

Blockchains & Distributed Ledgers

Lecture 07

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BFT protocols

1. The Permissioned and Permissionless setting
2. Digital signatures and certificates
3. BFT = Byzantine fault tolerance. A classical BFT protocol for a permissioned ledger
 - a. Graded Consensus
 - b. Binary Consensus

Permissionless Protocols

- Bitcoin and similar PoW-based blockchain protocols provide a **permissionless** setting:
- Anyone can participate in the protocol and receive BTC as rewards by performing the PoW-based mining operation.
- The mechanism of **pouring** currency in the system via proof of work, makes it feasible for anyone (possessing sufficient hashing power) to participate.
- The ledger itself is public, readable and writeable by anyone (the latter assuming one **possesses** bitcoin)

Permissioned Protocols

- Participation is restricted:
- Producing transactions and/or blocks can only be performed after being authorized by the other nodes.
- In their simplest form the set of nodes is **static**: the set of nodes implementing the protocol is fixed and determined at the onset of protocol execution.

Permissioning How-To

- Most straight approach: employ a PKI (=public-key infrastructure).
- Based on digital signatures / authentication protocols.
- **Certificate authorities** can authorize other entities.
- authorization includes a signature from the CA on the entity's public-key, identity information etc.
- Sharing certificate authority information is necessary; (how, where?)

X.509 Certificates

- Internet standard since 1988.
- Hierarchical.
- <http://www.ietf.org/rfc/rfc3280.txt>

Structure of x.509

Version
Serial Number
Algorithm / Parameters
Issuer
Period of Validity: not before date not after date
Subject
Algorithm/ Parameters/ Key
x509v3 extensions
...
<i>Signature</i>

X.509
does not
specify
cryptographic
algorithms

Digital Signatures and Certificates

- A certificate contains a digital signature.
- Recall that cryptographic design of digital signatures involves typically:
- A cryptographic signing operation that acts on a fixed input of a specific type and has a public-verifiability feature.
- A cryptographic hash function that takes arbitrary strings and maps them to the data type suitable for the signing operation.
- Common setting today: SHA2 with RSA or DSA.

Certification considerations

- All computer systems come with preloaded certificates from certificate authorities. This provides a **setup assumption**.
- Certificates need to be revoked in case the corresponding secret keys become exposed or the algorithms used are not safe anymore.
- In a blockchain system, certificate information can be provided as part of the genesis block.

Secure channels and certificates

- Possession of mutually acceptable certificates not only permits authenticated communication (exchanging signed mechanism between two entities) but also allows building a secure channel
- Protocol **TLS 1.3** is used to build such secure channel.
- It relies on cryptographic protocols such as the Diffie Hellman key exchange. It can ensure the confidentiality of the data exchanged.

Static Permissioned Blockchain

- All participants are identified by self-signed certificates in the genesis block.
- The set of participants remains the same throughout the execution.
- This is the simplest form of a PKI / public-key directory.

Permissioning

- Prior to system operation the nodes register their certificates that are included in the genesis block.
- Using such certificates, all the nodes are capable of authenticating each participant and allowing interaction with the shared state in a way that is prescribed by the participants' credentials.

A Centralised Permissioned Ledger

(let's focus on just a "LOG" of Transactions)

- One of participants acts as a server and maintains the LOG.
- Readers and writers to the LOG authenticate with the server and can perform read and write operations.
- Consistency of the LOG is guaranteed assuming the server is trusted.
- Liveness of the LOG is guaranteed assuming the server is trusted and functional.

Bitcoin Permissionless Ledger

- The genesis block contains no certificate information.
- Reading from the LOG is open (anyone can do it without credentials).
- Writing to the LOG can only be done in specific ways (issuing transactions).
- Nodes can obtain valid credentials (accounts) by generating a public and secret-key and either mining a block (which will reward their account with BTC) or buy BTC from another node.
- Once the LOG records their account credit, they can issue transactions.
- In essence: crediting a bitcoin account is creating a certificate that imparts the account holder with certain permissions w.r.t. the ledger.

Distributed Permissioned Ledger

- A number of servers maintain the ledger LOG individually.
- Each share the same genesis block that identifies all participants.
- Assuming a synchronous operation, at each round, Readers and Writers authenticate with the servers and interact with the LOG in a prescribed fashion.

Distributed Permissioned Ledger, II

- Readers authenticate to each server and obtain Read access.
- Writers authenticate to each server and provide their inputs.
- Servers run a **consensus protocol** to agree what inputs should be included in the LOG.

Reader/Writer Management

- Readers and Writers can authenticate to each server referring to the information in the genesis block.
- It is possible to introduce additional readers and writers by suitably issuing certificates to other users.
- Note that each participant would then need to show a valid certificate chain that establishes her privileges for the specific read or write access that is requested.

Read Requests

- Is it possible to restrict read requests as in the centralized setting?
- Nodes can maintain blocks of transactions private and issue them only to users that are authenticated.
- The TLS protocol can be used to build a secure channel between the reader and the responding node.
- Note that the above would require that all servers remain honest (as they all share the LOG).

“Classical” BFT Consensus

- Focus on write requests next. We want to ensure LOG liveness and consistency.
- We will build a “byzantine fault tolerant” (BFT) agreement protocol that uses two important tools:
 - a graded broadcast.
 - a binary consensus protocol.

Graded Consensus

- Parties involved : a single sender and several receivers.
 - The i -th receiver outputs (M_i, G_i) .
 - The value G_i is in $\{0,1,2\}$.
 - If the sender is honest then $M_i=M_j$ for all i,j and $G_i=2$.
 - If the sender is malicious and one receiver outputs $(M,2)$ then other honest receivers output (M, G_i) with $G_i \geq 1$.

Graded Broadcast Protocol, 1

- Round 1.** The sender sends the message M to all receivers.
- Round 2.** The i -th receiver obtains $M1i$ from round 1 and sends it to all receivers.
- Round 3.** The i -th receiver obtains $M2ji$ from the j -th receiver in round 2 and performs the following:
 - if there is a single message that was sent by $2n/3$ receivers then send it to all receivers. Else send nothing.

Graded Broadcast Protocol, 2

Output Generation. The i -th receiver obtains M_{3ji} from the j -th receiver in round 3.

- If there is a single message that was sent by more than $2n/3$ receivers output that message as M_i and set $G_i=2$.

- If there is a single message that was sent by more than $n/3$ receivers output that message as M_i and set $G_i=1$.

- In any other case output *fail* and $G_i=0$.

Graded Broadcast Protocol, 3

Analysis. Assume that malicious parties are $t < n/3$.

Observation #1

If the sender is honest, then each receiver will receive the same message $\geq 2n/3$ times in round 2 and 3. All honest receivers will output $G_{i=2}$ and that message.

Graded Broadcast Protocol, 4

Observation #2. If two honest receivers send a message in round 3 it **must be** the *same*.

Proof. Indeed, if they send messages M M' , they both have received them by at least $2n/3$ receivers from round 2.

Given this, observe that $2n/3 - t > n/3$ honest parties have sent M in round 2.

Thus $< n - n/3 = 2n/3$ parties are capable of sending M' (which is different than M), leading to a contradiction.

Graded Broadcast Protocol, 5

Observation #3

Suppose the i -th receiver returns $G_i=2$ and let M_i be the message it chooses. Consider the output of the j -th receiver (M_j, G_j)

The i -th receiver has received the message from at least $2n/3$ receivers in round 3.

=> More than $n/3$ honest receivers have sent M in round 3. Thus it cannot be that $M_j=0$. But it may still be the case that M_j is not equal to M_i

In that case, we deduce that there is another message M' sent by more $n/3$ receivers in round 3, at least one of them is honest; this leads to a

From Graded Broadcast to a BFT-Ledger

A simplistic approach: execute $n/3+1$ phases to guarantee an honest sender will be encountered. In each phase perform:

- A designated sender organizes all valid transactions it collected as **M** and performs a graded broadcast.
- A binary consensus protocol determines whether everyone's grade is 2 or not. If that is true each node signs the output to generate a public endorsement and appends **M** on their LOG (together with the signatures). Otherwise LOG remains the same.

Byzantine Binary Consensus

(RECALL) n parties $(1, 2, \dots, n)$, t adversarial.

Let $v_i \in \{0, 1\}$ be the input of party i .

Honest parties should *decide* on values $u_i \in \{0, 1\}$ satisfying the following properties.

- **Agreement:** if parties i and j are honest, then $u_i = u_j$.
- **Validity:** if there exists $v \in \{0, 1\}$ such that $v_i = v$ for each honest party i , then $u_i = v$ for each honest party i .
- **Termination:** values u_i are well defined for all honest parties.

Exponential Information Gathering Algorithm (EIG)

Algorithm Sketch.

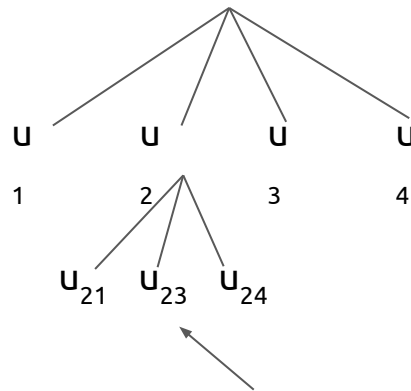
- At round 1, send to everyone your input.
- At round $r+1$, send to everyone all messages you received at round r (avoiding redundant messages).

Each party arranges the messages in its own EIG tree.

- Let u_1, \dots, u_n be the messages received in the first round (including itself)
- Subsequently, u_{xj} is the value received from j as the value u_x in j 's tree.

Note: there need be no repetitions in the label of a node (e.g., x in u_x should contain distinct identifiers).

What is the size of the tree?



The value party 3 told me that party 2 send him in the previous round.

EIG Termination

The EIG algorithm terminates after $t+1$ rounds. The output value of each party is defined as follows.

- For each leaf v in the EIG tree, set $z_v = u_v$.
- For an internal node v , set z_v equal to the majority of the z -values of its children. If the majority is not defined, set $z_v = z_0$, for some default value z_0 .
- Define the output as z_{root} .

Impossibility results I

Theorem[LSP1982] Impossible for $n < 3t + 1$.

Theorem[FL1982] Impossible in t rounds.

Example The EIG algorithm with $t=1$ needs at least 2 rounds.

1. If a party received a single 1, its output should be 0. (Because the 1 could be coming from the adversary.)
2. If a party received two 1s, its output should be 0. (Because one of them could have been sent from the adversary, while another party received a single 1 and will decide on 0 according to the previous statement.)
3. And so on... (by induction, the output will always be 0, contradicting validity)

Theorem[GM1998] Doable for $n > 3t$ in $t+1$ rounds.

Impossibility results II

Theorem[BT1985] Asynchronous Byzantine Consensus is impossible with $n < 3t + 1$, even if the parties have agreed on a PKI.

Proof Partition parties into sets A, B, C of size at most t . Consider 3 scenarios.

- A. A malicious, B and C honest with inputs 0. The adversary sends no messages. The honest parties should decide on 0 until some time T_A .
- B. B malicious, A and C honest with inputs 1. The adversary sends no messages. The honest parties should decide on 1 until some time T_B .
- C. C malicious, B and A honest with inputs 0 and 1 respectively. The adversary communicates with B as the honest C in scenario A and with A as the honest C in scenario B. At the same time every communication between A and B is delayed for time at least $\max\{T_A, T_B\}$.

The crux is that A has the same view in scenarios B and C. Similarly for B, in scenarios A and C. Agreement in scenario C is impossible, if validity is achieved in scenarios A and B.

A blockchain related to proof-of-stake

Servers S_1, \dots, S_n with shared verification keys pk_1, \dots, pk_n and private signing keys sk_1, \dots, sk_n .

B_0 : Genesis block containing the public info.

$B_i = (k, d, sl, \sigma_{sl}, \sigma_{block})$, where

k : hash of previous block

d : data

sl : slot number

σ_{sl} : signature on sl by $S_{sl \bmod n}$

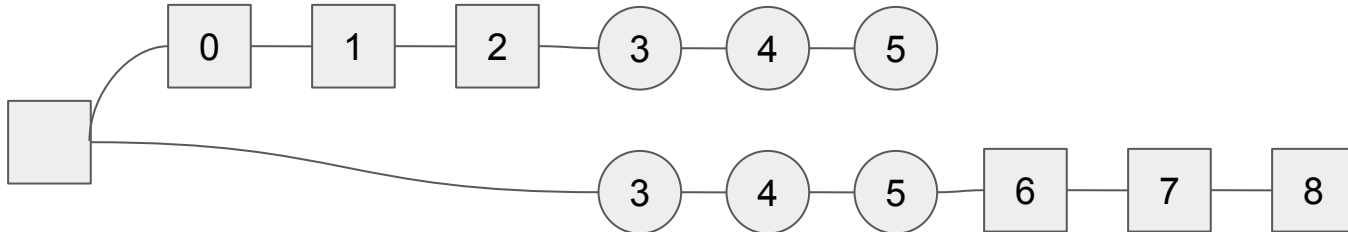
σ_{block} : signature on whole block by $S_{sl \bmod n}$

At any step, each server,
extends the longest
known blockchain

Characteristic sequences and executions

The characteristic sequence of an execution with L slots $0, 1, \dots, L-1$ is a binary string w in $\{0, 1\}^L$ such that $w_i = 1$ iff $S_{i \bmod n}$ is adversarial.

Example $w = 000111000$. Squares denote honest slots (including the genesis) and circles the adversarial ones. The adversary keeps the chain ending with slot 5 on top hidden so that S_6 extends the bottom chain. This results in a **fork**, two disjoint chains (except for the genesis block) of maximum length. The corresponding characteristic sequence w is called **forkable**.



Forkable sequences

Fact If $\text{weight}(w) < \text{length}(w)/3$, then w is not forkable.

Proof Let $n = \text{length}(w)$ and $t = \text{weight}(w)$ and assume w is forkable. The two chains must have length at least $n-t$ (prove formally by induction). Thus, $2(n-t)$ is a lower bound on the sum of their lengths. On the other hand, the $n-t$ honest parties have contributed at most $n-t$, while the adversarial parties have contributed at most $2t$ (because a given chain contains a slot at most once). Thus, $(n-t) + 2t$ is an upper bound on the sum of their lengths. We have

$$2(n-t) \leq (n-t) + 2t \implies n \leq 3t.$$

Consensus inspired from proof-of-stake [KR2018]

- Fix an arbitrary ordering of the servers: S_1, \dots, S_n .
- Construct a blockchain for $5t+2$ rounds, recording your own input bit as data in any block you create.
- Upon termination output the majority of the first $2t+1$ blocks of your chain.

Theorem If $n > 3t$, the protocol satisfies agreement and validity.

Proof [KR2018] It can be shown that the first $2t+1$ blocks are common to all honest parties; this implies agreement. Validity follows from the fact that among the first $2t+1$ at most t are adversarial and so the majority of them belong to honest parties.

Bitcoin Consensus

- Miners run the Bitcoin protocol recording their own input bit as data in any block they compute.
- When their chain has at least $2k$ blocks (for some security parameter k), the broadcast it and stop.
- Output is the majority of the bits recorded in the first k blocks.

Theorem [GKL15] If $t < n/3$, the above protocol satisfies Agreement and Validity with probability $1 - e^{-\Omega(k)}$.

Remark For Agreement, $t < n/2$ suffices.

Common-Prefix Property and Agreement

Common-Prefix Property For any pair of honest parties adopting the chains C_1 and C_2 at rounds r_1 and r_2 respectively. If $r_1 \leq r_2$, then $C_1[-k]$ is a prefix of C_2 , where $C_1[-k]$ is C_1 without its last k blocks.

Common-Prefix Property implies Agreement. This is because the parties are pruning at least k blocks from their chains when keeping only their initial k blocks. Thus, the initial k blocks are common to all honest parties.

In [GKL2015] it is shown that in Bitcoin the Common-Prefix fails with probability exponentially small in k , if the adversary's hashing power is sufficiently bounded below $\frac{1}{2}$. It follows that Agreement is satisfied with probability $1 - e^{-\Omega(k)}$, when t is sufficiently less than $n/2$.

Chain-Quality Property and Validity

Chain-Quality Property (informal) Among any sufficiently large number of consecutive blocks in an honest party's chain, a fraction of at least $(n-2t)/(n-t)$ have been computed by honest parties.

Chain-Quality implies Validity, when t is sufficiently less than $n/3$. This is because, in that case, the majority of the first k blocks have been computed by honest parties. Thus, if all honest parties have input v , the majority of values recorded in the first k blocks will be v .

In [GKL2015] it is shown that in Bitcoin Chain-Quality fails with probability exponentially small in k , if the adversary's hashing power is sufficiently bounded below $1/2$. It follows that Validity is satisfied with probability $1 - e^{-\Omega(k)}$, when t is sufficiently less than $n/3$.

References

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