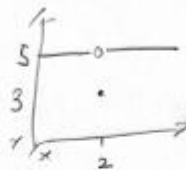


20223100 4월 15

1. $\frac{2}{p}$



2.

(a) $f(x)$ 은 -3 에서 양쪽으로
발산한다

(b) $f(x)$ 은 4 의 무극한에서
 $\frac{0}{0}$ 의 무극한으로 발산한다

3.

(a) 2 (b) 1

(c) 4 (d) 좌극한 \neq 우극한

(e) 3

4.

(a) 4 (b) 5 (c) 2

(d) 4

5.

(a) -4 (b) 4 (c) 4

(d) -4 (e) 4 (f) $x=1$

6.

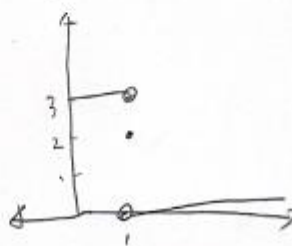
$a=0$

7.

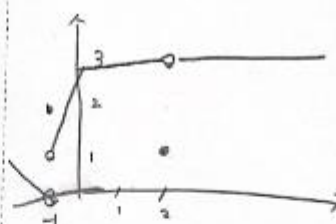
(a) $-\infty$ (b) ∞

(c) x 좌극한 \neq 우극한

8.



9.



10.

$$\lim_{x \rightarrow 3} \frac{(x-3)x}{(x-3)(x+3)} = \frac{1}{2}$$

11.

$$\frac{1 \cdot 1}{1+1} = \frac{1}{2}$$

12. $\frac{3}{2}$

13. 1

14.

양의 무한대

15

양의 무한대

16

음의 무한대

17.

$\frac{1}{x \cdot \cos x}$ 양의 무한대

$-\frac{18}{x(x+2)}$ 양의 무한대

19

$-x = -2$

20

$\ln \frac{1}{(x+1)(x^2+1)}$

1와 무한대



21

$1 - \frac{1}{500}, \frac{16}{25}, \dots$ (0)

20223100 상준 16

1.

a.

-6

b.

-8

6. 2

(d) -6

(e) $\frac{9}{2} \neq 0$

(f) 0

2.

$\lim_{x \rightarrow 5} x^2 - 5x = 75$

3. $8 \times 11 = 88$

4. 5

5.

$-\frac{3}{9}$

-3^{-3}

6. -13

7. 6

8. x.

9. $\frac{(x-3)(x+2)}{(3x-1)(x+2)}$

10

$\frac{(t^2-3)(3t+1)}{(t-2)(t+3)}$

(6)

$\frac{1}{6}$

11.

$\frac{5}{7}$

(-1)

12.

$$\frac{1}{h(\sqrt{4h+3})} \quad \frac{1}{6}$$

13

$$\left(\frac{3-x}{x^2} \times \frac{1}{x-3} \right) \quad \left(-\frac{1}{9} \right)$$

14.

$$\frac{2}{\sqrt{4t} + \sqrt{1-t}} \quad 1$$

15

$$\frac{(6-x)}{(x-2)x} \times \frac{1}{4\sqrt{x}} \quad \left(\frac{1}{128} \right)$$

16

$$\frac{1-\sqrt{1+t}}{t(\sqrt{1+t})} \quad \frac{-1}{t(\sqrt{1+t})(1+\sqrt{1+t})} \quad -\frac{1}{2}$$

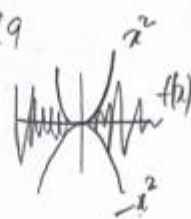
17

$$\frac{3x^3h + 3xh^2 + h^3}{h} \quad (3x^2)$$

18

$$\frac{1}{3} \times (\sqrt{43x+1}) \quad \left(\frac{2}{3} \right)$$

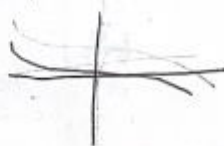
19



20

$$\eta \leq \lim_{x \rightarrow 0} f(x) \leq \eta \quad (\eta)$$

21



22.

8

23

$$\frac{2x-1}{x^2 \times (2x-1)} \quad \frac{0}{1} \neq \frac{2}{1} \neq \frac{2}{1}$$

24

$$\lim_{x \rightarrow 0} \frac{||x|-x|}{x|x|} \quad \frac{-2x}{x^2} \quad \frac{0}{0} \text{ is an indeterminate form}$$

25

$$\begin{array}{c} \text{---} \text{---} \text{---} \\ \text{---} \text{---} \text{---} \end{array} \quad \begin{array}{c} (i) \text{---} (ii) \text{---} \\ (iii) \times (iv) \text{---} \end{array}$$

26.

$$g(x) = \frac{f(x+3)(x-2)}{|x-2|}$$

(u)
(i) 5 (ii) -5

(b) x



27.

$$C=7$$

28

(i) -2 (ii) -2

(iii) -2

(b)

(i) n-1 (ii) n+1

(c) $a \neq n$ ($n \in \mathbb{Z}$)

29 $\lim_{x \rightarrow \infty} [f(x)]$ or $\lim_{x \rightarrow \infty} \frac{3x^2+5x+18}{x^2+2x-2}$

30

31. 8

32



33

$$\lim_{x \rightarrow a^+} f(x) = 1 \quad \lim_{x \rightarrow a^-} f(x) = 0$$

$$\lim_{x \rightarrow a^+} g(x) = 0 \quad \lim_{x \rightarrow a^-} g(x) = 1$$

34

$$12-a \quad a=15$$

$$\lim_{x \rightarrow 2} \frac{3x^2+5x+18}{x^2+2x-2} = \frac{(x+2)(3x+9)}{(x+2)(x-1)}$$

$$\frac{3}{-1} = -3$$

(-1)

13.

(n)

$$\ln \frac{1}{743}$$

$$f(3) = \frac{1}{6}$$

14

$$x = 2\pi \frac{1}{2}$$

15

$$\frac{\cos(t)}{(t+1)(1-t)}$$

16

$$221x$$

17

v

18

8

19

$$\frac{\pi^2}{16} \cdot 1 = \frac{\pi^2}{16}$$

20

$$g_1(n) > 1 \quad n = \frac{\pi}{2} + 2n\pi$$

21

$$f(1) = \lim_{x \rightarrow 1} f(x)$$

22

$$f(x) \quad x=1 \text{에 } 10^{\frac{1}{2}}$$

23



24

$$4c+4=8-2c \quad \frac{2}{3}$$

25

$$3a + 6a = 36 \quad (4)$$

26

$$g(x) = (x+1) \cdot 4 \quad 7$$

$$g(x) = 3(x+1)^{11} \quad 6$$

$$g(x) = 5 \ln x$$

27

$$c^2 + 1051c = 1000$$

$$x^2 \text{은 양의 무한대로 갈수록 } 510x \text{는 } 525$$

13.

(n)

$$\ln \frac{1}{743}$$

$$f(3) = \frac{1}{6}$$

14

$$x = 2\pi \frac{1}{2}$$

15

$$\frac{\cos(t)}{(t+1)(1-t)}$$

16

$$221x$$

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27

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$$x^2 \text{은 양의 무한대로 갈수록 } 510x \text{ 525}$$

28

$$1 - 4 + 1 = -2$$

$$-2 < f(x) < 0$$

$$-1 < x < 0$$

29

$$f(x) = \cos x - x = 0$$

$$x=0 \quad f(x)=1$$

$$f(x) \quad f(1) = -1$$

$$1 < f(x) < -1$$

30

?

31

$$a < x < b$$

$$f(a) < f(x) < f(b)$$

$$f(a) f(b) < 0$$

$$a=0 \quad b=2$$

$$-4 < f(x) < 24$$

32

sin

?

33

$$\lim_{h \rightarrow 0^-} f(a+h) = \lim_{x \rightarrow a^-} f(x)$$

$$\lim_{h \rightarrow 0^+} f(a+h) = \lim_{x \rightarrow a^+} f(x)$$

$$= f(a)$$

34

$$\cos x$$

$$\lim_{x \rightarrow \pi^+} \cos x = \lim_{x \rightarrow \pi^-} \cos x = \cos \pi$$

(102, 116)

$$7 \leq 1/2 \leq 6 \leq 6$$

35

$$7/8 \leq 8 \leq 8$$

36

$$f(x) = \frac{x}{x}$$

37

$$\lim_{x \rightarrow 0} f(x) x^3 \sin\left(\frac{1}{x}\right) = \lim_{x \rightarrow 0} x^3$$

$$= 0$$

38

$$f(1) = 0 \quad f(19) = a$$

$$g(1) = a \quad g(19) = 0$$

$$f(1) \leq g(19) \leq f(19)$$

20223100 1/2 2, 4

1. $3\cos x + 2\sin x$

2. $\frac{dt}{dx} = 2x - \csc^2 x$

3. $2\theta \sin \theta + \theta^2 \cos \theta$

4. $\sec x \tan^2 x + \sec^3 x$

5. $\sin + \sin^2 + \theta \cos \theta - \cos^2 \theta$

6. $2 \sin t \cos t$

7. $\frac{\sin - \sec}{\sin^2} \quad \frac{1}{5} - \cot \tan$

8. $\frac{2 - \tan x + x \sec^2 x}{(2 - \tan x)^2} \quad \begin{matrix} -\operatorname{cosec} \theta \cot \theta \\ -\operatorname{cosec}^2 \theta \end{matrix}$

9. $\frac{-2 \sec^2 \tan x}{(1 - \sec w)^2} \quad (1 - \sec w)$

10. $\frac{(\sin t + \cos t)(1+t) + t \sin t}{(1+t)^2}$

11. $\cos \theta \sin \theta - \theta \sin^2 \theta + \theta \cos^2 \theta$

12

$$\left(\frac{1}{\sin x} \right)' = -\frac{\cos x}{\sin^2 x}$$

13

$$\left(\frac{\cos x}{\sin x} \right)' = -\frac{\cos^2 x}{\sin^2 x} = -\frac{\sin^2 x}{\sin^2 x}$$

$$= -\cot^2 x - 1$$

$$= -\csc^2 x$$

14

$$\cos x - \sin x$$

$$y = x + 1$$

15

$$1 + \sec x$$

$$y = 2(x - \pi) + \pi$$

$$y = 2x - \pi$$

16

$$(2 + 2x \cos x)$$

$$\theta = 2\left(x - \frac{\pi}{2}\right) + \pi$$



17

$$\lim_{x \rightarrow 0} \sec x \tan x - 1$$



18

$$g(\theta) = \frac{\theta \cos \theta - \sin \theta}{\theta^2}$$

$$g'(\theta) = \left(\frac{\cos \theta}{\theta} - \frac{\sin \theta}{\theta^2} \right)'$$

$$= \frac{-\theta \sin \theta + \cos \theta}{\theta^2} - \frac{\theta^2 \cos \theta - 2\theta \sin \theta}{\theta^4}$$

$$= -\frac{\sin \theta}{\theta} + \frac{\cos \theta}{\theta^2} - \frac{\cos \theta}{\theta^2} + \frac{2 \sin \theta}{\theta^3}$$

$$= -\frac{\sin \theta}{\theta} + \frac{2 \sin \theta}{\theta^3}$$

19

$$\frac{\sec^2 x \sec x - (\tan x - 1) \sec x \tan x}{(\sec x)^2}$$

$$= \frac{\sec^3 x - \sec x \tan^2 x + \sec x \tan x}{\sec^2 x}$$

$$= \sec x - \sin^2 x \cos x + \sin x$$

20

$$f'(a) = 0 \text{ or } 1/2 \text{ is } a$$

$$1 + 2 \cos x = 0 \quad \cos x = -\frac{1}{2}$$

$$\frac{2\pi}{3}, \frac{4\pi}{3}, \frac{8\pi}{3}, \frac{10\pi}{3}, \frac{14\pi}{3}, \dots$$

$$\frac{2\pi}{3}, \frac{4\pi}{3}, \dots$$

21

$$\frac{1}{5} : 8 \cos t$$

$$2t : -8 \sin t$$

(c)

$$4\sqrt{3}, 4, -4\sqrt{3}$$

$$0 \leq t \leq \frac{\pi}{2}$$

22



$$\lim_{h \rightarrow 0} \frac{f(h + \frac{\pi}{2}) - f(\frac{\pi}{2})}{h} =$$

23

$$\frac{5}{3}$$

24

$$3$$

25

$$\frac{5(1 - \cos x)}{x^2} = \frac{5}{x} \times \frac{1 - \cos x}{x} = 1$$

26

$$2$$

27

$$\left(-\frac{3}{4}\right) \frac{\sin 3x}{3x} \times \frac{3x}{x^3+1}$$

28

$$\frac{\sin \theta}{\theta} \times \frac{\theta}{\theta + \tan \theta} = 1 \times \frac{1}{1 + \frac{\tan \theta}{\theta}} = \frac{1}{2}$$

29

$$-\frac{1}{2}$$

30

$$\frac{\cos x - \sin x}{(\sin x + \cos x) \cos x} = -\frac{1}{\cos x}$$

$$= -\sqrt{2}$$

31

$$\sin x \rightarrow \cos x \rightarrow -\sin x$$

$$-\cos x \rightarrow \sin x$$

$$\text{4th Der } \sin x \rightarrow \sin x$$

32

$$y'' = -A \sin x - B \cos x \quad A=3B$$

$$y' = A \cos x - B \sin x \quad -3A - B = 1$$

$$-2A \sin x - 2B$$

$$(-3A-B) \sin x + (A-3B)$$

$$A = -\frac{3}{10}$$

$$B = -\frac{1}{10}$$

33

(a)

$$\sec^2 x = \frac{1 + \tan^2 x}{\cos^2 x} = 4$$

(b)

$$\sec x \tan x = \frac{\sin x}{\cos^2 x}$$

(c)

$$\cos x - \sin x = \frac{-\csc^2 x + \csc x + \csc x \cot^2 x}{(\csc x)^2}$$

(34

$$d = 2\theta \times \sin\left(\frac{\theta}{2}\right)$$

$$s = 2\theta$$

$$\ln \frac{\theta}{2 \sin \frac{\theta}{2}} = 1$$

2022 360 163 2.5

1.

$$y = 3x(-4x^3)(5-x^4)^2$$

2. $-\sin x \times \cos(\cos x)$

3. $\frac{1}{2} \times \cos x \times (\sin x)^{-\frac{1}{2}}$

4.

$$4(6x^2 - 10x)(2x^3 - 9x^2 + 4)^4$$

5.

$$5x^{\frac{1}{2}} \times (5x+1)^{-\frac{1}{2}}$$

6.

$$\frac{-2x2(2t+1)}{(2t+1)^4}$$

7.

$$\frac{-2 \times (-\sin t + \sec^2 x)(\cos t + \tan x)}{(\cos t + \tan)^4}$$

8.

$$2\theta \times (-\sin \theta^2)$$

9.

$$\frac{2}{3} \sqrt{1+v^2} + v \times \frac{1}{2} \times 2v \times (1+v^2)^{-\frac{2}{3}}$$

10

$$3 \times 4(4x+5)^2(x^2-2x+5)^4 + 4 \times (2x-2)(4x+5)^3(x^2-2x+5)^3$$

11

$$\frac{2}{3} \times (t+1)^{-\frac{1}{3}} \times (2t^2-1)^3 + (t+1)^{\frac{2}{3}} \times 3 \times 4t(2t^2-1)$$

12

$$\frac{1}{2} \times \frac{(x+1)^{-x}}{(x+1)^2} \times \left(\frac{x}{x+1}\right)^{-\frac{1}{2}}$$

13

$$8 \times \frac{3u^2(u^3+1) - 3u^2(u^3-1)}{(u^3+1)^2} \times \left(\frac{u^3-1}{u^3+1}\right)^7$$

14

$$\frac{3 \times 28(8^2-1)^2 \times (28+1)^5 - 10(8^2-1)(28+1)^4}{(28+1)^{10}}$$

15

$$-4 \times \sec 4x \tan x \times \sin(\sec^4 x)$$

16

$$\sqrt{\frac{c^2}{1+s}} = \sqrt{1+s} = \frac{1}{2} \times \cos x \times (1+s)^{\frac{1}{2}}$$

17

$$\frac{2\sin 2x (1 + \cos 2x) + 2\sin 2x (1 - \cos 2x)}{(1 + \cos 2x)^2} \times 4x \left(\frac{1 - \cos 2x}{1 + \cos 2x} \right)^3$$

18

$$\cos x \times \cos(1 - x^2) \\ - \sin x \times 2x \times \sin(1 - x^2)$$

19

$$\frac{1}{2} x 2t x (1 + t^2)^{-\frac{1}{2}} \times \sec^2 \sqrt{1 + t^2}$$

20

$$2x \times 2x \sin(x^2 + 1) \cos(x^2 + 1)$$

21

$$-3 \sin^2 \cos x \times 4 \cos^3 \sin(\sin^3 x)$$

22

$$\sec^2(\sec(\cos t)) \times \sec(\cos t) \\ \tan(\cos t) \times -\sin t$$

23

$$2\theta^2 p [2\theta \sin \theta x + n]^{p-1} \cos \theta x$$

24

?

25

$$1711: 3 \times \cos 3\theta \times -\sin(\sin 3\theta)$$

2711

$$+ \sin 3\theta \times \sin(\sin 3\theta) \\ + \cos^2 3\theta \times \sin(\sin 3\theta)$$

26

$$\frac{1}{2} x - \sin x \times (\cos)^{-\frac{1}{2}} \\ + \frac{1}{4} x \sin^2 x (\cos)^{-\frac{3}{2}} - \frac{1}{2} \cos^{\frac{1}{2}} \cos$$

27

$$-6 \times 3 \times (3x+1)^{-7}$$

$$y = 18x + 1$$

28

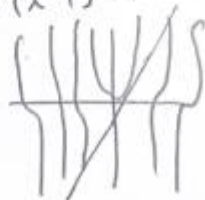
$$\cos x \times \cos(\sin x)$$

$$y = -x + \pi$$

29

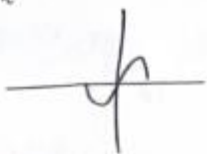
$$\frac{\pi}{2} x \times \sec\left(\frac{\pi}{6} x^2\right)$$

$$\frac{\sqrt{2}}{2} \pi (x+1) + 1$$



30

$$\sqrt{2x^2} \rightarrow x^2 \sqrt{2x^2}^{-\frac{1}{2}}$$



31

$$g=3 \quad g=-1$$



32

$$f'(x) = g'(x) \times f'(g(x))$$

$$6 \times 4 = 24$$

33

$$f'(x) \times g'(f(x)) \quad 4 \times 2 = 8$$

$$g'(x) \times f'(g(x)) \quad 6 \times 5 = 30$$

34

$$g'(x) \times f'(g(x)) \quad -1 \times \frac{1}{3} = -\frac{1}{3}$$

$$f'(x) \times g'(f(x)) \quad 2x - 1 = -2$$

$$g'(x) \times g'(g(x)) \quad -1 \times \frac{1}{2}$$

35

$$\frac{1}{2} \times f'(x) \times f(x)^{-\frac{1}{2}}$$

$$-\frac{3}{2} \times \frac{1}{2} \times \sqrt{2} = -\frac{3\sqrt{2}}{8}$$

36

f'

$$3f(4f(x)) = 1(x)$$

$$\frac{g'(x) \times f'(g(x))}{\downarrow}$$

$$\frac{4f'(x) \times 3f'(4f(x)) \times f'(3f(4f(x)))}{8 \quad 6 \quad 2}$$

$$96$$

37

$$\frac{g(h(x))' \times f'(g(h(x)))}{\downarrow}$$

$$h'(x) \times g'(h(x)) \times f'(g(h(x)))$$

$$4 \times 5 \times 6 = 120$$

38

$$\cos 2x \rightarrow -2 \sin 2x \rightarrow -4 \cos 2x$$

$$\rightarrow 8 \sin 2x \rightarrow$$

$$2^n <$$

$$2^{103} \times \cos 2x$$

39.

$$\frac{1}{6} \times 10\pi \sqrt{\cos(10\pi t)}$$

40

$$\frac{\pi}{20} \times \frac{10}{2\pi} \times \cos\left(\frac{10}{2\pi} \pi t\right)$$

$$\frac{\pi}{54} \times \cos \frac{10}{2\pi} \pi$$

41

$$s'(t) = v(t) \Rightarrow \frac{ds}{dt} = \frac{4}{5} t$$

$$v'(t) = a(t)$$

$$\frac{dv}{dt} \Rightarrow \text{가속도의 변화량} \left(\frac{4}{5} t\right)$$

$$\frac{ds}{dt} \Rightarrow \text{속도의 변화량} \left(\frac{4}{5} t\right)$$

42

$$f(-x) = f(x)$$

$$-f(-x) = -f(x)$$

43

?

44

$$y = F(x) = f(g(h(x)))$$

$$h' = g'(h(x)) \quad j' = h'(x)$$

$$\frac{dy}{dx} = \frac{dy}{dz} \times \frac{dz}{dj} \times \frac{dj}{dx}$$

$$F'(x) = \frac{dx}{dz} + (h'(x)) \times g'(h(x))$$

$$h'(x) \times g'(h(x)) + g'(h(x)) \times h'(x) + (g'(h(x)))$$

20223100 43 2.6

2.

$$\frac{1}{2} x^{-\frac{1}{2}} + \frac{dy}{dx} \cdot \frac{1}{2} x y^{\frac{1}{2}} = 0$$

$$-\frac{\sqrt{x} \sqrt{y}}{2}$$

8

$$\frac{1}{y} \times \sec^2\left(\frac{\pi}{y}\right) = 1 + \frac{dy}{dx}$$

$$\frac{dy}{dx} = \frac{1}{y} \times \sec^2\left(\frac{\pi}{y}\right)$$

12

$$4x^3 y^2 + 2x^4 y \times \frac{dy}{dx} - 3x^2 y - x^3 \times \frac{dy}{dx}$$

$$+ 2y^3 + 6x y \frac{dy}{dx} = 0$$

$$\frac{4x^3 y^2 - 3x^2 y + 2y^3}{x^3 - 2x^2 y - 6x y^2}$$

14

$$\frac{dy}{dx} = \frac{4(x^2 y^2)(2x + \frac{dy}{dx})}{25(2x)}$$

$$\frac{2(25 - 3x - y)}{1 \times (3(1 + 4 + 25))} \times \frac{-4y}{y^2 - \frac{9}{13}(x - y + 1)}$$

16

$$\frac{2}{3x^{\frac{1}{3}}} + \frac{2 \frac{dy}{dx}}{3y^{\frac{1}{3}}} = 0$$

$$\left(\frac{y}{x}\right)^{\frac{1}{3}}$$

$$-\frac{2}{3^{\frac{1}{3}}}(x + y^{\frac{1}{3}}) + 1$$

21

$$y + \frac{dy}{dx} \times x + \frac{dy}{dx} \times 3y^2 = 0$$

$$\left(\frac{-x}{x+3y^2} \right)'$$

0,1

$$\frac{y}{x+3y^2}$$

$$\left(-\frac{1}{3} \right)$$

23

og₂ 27 14,...

31

$$2xy^2 + 2x^2y \frac{dy}{dx} + y + x \frac{dy}{dx} = 0$$

$$- \left(\frac{2xy^2 + y}{2x^2y + x} \right)$$

$$2xy^2 = 2x^2y = x - y$$

$$2xy(y-2) = x-y$$

$$y = x$$

$$\frac{\sqrt{2} \sqrt{x} y}{2,2} = 5$$

33

$$y = m(x+5)$$

$$x^2 + m^2(x+5)^2 = 5$$

$$m = \frac{1}{4}$$

$$(2)$$

20223100 43 2.9

1,

$$x^3 - x^2 + 3 + (3x^2 - 2x)(x+2)$$

$$-9 + 16(x+2)$$

2,

$$x^{\frac{1}{3}} + \frac{1}{3} x^{-\frac{2}{3}} (x-8)$$

$$2 + \frac{1}{12} (x-8)$$

10

$$dy \Rightarrow 90^2 \pi dx$$

$$(b) -0.2$$

16

$$x^4$$

$$a=2$$

$$15.968$$

$$16 + 320 \times 0.001$$

18

$$\pi = 18^\circ \quad 2 = \frac{\pi}{9}$$

$$0+x$$

$$\tan \frac{\pi}{9}$$

19

$$1 + 0(x-0)$$

$$(9)$$