dummy

Africa dummy

Instrument

Results: Improving Nigeria's institutions to Chile's level would raise GDP 7-fold

Section 3

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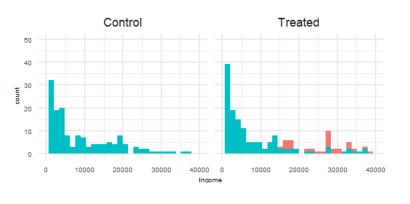
Instrumental Variables

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- ► We cannot just compare units that *actually* received treatment to those that did not
- ► Those groups are no longer 'balanced'
- Omitted variable bias has returned!



0

Complier

We can divide our units into four types depending on how they accept or reject treatment assignment:

Treatment Status:

If Assigned to Control	If Assigned to Treatment	Unit Type
0	1	Complier
0	0	Never-taker
1	1	Always-taker
1	0	Defier

Assignment to Treatment is now a separate step prior to treatment - so we can consider it like an instrument, Z_i

$D_i(Z_i=0)$	$D_i(Z_i=1)$	
Treatment Sta-	Treatment Sta-	Type?
tus If Assigned	tus If Assigned	
to Control	to Treatment	
0	1	
0	0	
0	1	
1	0	
1	1	
0	0	
0	1	
1	0	

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- ► We also need to **assume** Defiers don't exist

- ► Two methodologies for Experiments with Non-Compliance
- ► 1. Intention-to-Treat Analysis

Instrumental Variables

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- 1. Intention-to-Treat **Analysis**

Instrumental Variables

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- ➤ The 'Strong First-Stage' assumption here requires that treatment assignment affects treatment for at least some people
- ► The 'Exclusion Restriction' assumption requires that outcomes depend on treatment and not treatment assignment
 - So being labelled 'treatment group' (without treatment) doesn't affect your outcome