**How are cross-validated decoding accuracies**

**distributed across subjects?**

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**Introduction:**

In multivariate pattern analysis (MVPA) for functional magnetic resonance imaging (fMRI) data, cross-validated decoding accuracy (cvDA) maps from first-level decoding analyses are typically subjected to second-level t-tests [1] in order to make population inference. This practice has been criticized as making questionable assumptions about cvDAs and effectively performing a fixed-effects analysis instead of a more appropriate random-effects analysis which is usually insinuated by the interpretation of the results [2]. The second-level t-test for cvDAs can also be challenged based on the nature of accuracies which, unlike the variates going into a t-test, (i) are neither in an *infinite range* (but bounded between 0 and 1), (ii) nor are they *normally distributed* (because they are proportions). Here, we estimate Beta distributions [5,6] from cvDAs across subjects to overcome those problems and provide a number of summary statistics to make statements about the observed accuracies.

**Methods:**

The cross-validated decoding accuracies from subjects are assumed to be independent and come from an underlying Beta distribution [5]:

The parameters and can be obtained using maximum likelihood estimation (MLE) for the Dirichlet distribution [6], a generalization of the Beta distribution:

From the estimated concentration parameters, one can then calculate (see Figure 1)

1. the expected frequency, i.e. the mean of the accuracy distribution
2. the likeliest frequency, i.e. the most likely decoding accuracy
3. the exceedance probability that the decoding accuracy is larger than chance level
4. a confidence interval for the most likely accuracy, given a confidence level ()

**Results:**

We analyzed a set of cvDA maps [4] that comes from an earlier study on object recognition [3] and was previously used in methods development for second-level decoding inference [2]. We show that the above-mentioned summary statistics can give an intuitive understanding of the amount of information contained in a voxel or searchlight when decoding accuracies are significantly above (see Figure 1A) or when they are around chance level (see Figure 1B). Moreover, we observe that estimated concentration parameters across all voxels are compatible with a null distribution when labels were exchanged between classes (see Figure 2B), but not when unpermuted data were used (see Figure 2A).

**Discussion:**

We have provided a method for second-level analysis of cvDA maps and validated it using empirical data. Unlike the currently received approach, i.e. the one-sample t-test, this type of analysis (i) acknowledges the domain of accuracies as proportions and (ii) allows the distribution of accuracies to be non-symmetric. A downside of the proposed method is that it, like the t-test, does not take into account that *true* accuracies cannot be below chance level and inference therefore only pertains to *observed* accuracies [2]. In the future, we want to evaluate asymptotic properties of this approach using simulated data and implement multiple comparison correction for the analysis of empirical data.

**References:**

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