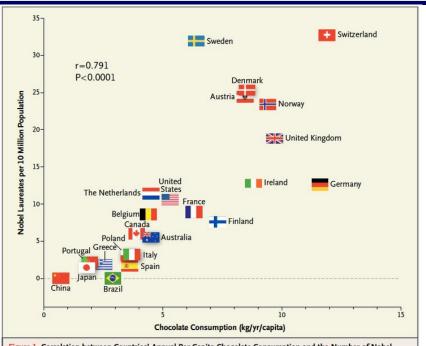
FLS 6441 - Methods III: Explanation and Causation

Week 2 - A Framework for Explanation

Jonathan Phillips

March 2019

Explanation	Causal Inference	Why Observational Data is Biased	Rest of the Course



► Why isn't correlation enough?

Rest of the Course

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 - For prediction, correlation is fine: If we know a country has chocolate consumption of 10kg/yr/capita we can reasonably predict it will have about 25 Nobel Laureates
 - ► But for **intervention**, correlation does not help: forcing people to eat more chocolate does nothing on its own to produce more Nobel Laureates
 - ► For **explanation**, correlation also fails it is no *explanation* to say that Switzerland has the most Nobel Laureates because it has the highest chocolate consumption

► What does it mean to explain something?

Why Observational Data is Biased

Explanation

- ▶ What does it mean to explain something?
- ► To give an account of what happens, and why
 - ► The 'chain of causation'

Explanation

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Why Observational Data is Biased

- ▶ What does it mean to explain something?
- ► To give an account of what happens, and why
 - ▶ The 'chain of causation'
- ► If *D* explains *y*, we are saying that the *absence* of *D* would have led to a different value of *y*
- ► There exists a 'counterfactual' possibility that did not happen

Deterministic Explanation

Why Observational Data is Biased

Explanation

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Probabilistic Explanation

Why Observational Data is Biased

- ▶ If D happens, the **probability** of Y increases
- ▶ Treatment effects are a distribution, not a single value

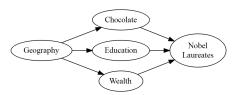
► Two perspectives on explanation:

Rest of the Course

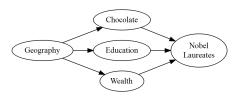
► Two perspectives on explanation:

Causes of Effects	Effects of Causes		
What caused Y?	Does D cause Y?		
Why does Switzerland have so many Nobel laureates?	Does chocolate cause more Nobel laureates?		
Backward-looking	Forward-looking		

► Two perspectives on explanation:



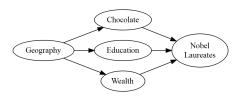
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 Identifying the source of ALL of the variation in Nobel Laureates Why Observational Data is Biased

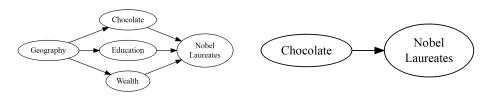
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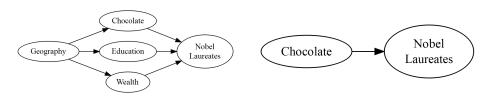
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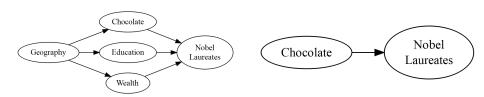


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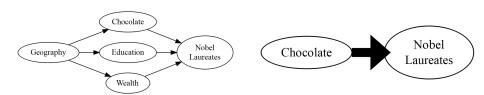


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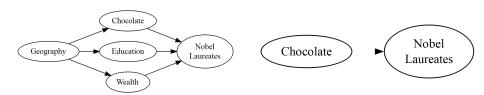
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Explanation

► A focus on a single explanatory variable *D* requires a clear definition of 'Treatment'

Why Observational Data is Biased

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Why Observational Data is Biased

- AND to clearly define a 'Control'
 - What is the opposite of investing \$1bn in education?
 - No investment, or investing it elsewhere?
- Define treatment:

$$D_i = \begin{cases} 1, & \text{if treated} \\ 0, & \text{if not treated} \end{cases}$$

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- ► So we usually want to study a single outcome

Explanation

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Rest of the Course

Explanation

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 - But our analysis needs to take account of the 'clustered' treatment
- ▶ Units are **time-specific**: the same person 10 minutes later is a different unit

Section 2

Why Observational Data is Biased

Causal Inference

Explanation

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Why Observational Data is Biased

▶ This means comparing the **Potential Outcomes** for unit *i*:

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$$Y_{Di} = \begin{cases} Y_{1i} \text{ GDP Growth of Brazil in 2010 if a Democracy} \\ Y_{0i} \text{ GDP Growth of Brazil in 2010 if NOT a Democracy} \end{cases}$$

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Potential Outcomes are just another Variable for each Unit

	GDP Growth if		
	Democracy	NOT Democ-	Effect
		racy	
	Y ₁	Y ₀	$Y_1 - Y_0$
Brasil	4	1	3
Argentina	7	4	3
Bolivia	2	4	-2
Colombia	7	7	0
Peru	5	4	1

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We want to calculate an Average Treatment Effect

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We want to calculate an Average Treatment Effect

$$ATE = E(\alpha_i) = E(Y_1 - Y_0) = E(Y_1) - E(Y_0) = \frac{\sum_i (Y_{1i} - Y_{0i})}{N}$$

Explanation

Potential Outcomes are just another Variable for each Unit

	GDP Growth if	GDP Growth if	Treatment
	Democracy	NOT Democ-	Effect
		racy	
	Y_1	Y ₀	$Y_1 - Y_0$
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Average Treatment Effect	5	4	1

Explanation

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Why Observational Data is Biased

Average Treatment Effect on the Treated

$$\mathsf{ATT} = \mathsf{E}(\alpha_i | D = 1) = E(Y_1 - Y_0 | D = 1) = \frac{\sum_i (Y_{1i} - Y_{0i} | D = 1)}{N_{Treated}} \quad (1)$$

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Average Treatment Effect on the Untreated (Control)

ATU=E(
$$\alpha_i|D=0$$
) = $E(Y_1-Y_0|D=0)=\frac{\sum_i(Y_{1i}-Y_{0i}|D=0)}{N_{Control}}$ (2)

Explanation

▶ In reality, some units are **actually treated** (D = 1), others are actually control (D=0)

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Average Treatment Effect on the Treated

$$\mathsf{ATT} = \mathsf{E}(\alpha_i | D = 1) = \mathsf{E}(Y_1 - Y_0 | D = 1) = \frac{\sum_i (Y_{1i} - Y_{0i} | D = 1)}{N_{Treated}}$$

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) = $E(Y_1-Y_0|D=0)=\frac{\sum_i(Y_{1i}-Y_{0i}|D=0)}{N_{Control}}$

- ► The three effect estimates are usually different
 - ► The effect democracy has had in Europe is different to the effect if it were introduced in Africa

(2)

(1)

Explanation

Potential Outcomes Example

	Democracy?	GDP Growth if Democ-	GDP Growth if NOT Democ-	Treatment Effect
		racy	racy	
	Di	Y ₁	Y ₀	Y_1-Y_0
Brasil	1	4	1	3
Argentina	0	7	4	3
Bolivia	1	2	4	-2
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Explanation

Potential Outcomes Example

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	Di	Υ ₁	Y ₀	$Y_1 - Y_0$
Brasil	1	4	1	3
Bolivia	1	2	4	-2
ATT	1	3	2.5	0.5

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Peru	0	5	4	1
ATU	0	6.3	5	1.3

The Fundamental Problem of Causal Inference

► No units can receive **both** treatment and control

Explanation

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$$Y_{i}^{obs} = \begin{cases} Y_{1i} \text{ if } D_{i} = 1\\ Y_{0i} \text{ if } D_{i} = 0 \end{cases}$$
$$Y_{i}^{obs} = D_{i} \cdot Y_{1i} + (1 - D_{i}) \cdot Y_{0i}$$

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		racy	racy	
	Di	Y ₁	Y ₀	Y ^{obs}
Brasil	1	4	?	4
Argentina	0	?	4	4
Bolivia	1	2	?	2
Colombia	0	?	7	7
Peru	0	?	4	4

Potential Outcomes Example

	Democracy?	Observed GDP Growth
	Di	Y ^{obs}
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Argentina	0	4
Bolivia	1	2
Colombia	0	7
Peru	0	4

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Average Treat- ment Effect		3	5	-2

Why Observational Data is Biased

Causal Inference

Explanation

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Explanation

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- ► The potential outcomes we observe are a biased **representation** of the potential outcomes of all the units

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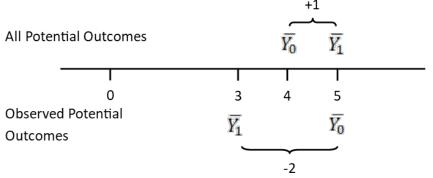
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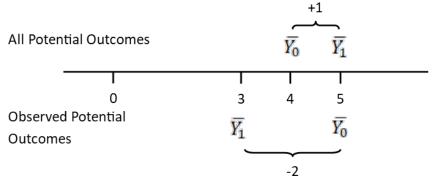
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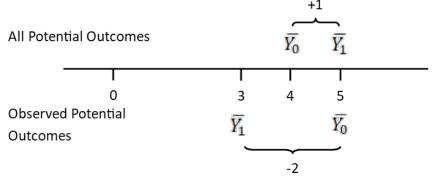
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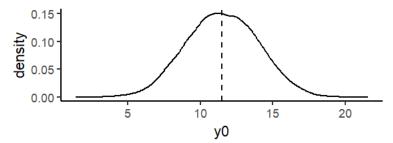
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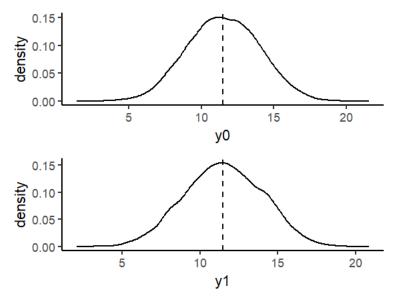
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Explanation

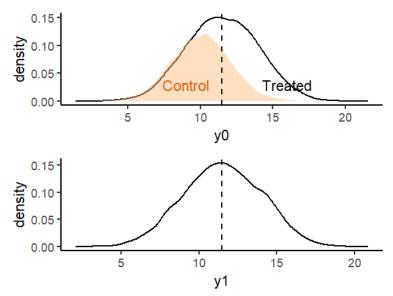


Rest of the Course

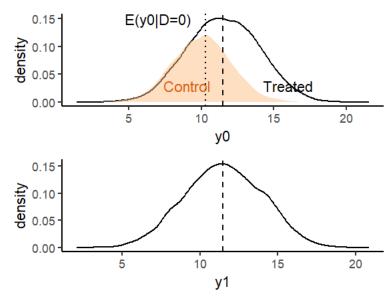
Explanation



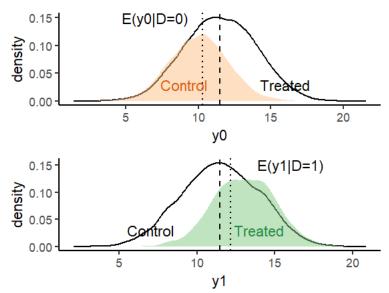
Explanation



Explanation



Explanation



► Lots of averages:

		Hypothetical outcome	
		Y0 Y1	
Actual Treatment	D = 0	$E(Y_{0i} D=0)$	$E(Y_{1i} D=0)$
	D = 1	$E(Y_{0i} D=1)$	$E(Y_{1i} D=1)$

Causal Inference

Explanation

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► All our causal estimates are **averages**

Causal Inference

Explanation

- All our causal estimates are averages
 - We cannot distinguish the null hypothesis of no average effect from the sharp null hypothesis of no individual effects

Causal Inference

- All our causal estimates are averages
 - We cannot distinguish the null hypothesis of no average effect from the sharp null hypothesis of no individual effects

	No Average Effect $E(Y_1 - Y_0) = 0$	"Sharp null": No individual effects $(Y_{1i} - Y_{0i} = 0)$
Brasil	2	0
Argentina	-1	0
Bolivia	1	0
Colombia	0	0
Peru	-2	0
Average	0	0

Section 3

Explanation

▶ Why are potential outcomes biased in our data?

- ▶ Why are potential outcomes biased in our data?
 - 1. Omitted Variables

- ▶ Why are potential outcomes biased in our data?
 - 1. Omitted Variables
 - 2. Reverse Causation

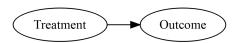
- ▶ Why are potential outcomes biased in our data?
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- ▶ Why are potential outcomes biased in our data?
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- In all of these cases the potential outcomes are distorted
- ► So basic regression is biased

Explanation

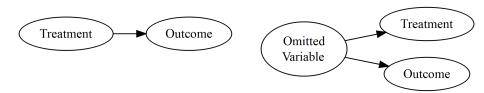
A real causal relationship:



Rest of the Course

A real causal relationship:

Being misled by omitted variable bias:



A real causal relationship:

Being misled by omitted variable bias:



▶ A third variable causes some units to have **different** values of potential outcomes, AND for those same units to be treated

A real causal relationship:

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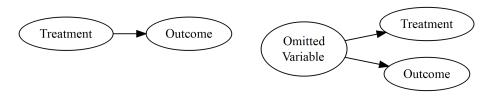


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Explanation

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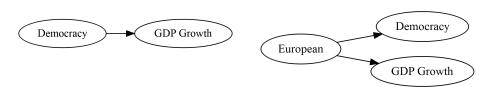


- ► A third variable causes some units to have different values of potential outcomes, AND for those same units to be treated
- ► So treated units have non-representative Y₁
- ► And control units have non-representative Y₀

Rest of the Course

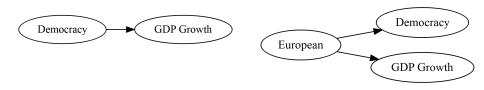
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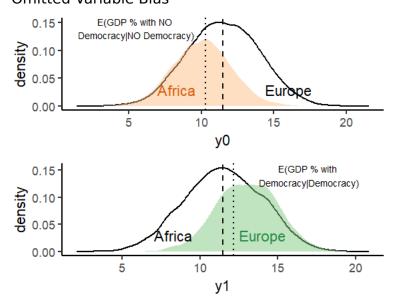


A real causal relationship:

Being misled by omitted variable bias:



 European countries faced conditions that encouraged both democracy and rapid GDP growth



Explanation

▶ Let's say that $Y_{1i} = Y_{0i} + \alpha$, where α is the real constant treatment effect

$$A\hat{T}E = E(Y_1|D=1) - E(Y_0|D=0)$$

Explanation

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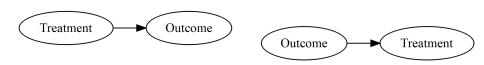
$$A\hat{T}E = \underbrace{\alpha}_{\text{Real ATE}} + \underbrace{E(Y_0|D=1) - E(Y_0|D=0)}_{\text{Bias}}$$

A real causal relationship:



A real causal relationship:

Being misled by reverse causation:

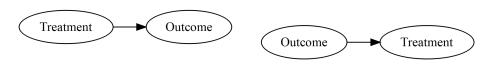


Explanation

A real causal relationship:

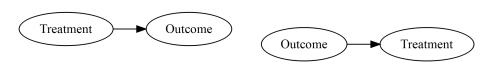
Being misled by reverse causation:

Why Observational Data is Biased



▶ D does not affect Y, but higher Y makes treatment (D) more likely

Explanation



- ► D does not affect Y, but higher Y makes treatment (D) more likely
- ► So the two variables are correlated

Rest of the Course

A real causal relationship:

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A real causal relationship:

Being misled by reverse causation:



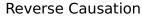
► GDP Growth encourages democratization

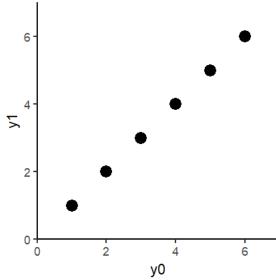
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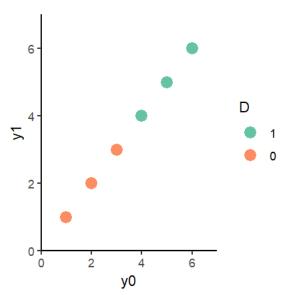


- ► GDP Growth encourages democratization
- ► So democracies are more likely to have experienced high growth rates



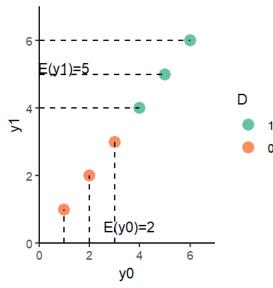


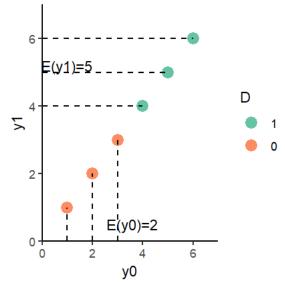
►
$$E(Y_1 - Y_0) = 0$$



Why Observational Data is Biased

Reverse Causation

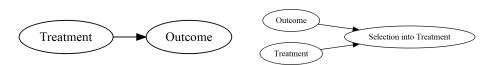




$$E(Y_1|D=1) - E(Y_0|D=0) = 5 - 2 = 3$$

A real causal relationship:

Being misled by Selection Bias:

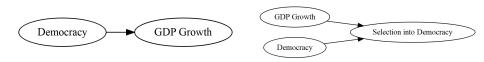


Explanation

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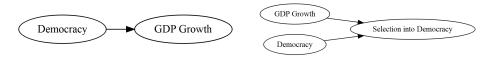
Being misled by Selection Bias:

Rest of the Course



Explanation

A real causal relationship: Being misled by Selection Bias:

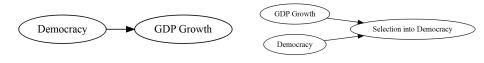


► The units which benefit most from treatment (largest $y_1 - y_0$) choose treatment

Rest of the Course

A real causal relationship:

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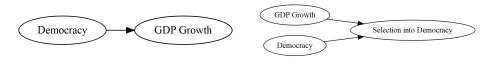


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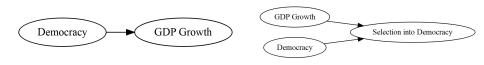


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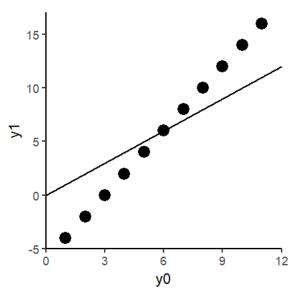
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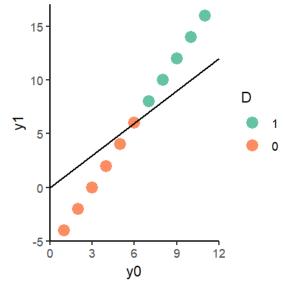
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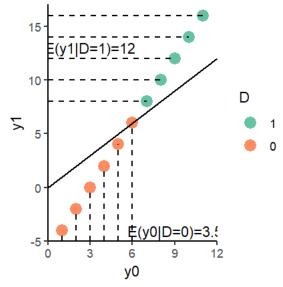
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 - ► Ex. Mexico? Myanmar?

Explanation





►
$$E(y_1) - E(y_0) = 0$$



$$E(y_1|D=1) - E(y_0|D=0) = 8.5$$

▶ Allow treatment effects to vary across individuals, so $Y_{1i} = Y_{0i} + \alpha_i$

Why Observational Data is Biased

Explanation

▶ Allow treatment effects to vary across individuals, so $Y_{1i} = Y_{0i} + \alpha_i$

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(3)

Why Observational Data is Biased

NB: For equal-sized treatment and control groups

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between D and Y

Explanation

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 - ► It means our comparison control cases are really misleading
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 - What would happen if the control units got treated?

► The comparability of treatment and control units depends on how they got to be treated

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Treatment Assignment Mechanism

The set of factors that determine why some units have D=0and others have D=1

Explanation is more reliable where the Treatment Assignment Mechanism is Independent of Potential **Outcomes**

Outcomes

► Explanation is more reliable where the **Treatment**Assignment Mechanism is Independent of Potential

► Independent means the values of the potential outcomes give us no information about whether that unit was treated

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 $Pr(D|(Y_1, Y_0)) = Pr(D)$
 $E(Y|D=1) = E(Y|D=0) = E(Y)$

Explanation

- ► Template to analyze a paper:
 - 1. What are the treatment and outcome variables?

Explanation

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- ► Template to analyze a paper:
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 - Omitted Variable Bias?
 - Reverse Causation?
 - Self-Selection?

DOES OIL HINDER DEMOCRACY?

By MICHAEL L. ROSS*

INTRODUCTION

DOLITICAL scientists believe that oil has some very odd properties. Many studies show that when incomes rise, governments tend to become more democratic. Yet some scholars imply there is an exception to this rule: if rising incomes can be traced to a country's oil wealth, they suggest, this democratizing effect will shrink or disappear. Does oil really have antidemocratic properties? What about other minerals and other commodities? What might explain these effects?

The claim that oil and democracy do not mix is often used by area specialists to explain why the high-income states of the Arab Middle East have not become democratic. If oil is truly at fault, this insight could help explaim—and perhaps, predict—the political problems of oil dexporters around the world, such as Niggiral, Indonesia, Venezuela, and the oil-rich states of Central Asia. If other minerals have similar properties, this effect might help account for the absence or weakness of democracy in dozens of additional states in sub-Saharan Africa, Latin America, and Southeast Asia. Yet the "oil impedes democracy" claim has received little attention outside the circle of Mideast scholars; moreover, it has not been carefully tested with regression analysis, either within or bewond the Middle East.

I use pooled time-series cross-national data from 113 states between 1971 and 1997 to explore three aspects of the oil-impedes-democracy claim. The first is the claim's validity: is it rute? Although the claim has been championed by Mideast specialists, it is difficult to test by examining only cases from the Middle East because the reion provides scholars with

Perious various of this article were presented to seniment at Princeton University, Vile University and the University of California, Los Angles, and at the September 2000 annual meeting of the American Political Science Association in Weshington, D.C. For their thoughtful comment on earter during, In amy article to Pradeer Challes for Jonat & Soyas, Centrofy Cantert, Plat Keefer, Sever Kanck, Mirina Lowi, Dilen Laur Chao, Laur Princhert, Nicobais Sambania, Jennietr Widner, Michael Workock, and these anonymous reviewers. To one special fundars to Info Norondful for the International Confession of the Confession of th

World Politics 53 (April 2001), 325-61

Why Observational Data is Biased

Summary

Explanation

► Try experimenting with the https://poliong.shinyapps.io/DAGs/

Explanation

- ► Try experimenting with the https://poliong.shinyapps.io/DAGs/
- ► Can you create an artificial effect between *D* and *Y* even when there is no direct causal effect?

- ► Try experimenting with the https://poliong.shinyapps.io/DAGs/
- ► Can you create an artificial effect between *D* and *Y* even when there is no direct causal effect?
- ▶ Under what conditions can you recover the real treatment effect?

- ▶ The rest of the course is mostly about:
 - Design-Based Solutions to the Fundamental Problem of Causal Inference: Which treatment assignment mechanisms avoid these biases and provide plausible counterfactuals

Why Observational Data is Biased

- ► The rest of the course is mostly about:
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 - Design-Based Solutions to the Fundamental Problem of Causal Inference: Which treatment assignment mechanisms avoid these biases and provide plausible counterfactuals
 - How much can we learn with better research design?
 - Model-Based Solutions: Not so much.

Explanation

		Independence of Treatment Assignment	Researcher Controls Treatment Assignment?
Controlled Experi- ments	Field Experiments	✓	✓
	Survey and Lab Experiments	✓	✓
liicites			
Natural Ex- periments	Randomized Natural Experiments	√	
	Instrumental Variables	√	
	Discontinuities	✓	
Observational Studies	Difference-in-Differences		
	Controlling for Confounding		
	Matching		
	Comparative Cases and Process Tracing		

Why Observational Data is Biased