- ji kale aana marka m

Figure 1: At low temperatures we observed smaller groups of aligned spins. We concluded that the influence of the heat (i.e. $\tau\sigma$) on the free energy was low and therefore, that the energy U was minmised.

Given the partition function $Z = (2\cosh(\epsilon/\tau))^N$, we calculated the internal energy using,

$$U = \tau^{2} \partial_{\tau} \ln(Z)$$

$$= \tau^{2} \partial_{\tau} \ln\left(2 \cosh\left(\frac{\epsilon}{\tau}\right)^{N}\right)$$

$$= N\tau^{2} \partial_{\tau} \ln\left(2 \cosh\left(\frac{\epsilon}{\tau}\right)\right)$$

$$= N\tau^{2} \partial_{\tau} \left(2 \cosh\left(\frac{\epsilon}{\tau}\right)\right) \frac{1}{2 \cosh\left(\frac{\epsilon}{\tau}\right)}$$

$$= N\tau^{2} \partial_{\tau} \left(\frac{\epsilon}{\tau}\right) \frac{\sinh\left(\frac{\epsilon}{\tau}\right)}{\cosh\left(\frac{\epsilon}{\tau}\right)}$$

$$= -\epsilon N \tanh\left(\frac{\epsilon}{\tau}\right)$$
(2)