

# FLS 6441 - Methods III: Explanation and Causation

Week 10 - Matching

Jonathan Phillips

June 2019

# Classification of Research Designs

		Independence of Treatment Assignment	Researcher Controls Treatment Assignment?
<b>Controlled Experiments</b>	Field Experiments	✓	✓
	Survey and Lab Experiments	✓	✓
<b>Natural Experiments</b>	Natural Experiments	✓	
	Instrumental Variables	✓	
	Discontinuities	✓	
<b>Observational Studies</b>	Difference-in-Differences		
	Controlling for Confounding		
	Matching		
	Comparative Cases and Process Tracing		

## Matching













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- ▶ The solution? **Non-parametric** methods for controlling for confounding
  1. We use *ONLY SOME* of the data
  2. We do not specify the parameters of any model
- ▶ **Matching** is a non-parametric method
  - ▶ A **pre-processing** stage
  - ▶ Analysis of the results is separate and comes later

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  1. One way of forcing balance is by **adjusting** each treated observation to predict what it would 'look like' if it were identical to a control observation - a regression model
  2. An alternative is just to **throw out** all of the treated observations that do not have a comparable control observation - this is matching

## Matching

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- ▶ Matching is **NOT** an experimental method

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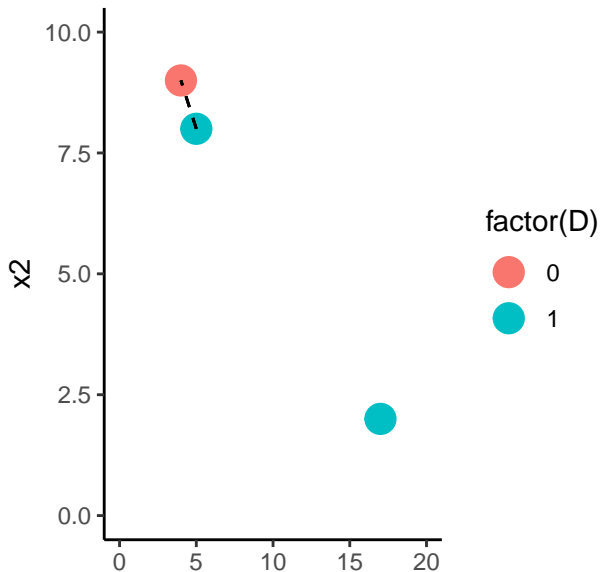
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2. Repeat for every treated unit
3. Drop all the unmatched units (eg. 'extra' treated units that are 'far away' from any control units)
4. Assess balance - re-run the matching process as many times as you can to maximize balance!





## Matching

1. For example:





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- ▶ After matching, for the analysis we can either:
  1. Calculate the difference in means between treated and control groups



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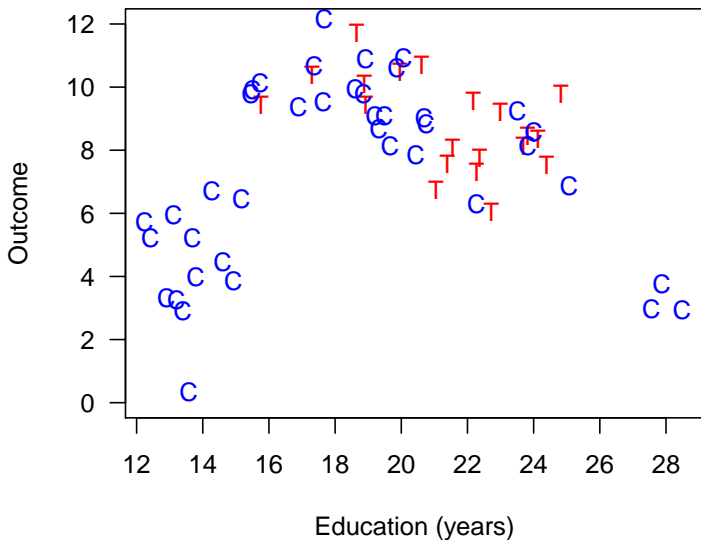


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  - ▶ Pre-treatment Confounders? **Yes!** We want to remove imbalance due to confounders

# Matching to Reduce Model Dependence

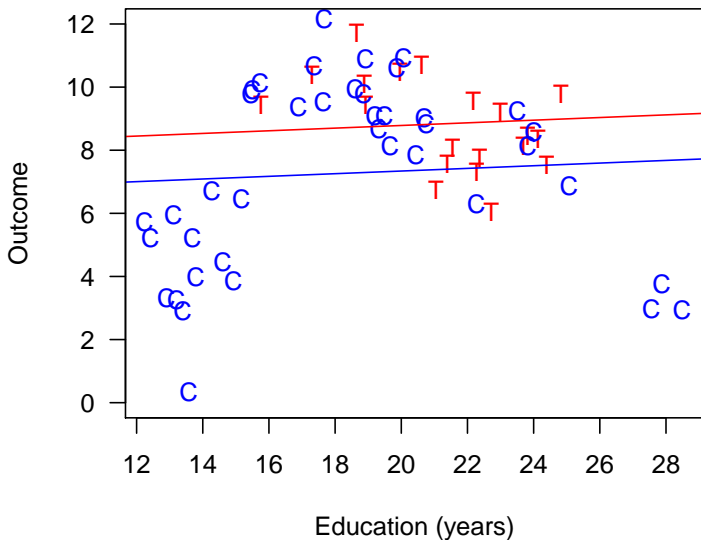
(Ho, Imai, King, Stuart, 2007: fig.1, *Political Analysis*)





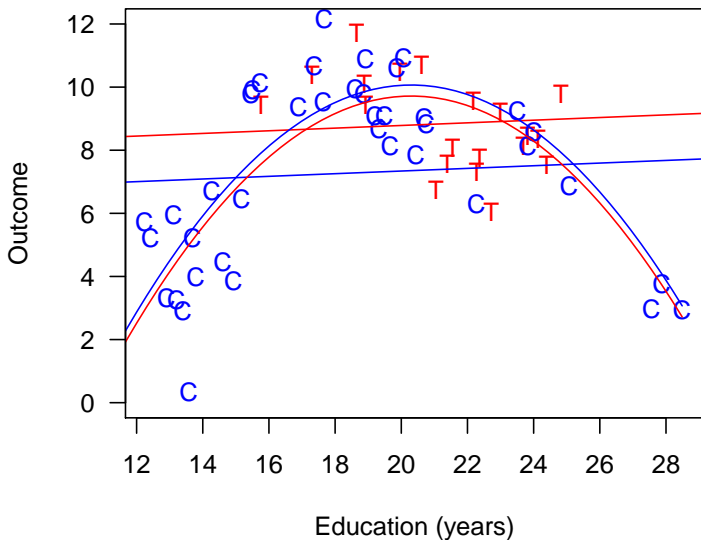
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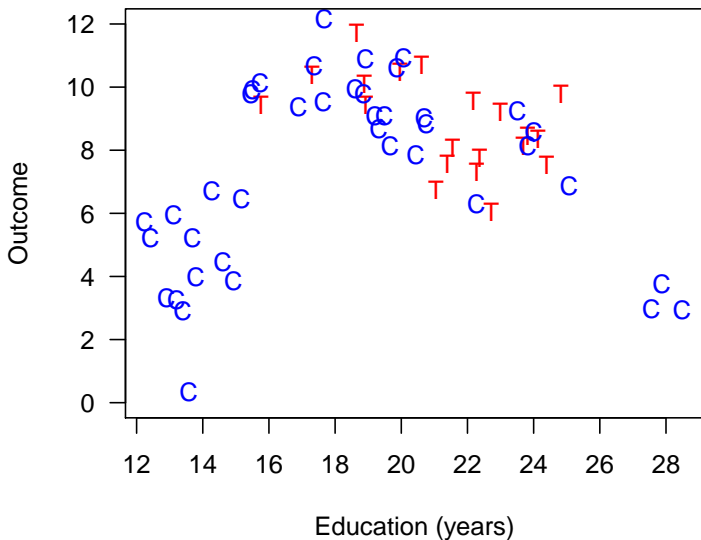
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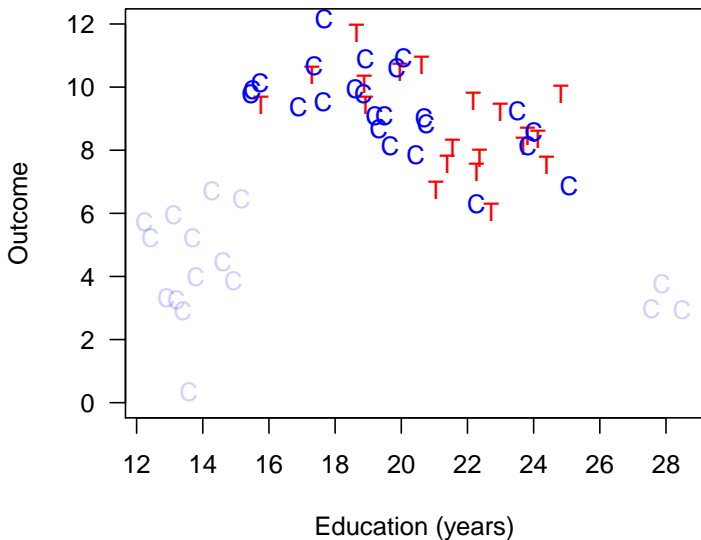
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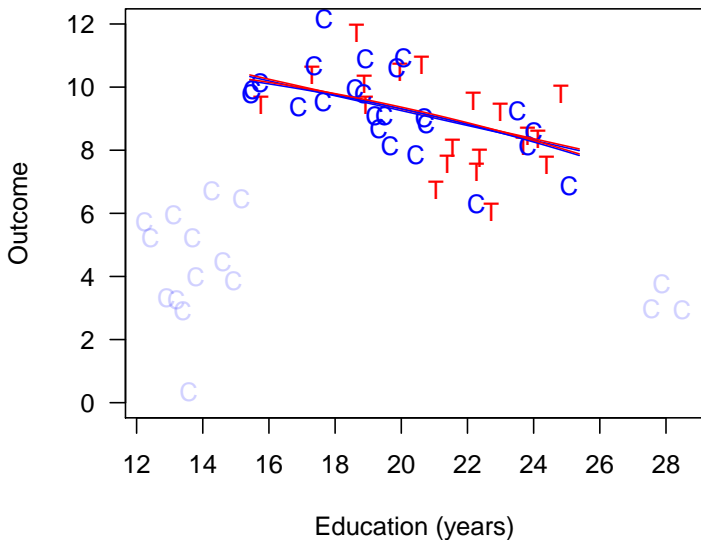
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## Matching

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- 1. Matching on few categorical variables: **Exact Matching**
- 2. Matching on continuous variables (sequential):  
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- 3. Matching to maximize balance: **Optimal/Genetic Matching**



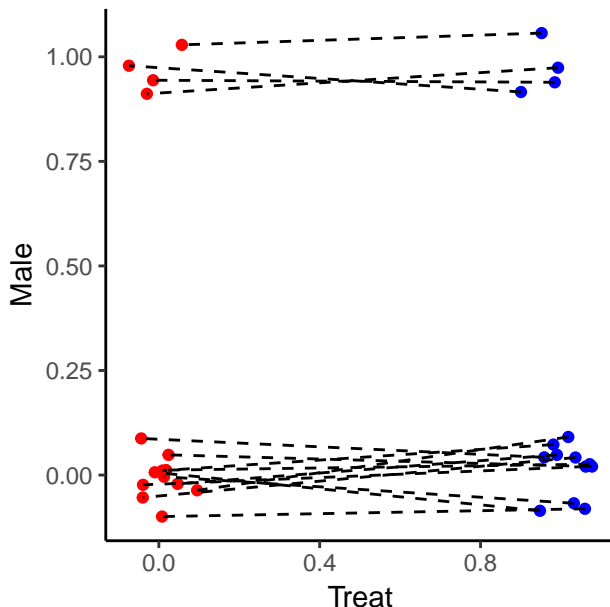








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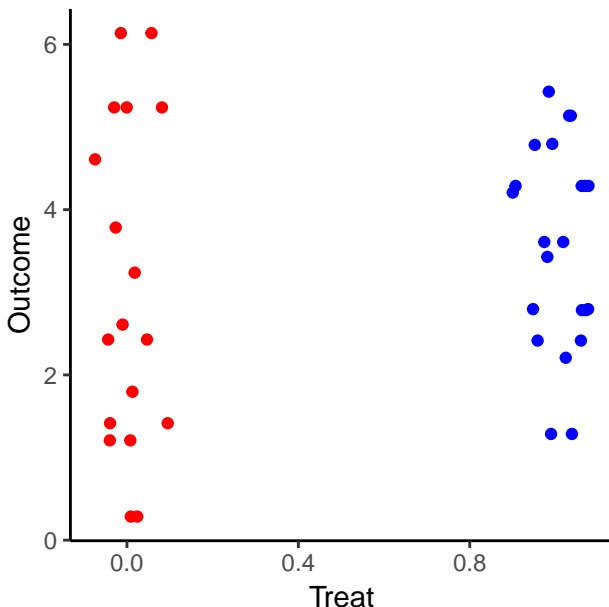
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- ▶ Then compare the outcome of the **remaining** treated and control units
  - ▶ Difference in means
  - ▶ Or regression of outcome on treatment

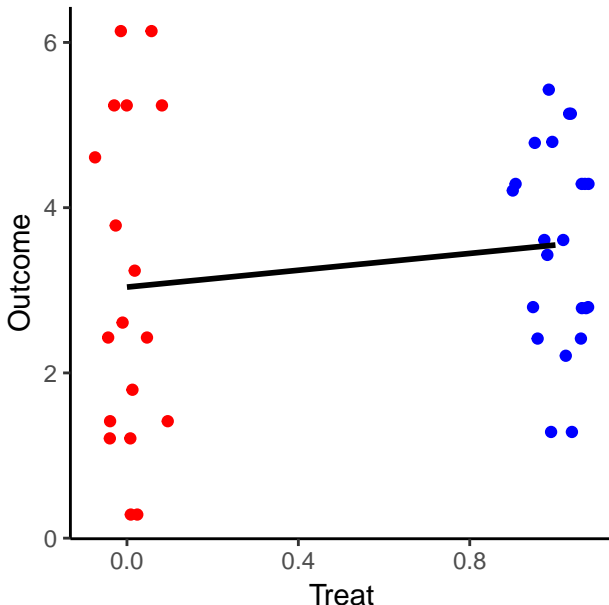
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2	Matched	0.27	0.27	0.00

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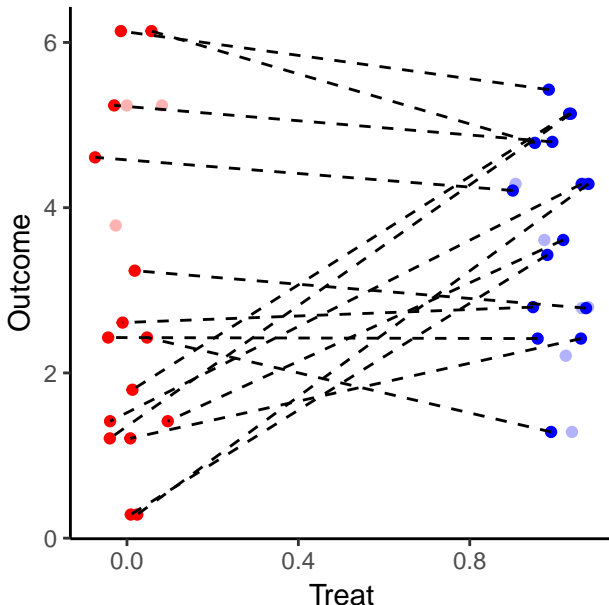


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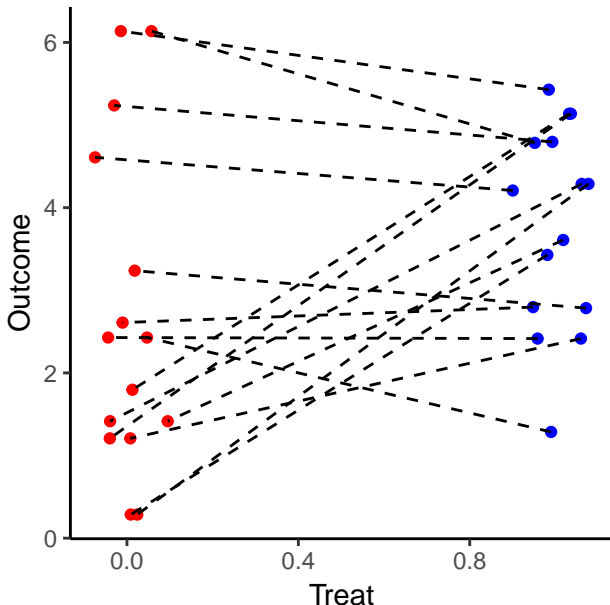




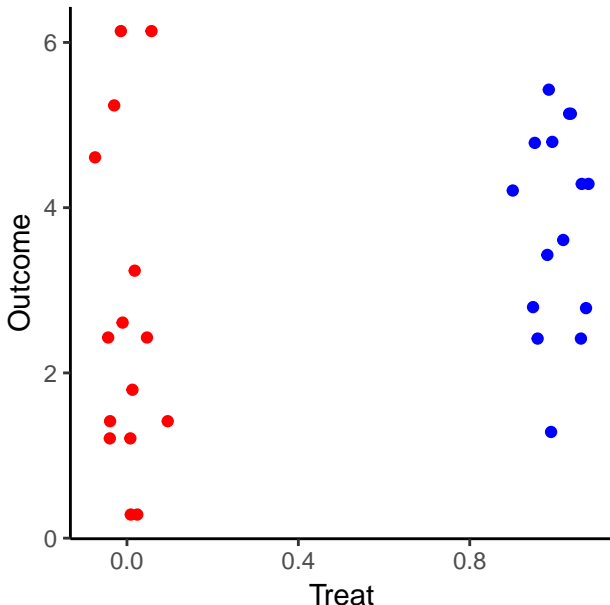
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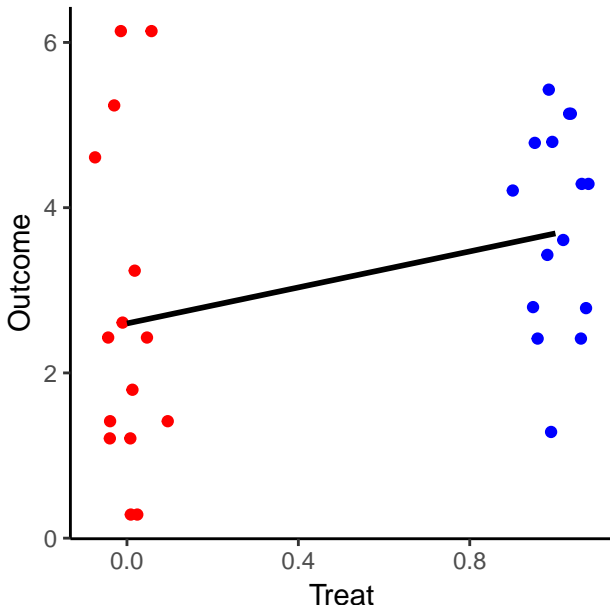
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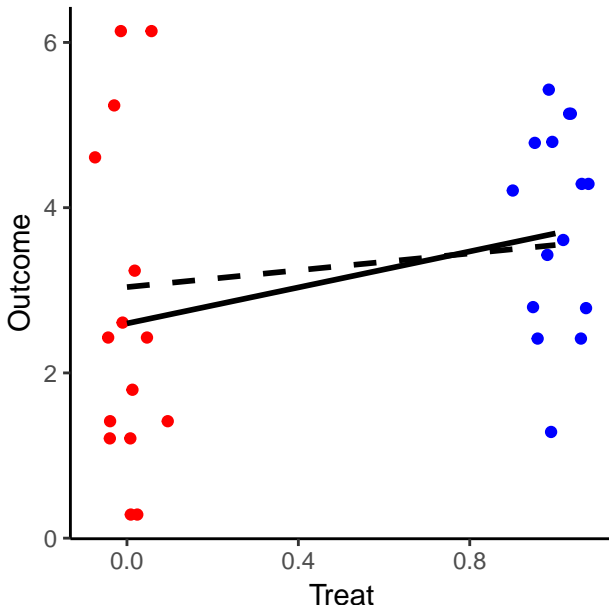
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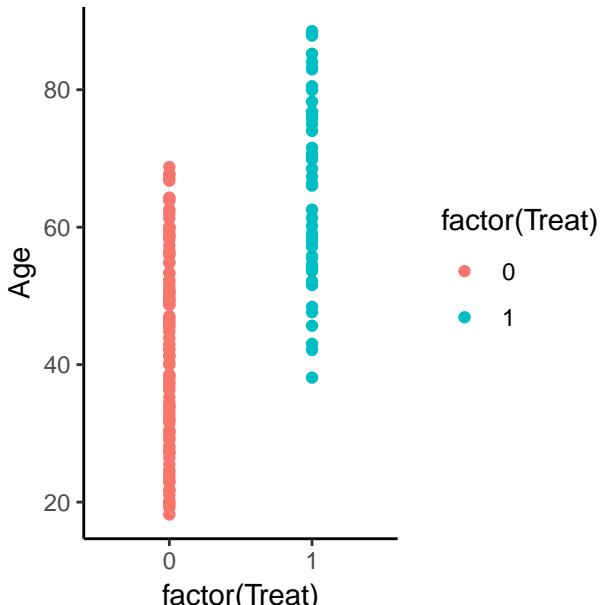
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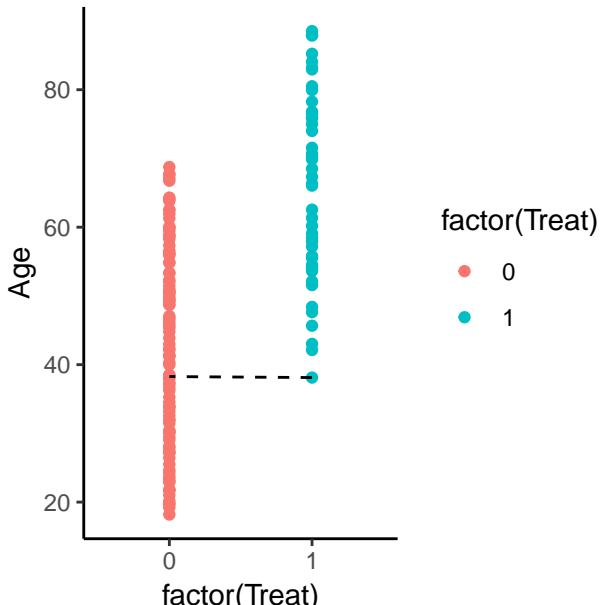
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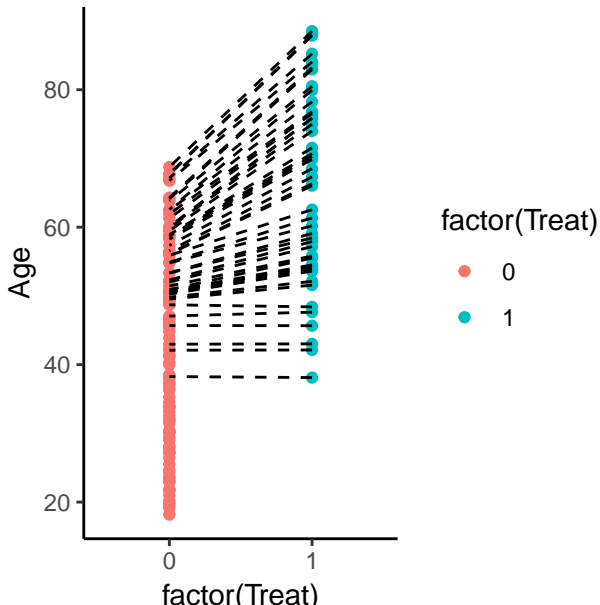
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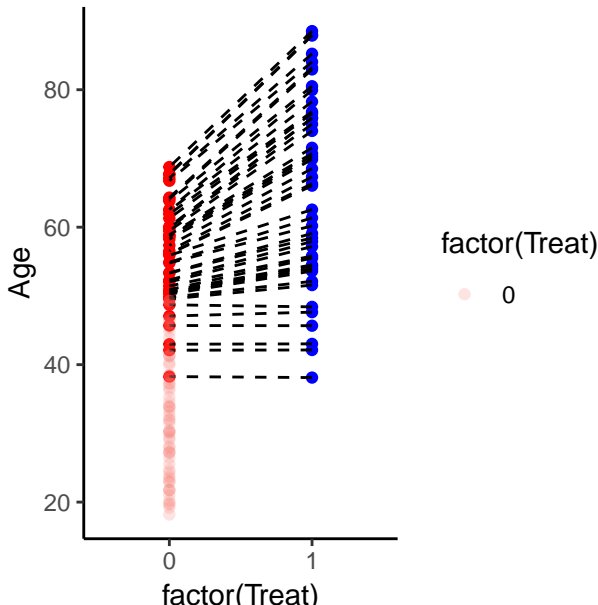


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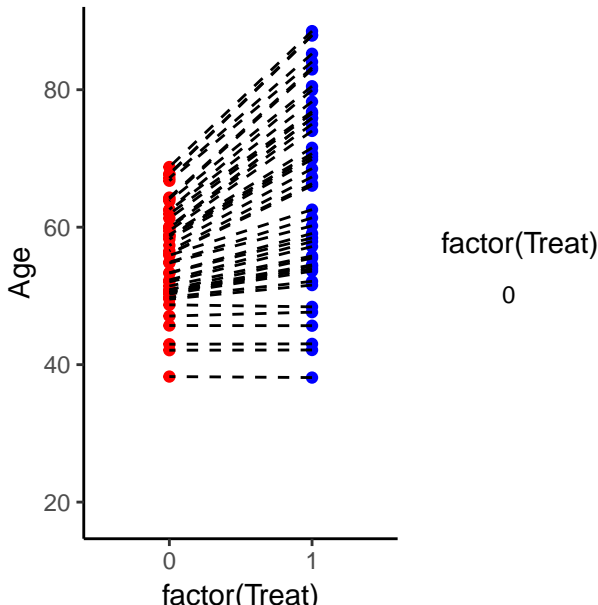




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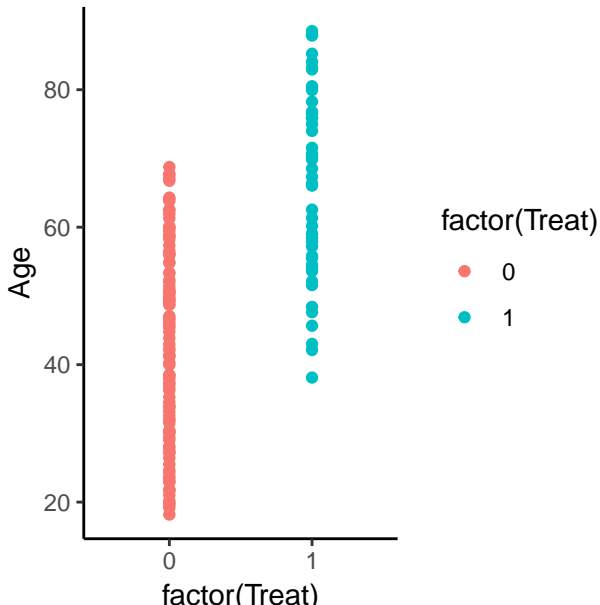
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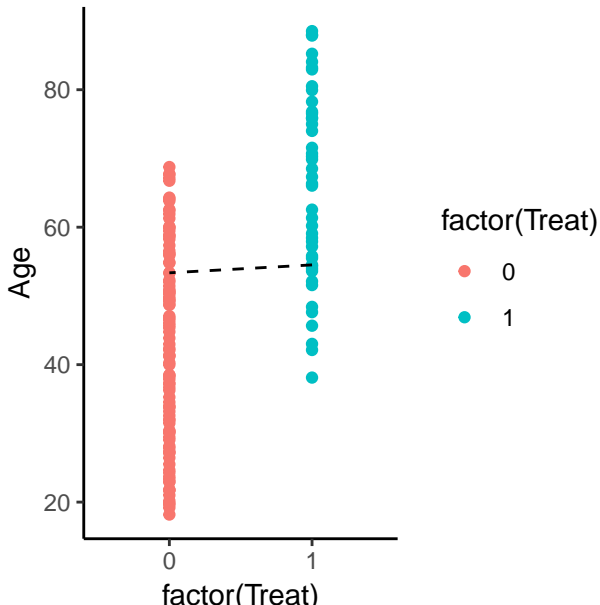
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    - ▶ To maximize balance we need to 'look ahead' and match in the right order
    - ▶ For this we can use optimal or genetic matching, which is fully automated

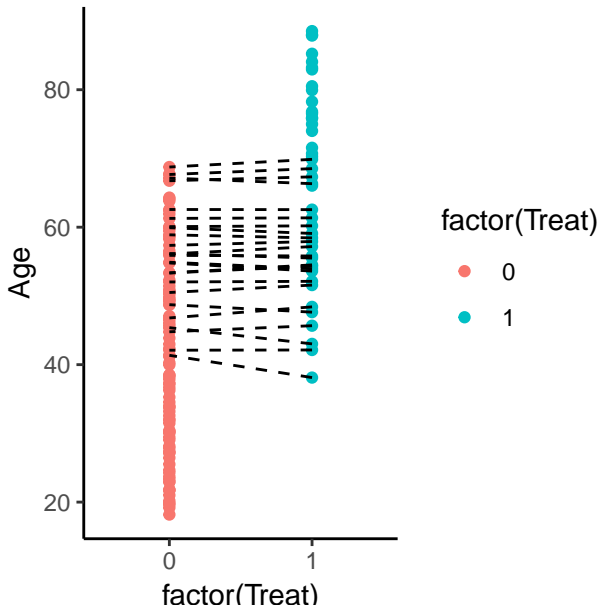
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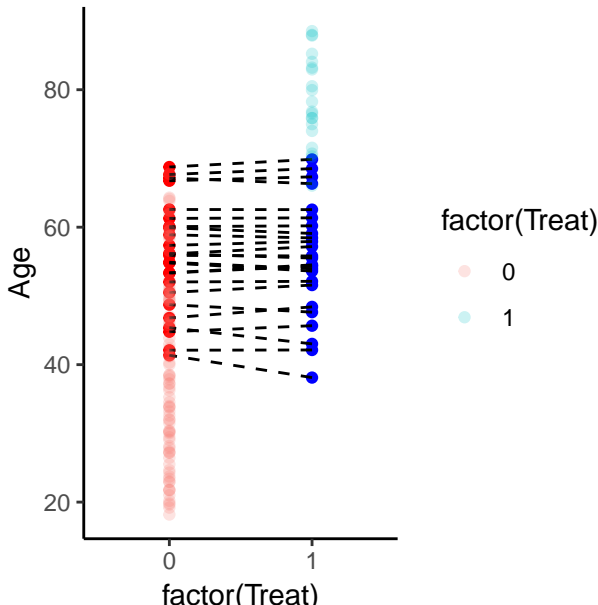
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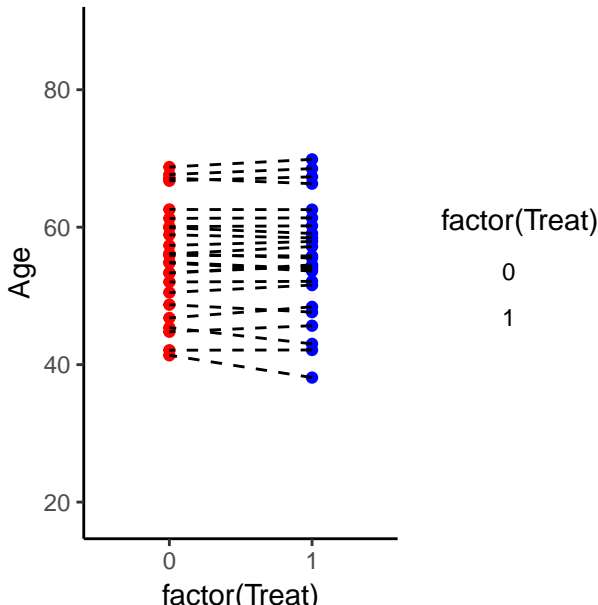
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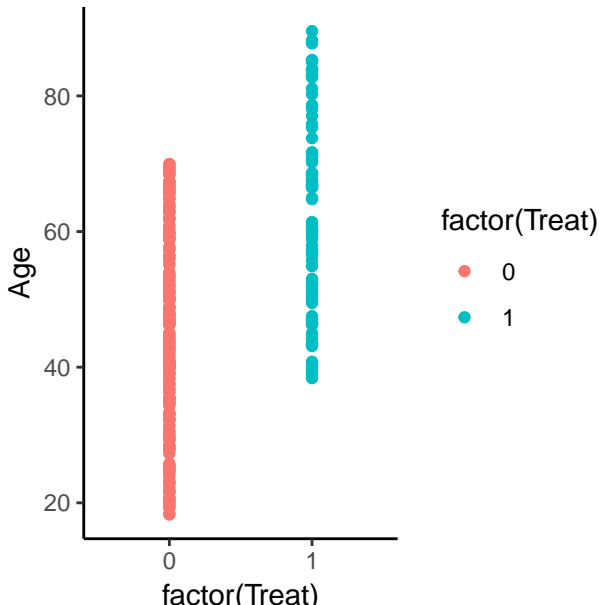
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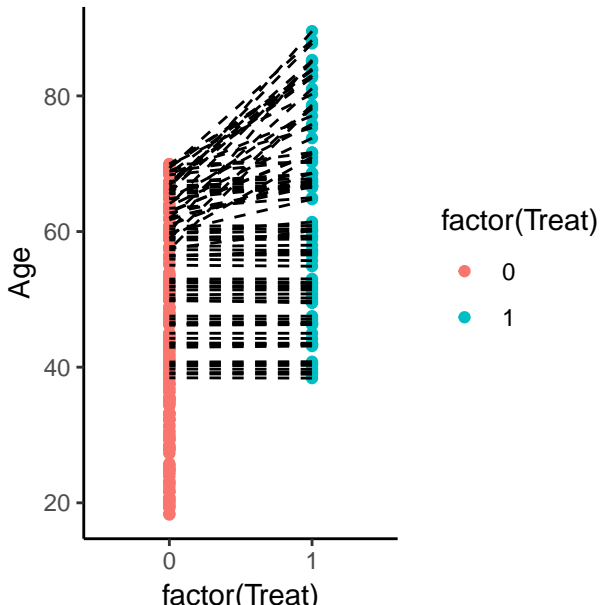
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- We always want to improve balance as much as possible
- Better to compare (standardized) difference in means

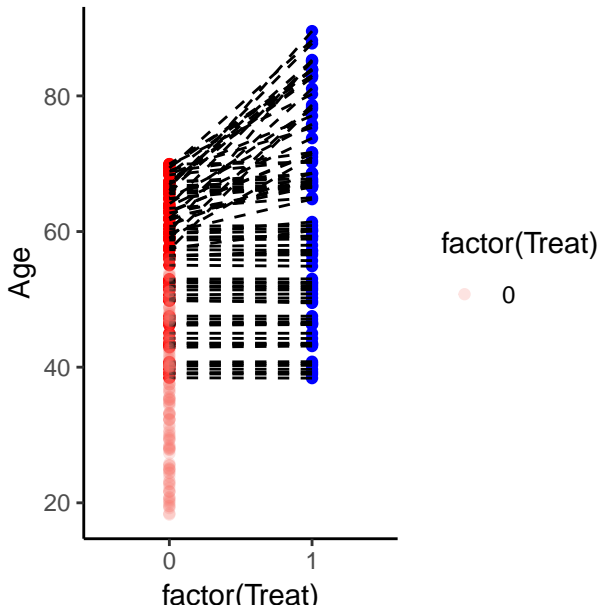
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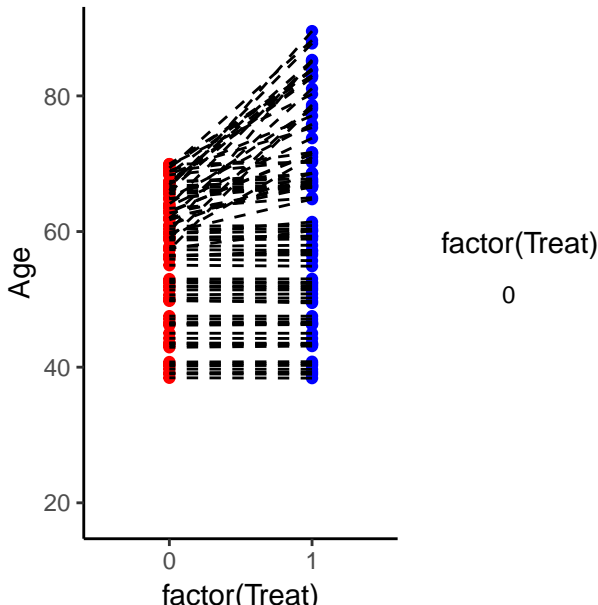
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## Optimal Matching

	Units	Means Treated	Means Control	Mean Diff
1	All	62.60	44.64	17.96
2	Matched	62.60	57.57	5.03

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  - ▶ So let's use the confounders to **predict treatment**
  - ▶ That's different to actual treatment status, with the remainder due to 'random' factors (if we include all confounders)
- ▶ Then use the propensity score (probability 0-1) to match treated and control units which have the same ex ante probability of treatment

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- ▶ Balance may get worse as we remove more units



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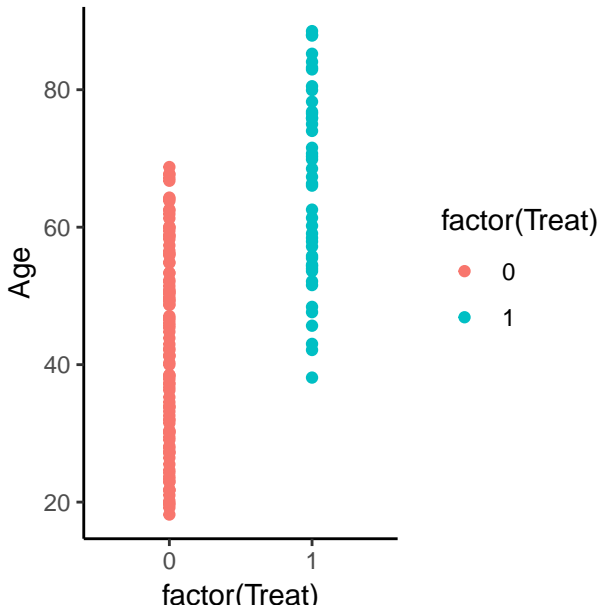
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- ▶ Match on the values of  $Predicted\_Treat_i$  (fitted values of the regression)
- ▶ I.e. match units with a similar *probability* of treatment

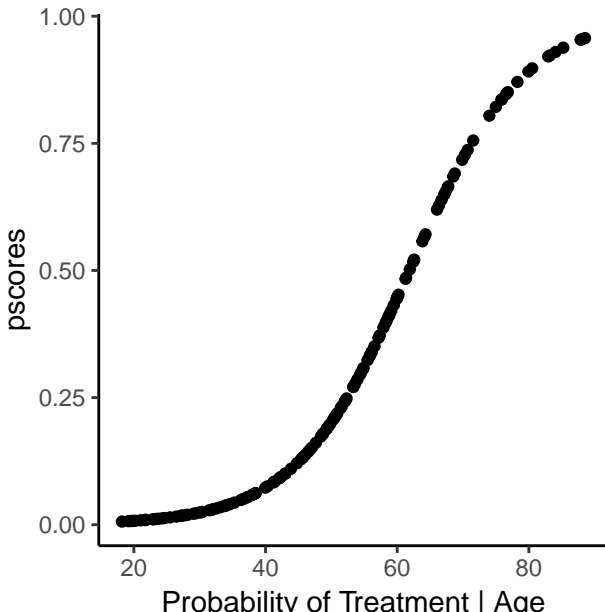


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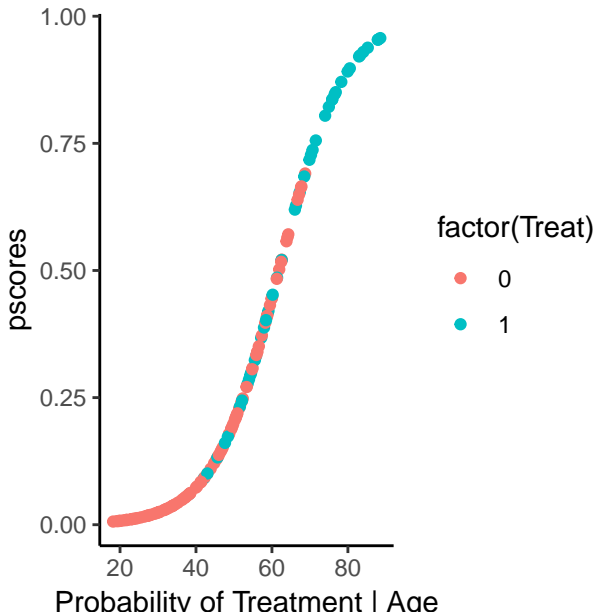




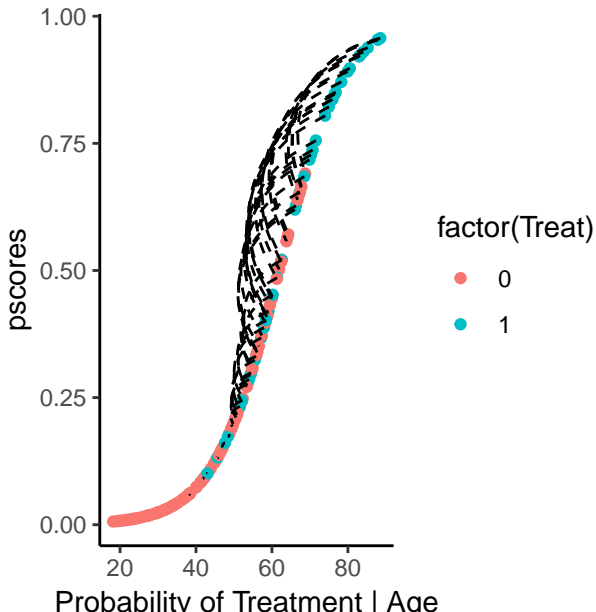
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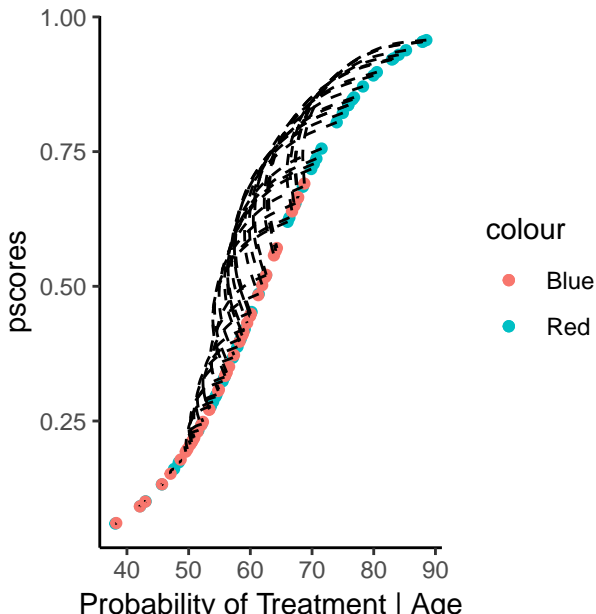
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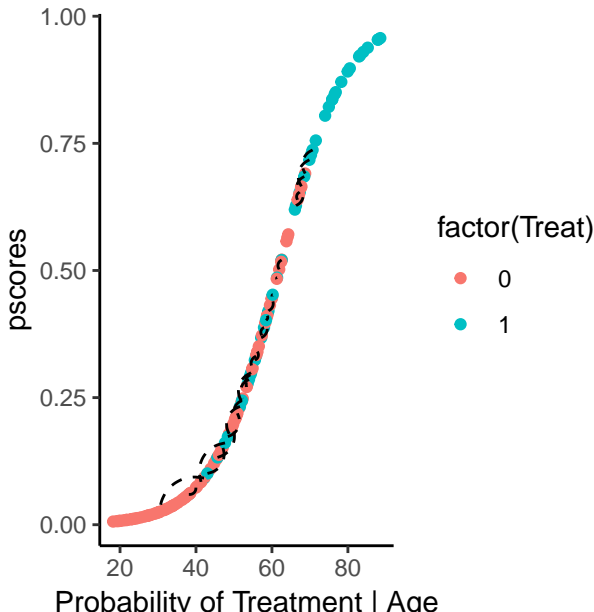
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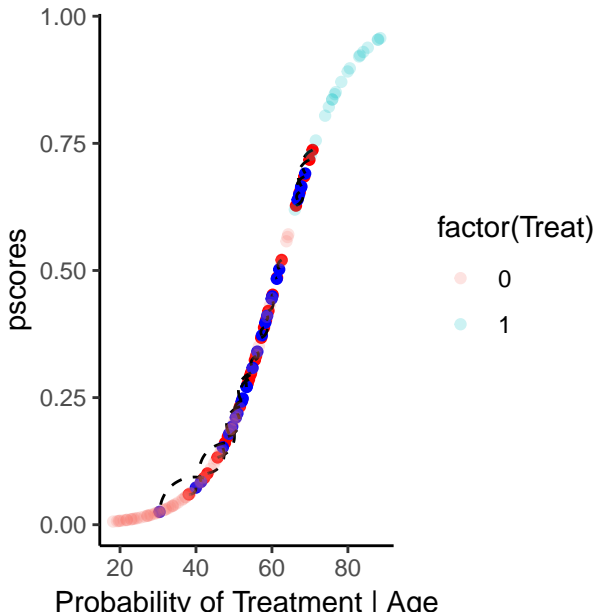
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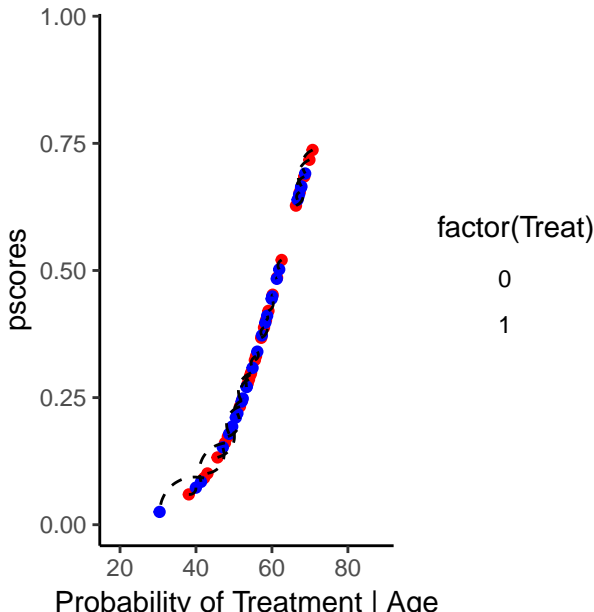
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- ▶ That's okay! Regression has no measure of 'success', but with matching we want to maximize balance
  - ▶ **Without** looking at the outcome variables
- ▶ How much trimming/pruning should we undertake?

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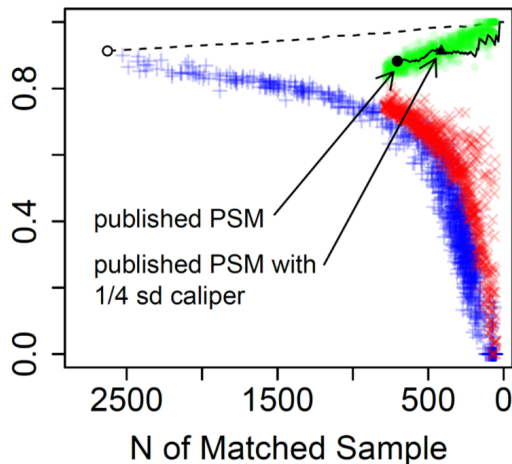




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- ▶ But our N will approach zero, so little statistical power
- ▶ A Bias-variance trade-off
- ▶ Try alternative specifications

# Matching



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- ▶ Matching + Regression = "Doubly Robust"
  - ▶ If **either** matching produces balance **OR** we have the correct functional form for regression, we can make causal inference

## Section 3

## Matching vs. Experiments

## Matching

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## Matching

- ▶ Arceneaux, Gerber and Green (2005)
- ▶ How does matching work on experimental (IV) data? (eg. for how to get voters to vote)
- ▶ Matching is biased compared to the experimental results
- ▶ Lots of controls
- ▶ But unobserved confounders mean matching can't recover causal estimates





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- ▶ Matching estimate: 2.8



