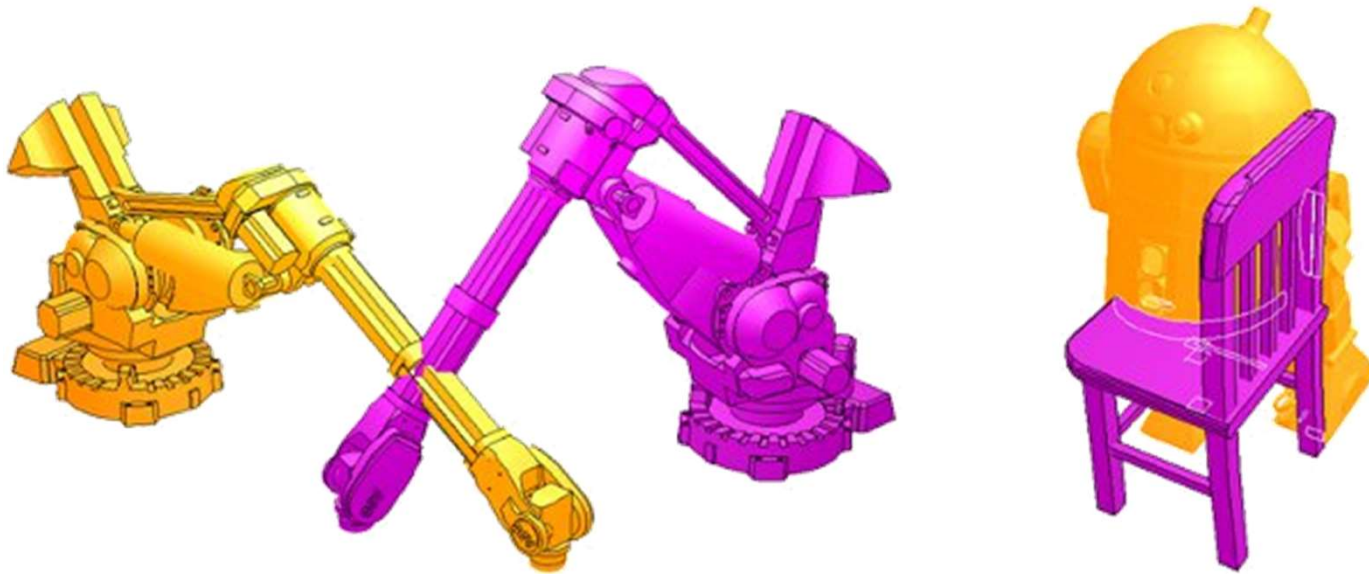
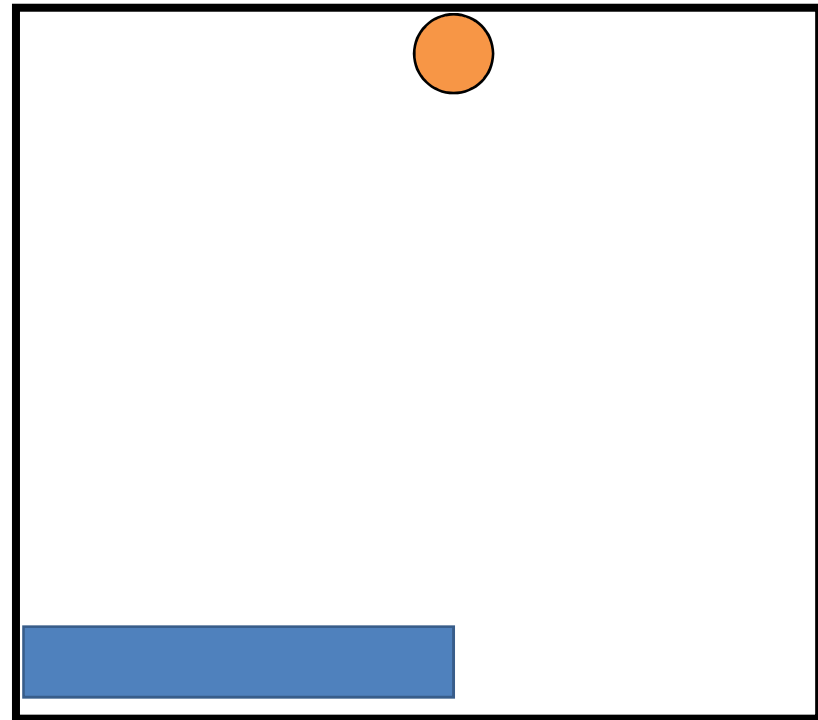
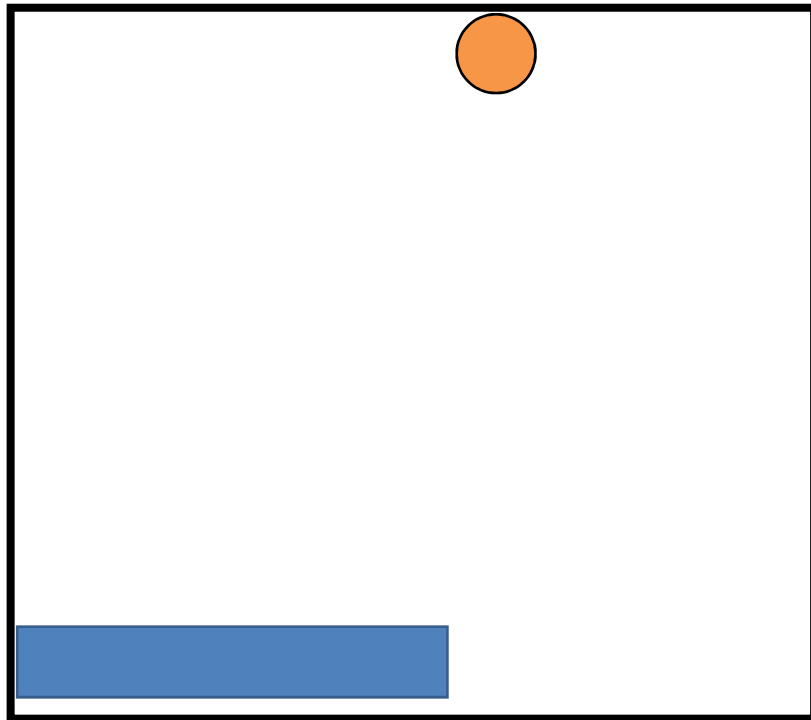


Handling Collisions



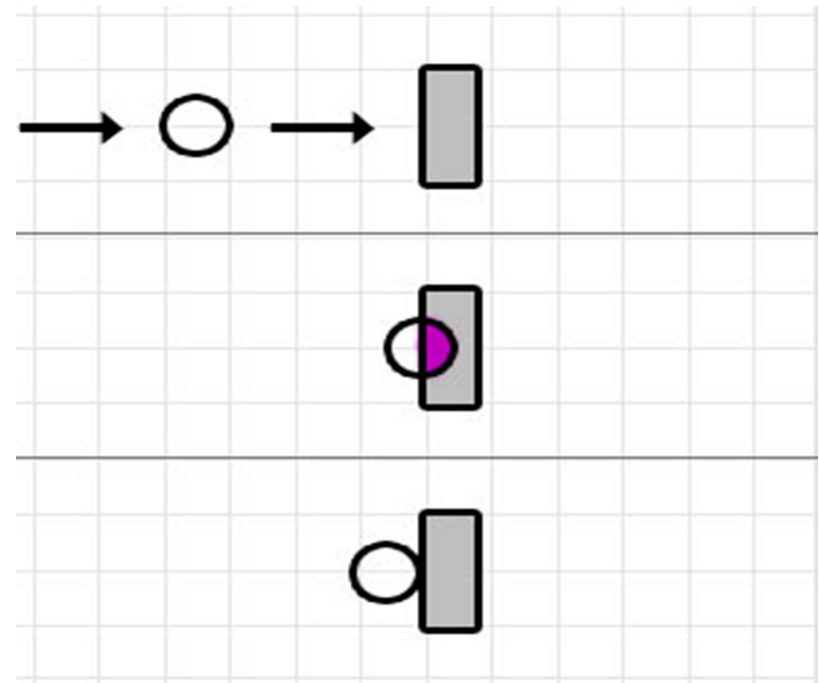
Why?

- Realisme / game play
 - Without objects pass through other objects



Three Major Parts

- Collision detection
 - Do the objects collide?
- Collision determination
 - Where do they collide?
- Collision response
 - What happens now?



Three Major Parts

- Collision detection
 - Do the objects collide?

Always needed



- Collision determination
 - Where do they collide?

Not always needed



- Collision response
 - What happens now?

Specific to application domain

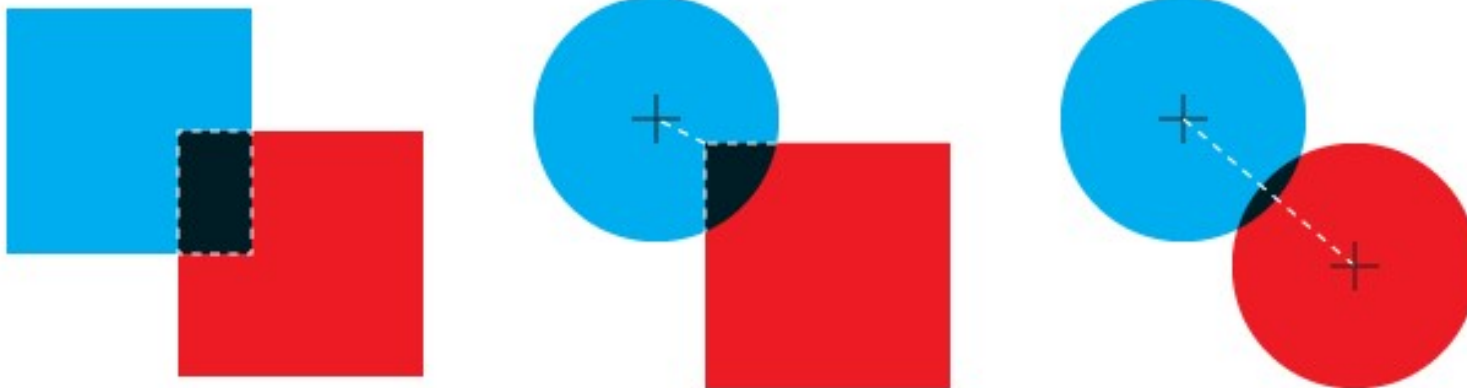


Collision Detection



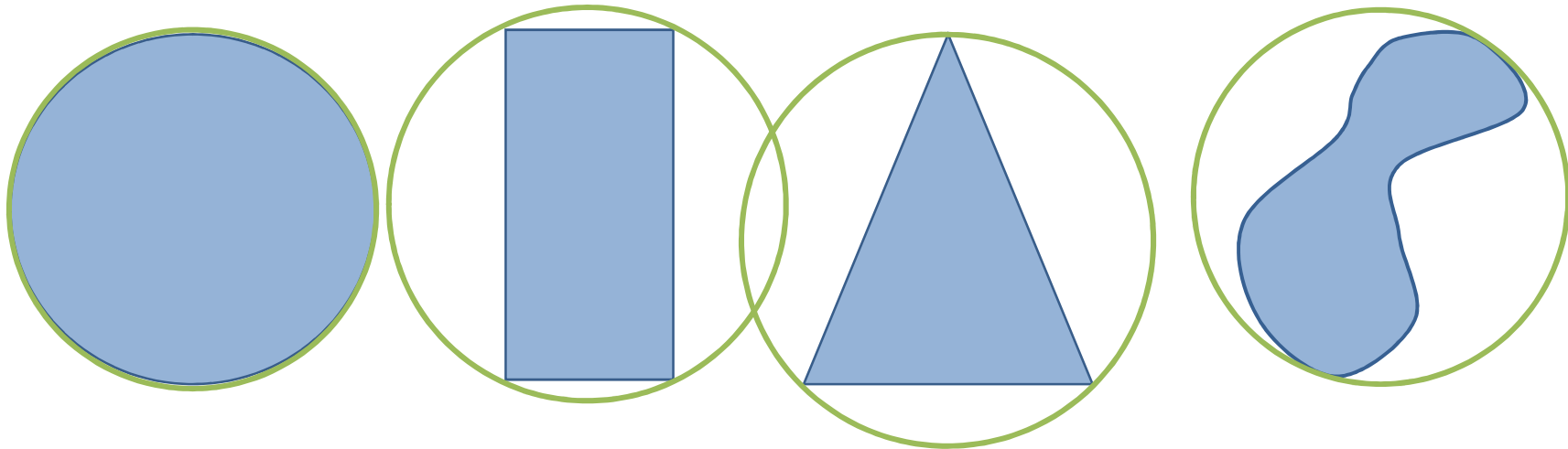
Collision Detection

- Many specialized algorithms for specific geometry
www.realtimerendering.com/intersections.html



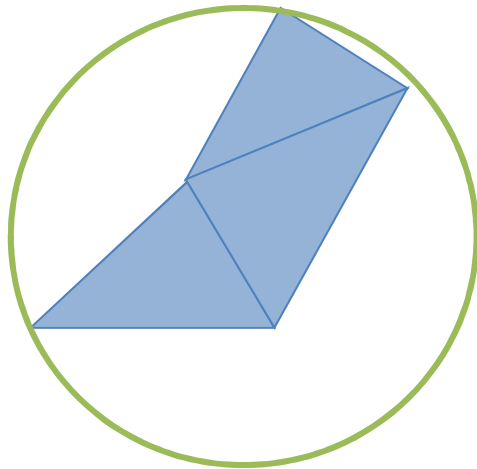
Practical Collision Detection

- Start with coarse approximation
 - Instead of complex objects **bounding geometry** is used
- Often exact result not needed
 - In games often one type of **bounding geometry** is used for all objects



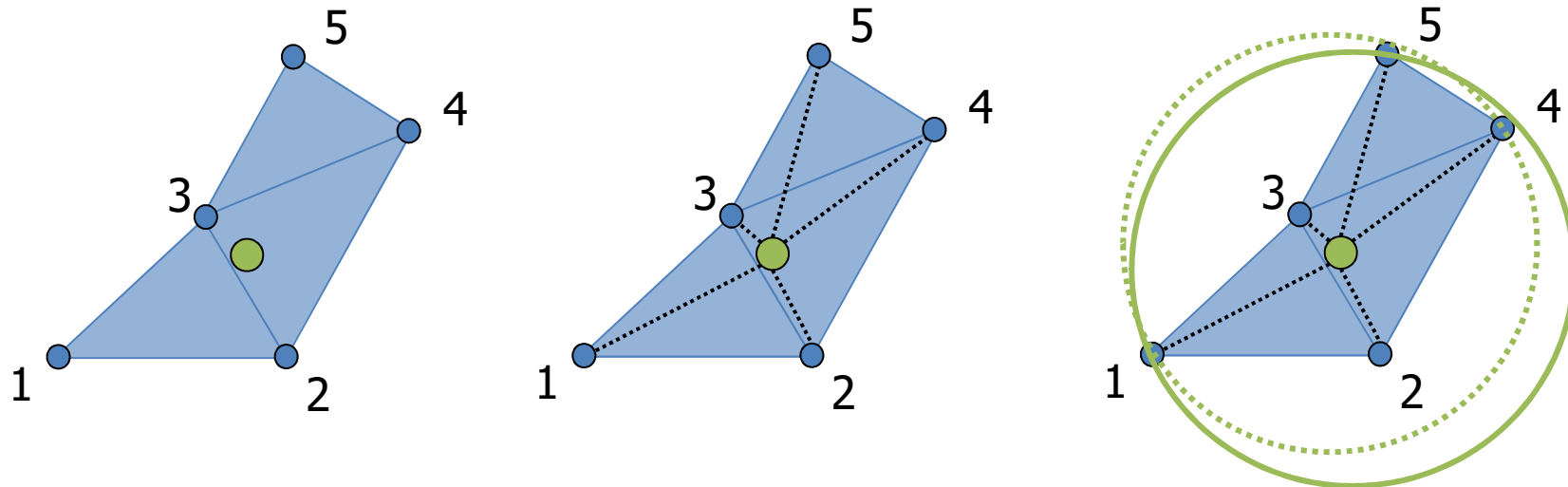
How do we find a bounding geometry?

- Calculation (again many algorithms)
- Artists defines the bounding geometry alongside the object



Bounding Sphere – Calculation

- Find the center
 - Average of all vertices
- Find radius
 - For all vertices: calculate max. distance to M
- In mathematics: minimal bounding sphere problem

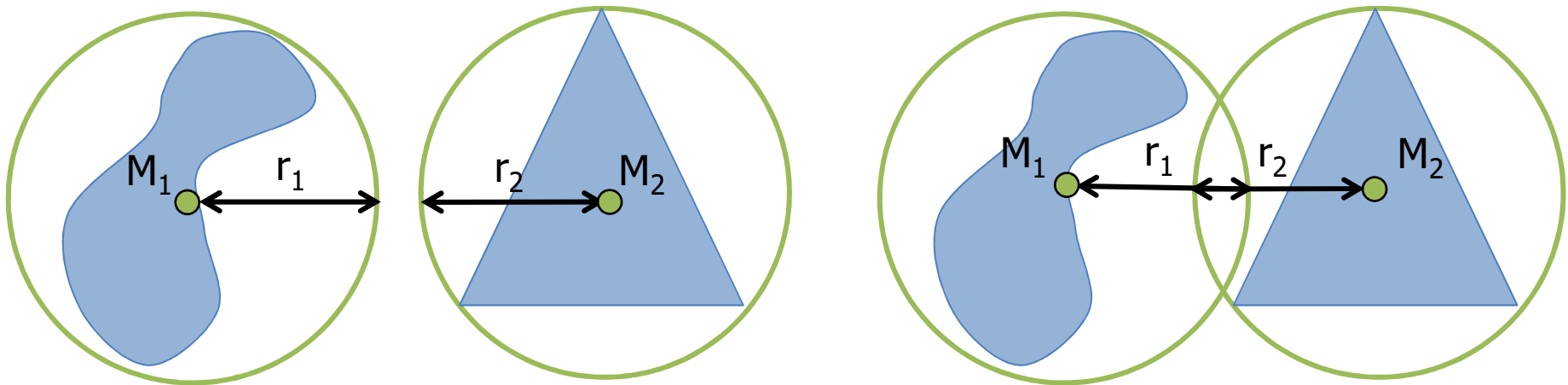


Bounding Sphere – Collision Detection

- Collision iff

$$\text{distance}(M_1, M_2) < r_1 + r_2$$

$$\Leftrightarrow \text{distance}(M_1, M_2)^2 < (r_1 + r_2)^2$$



Creative Use of Bounding Spheres

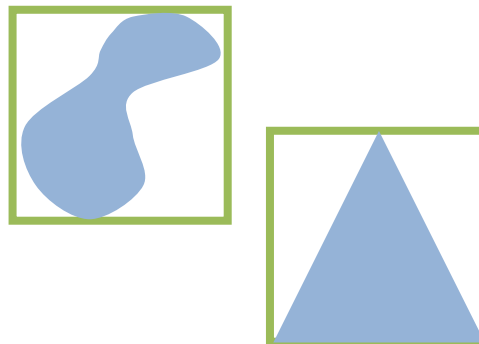
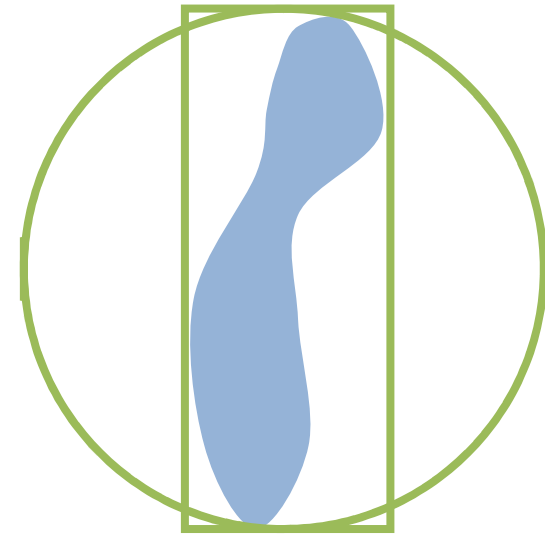


Assassin's Creed III

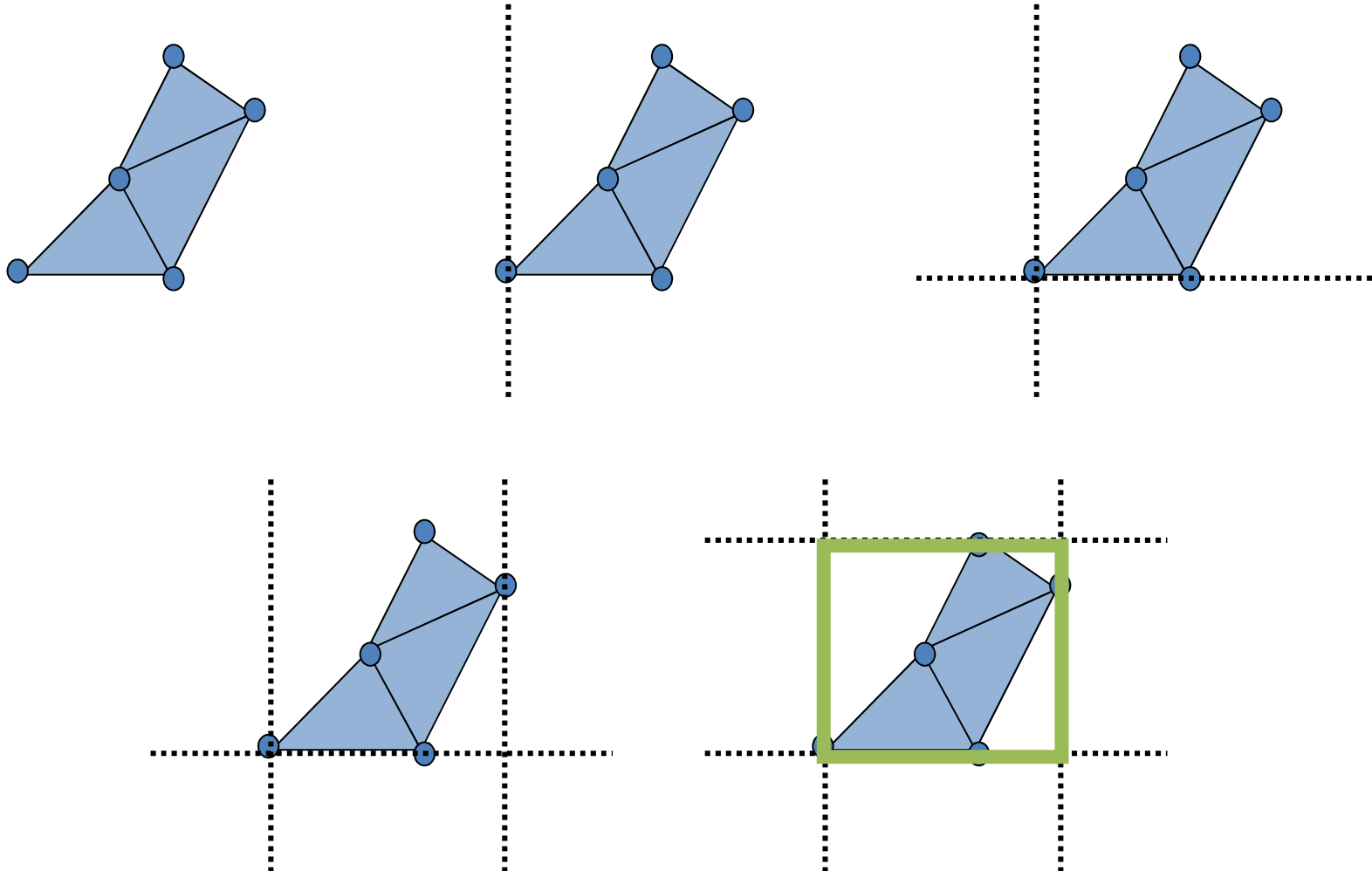
immersed partition

AABB-Algorithm

- Bounding-Spheres:
 - Efficient
 - Inaccurate
- Axis Aligned Bounding Boxes
 - Better fit for elongated objects
 - Only slightly more complicated

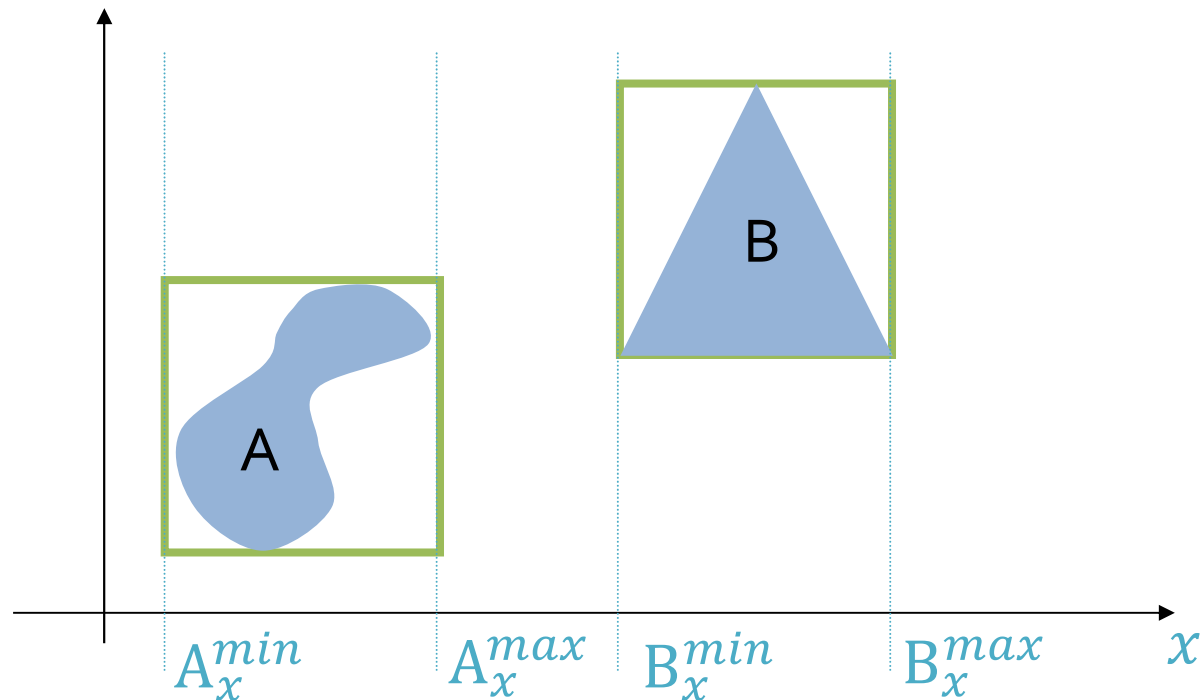


AABB – Calculation



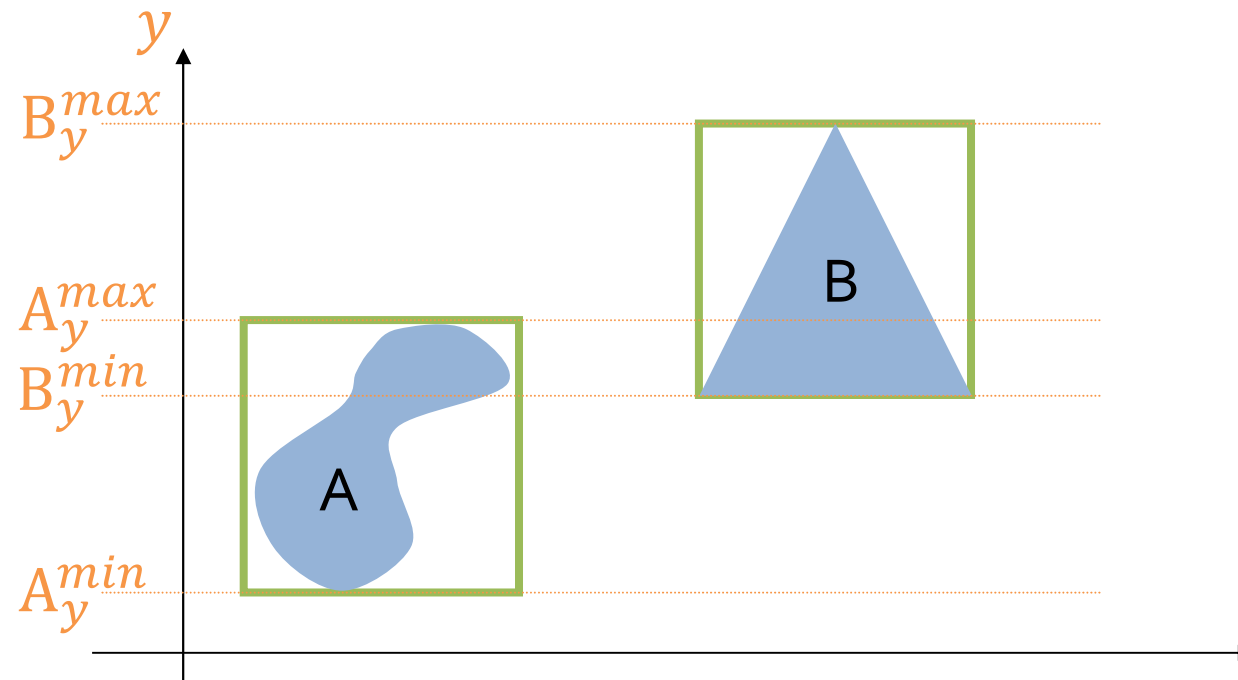
AABB-Algorithm

- No collision if
- $(A_x^{min} > B_x^{max}) \text{ or } (B_x^{min} > A_x^{max})$



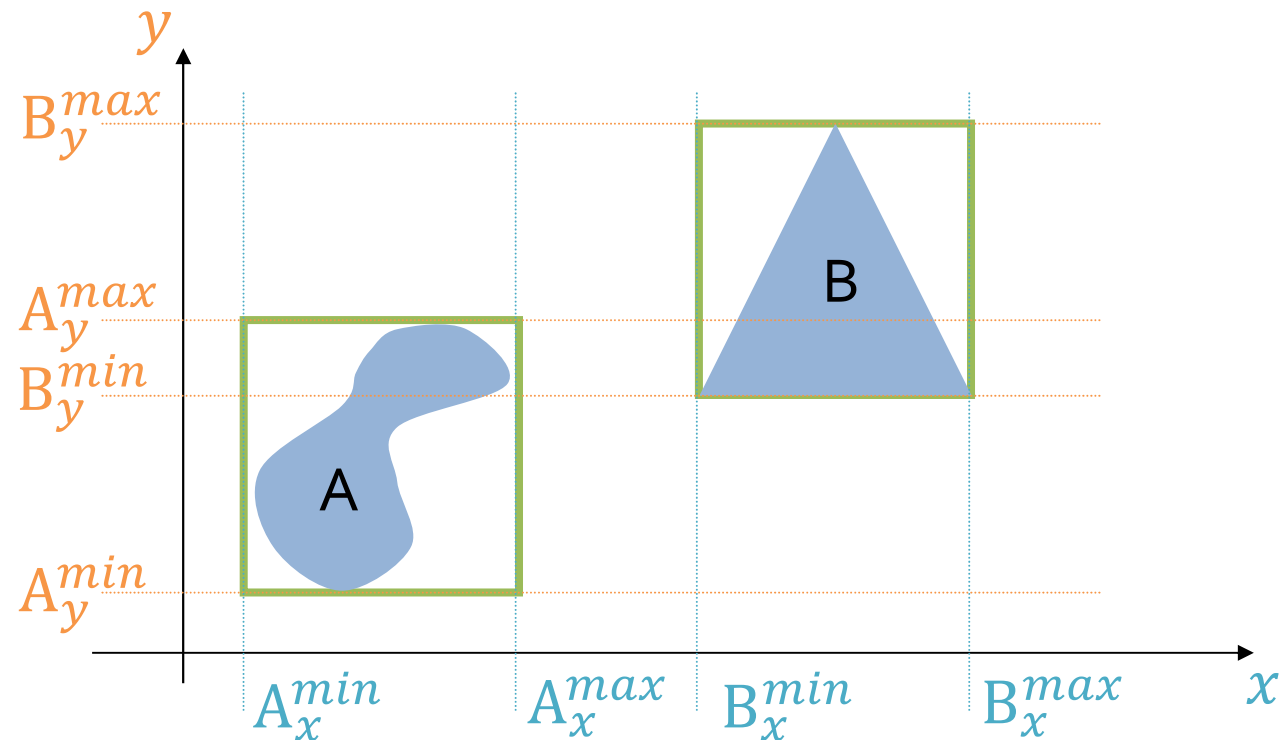
AABB-Algorithm

- No collision if
- $(A_y^{min} > B_y^{max}) \text{ or } (B_y^{min} > A_y^{max})$



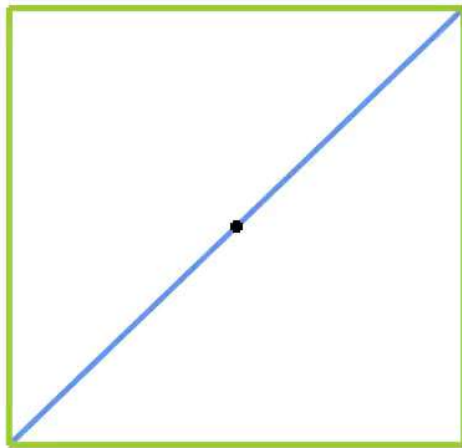
AABB-Algorithm

- No collision if
- $\exists i \in \{x, y\} | (A_i^{min} > B_i^{max}) \text{ or } (B_i^{min} > A_i^{max})$
 - Separating axis theorem (same for z)



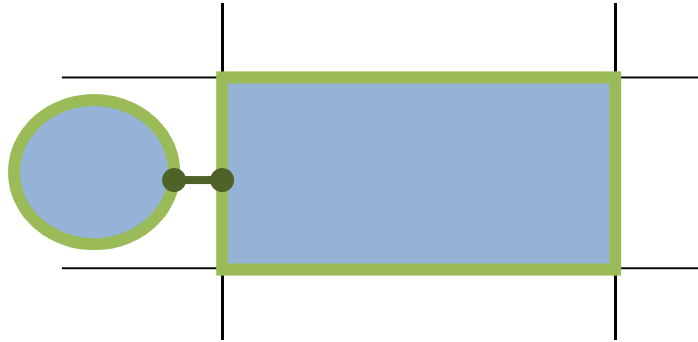
AABB - Problems

- While rotating an object, we have to recalculate the bounding box
- Avoid recalculation with Bounding sphere

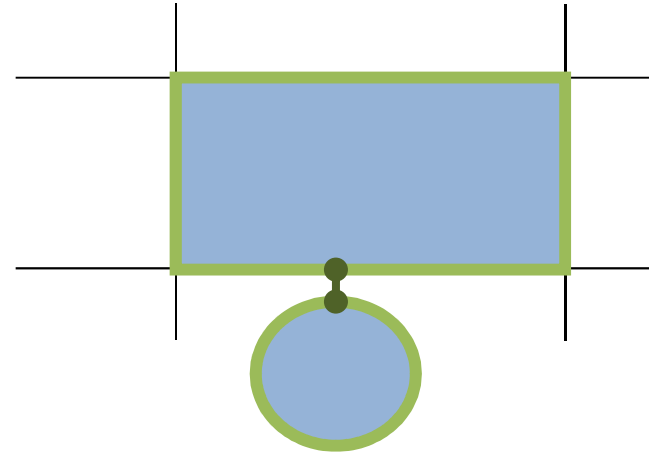


Sphere-Box Intersection

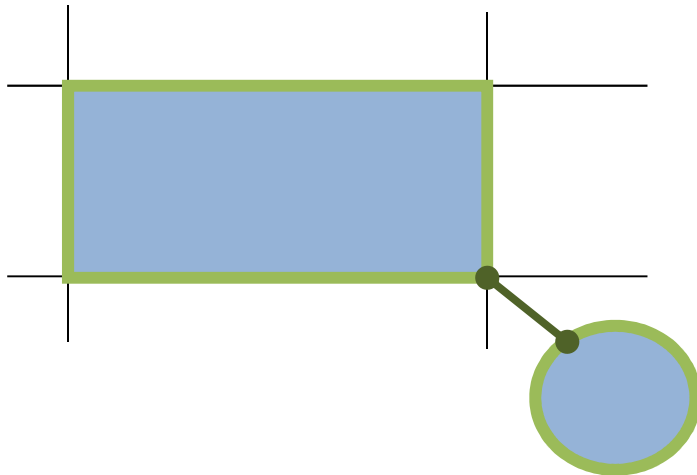
(1)



(2)



(3)

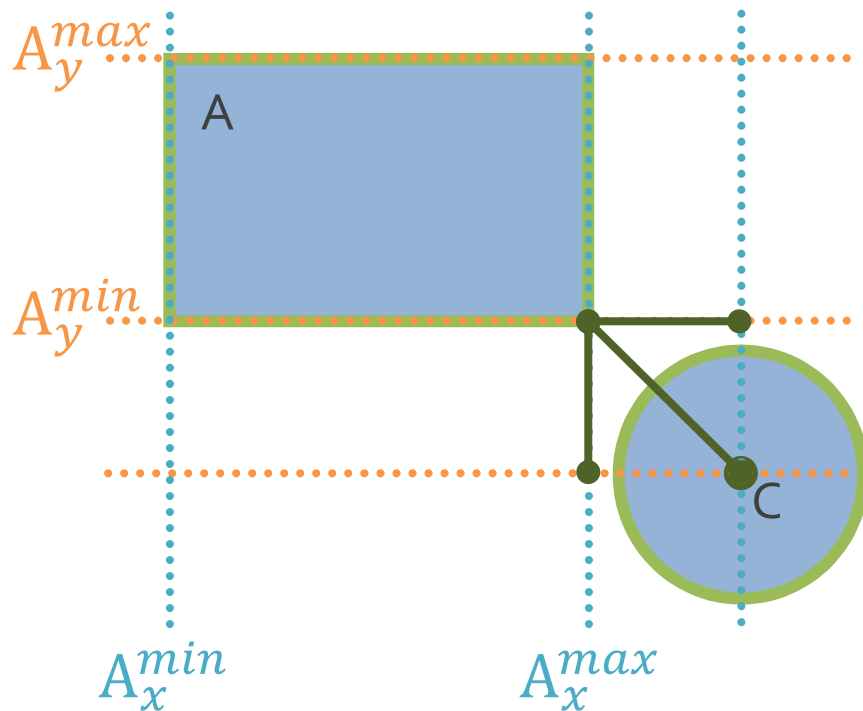


(4)

3D?

Sphere-Box Intersection

- Idea: Coordinate-wise Euclidean distance



```
d = 0
for each i ∈ {x, y, z}
{
```

```
    if ( $C_i < A_i^{min}$ )
        d = d + ( $C_i - A_i^{min}$ )2
```

```
    else if ( $C_i > A_i^{max}$ )
        d = d + ( $C_i - A_i^{max}$ )2
```

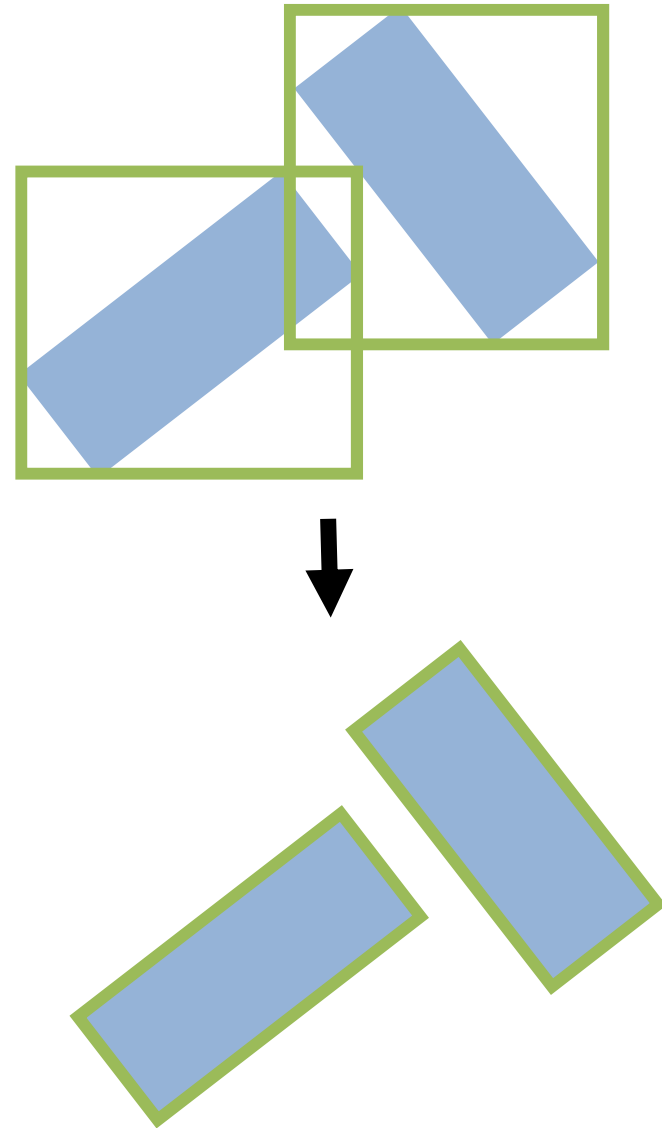
```
}
```

```
if ( $d > r^2$ )
    return DISJOINT
```

```
else
    return OVERLAP
```

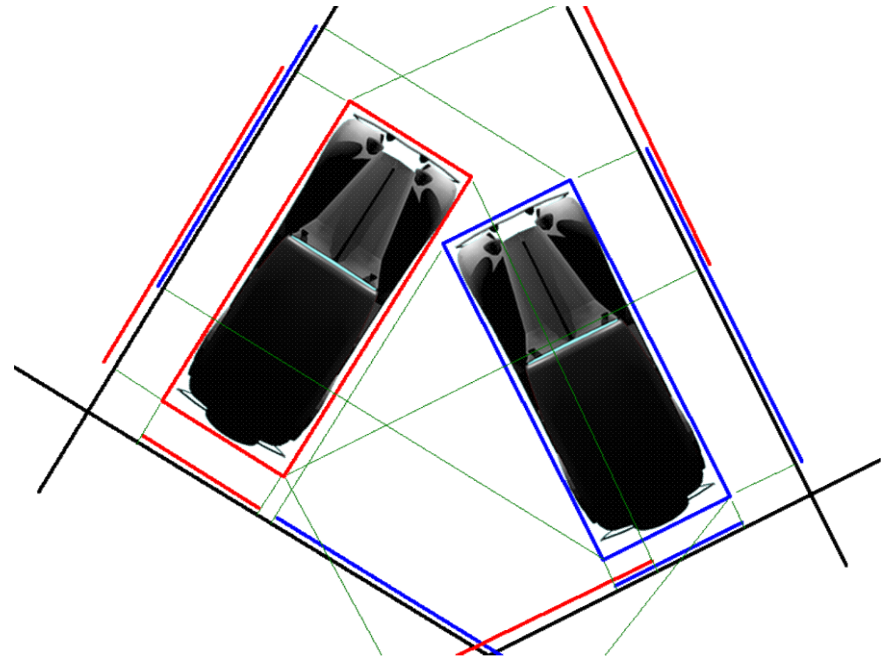
Oriented Bounding Box

- Rotation is no problem
- More complicated to calculate than AABB



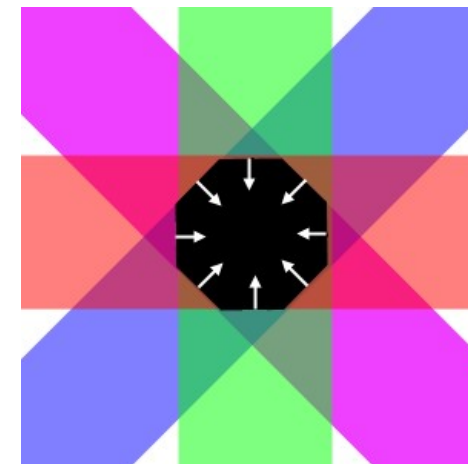
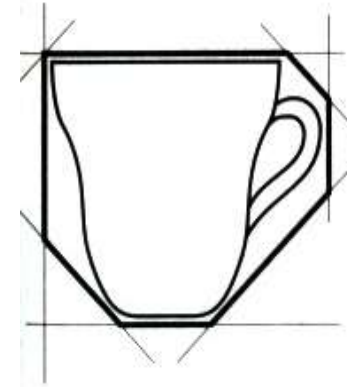
Oriented Bounding Box

- Rotation is no problem
- More complicated to calculate than AABB
- Separating axis theorem still works
- More information
 - www.gamasutra.com
 - Game Prog Gems (I, II, III)



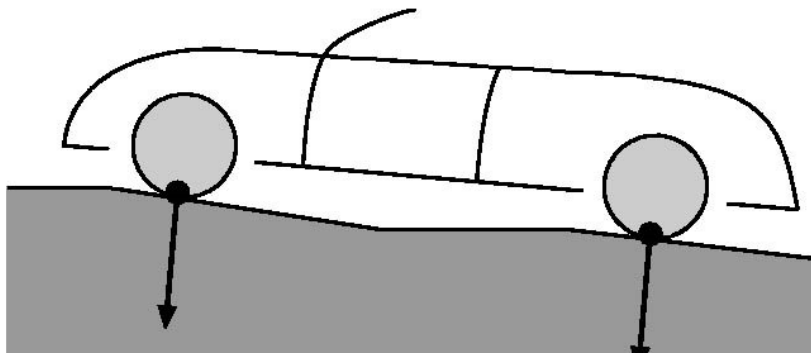
k-DOP

- k-Discrete Oriented Polytop
- OBB and AABB are 6-DOPs
- Optimal bounding boxes
- If convex separating axis theorem applies

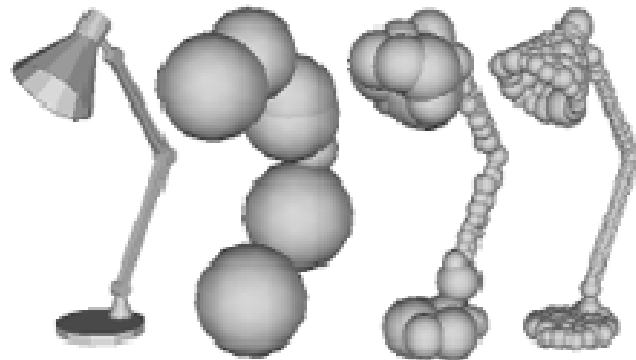
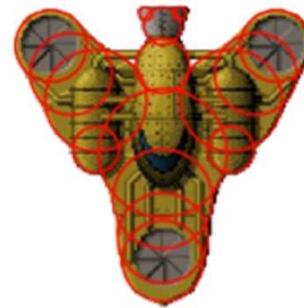
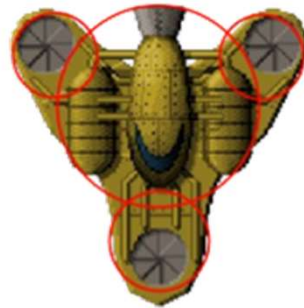
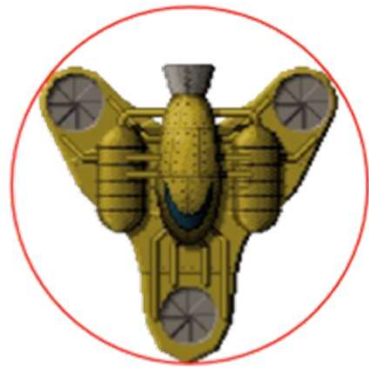


Collision Detection with Rays

- E.x.: car on road, player on terrain
- Test all triangles of all wheels against road geometry
- Often approximation good enough
- Idea: approximate complex object with set of rays

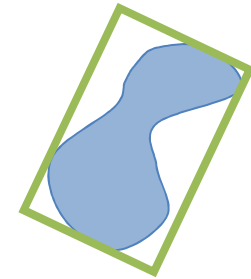
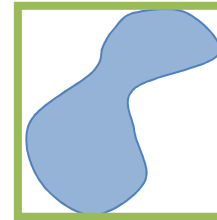


Hierarchy Trees



Phases

- Broad Phase (use spacial data structure for speed)
 - Grids
 - Spatial subdivisions hierarchies
 - Sweep and prune
- Narrow Phase (real object is intersected)
 - Bounding objects
 - Point-Line
 - Point-Triangle
 - Triangle-Triangle
 - ...

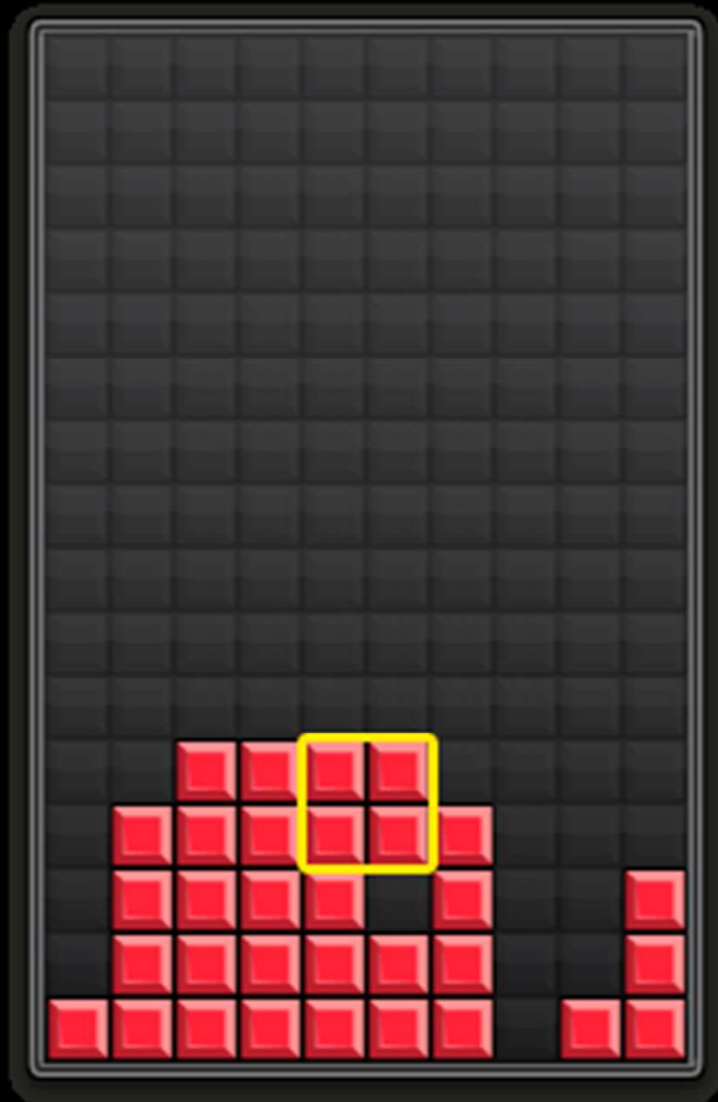


Broad Phase

Handling High Numbers of Objects

- Have to check each object with every other
 - $N \cdot (N-1) \approx N^2$
- Hierarchical irregular subdivision
- Hierarchical Regular subdivision
- Regular subdivision

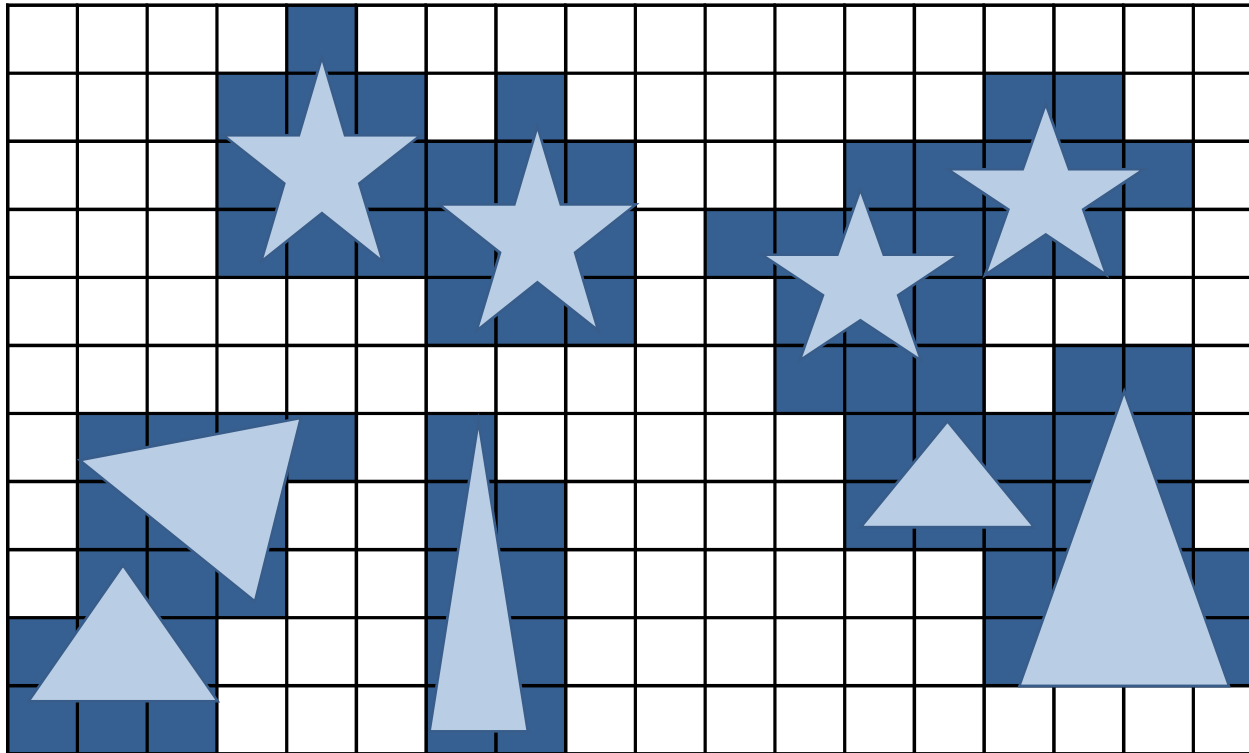
Regular Subdivision



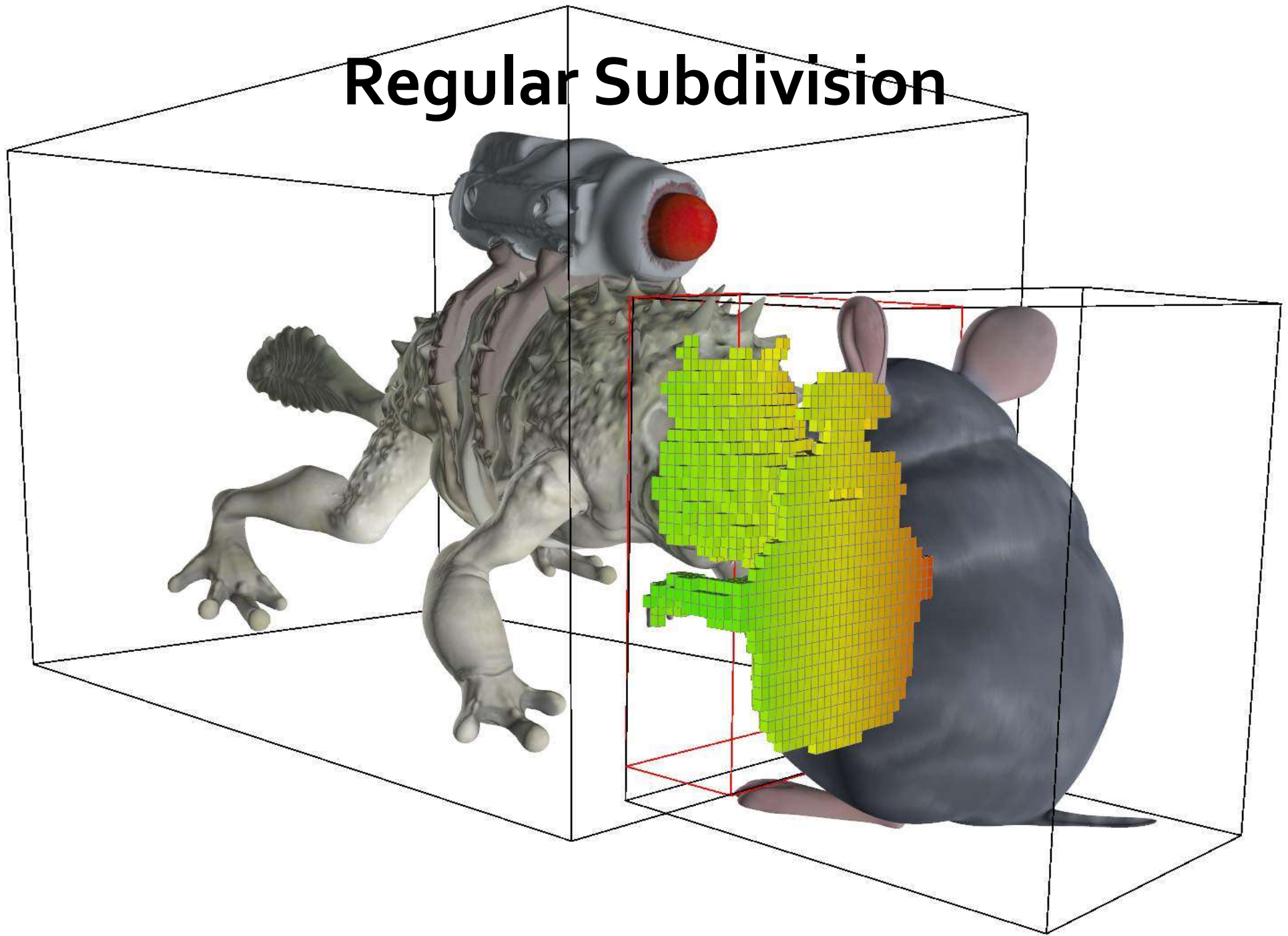
```
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  [0,0,0,0,0,0,0,0,0,0],  
  [0,0,0,0,0,0,0,0,0,0],  
  [0,0,0,0,0,0,0,0,0,0],  
  [0,0,0,0,0,0,0,0,0,0],  
  [0,0,0,0,0,0,0,0,0,0],  
  [0,0,0,0,0,0,0,0,0,0],  
  [0,0,1,1,0,0,0,0,0,0],  
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  [0,1,1,1,1,1,1,0,0,1],  
  [1,1,1,1,1,1,1,0,1,1]]
```

Regular Subdivision

- Test with regular grid

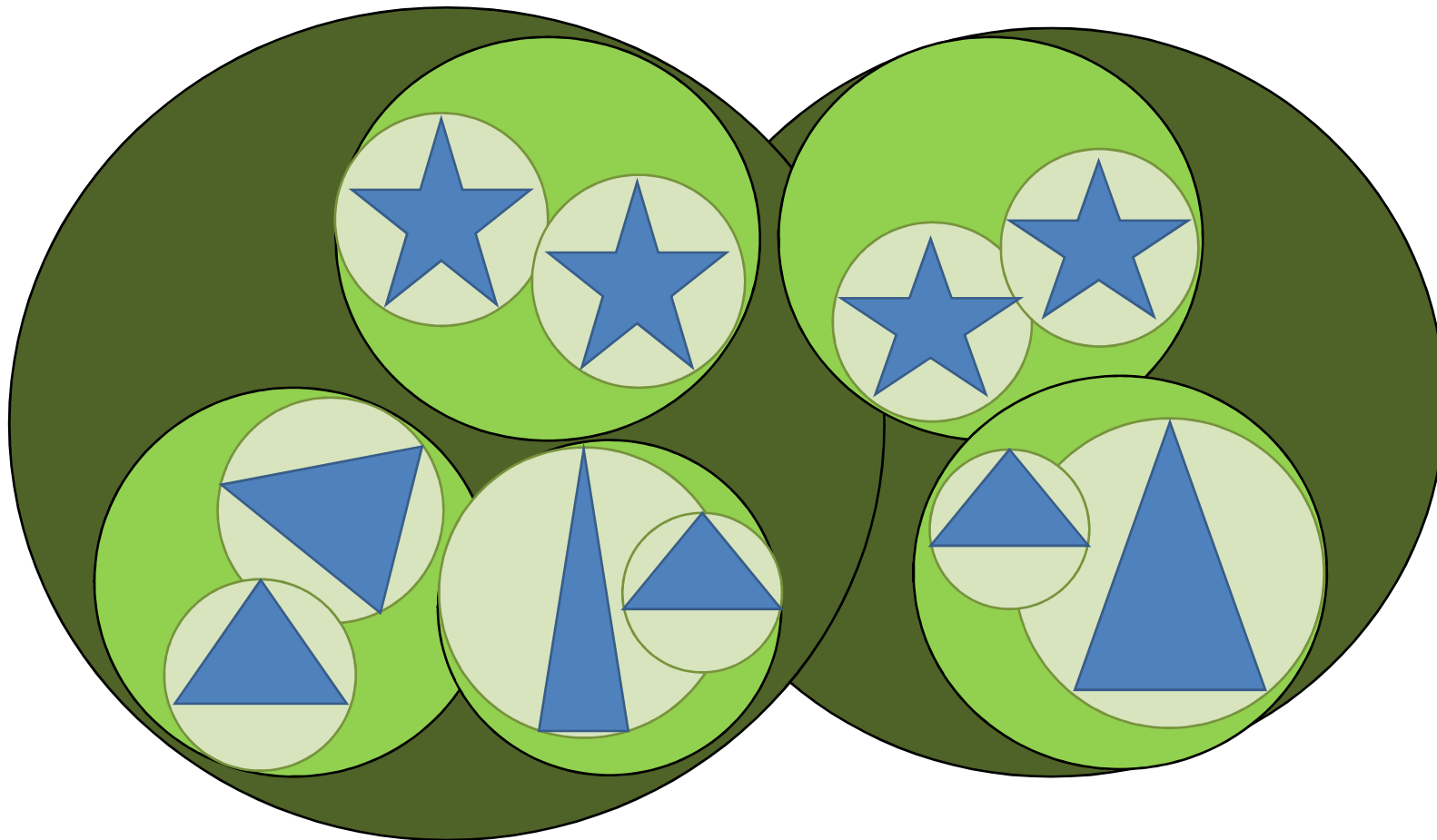


Regular Subdivision



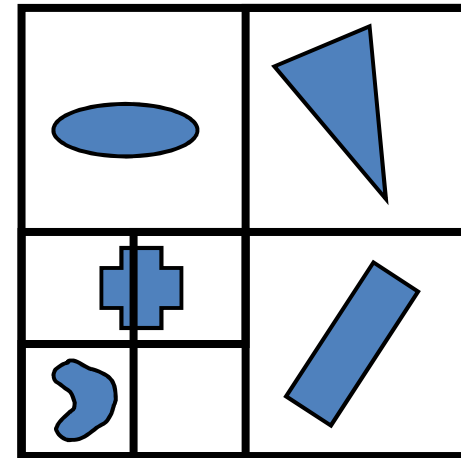
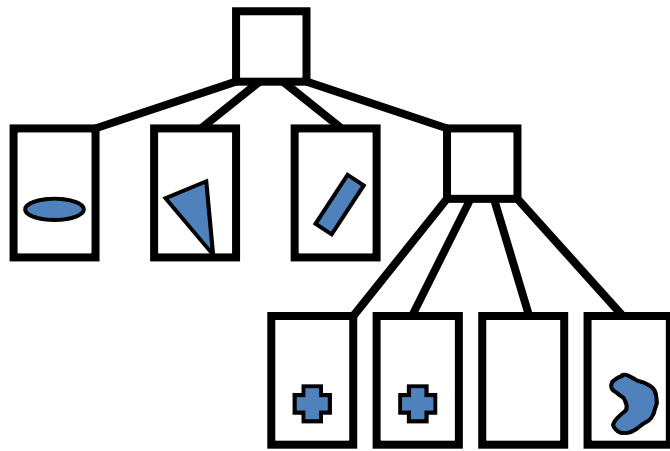
Hierarchy Trees

- Bounding Volume Hierarchy = BVH

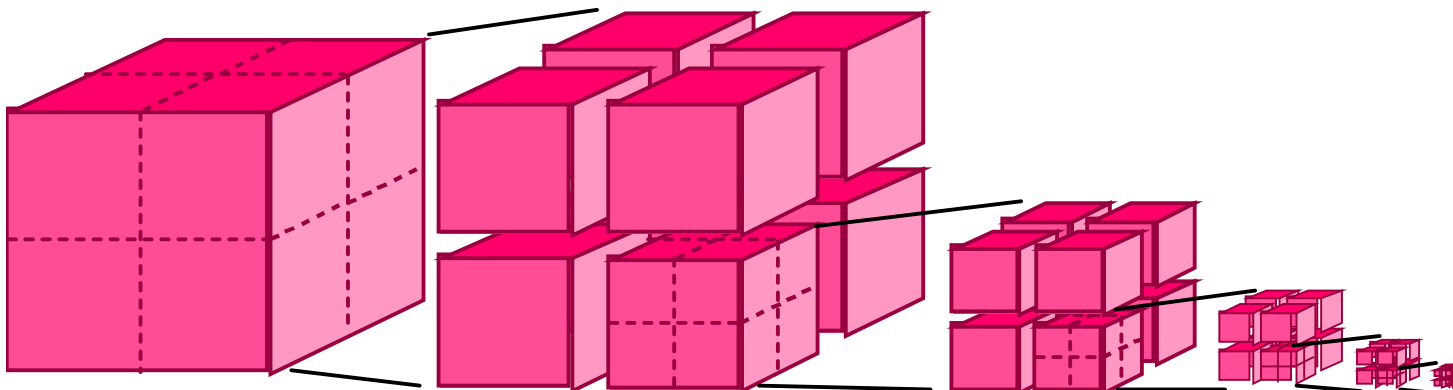


Quad/Octrees

- Quadtree (2D)

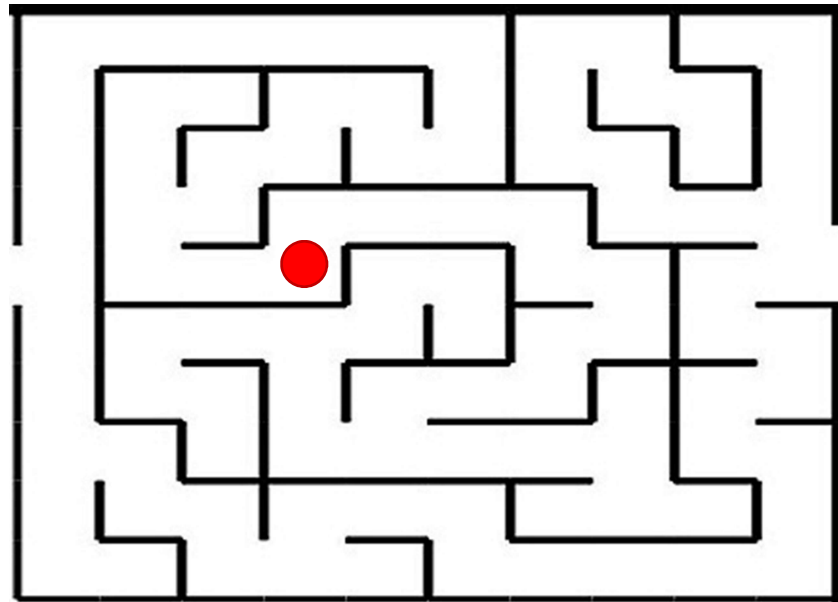


- Octree (3D)

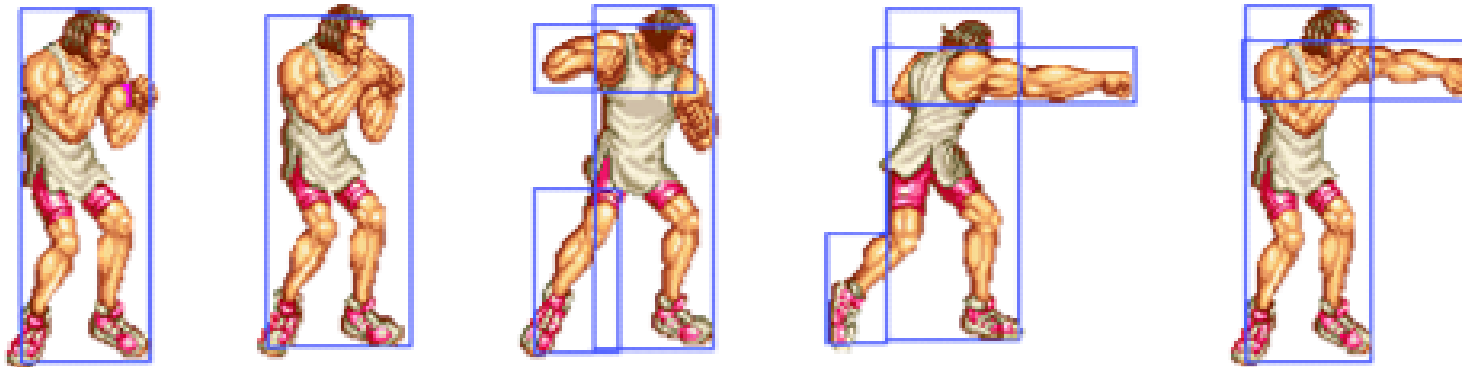


Another Simplification

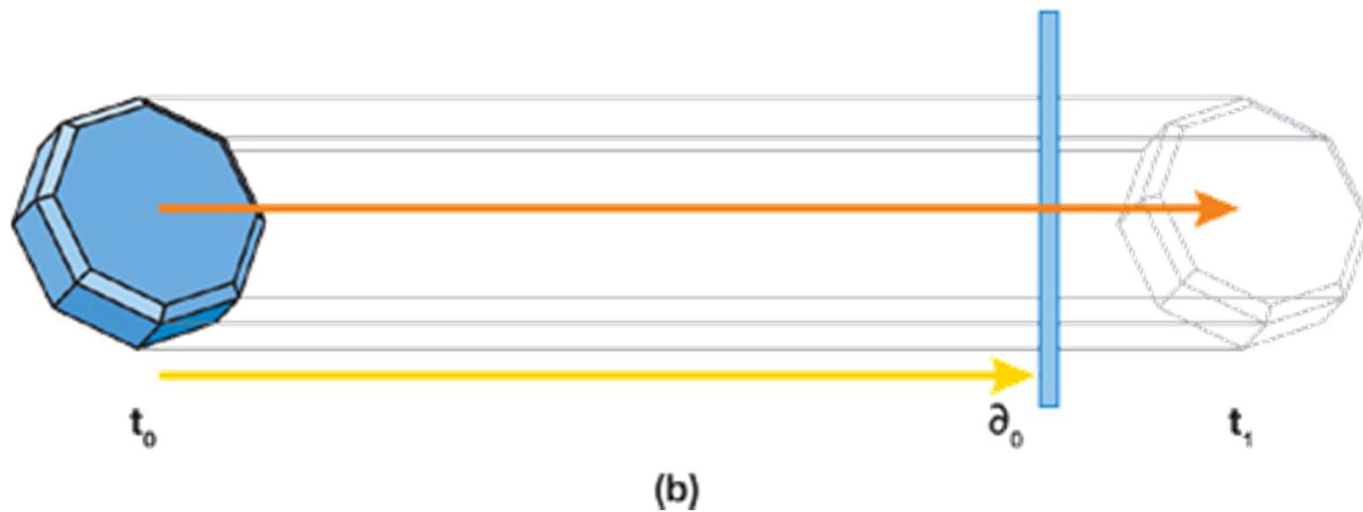
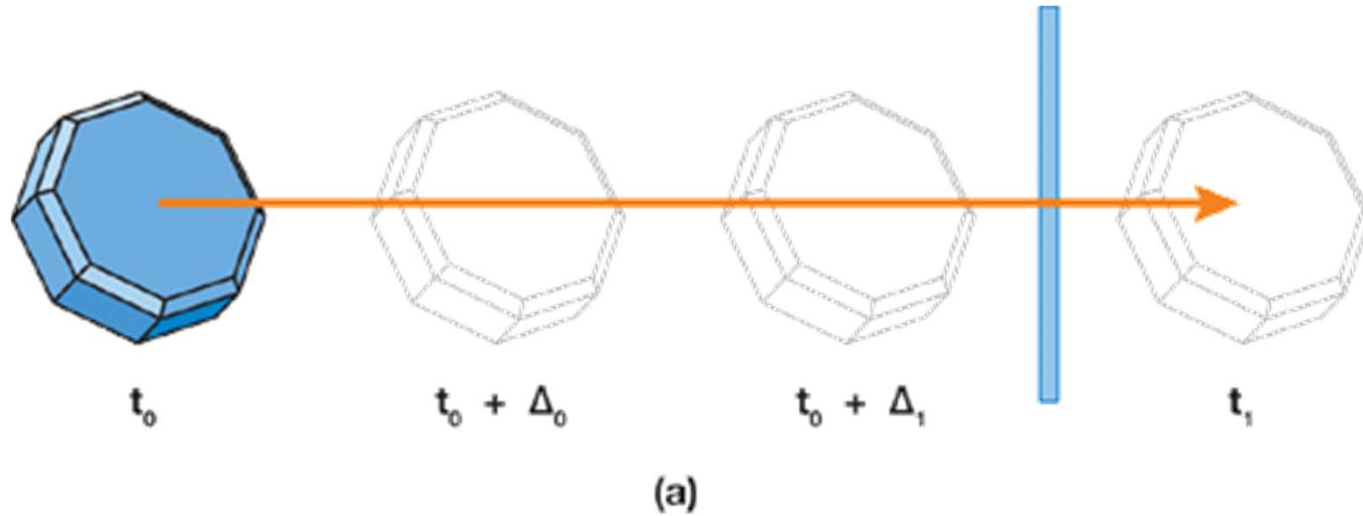
- Sometimes 3D can be turned into 2D operations
- Example: maze
- Approximate player by circle
- Test circle against lines of maze

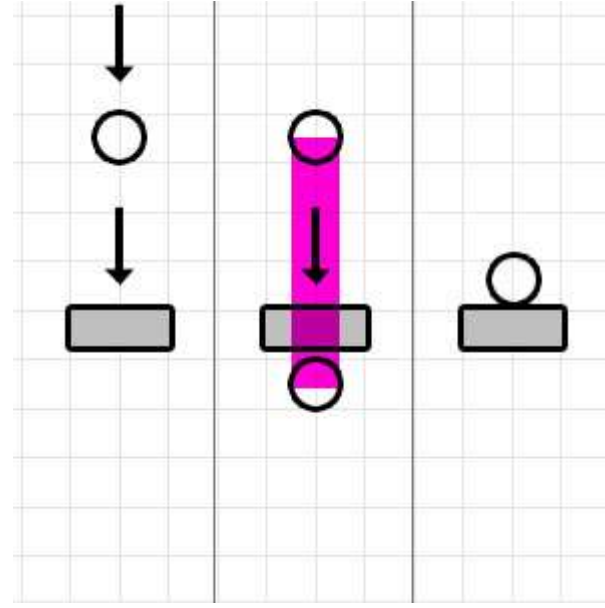
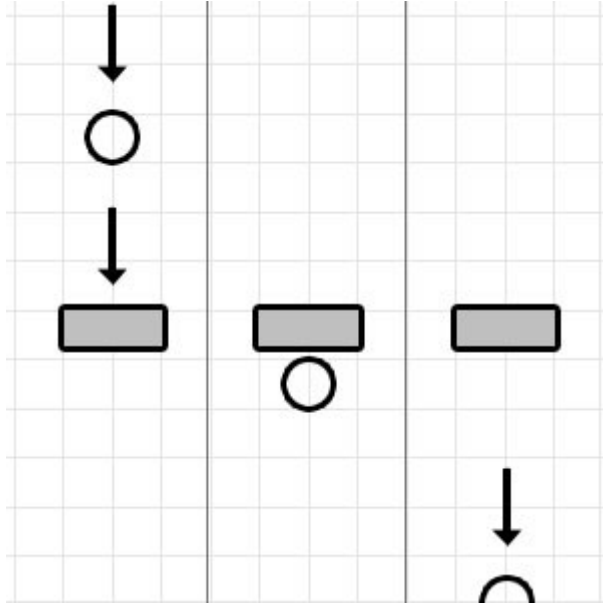


Animated Objects



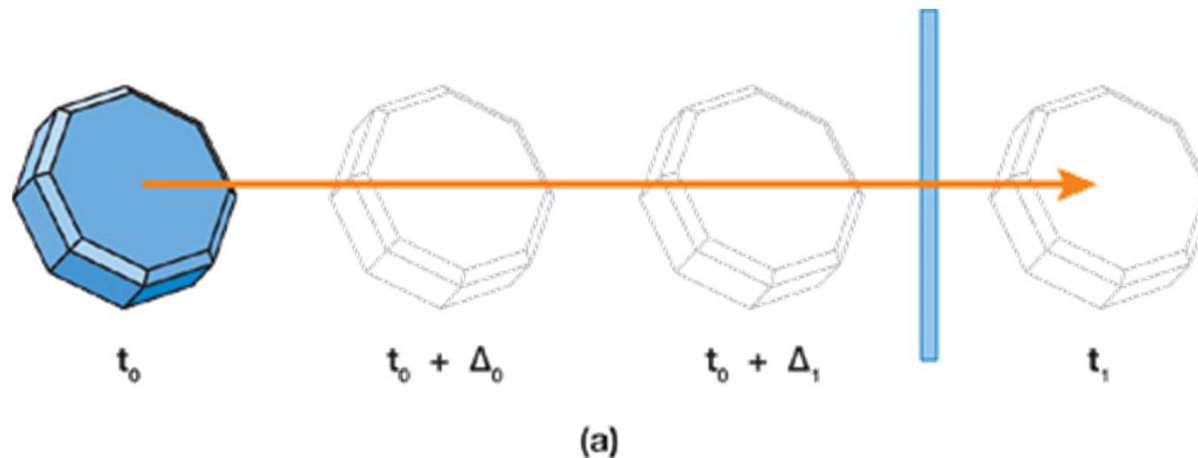
Trouble with Animated Objects





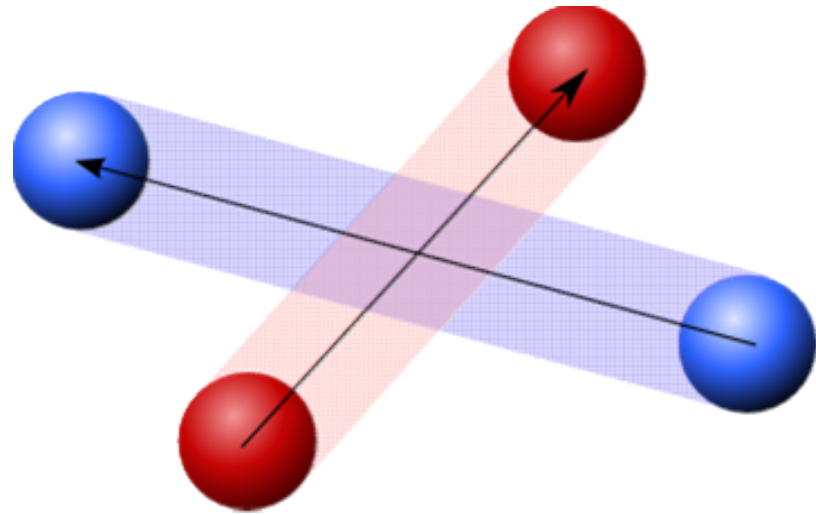
A posteriori (Discrete)

- Advance physics by time step then check for collision
- Simple
 - List of objects \rightarrow return list of intersections
 - No time variable in calculations
 - Miss actual time of collision
- Need to “fix”



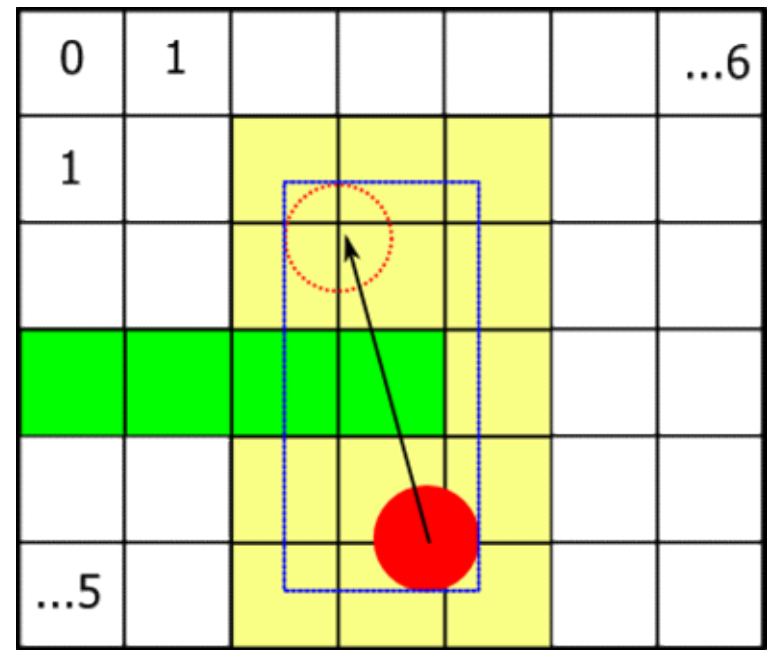
A priori (Continuous)

- A priori (continuous)
 - Predict future movement
 - Trajectories
 - Can be more precise
 - Can be more stable
 - More complex
 - Dimension of time
 - Often no closed form solution (numerical approach)
 - Aware of how objects move
 - Elastic objects (deforming)



Animated Objects - Practical Solutions

- Use extruded geometry
- Use oversized geometry
- ...
- Cast ray(s)
- Evaluate often enough
 - Restrict speed
- Extensive testing
- Some cases will be missed



Independent Render and Game Loop

- Do update in predefined intervals
- Independent from rendering loop
 - Slow rendering does not impact update cycle