

Machine Learning

Homework 2 -

Backpropagation

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Problem #1: Sklearn

- You will study the API function for NN in sklearn
 - sklearn.neural_network.MLPRegressor
- Apply NN on the previous dataset: data2_200x30.csv
- Find a good network that has low validation error

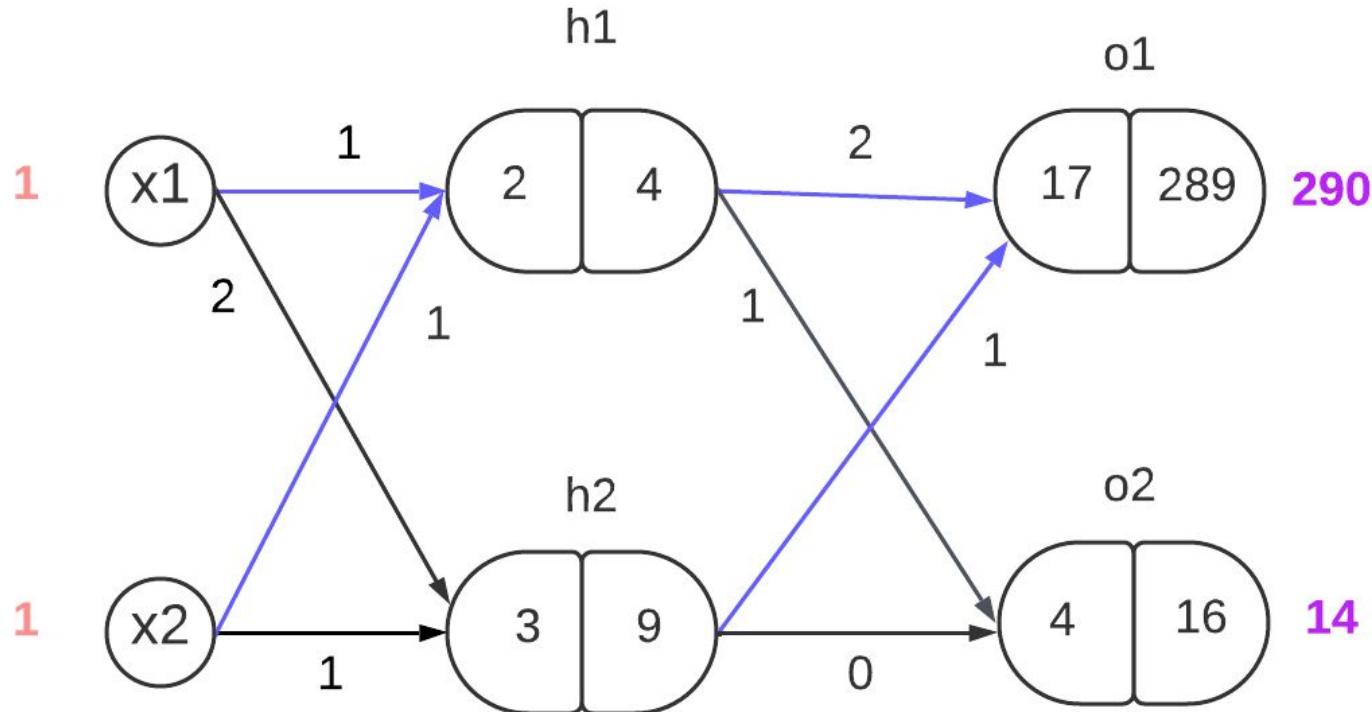
```
if __name__ == '__main__':
    parser = argparse.ArgumentParser(description='Regressors Homework')

    parser.add_argument('--dataset', type=str, default='data2_200x30.csv')
    parser.add_argument('--preprocessing', type=int, default=1,
                        help='0 for no processing, 1 for min/max scaling and 2 for standrizing')
```

Problem #2: Backpropagation

- In this homework, we would like to implement a neural network
- Specifically, we would like to do a single backpropagation step
 - Then training is just to keep repeating it
- We will focus only with 3 layers nn: input, hidden, output. **No bias**
- Implement the network and validate it using the lecture example
 - Then extend it to also allow sigmoid activation function
 - Use activation on all nodes, as we did in the lecture example
- We will feed a specific input/weights/outputs to compare and judge correctness
- The project requires project building skills
 - And also preferred OOP skills

Review by paper and pencil



One way

- This is just one way suggested for you
- Create the following classes
- **NeuralNetwork, NeuronLayer, Neuron**
 - NeuralNetwork class has 2 NeuronLayers: hidden and output
 - Each layer has its Neuron nodes
 - Each neuron is connected with weights to the previous layer
 - Matrices are usually backward: from a layer to previous one
 - E.g. if input is 5 values and hidden is 10, then the weight matrix is 10x5 NOT 5x10

Classes Methods

- **NeuralNetwork**
 - feed_forward
 - compute_delta (for output and hidden)
 - update_weights (for output and hidden)
 - **train_step**: it just calls the previous 3 methods
- **NeuronLayer**
 - feed_forward over its nodes
- **Neuron**
 - compute activation: supports {polynomial, sigmoid and identity}
 - compute activation derivative
 - Calc_net_out: compute the input net and apply activation ont

```
def poly():      # 2 x 2 x 2
    hidden_layer_weights = np.array([[1, 1],
                                     [2, 1]])
    output_layer_weights = np.array([[2, 1],
                                     [1, 0]])

    nn = NeuralNetwork(hidden_layer_weights, output_layer_weights, 'poly')

    nn.train_step([1, 1], [290, 14])
```

```
network output: [289, 16]
Delta o[0]: -34.0
Delta o[1]: 16.0
Delta h[0]: -208.0
Delta h[1]: -204.0
node o: 0 - w_ho: 0: Delata -136.0 => new w = 70.0
node o: 0 - w_ho: 1: Delata -306.0 => new w = 154.0
node o: 1 - w_ho: 0: Delata 64.0 => new w = -31.0
node o: 1 - w_ho: 1: Delata 144.0 => new w = -72.0
node h: 0 - w_ih: 0: Delata -208.0 => new w = 105.0
node h: 0 - w_ih: 1: Delata -208.0 => new w = 105.0
node h: 1 - w_ih: 0: Delata -204.0 => new w = 104.0
node h: 1 - w_ih: 1: Delata -204.0 => new w = 103.0
```

```
def sigm():      # 2 4 3
    hidden_layer_weights = np.array([[0.1, 0.1],           # 4x2 NOT 2x4
                                      [0.2, 0.1],
                                      [0.1, 0.3],
                                      [0.5, 0.01]]))

    output_layer_weights = np.array([[0.1, 0.2, 0.1, 0.2],
                                     [0.1, 0.1, 0.1, 0.5],
                                     [0.1, 0.4, 0.3, 0.2]])

nn = NeuralNetwork(hidden_layer_weights, output_layer_weights, 'sigmoid')

nn.train_step([1, 2], [0.4, 0.7, 0.6])
```

```
network output: [0.5913212667539777, 0.6219200057374265, 0.6508562785102494]
Delta o[0]: 0.04623477887224621
Delta o[1]: -0.01835937944358026
Delta o[2]: 0.011556701931083076
Delta h[0]: 0.000963950492482261
Delta h[1]: 0.0028912254002713203
Delta h[2]: 0.001386714367431997
Delta h[3]: 0.000556197739142091
node o: 0 - w_ho: 0: Delata 0.026559222739603632 => new w = 0.0867203886301982
node o: 0 - w_ho: 1: Delata 0.027680191578841717 => new w = 0.18615990421057915
node o: 0 - w_ho: 2: Delata 0.030893513891333994 => new w = 0.08455324305433301
node o: 0 - w_ho: 3: Delata 0.028996038295713737 => new w = 0.18550198085214314
node o: 1 - w_ho: 0: Delata -0.010546408134670482 => new w = 0.10527320406733524
node o: 1 - w_ho: 1: Delata -0.010991533920193718 => new w = 0.10549576696009687
node o: 1 - w_ho: 2: Delata -0.01226751284879592 => new w = 0.10613375642439797
node o: 1 - w_ho: 3: Delata -0.01151404380893776 => new w = 0.5057570219044689
node o: 2 - w_ho: 0: Delata 0.006638660943333523 => new w = 0.09668066952833325
node o: 2 - w_ho: 1: Delata 0.006918854837737182 => new w = 0.39654057258113146
node o: 2 - w_ho: 2: Delata 0.007722046916941944 => new w = 0.29613897654152904
node o: 2 - w_ho: 3: Delata 0.007247759802026145 => new w = 0.19637612009898694
```

Code Namings

- You may use good variables **naming** that match the rules
- dE_dO_{net} for $\partial E / \partial o_{\text{net}}$
- dE_dO_{out} for $\partial E / \partial o_{\text{out}}$
- dE_dH_{net} for $\partial E / \partial h_{\text{net}}$
- dE_dH_{out} for $\partial E / \partial h_{\text{out}}$
- $d_{\text{net}}_d_{\text{out}}$ for $\partial o_{\text{net}} / \partial o_{\text{out}}$ and $\partial h_{\text{net}} / \partial h_{\text{out}}$
- $d_{\text{out}}_d_{\text{net}}$ for $\partial o_{\text{out}} / \partial o_{\text{net}}$ and $\partial h_{\text{out}} / \partial h_{\text{net}}$
- dE_dW for $\partial E / \partial w$

Problem #3: Derivatives

- Compute the **derivative** of the following functions:
 - Sigmoid
 - Tanh
 - Reul
 - See [here](#) or google
- Show that $\tanh(\text{net}) = 2 \times \text{sigmoid}(2 \times \text{net}) - 1$

“Acquire knowledge and impart it to the people.”

“Seek knowledge from the Cradle to the Grave.”

