

FLS 6441 - Methods III: Explanation and Causation

Week 9 - Controlling for Confounding

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Classification of Research Designs

		Independence of Treatment Assignment	Researcher Controls Treatment Assignment?
Controlled Experiments	Field Experiments	✓	✓
	Survey and Lab Experiments	✓	✓
Natural Experiments	Natural Experiments	✓	
	Instrumental Variables	✓	
	Discontinuities	✓	
Observational Studies	Difference-in-Differences		
	Controlling for Confounding		
	Matching		
	Comparative Cases and Process Tracing		

Section 1

Controlling for Confounding

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- ▶ Adding control variables changes the comparison we are making: **Treatment is associated with higher values of the Outcome...holding constant the values of X**
- ▶ But when does controlling allow us to move from "**is associated with**" to **causes**?

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 - ▶ We have to make an argument and provide supporting evidence

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 - ▶ Equivalently, it means separating our data for each value of the confounder: **Subclassification**
 - ▶ Then, within each group, the confounder is **constant** and can't affect the relationship between D and Y .
 - ▶ We have **created balance** between the treated and control groups on all other characteristics

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Section 2

Which Variables to Control For

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 - ▶ A **Directed Acyclical Graph** (DAG)
 - ▶ Arrows only in one direction
 - ▶ No circular loops!

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- ▶ Causation is like **Water**, flowing along the graph
 - ▶ We want to focus on one 'flow' of causation from treatment to outcomes
 - ▶ Avoiding mixing with the other flows of causation in the network

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 1. Include as controls enough variables to **block all back-door paths** from treatment to the outcome
 2. Exclude any variables that are **post-treatment**
 3. Exclude any variables that are **colliders**

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- ▶ **Block back-door paths** by controlling for any variable along the path
- ▶ Identify the **Minimum set of controls** to achieve conditional independence

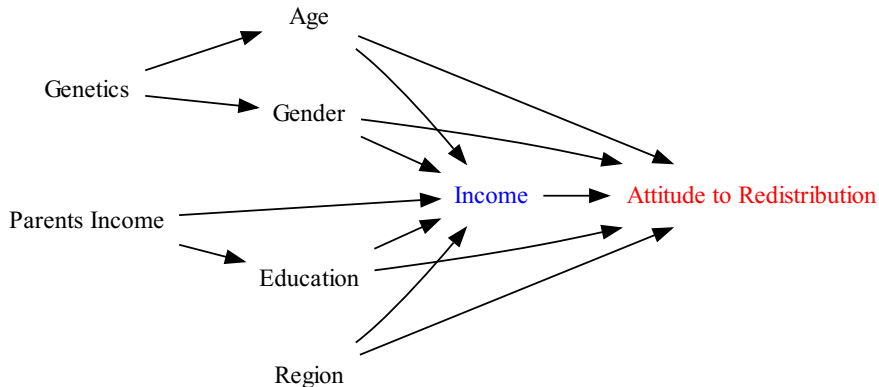
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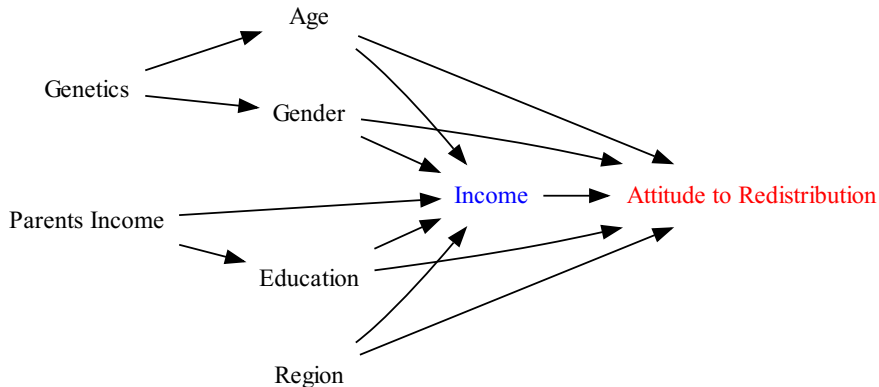
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- ▶ **Block back-door paths** by controlling for any variable along the path
- ▶ Identify the **Minimum set of controls** to achieve conditional independence
 - ▶ *Any* set of variables which blocks *All* back-door paths
 - ▶ Include these as control variables in our regression

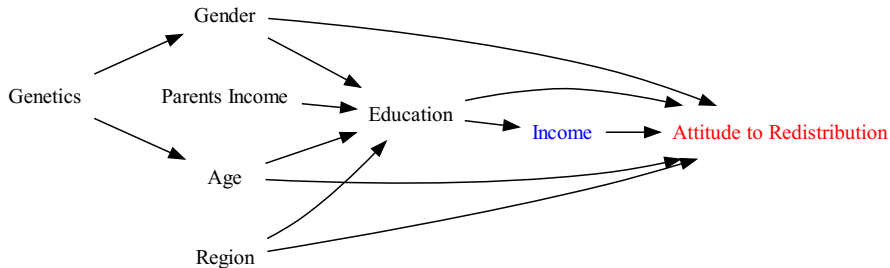
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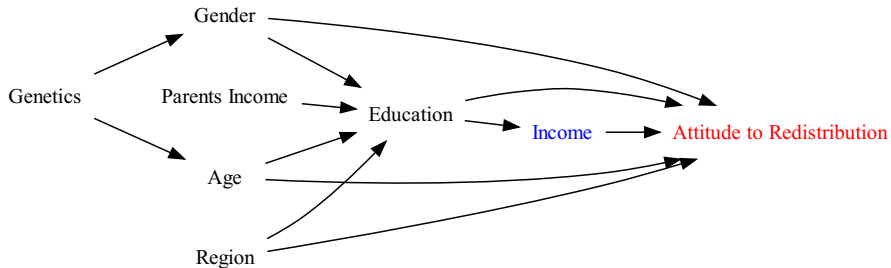
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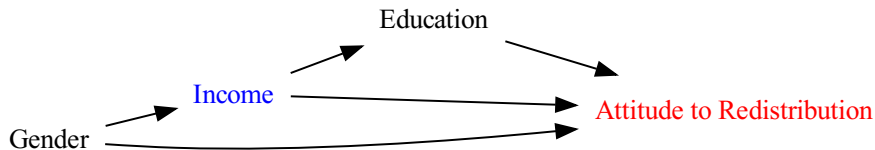
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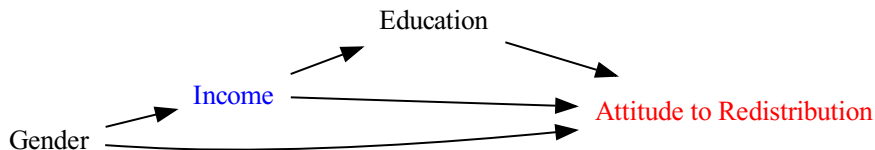
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- ▶ Including **post-treatment** variables will introduce bias
 - ▶ Because variables measured 'after' treatment can also be affected by treatment
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 - ▶ Controlling for them changes the definition of the causal effect we are estimating

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- ▶ The water 'collides' in both directions and 'cancels out'
- ▶ But if we do 'control' for a collider we *introduce* a bias in the relationship between D and Y
- ▶ So we must avoid controlling for them
- ▶ Hard!

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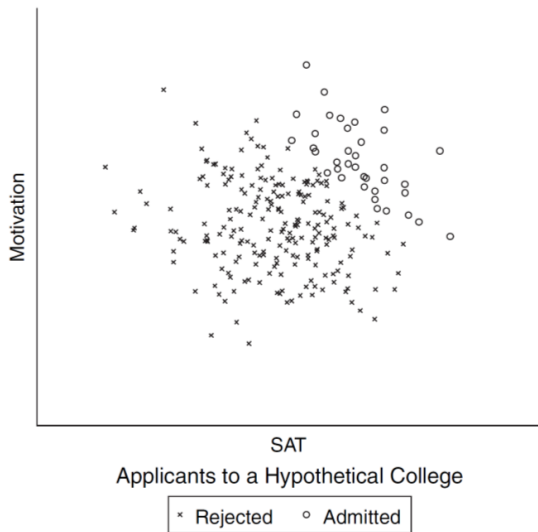
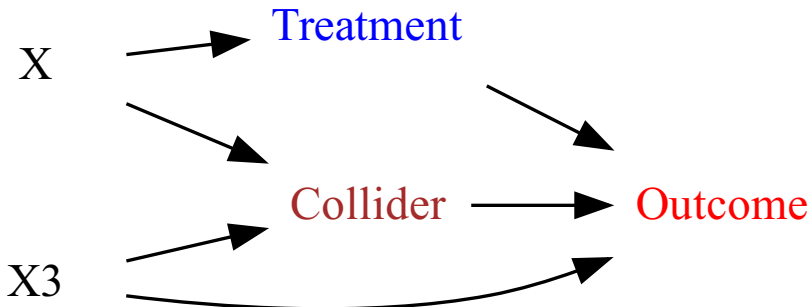


Figure 3.4: Simulation of conditional dependence within values of a collider variable.

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Example adapted from MW, p.72

1. List all of the **back-door paths** from D to Y
2. Identify any **post-treatment** variables: Do NOT include as controls
3. Identify any back-door paths with **collider** variables: Mark these as already blocked
4. Find a minimum set of variables that blocks all remaining back-door paths
5. Double-check your minimum set of control variables does not contain any post-treatment or collider variables

