Quartz resonator

SCI-C0200

Joonatan Bergholm 507260 Osama Abuzaid 524832

 $\mathrm{June}\ 1,\ 2016$

CONTENTS CONTENTS

Contents

1	Intr	oduction		2
2	The	ory		3
3	Res	ults		3
\mathbf{A}	Sou	rce code		3
В	Pret	tasks		4
	B.1	Session 1		 4
		B.1.1 Task 1		 4
		B.1.2 Task 2		 4
	B.2	Session 2		 6
		B.2.1 Task 2		 6
		B.2.2 Task 3		 6
		B.2.3 Task 4		 6
	B.3	Session 3		 6
		B.3.1 Task 1		 6
		B.3.2 Task 2		 6
	B.4	Session 4		 6
		B.4.1 Task 1		 6
		B.4.2 Task 2		 6
	B.5	Session 5		 6
		B.5.1 Task 1		 6
		R 5.9 Tagk 9		6

1 | Introduction

In this assignment we investigated electronic properties of one of the most common electronic components, the quartz tuning fork or quartz resonator, like one in figure 1. It is used in watches and other every day electrical appliances to provide a stable clocking frequency. Typically the frequency is $f_0 = 32\,768\,\text{Hz}$, because is is a round number $(32768_{10} = 2^{15}_{10} = 1000000000000000_2)$ in base 2, which is commonly used in electrical appliances.

Contrary to conventional tuning fork, one does not need generate mechanical excitation on the quartz tuning fork, because quartz has piezoelectric properties and thus mechanical excitation can be replaced with electronic one.

2 | Tuning fork

Piezoelectricity is a phenomena, where deformation of a material causes electrical current and vice versa. Crystal oscillators are made of piezoelectric materials, and in electric circuits they are used to produce an electrical signal with precise frequency. The Q-value of crystal oscillator is defined to be the oscillators energy per dissipated energy at one oscillation:

$$Q \equiv 2\pi \frac{E}{\Lambda E}.\tag{1}$$

In our work we are using quartz tuning forks. The fundamental frequency of a tuning fork is given by equation

$$f_0 \approx 0.16 \frac{T}{L^2} \sqrt{\frac{E}{\rho}},\tag{2}$$

where $L=3.98 \mathrm{mm}$ is the length of one quartz bar, $T=0.60 \mathrm{mm}$ the width of the bar, $E=79 \mathrm{GPa}$ the Young modulus and $\rho=2660 \frac{\mathrm{kg}}{\mathrm{m}^3}$ the density of quartz. Also the thickness of fork we are using in our work is $H=0.30 \mathrm{mm}$. Advantage of having two bars instead of one is that the oscillations of two bars at the fulcrum cancel each other, resulting to better Q-value.

We can estimate the Q-value of the tuning fork from figure 2 by using

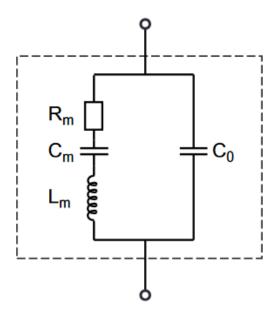


Figure 1: Equivalence circuit of a tuning fork.

equation^[?]

$$t = \frac{f_0}{Q}$$

$$\Rightarrow Q = tf_0 \approx 13000$$

where $t \approx 0.4$ s is the time constant, which tells the time it takes for the resonator to stabilize to the equilibrium amplitude.

An equivalence circuit of tuning fork is an electrical circuit which can't be distinguished from tuning fork in a black box. The components of equivalence circuit in figure ?? are obtained from following equations:

$$\begin{cases}
L_m = \frac{2\rho L^3}{9e_p^2 HT} \\
C_m = \frac{1}{\omega_0^2 L_m} \\
R_m = \frac{\omega_0 L_m}{Q} = \gamma L_m \\
C_0 = \frac{\epsilon_0 \epsilon_r A}{T}
\end{cases} , \tag{3}$$

where $e_p \approx 0.18 \frac{\text{C}}{\text{m}^2}$ is the piezoelectric modulus of tuning fork, ϵ_0 and ϵ_r are the vacuum and relative permittivity, respectively, and A = TL the effective



Figure 2: Quartz resonator

area. Equivalence circuit of our tuning fork would have following components:

$$\begin{cases} L_m \approx 3.3 \cdot 10^{-20} \text{ H} \\ C_m \approx 7.1 \cdot 10^8 \text{ F} \\ R_m \approx 5.3 \cdot 10^{-19} \Omega \\ C_0 \approx 3.5 \cdot 10^{-9} \text{ F} \end{cases}$$

3 | Results

References

[1] https://mycourses.aalto.fi/pluginfile.php/211810/mod_resource/content/1 /projekti_kertaohje4.pdf, "Kvartsiresonaattorin mittaus", accessed 2016.06.01

REFERENCES REFERENCES

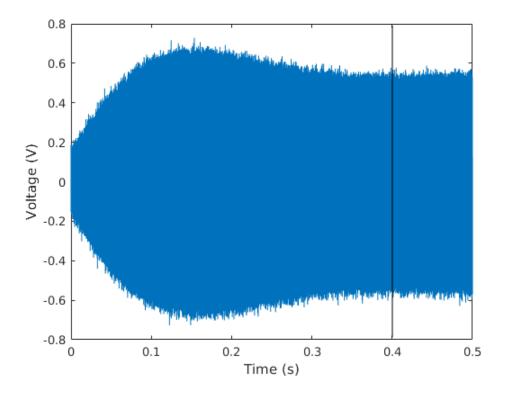


Figure 3: Steady state

A | Source code

```
Listing 1: ac.m
g data = [];
ps data = [];
f data = linspace(32.74e3, 32.752e3, 100);
for f = f data
    [g, ps] = DAQreadout(f);
    g_{data}(end + 1) = g;
    ps_{data}(end + 1) = ps;
    length (ps data)
end
figure
plot(f_data, g_data)
title ('Vahvistus')
figure
plot (f data, ps data)
title ('Vaihe-ero')
```

B | Pretasks

B.1 | Session 1

B.1.1 | Task 1

In this project we are supposed to study electric properties of quartz resonators and build a circuit, which is used to collect data from the resonator. Data is then analyzed with MATLAB. Also we are going to measure some properties of the circuit itself.

B.1.2 | Task 2

 V_{+} is connected to ground, so $V_{+} = 0$.

$$V_{out} = A(V_{+} - V_{-})$$

$$\Rightarrow V_{out} = -AV_{-}$$

B.2 Session 2 B PRETASKS

Then according to Kirchoff II and Ohm's law,

$$\begin{split} V_{-} - V_{out} &= R_f I \quad \wedge \quad I = \frac{V_{in} - V_{out}}{R_f + R_{in}} \\ \Rightarrow V_{-} &= R_f \frac{V_{in} - V_{out}}{R_f + R_{in}} + V_{out} \\ \Rightarrow V_{-} &= \frac{R_f V_{in} - R_f V_{out}}{R_f + R_{in}} + \frac{R_f V_{out} + R_{in} V_{out}}{R_f + R_{in}} \\ \Rightarrow V_{-} &= \frac{R_f V_{in} + R_{in} V_{out}}{R_f + R_{in}} \end{split}$$

Then combining these two equations, we obtain V_{out} as function of V_{in} .

$$V_{out} = -A \frac{R_f V_{in} + R_{in} V_{out}}{R_f + R_{in}}$$

$$\Leftrightarrow V_{out} + A \frac{R_{in} V_{out}}{R_f + R_{in}} = -\frac{A R_f V_{in}}{R_f + R_{in}}$$

$$\Leftrightarrow V_{out} \frac{R_f + R_{in} + A R_{in}}{R_f + R_{in}} = -\frac{A R_f V_{in}}{R_f + R_{in}}$$

$$\Leftrightarrow V_{out} = -\frac{A R_f}{R_f + R_{in} + A R_{in}} V_{in}$$

When A is very large, we obtain the following form.

$$V_{out} \approx -\frac{R_f}{R_{in}} V_{in}$$

And thus,

$$G = -\frac{R_f}{R_{in}} \tag{4}$$

B.2 | Session 2

B.2.1 | Task 2

In old western movies the wagon wheel seems to be rotating in the wrong direction because camera's frame rate

B.3 Session 3 B PRETASKS

- B.2.2 | Task 3
- B.2.3 | Task 4
- B.3 | Session 3
- $B.3.1 \ | \ Task \ 1$
- B.3.2 | Task 2
- B.4 | Session 4
- B.4.1 | Task 1
- B.4.2 | Task 2
- B.5 | Session 5
- B.5.1 | Task 1
- B.5.2 | Task 2