Graph Theory

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Figure 1: Robert Floyd

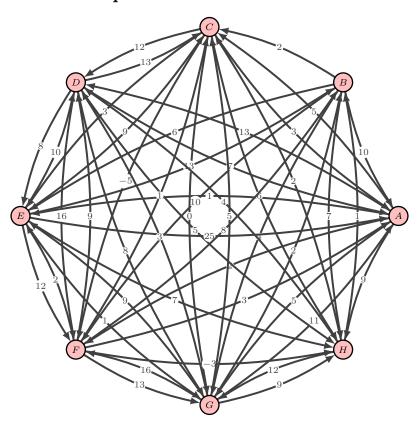
1 Floyd's Algorithm

This program consists of Floyd's algorithm to obtain the shortest path between any pair of nodes in a graph with weighted distances. Floyd's algorithm compares the distance between any two given nodes and by passing through another city in between, if the result is less than the original then it chooses the shortest one. After contemplating all nodes in the graph, the graph is guaranteed to have all the shortest distances between any two nodes in the graph. These changes are recorded in another matrix called P that helps determine the shortest path between any two nodes.

2 Robert W. Floyd (1936–2001)

Robert Willoughby Floyd was a computer scientist that lived from 1936 to 2001. He made great advances in computer science and developed an algorithm to find the shortest paths between any two nodes for a directed graph. He was awarded a Turing Award in 1978.

3 Initial Graph



4 Table D_0

D	A	В	\mathbf{C}	D	\mathbf{E}	F	G	H
A	0	∞	5	13	1	2	5	9
В	10	0	2	∞	6	10	4	7
\mathbf{C}	3	∞	0	12	3	-5	0	6
D	7	∞	13	0	8	16	8	5
\mathbf{E}	25	13	9	10	0	12	1	7
\mathbf{F}	3	8	1	9	2	0	13	-3
G	11	2	5	3	9	16	0	9
Н	∞	1	2	4	∞	∞	12	0

5 Table P_0

P	A	В	C	D	\mathbf{E}	F	G	Н
A	0	0	0	0	0	0	0	0
В	0	0	0	0	0	0	0	0
\mathbf{C}	0	0	0	0	0	0	0	0
D	0	0	0	0	0	0	0	0
\mathbf{E}	0	0	0	0	0	0	0	0
F	0	0	0	0	0	0	0	0
G	0	0	0	0	0	0	0	0
H	0	0	0	0	0	0	0	0

6 Table D_1

D	A	В	\mathbf{C}	D	E	F	G	H
A	0	∞	5	13	1	2	5	9
В	10	0	2	23	6	10	4	7
\mathbf{C}	3	∞	0	12	3	-5	0	6
D	7	∞	12	0	8	9	8	5
\mathbf{E}	25	13	9	10	0	12	1	7
F	3	8	1	9	2	0	8	-3
G	11	2	5	3	9	13	0	9
H	∞	1	2	4	∞	∞	12	0

7 Table P_1

P	A	В	C	D	\mathbf{E}	F	\mathbf{G}	Н
A	0	0	0	0	0	0	0	0
В	0	0	0	1	0	0	0	0
\mathbf{C}	0	0	0	0	0	0	0	0
D	0	0	1	0	0	1	0	0
\mathbf{E}	0	0	0	0	0	0	0	0
\mathbf{F}	0	0	0	0	0	0	1	0
\mathbf{G}	0	0	0	0	0	1	0	0
Н	0	0	0	0	0	0	0	0

8 Table D_2

D	A	В	\mathbf{C}	D	\mathbf{E}	\mathbf{F}	G	H
A	0	∞	5	13	1	2	5	9
В	10	0	2	23	6	10	4	7
\mathbf{C}	3	∞	0	12	3	-5	0	6
D	7	∞	12	0	8	9	8	5
\mathbf{E}	23	13	9	10	0	12	1	7
F	3	8	1	9	2	0	8	-3
G	11	2	4	3	8	12	0	9
H	11	1	2	4	7	11	5	0

9 Table P_2

P	A	В	\mathbf{C}	D	E	F	\mathbf{G}	Н
A	0	0	0	0	0	0	0	0
В	0	0	0	1	0	0	0	0
\mathbf{C}	0	0	0	0	0	0	0	0
D	0	0	1	0	0	1	0	0
\mathbf{E}	2	0	0	0	0	0	0	0
F	0	0	0	0	0	0	1	0
G	0	0	2	0	2	2	0	0
H	2	0	0	0	2	2	2	0

10 Table D_3

D	A	В	C	D	\mathbf{E}	F	G	Н
A	0	∞	5	13	1	0	5	9
В	5	0	2	14	5	-3	2	7
\mathbf{C}	3	∞	0	12	3	-5	0	6
D	7	∞	12	0	8	7	8	5
\mathbf{E}	12	13	9	10	0	4	1	7
\mathbf{F}	3	8	1	9	2	0	1	-3
\mathbf{G}	7	2	4	3	7	-1	0	9
Н	5	1	2	4	5	-3	2	0

11 Table P_3

P	A	В	\mathbf{C}	D	\mathbf{E}	F	\mathbf{G}	H
A	0	0	0	0	0	3	0	0
В	3	0	0	3	3	3	3	0
\mathbf{C}	0	0	0	0	0	0	0	0
D	0	0	1	0	0	3	0	0
\mathbf{E}	3	0	0	0	0	3	0	0
F	0	0	0	0	0	0	3	0
G	3	0	2	0	3	3	0	0
H	3	0	0	0	3	3	3	0

12 Table D_4

D	A	В	\mathbf{C}	D	\mathbf{E}	F	G	H
A	0	∞	5	13	1	0	5	9
В	5	0	2	14	5	-3	2	7
\mathbf{C}	3	∞	0	12	3	-5	0	6
D	7	∞	12	0	8	7	8	5
\mathbf{E}	12	13	9	10	0	4	1	7
\mathbf{F}	3	8	1	9	2	0	1	-3
G	7	2	4	3	7	-1	0	8
Н	5	1	2	4	5	-3	2	0

13 Table P_4

P	A	В	\mathbf{C}	D	\mathbf{E}	F	\mathbf{G}	Η
A	0	0	0	0	0	3	0	0
В	3	0	0	3	3	3	3	0
\mathbf{C}	0	0	0	0	0	0	0	0
D	0	0	1	0	0	3	0	0
\mathbf{E}	3	0	0	0	0	3	0	0
F	0	0	0	0	0	0	3	0
G	3	0	2	0	3	3	0	4
Н	3	0	0	0	3	3	3	0

14 Table D_5

D	A	В	\mathbf{C}	D	E	F	G	H
A	0	14	5	11	1	0	2	8
В	5	0	2	14	5	-3	2	7
\mathbf{C}	3	16	0	12	3	-5	0	6
D	7	21	12	0	8	7	8	5
\mathbf{E}	12	13	9	10	0	4	1	7
F	3	8	1	9	2	0	1	-3
G	7	2	4	3	7	-1	0	8
Н	5	1	2	4	5	-3	2	0

15 Table P_5

P	A	В	\mathbf{C}	D	\mathbf{E}	F	\mathbf{G}	H
A	0	5	0	5	0	3	5	5
В	3	0	0	3	3	3	3	0
\mathbf{C}	0	5	0	0	0	0	0	0
D	0	5	1	0	0	3	0	0
\mathbf{E}	3	0	0	0	0	3	0	0
F	0	0	0	0	0	0	3	0
G	3	0	2	0	3	3	0	4
H	3	0	0	0	3	3	3	0

16 Table D_6

D	A	В	\mathbf{C}	D	\mathbf{E}	\mathbf{F}	G	H
A	0	8	1	9	1	0	1	-3
В	0	0	-2	6	-1	-3	-2	-6
\mathbf{C}	-2	3	0	4	-3	-5	-4	-8
D	7	15	8	0	8	7	8	4
E	7	12	5	10	0	4	1	1
F	3	8	1	9	2	0	1	-3
G	2	2	0	3	1	-1	0	-4
H	0	1	-2	4	-1	-3	-2	0

17 Table P_6

P	A	В	\mathbf{C}	D	\mathbf{E}	F	\mathbf{G}	H
A	0	6	6	6	0	3	6	6
В	6	0	6	6	6	3	6	6
\mathbf{C}	6	6	0	6	6	0	6	6
D	0	6	6	0	0	3	0	6
\mathbf{E}	6	6	6	0	0	3	0	6
F	0	0	0	0	0	0	3	0
G	6	0	6	0	6	3	0	6
H	6	0	6	0	6	3	6	0

18 Table D_7

D	A	В	\mathbf{C}	D	\mathbf{E}	\mathbf{F}	G	Н
A	0	3	1	4	1	0	1	-3
В	0	0	-2	1	-1	-3	-2	-6
\mathbf{C}	-2	-2	0	-1	-3	-5	-4	-8
D	7	10	8	0	8	7	8	4
\mathbf{E}	3	3	1	4	0	0	1	-3
F	3	3	1	4	2	0	1	-3
G	2	2	0	3	1	-1	0	-4
H	0	0	-2	1	-1	-3	-2	0

19 Table P_7

P	A	В	\mathbf{C}	D	\mathbf{E}	F	G	Η
A	0	7	6	7	0	3	6	6
В	6	0	6	7	6	3	6	6
\mathbf{C}	6	7	0	7	6	0	6	6
D	0	7	6	0	0	3	0	6
\mathbf{E}	7	7	7	7	0	7	0	7
F	0	7	0	7	0	0	3	0
G	6	0	6	0	6	3	0	6
Н	6	7	6	7	6	3	6	0

20 Table D_8

D	A	В	C	D	${f E}$	\mathbf{F}	G	H
Α	0	-3	-5	-2	-4	-6	-5	-3
В	-6	0	-8	-5	-7	-9	-8	-6
\mathbf{C}	-8	-8	0	-7	-9	-11	-10	-8
D	4	4	2	0	3	1	2	4
\mathbf{E}	-3	-3	-5	-2	0	-6	-5	-3
\mathbf{F}	-3	-3	-5	-2	-4	0	-5	-3
\mathbf{G}	-4	-4	-6	-3	-5	-7	0	-4
Н	0	0	-2	1	-1	-3	-2	0

21 Table P_8

P	A	В	\mathbf{C}	D	\mathbf{E}	F	G	Н
A	0	8	8	8	8	8	8	6
В	8	0	8	8	8	8	8	6
\mathbf{C}	8	8	0	8	8	8	8	6
D	8	8	8	0	8	8	8	6
\mathbf{E}	8	8	8	8	0	8	8	7
\mathbf{F}	8	8	8	8	8	0	8	0
\mathbf{G}	8	8	8	8	8	8	0	6
Н	6	7	6	7	6	3	6	0

22 Final Graph

