

# CSCI 2600 - Homework 3

## Problem 2

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### Problem 2 Written Answers

- (a) We have chosen the array representation of a polynomial: `RatNum[] coeffs`, where `coeffs[i]` stores the coefficient of the term of exponent `i`. An alternative data representation is the list-of-terms representation: `List<Term> terms`, where each `Term` object stores the term's `RatNum` coefficient and integer exponent. The beauty of the ADT methodology is that we can switch from one representation to the other without affecting the clients of our `RatPoly`. Briefly list the advantages and disadvantages of the array representation versus the list-of-terms representation.

**Answer:**

The array representation offers  $O(1)$  direct access to coefficients by exponent, making it efficient for operations that need to access terms by degree. It is memory-efficient for dense polynomials where most exponents have non-zero coefficients. However, it wastes space for sparse polynomials with large gaps between terms, requires allocating space for all terms from 0 to the highest degree, and operations like addition may require resizing arrays.

The list-of-terms representation is more space-efficient for sparse polynomials with few terms, making it easier to maintain terms in sorted order without wasting space for zero coefficients. Its disadvantages include  $O(n)$  access time to specific terms (requiring linear search), more complex implementation for operations needing coefficients by degree, and the overhead of storing the exponent with each term.

- (b) Where did you include calls to `checkRep()` in `RatPoly` (at the beginning of methods, the end of methods, the beginning of constructors, the end of constructors, some combination)? Why?

**Answer:**

I included calls to `checkRep()` at the end of all constructors and at the end of methods that create new `RatPoly` objects. This approach is sufficient because `RatPoly` is an immutable class (all fields are final), so once a valid object is constructed, it cannot be modified to violate the representation invariant.

Since methods like `add()`, `sub()`, `mul()`, etc., don't modify existing objects but return new ones, checking the representation at the end of these object-creating operations ensures the invariant is preserved for all `RatPoly` objects. Including `checkRep()` at the beginning of methods would be redundant since the existing objects have already been verified at construction time and cannot be modified afterward.