

2.1 — Data 101 & Descriptive Statistics

ECON 480 • Econometrics • Fall 2022

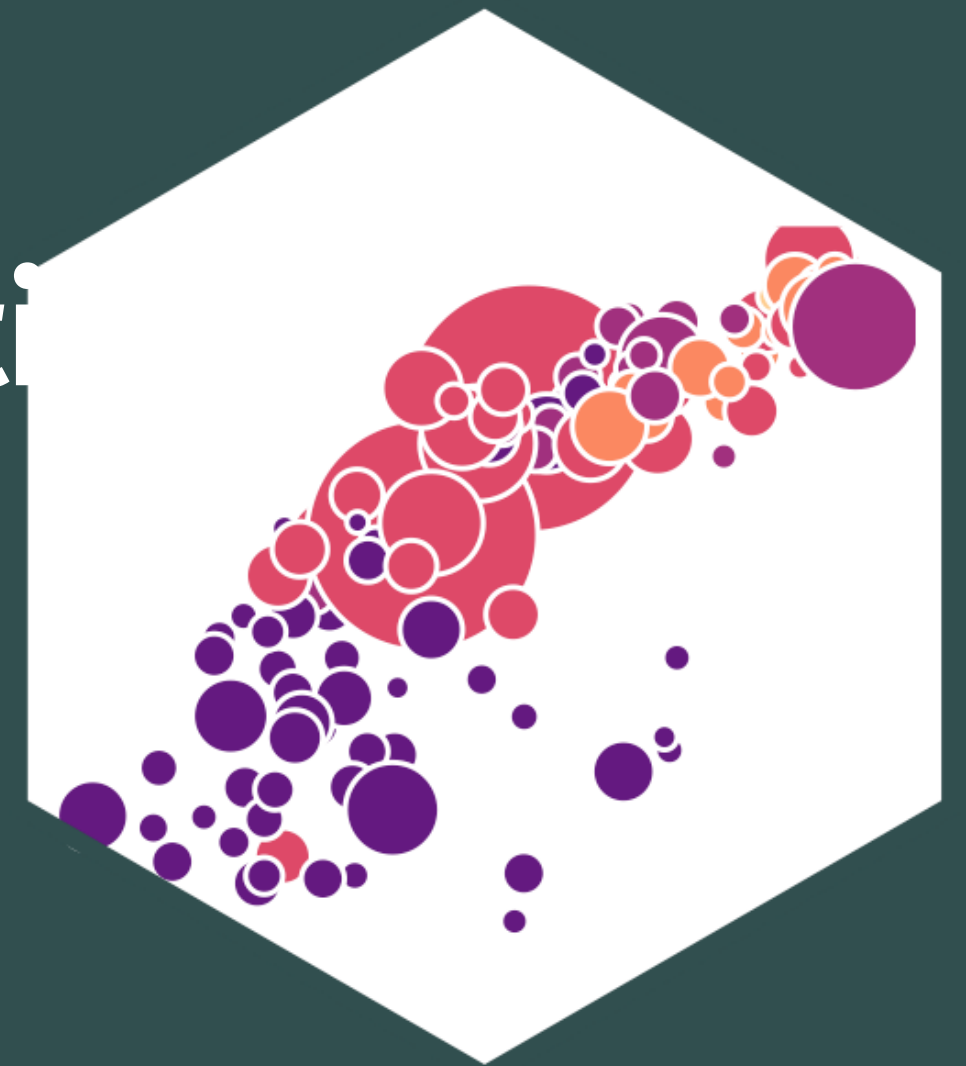
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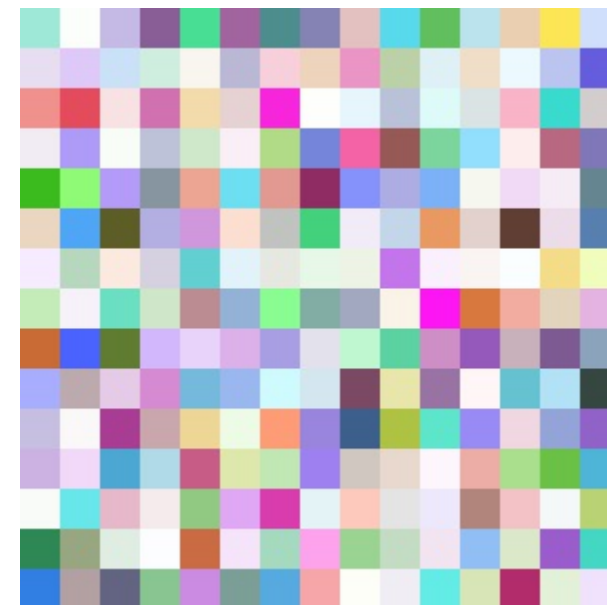


The Two Big Problems with Data



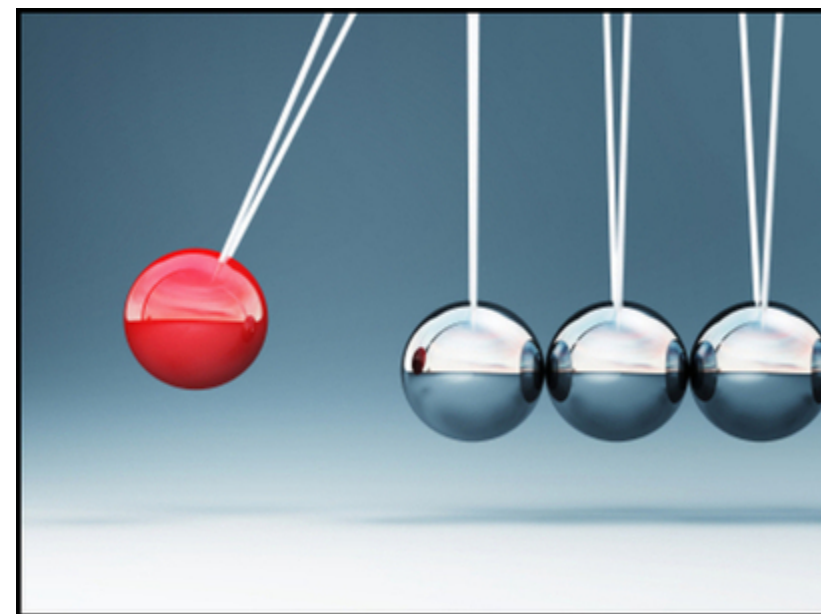
Two Big Problems with Data

- We want to use econometrics to **identify** causal relationships and make **inferences** about them
1. Problem for **identification**: **endogeneity**
 2. Problem for **inference**: **randomness**



Identification Problem: Endogeneity

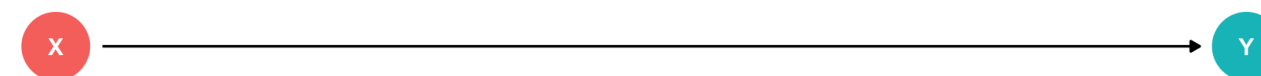
- An independent variable (X) is **exogenous** if its variation is **unrelated** to other factors that affect the dependent variable (Y)
- An independent variable (X) is **endogenous** if its variation is **related** to other factors that affect the dependent variable (Y)
- Note: unfortunately this is different from how economists talk about “endogenous” vs. “exogenous” variables in theoretical models...



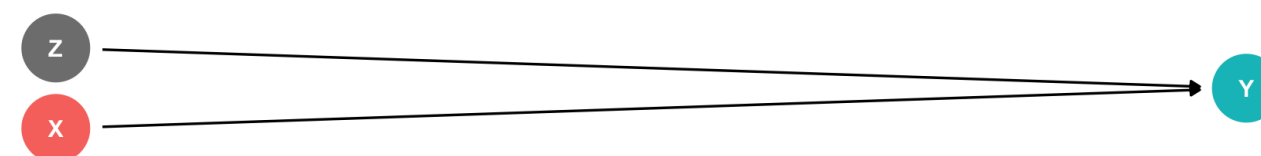
Identification Problem: Endogeneity

- An independent variable (X) is **exogenous** if its variation is **unrelated** to other factors that affect the dependent variable (Y)

X causes Y



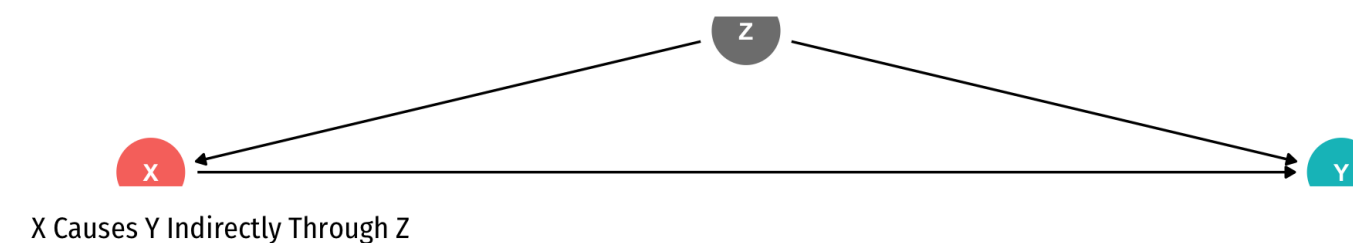
X and Z (independently) cause Y



Identification Problem: Endogeneity

- An independent variable (X) is **endogenous** if its variation is **related** to other factors that affect the dependent variable (Y), e.g. Z

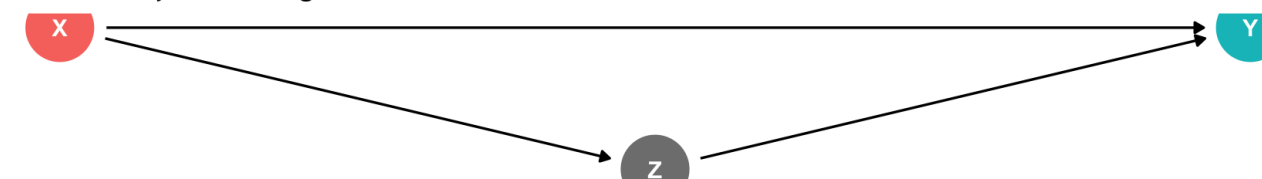
Z causes X and Y



X Causes Y Indirectly Through Z



X Causes Y Directly and Through Z



Inference Problem: Randomness

- Data is **random** due to **natural sampling variation**
 - Taking one sample of a population will yield slightly different information than another sample of the same population
- Common in statistics, *easy to fix*
- **Inferential Statistics**: making claims about a wider population using sample data
 - We use common tools and techniques to deal with randomness



The Two Problems: Where We're Heading...Ultimately



- We want to **identify** causal relationships between **population** variables
 - Logically first thing to consider
 - **Endogeneity problem**
- We'll use **sample** *statistics* to **infer** something about population *parameters*
 - In practice, we'll only ever have a finite *sample distribution* of data
 - We *don't* know the *population distribution* of data
 - **Randomness problem**



Data 101



Data 101

- **Data** are information with context
- **Individuals** are the entities described by a set of data
 - e.g. persons, households, firms, countries



Data 101

- **Variables** are particular characteristics about an individual
 - e.g. age, income, profits, population, GDP, marital status, type of legal institutions
- **Observations** or **cases** are the separate individuals described by a collection of variables
 - e.g. for one individual, we have their age, sex, income, education, etc.
- individuals and observations are *not necessarily* the same:
 - e.g. we can have multiple observations on the same individual over time



Categorical Variables

- **Categorical variables** place an individual into one of several possible *categories*
 - e.g. sex, season, political party
 - may be responses to survey questions
 - can be quantitative (e.g. age, zip code)
- In R: **character** or **factor** type data
 - **factor** \implies specific possible categories

Question	Categories or Responses
Do you invest in the stock market?	<input type="checkbox"/> Yes <input type="checkbox"/> No
What kind of advertising do you use?	<input type="checkbox"/> Newspapers <input type="checkbox"/> Internet <input type="checkbox"/> Direct mailings
What is your class at school?	<input type="checkbox"/> Freshman <input type="checkbox"/> Sophomore <input type="checkbox"/> Junior <input type="checkbox"/> Senior
I would recommend this course to another student.	<input type="checkbox"/> Strongly Disagree <input type="checkbox"/> Slightly Disagree <input type="checkbox"/> Slightly Agree <input type="checkbox"/> Strongly Agree
How satisfied are you with this product?	<input type="checkbox"/> Very Unsatisfied <input type="checkbox"/> Unsatisfied <input type="checkbox"/> Satisfied <input type="checkbox"/> Very Satisfied



Categorical Variables: Visualizing I

```
1 diamonds %>%
2   count(cut) %>%
3   mutate(frequency = n / sum(n),
4           percent = round(frequency * 100, 2))
```

Summary of diamonds by cut

cut	n	frequency	percent
Fair	1610	0.0298480	2.98
Good	4906	0.0909529	9.10
Very Good	12082	0.2239896	22.40
Premium	13791	0.2556730	25.57
Ideal	21551	0.3995365	39.95

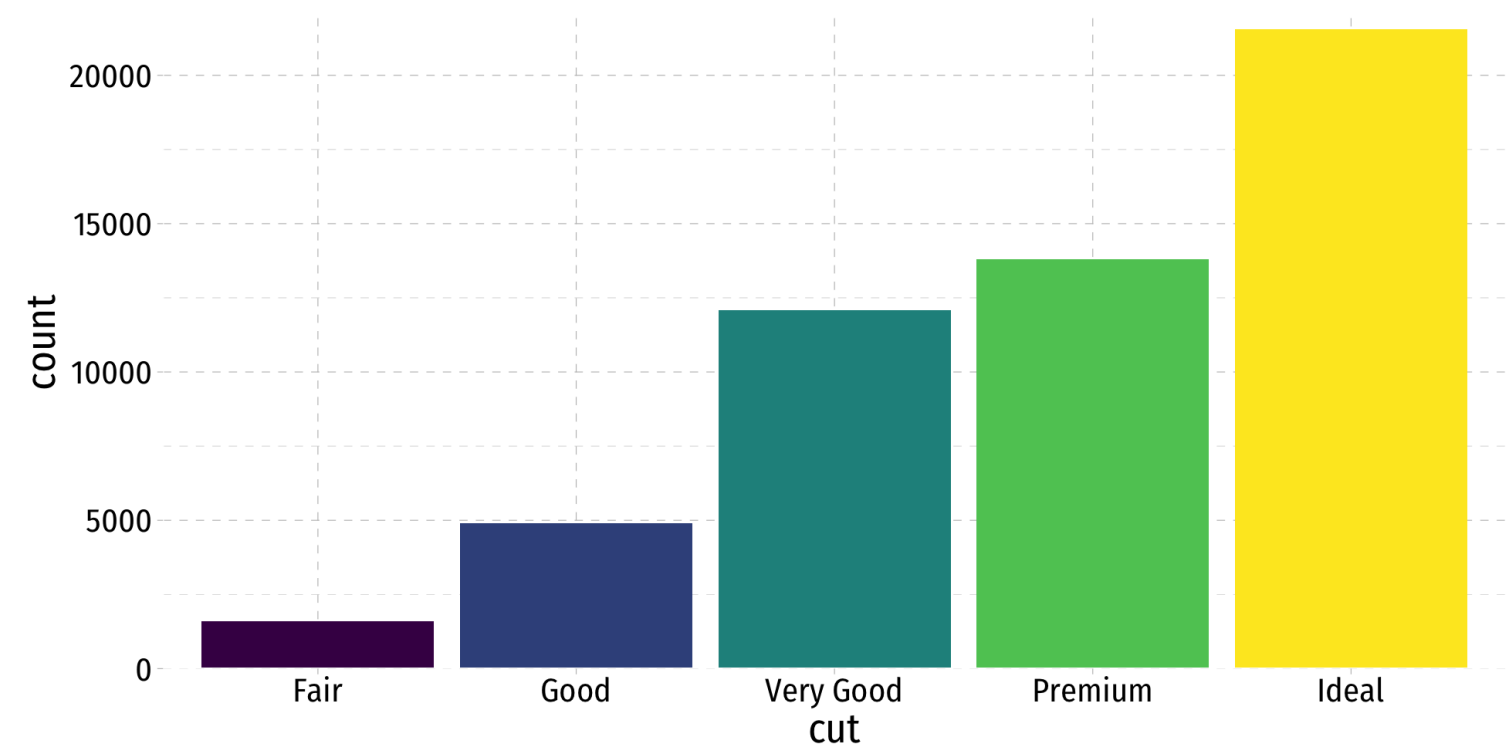
- Good way to represent categorical data is with a **frequency table**
- **Count (n)**: total number of individuals in a category
- **Frequency: proportion** of a category's occurrence relative to all data
 - Multiply proportions by 100% to get **percentages**



Categorical Variables: Visualizing II

- Charts and graphs are *always* better ways to visualize data
- A **bar graph** represents categories as bars, with lengths proportional to the count or relative frequency of each category

```
1 ggplot(diamonds, aes(x=cut,  
2                       fill=cut))+  
3   geom_bar()+  
4   guides(fill=F)+  
5   theme_pander(base_family = "Fira Sans Condensed"  
6               base_size=20)
```



Categorical Data: Pie Charts

- Avoid pie charts!
- People are *not* good at judging 2-d differences (angles, area)
- People *are* good at judging 1-d differences (length)



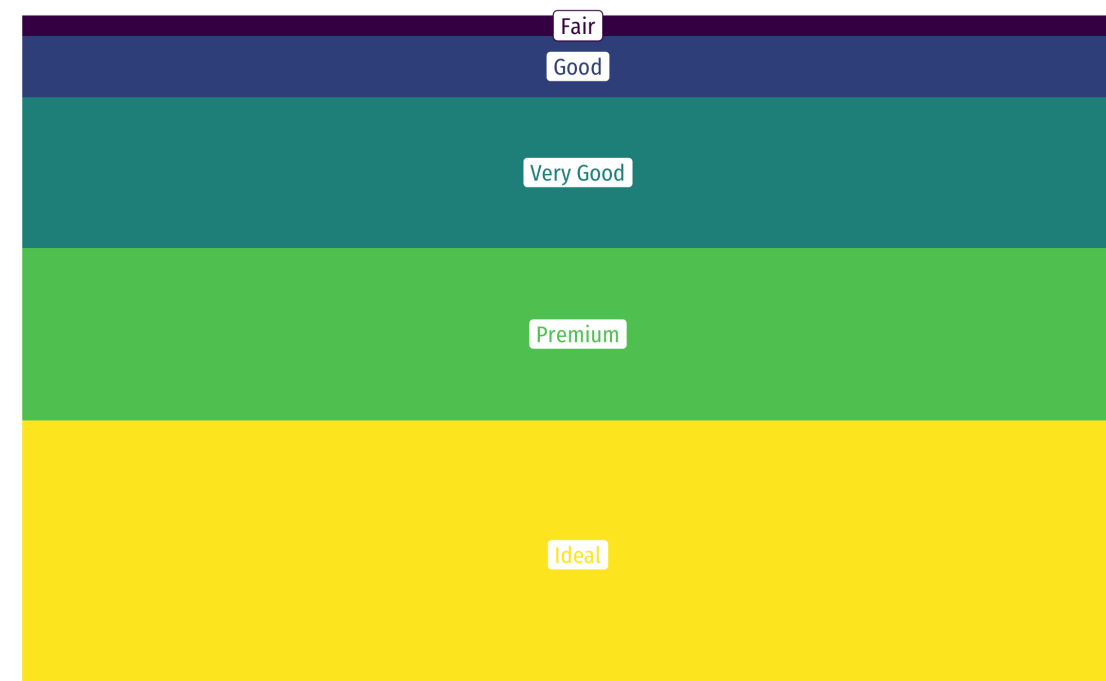
Categorical Data: Alternatives to Pie Charts I

- Try something else: a *stacked bar chart*

```

1 diamonds %>%
2   count(cut) %>%
3   ggplot(data = .)+
4     aes(x = "",
5         y = n)+
6     geom_col(aes(fill = cut))+
7     geom_label(aes(label = cut,
8                   color = cut),
9               position = position_stack(vjust = 0.5
10            )+
11     guides(color = F,
12            fill = F)+
13     theme_void()

```



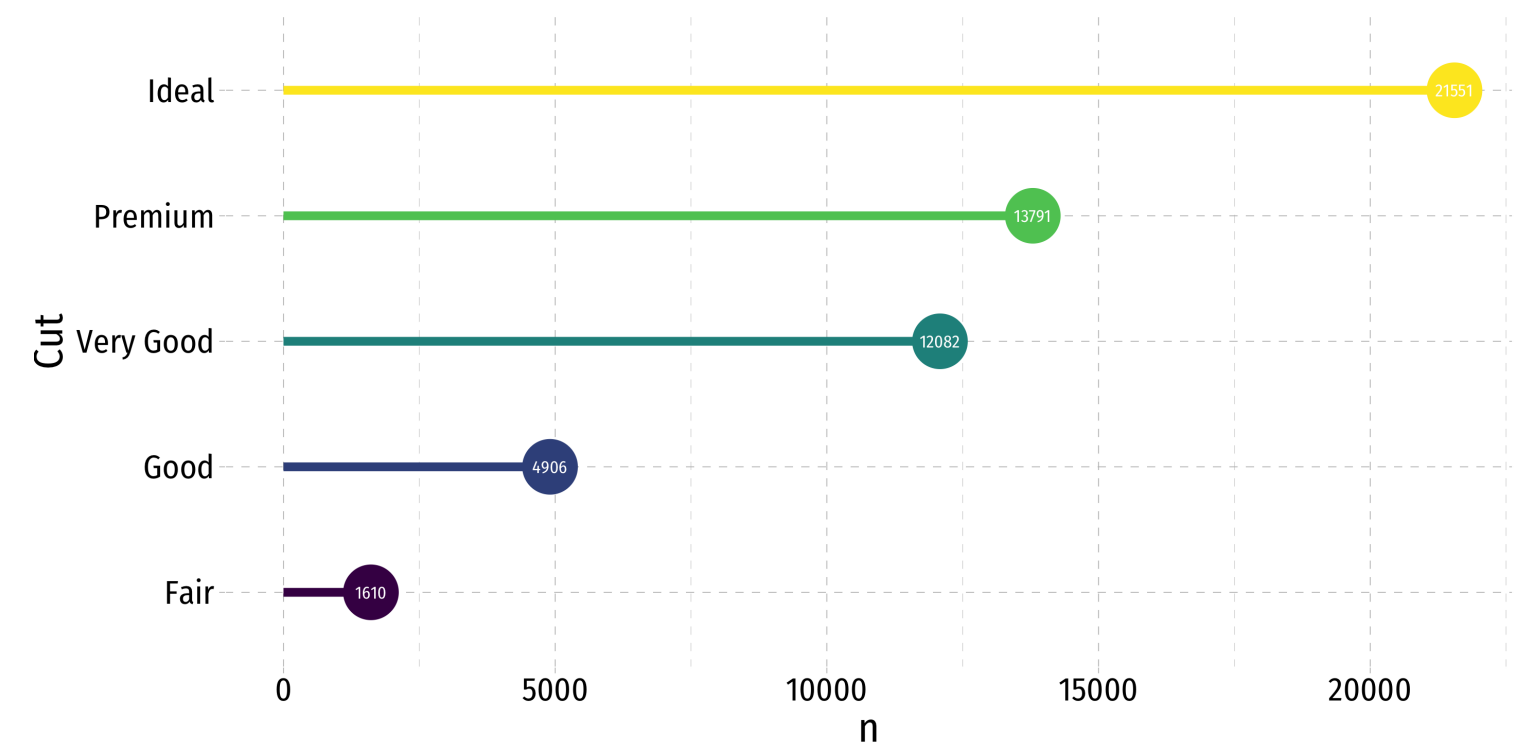
Categorical Data: Alternatives to Pie Charts II

- Try something else: a *lollipop chart*

```

1 diamonds %>%
2   count(cut) %>%
3   mutate(cut_name = as.factor(cut)) %>%
4   ggplot(., aes(x = cut_name, y = n, color = cut))+
5   geom_point(stat="identity",
6             fill="black",
7             size=12) +
8   geom_segment(aes(x = cut_name, y = 0,
9                   xend = cut_name,
10                  yend = n), size = 2)+
11   geom_text(aes(label = n),color="white", size=3)
12   coord_flip()+
13   labs(x = "Cut")+
14   theme_pander(base_family = "Fira Sans Condensed"
15               base_size=20)+
16   guides(color = F)

```



Categorical Data: Alternatives to Pie Charts III

- Try something else: a *treemap*

```

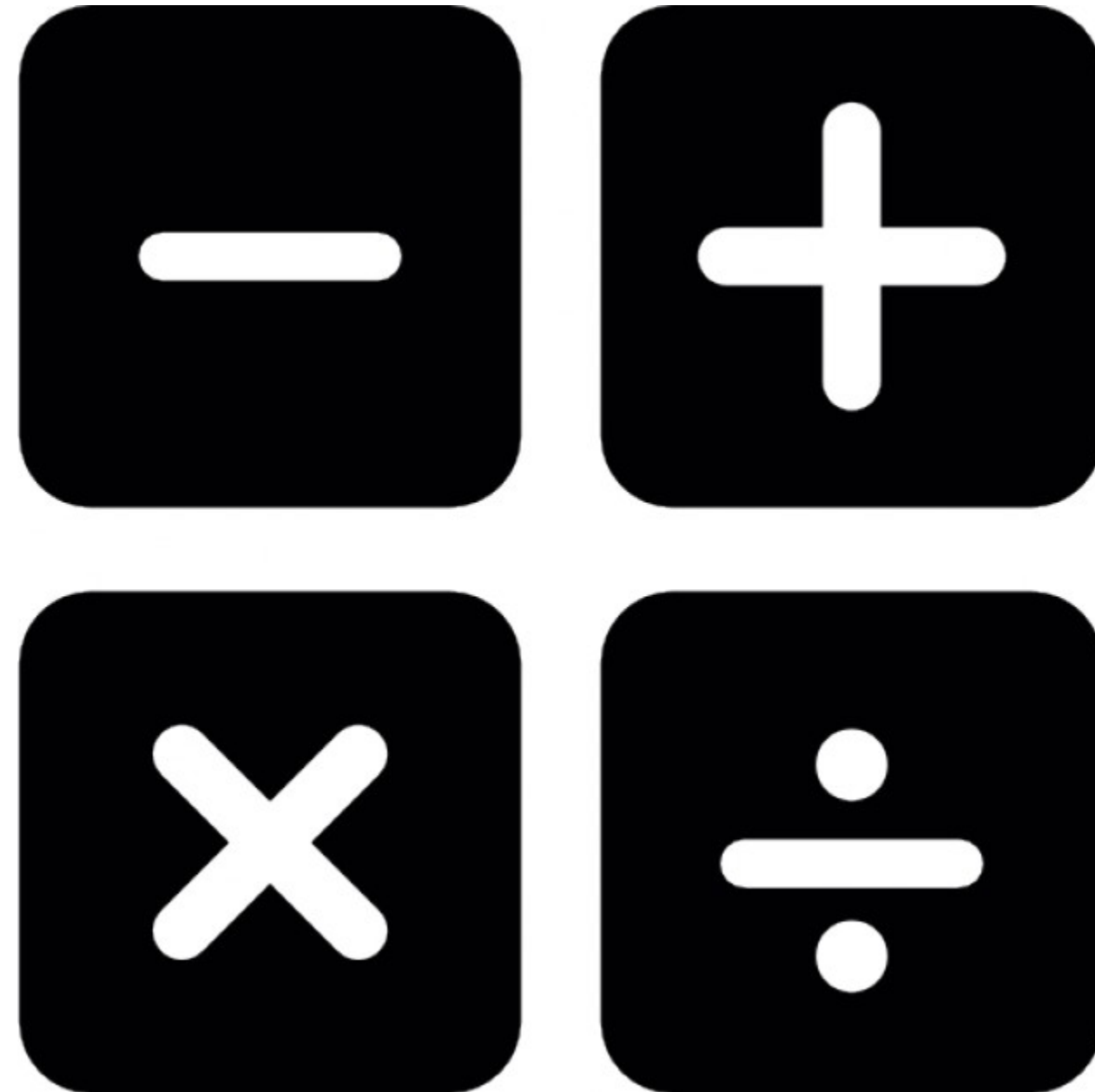
1 library(treemapify)
2 diamonds %>%
3   count(cut) %>%
4   ggplot(., aes(area = n, fill = cut)) +
5     geom_treemap() +
6     guides(fill = FALSE) +
7     geom_treemap_text(aes(label = cut),
8                          colour = "white",
9                          place = "topleft",
10                         grow = TRUE)

```



Quantitative Data I

- **Quantitative variables** take on numerical values of equal units that describe an individual
 - Units: points, dollars, inches
 - Context: GPA, prices, height
- We can mathematically manipulate *only* quantitative data
 - e.g. sum, average, standard deviation
- In R: `numeric` type data
 - `integer` if whole number
 - `double` if has decimals



Discrete Data

- **Discrete data** are finite, with a countable number of alternatives
- **Categorical**: place data into categories
 - e.g. letter grades: A, B, C, D, F
 - e.g. class level: freshman, sophomore, junior, senior
- **Quantitative**: integers
 - e.g. SAT Score, number of children, age (years)



Continuous Data

- **Continuous data** are infinitely divisible, with an uncountable number of alternatives
 - e.g. weight, length, temperature, GPA
- Many discrete variables may be treated as if they are continuous
 - e.g. SAT scores (whole points), wages (dollars and cents)



Spreadsheets

id	name	age	sex	income
1	John	23	Male	41000
2	Emile	18	Male	52600
3	Natalya	28	Female	48000
4	Lakisha	31	Female	60200
5	Cheng	36	Male	81900

- The most common data structure we use is a **spreadsheet**
 - In *R*: a `data.frame` or `tibble`
- A **row** contains data about all variables for a single **individual**
- A **column** contains data about a single **variable** across all individuals



Spreadsheets: Indexing

id	name	age	sex	income
1	John	23	Male	41000
2	Emile	18	Male	52600
3	Natalya	28	Female	48000
4	Lakisha	31	Female	60200
5	Cheng	36	Male	81900

- Each `df[row, column]` can be referenced by its row and column (in that order!),
`df[row, column]`

```
1 example[3,2] # value in row 3, column 2
```

```
# A tibble: 1 × 1
```

```
name
```

```
<chr>
```

```
1 Natalya
```

- Recall with `tidyverse` you can do this with `select()` and `filter()` or `slice()`



Spreadsheets: Notation

- It is common to use some notation like the following:
- Let $\{x_1, x_2, \dots, x_n\}$ be a simple data series on variable X
 - n individual observations
 - x_i is the value of the i^{th} observation for $i = 1, 2, \dots, n$

Quick Check

Let x represent the score on a homework assignment:

75, 100, 92, 87, 79, 0, 95

1. What is n ?
2. What is x_1 ?
3. What is x_6 ?



Datasets: Cross-Sectional

id	name	age	sex	income
1	John	23	Male	41000
2	Emile	18	Male	52600
3	Natalya	28	Female	48000
4	Lakisha	31	Female	60200
5	Cheng	36	Male	81900

- **Cross-sectional data**: observations of individuals at a given point in time
- Each observation is a unique individual

$$x_i$$

- Simplest and most common data
- A “**snapshot**” to compare differences across individuals



Datasets: Time-Series

Year	GDP	Unemployment	CPI
1950	8.2	0.06	100
1960	9.9	0.04	118
1970	10.2	0.08	130
1980	12.4	0.08	190
1985	13.6	0.06	196

- **Time-series data**: observations of the *same* individual(s) over time
- Each observation is a time period

$$x_t$$

- Often used for macroeconomics, finance, and forecasting
- Unique challenges for time series
- A “**moving picture**” to see how individuals change over time



Datasets: Panel

City	Year	Murders	Population
Philadelphia	1986	5	3.700
Philadelphia	1990	8	4.200
D.C.	1986	2	0.250
D.C.	1990	10	0.275
New York	1986	3	6.400

- **Panel**, or **longitudinal** dataset: a time-series for *each* cross-sectional entity
 - Must be *same* individuals over time
- Each obs. is an individual in a time period

$$x_{it}$$

- More common today for serious researchers; unique challenges and benefits
- A **combination** of “snapshot” comparisons over time



Descriptive Statistics



Variables and Distributions

- Variables take on different values, we can describe a variable's *hi*[distribution] (of these values)
- We want to *visualize* and *analyze* distributions to search for meaningful patterns using **statistics**



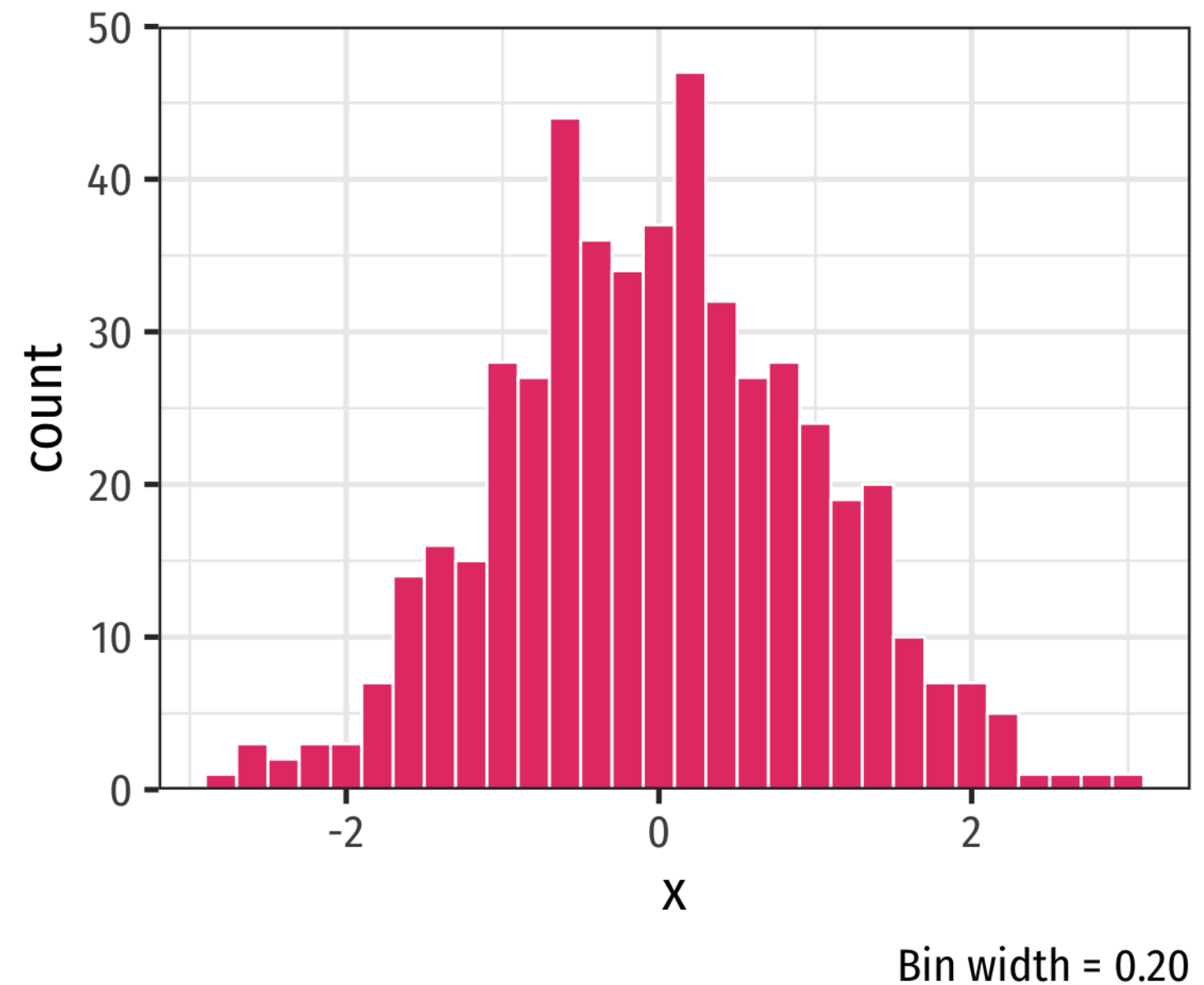
Two Branches of Statistics

- Two main branches of statistics:
 1. **Descriptive Statistics:** describes or summarizes the properties of a sample
 2. **Inferential Statistics:** infers properties about a larger population from the properties of a sample¹



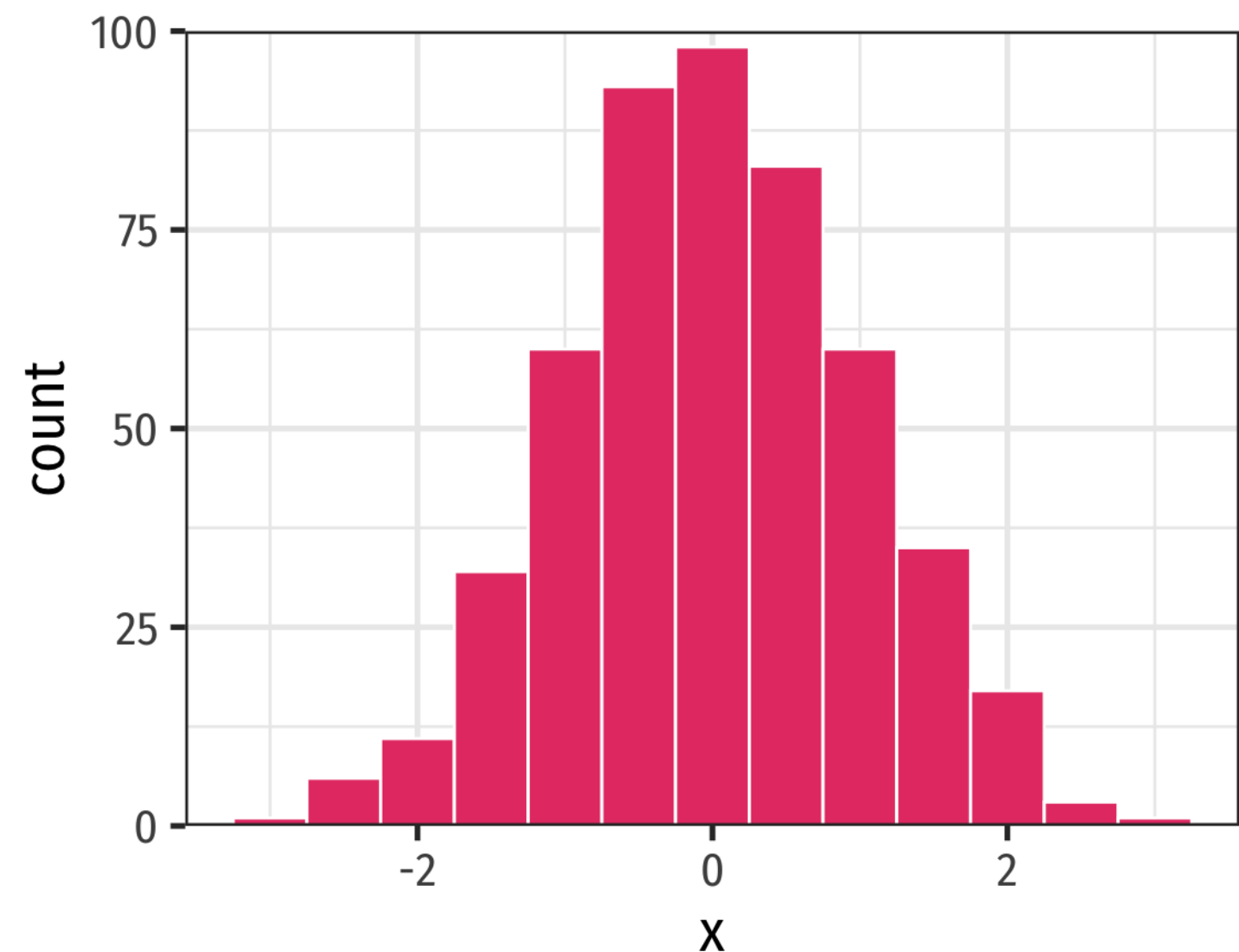
Histogram

- A common way to present a *quantitative* variable's distribution is a **histogram**
 - The quantitative analog to the bar graph for a categorical variable
- Divide up values into **bins** of a certain size, and count the number of values falling within each bin, representing them visually as bars



Histogram: Bin Size

- A common way to present a *quantitative* variable's distribution is a **histogram**
 - The quantitative analog to the bar graph for a categorical variable
- Divide up values into **bins** of a certain size, and count the number of values falling within each bin, representing them visually as bars
 - Changing the **bin-width** will affect the bars



Bin width = 0.50



Histogram: Example

Example

A class of 13 students takes a quiz (out of 100 points) with the following results:

$\{0, 62, 66, 71, 71, 74, 76, 79, 83, 86, 88, 93, 95\}$



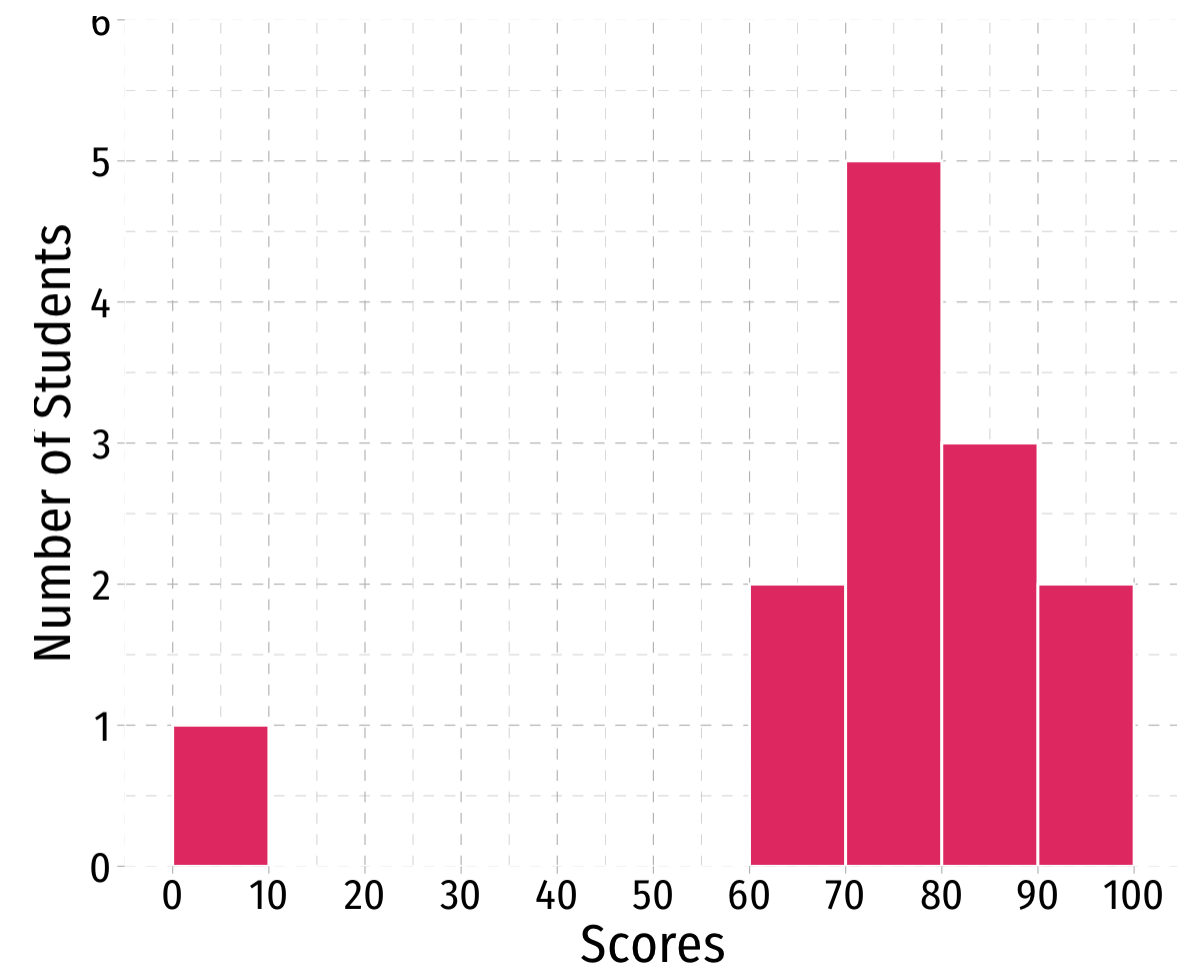
Histogram: Example

Example

A class of 13 students takes a quiz (out of 100 points) with the following results:

{0, 62, 66, 71, 71, 74, 76, 79, 83, 86, 88, 93, 95}

```
1 ggplot(quizzes, aes(x=scores)) +
2   geom_histogram(breaks = seq(0, 100, 10),
3                 color = "white",
4                 fill = "#e64173") +
5   scale_x_continuous(breaks = seq(0, 100, 10)) +
6   scale_y_continuous(limits = c(0, 6), expand = c(0, 0.1)) +
7   labs(x = "Scores",
8        y = "Number of Students") +
9   theme_bw(base_family = "Fira Sans Condensed",
10           base_size=20)
```



Descriptive Statistics

- We are often interested in the *shape* or *pattern* of a distribution, particularly:
 - Measures of **center**
 - Measures of **dispersion**
 - **Shape** of distribution



Measures of Center



Mode

- The `.hmode` of a variable is simply its most frequent value
- A variable can have multiple modes

Example

A class of 13 students takes a quiz (out of 100 points) with the following results:

$\{0, 62, 66, \mathbf{71}, \mathbf{71}, 74, 76, 79, 83, 86, 88, 93, 95\}$



Mode

- There is no dedicated `mode()` function in R, surprisingly
- A workaround in `dplyr`:

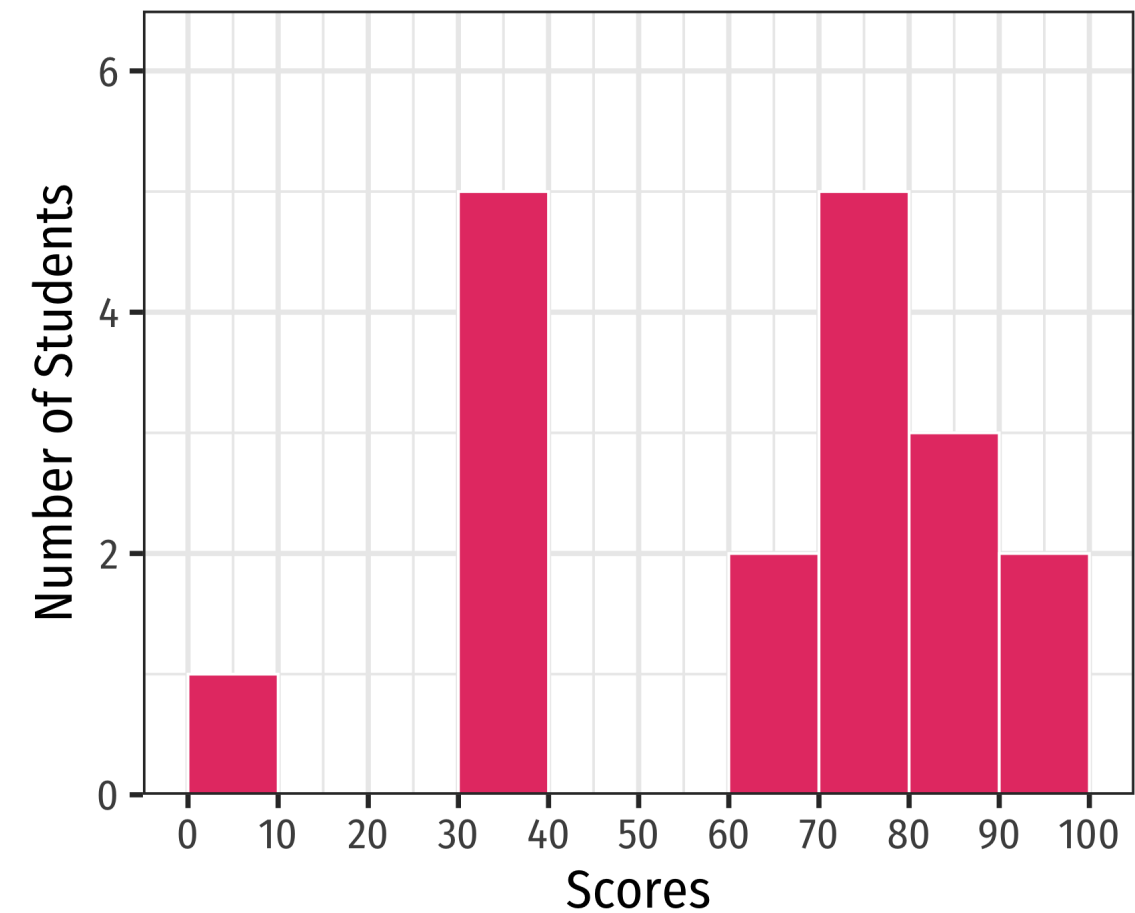
```
1 quizzes %>%
2   count(scores) %>%
3   arrange(desc(n))
```

	scores <dbl>	n <int>
	71	2
	0	1
	62	1
	66	1
	74	1
1-5 of 12 rows		Previous 1 2 3 Next



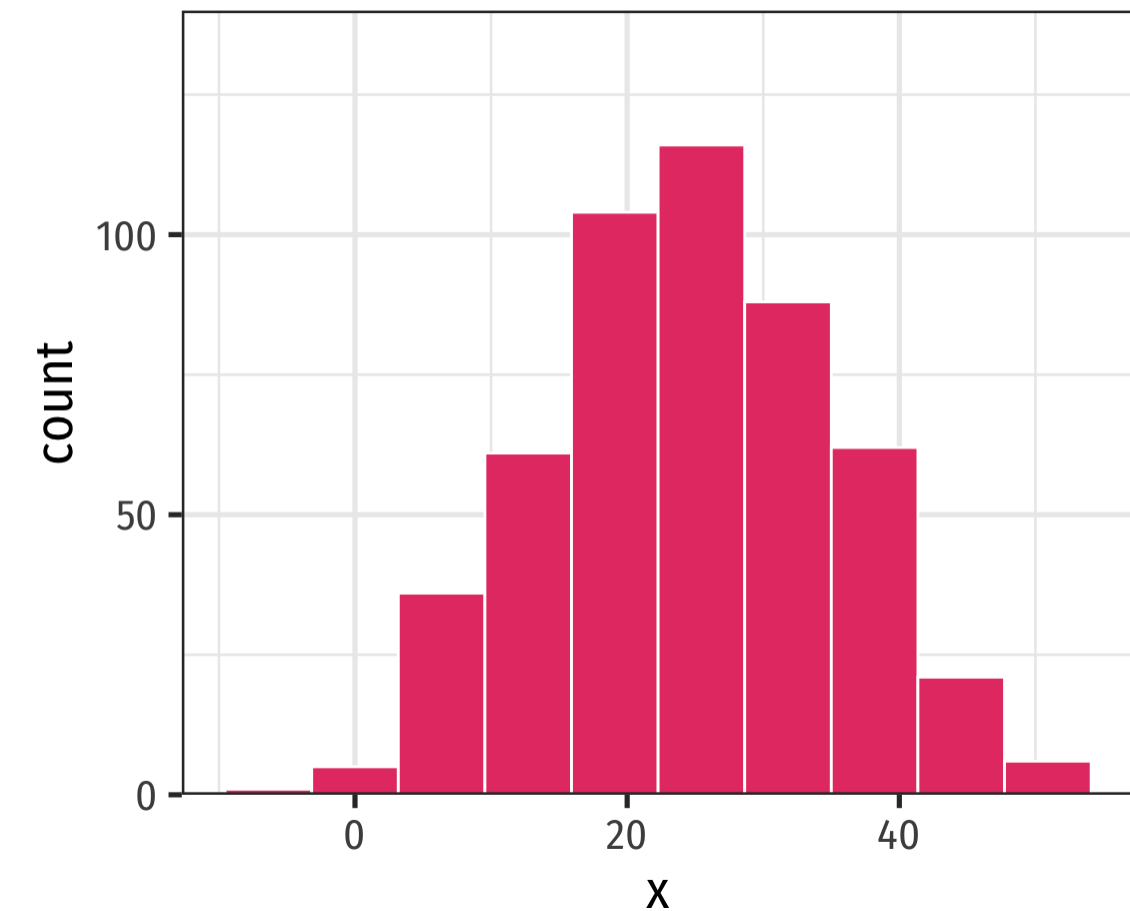
Multi-Modal Distributions

- Looking at a histogram, the modes are the “peaks” of the distribution
 - Note: depends on how wide you make the bins!
- May be unimodal, bimodal, trimodal, etc



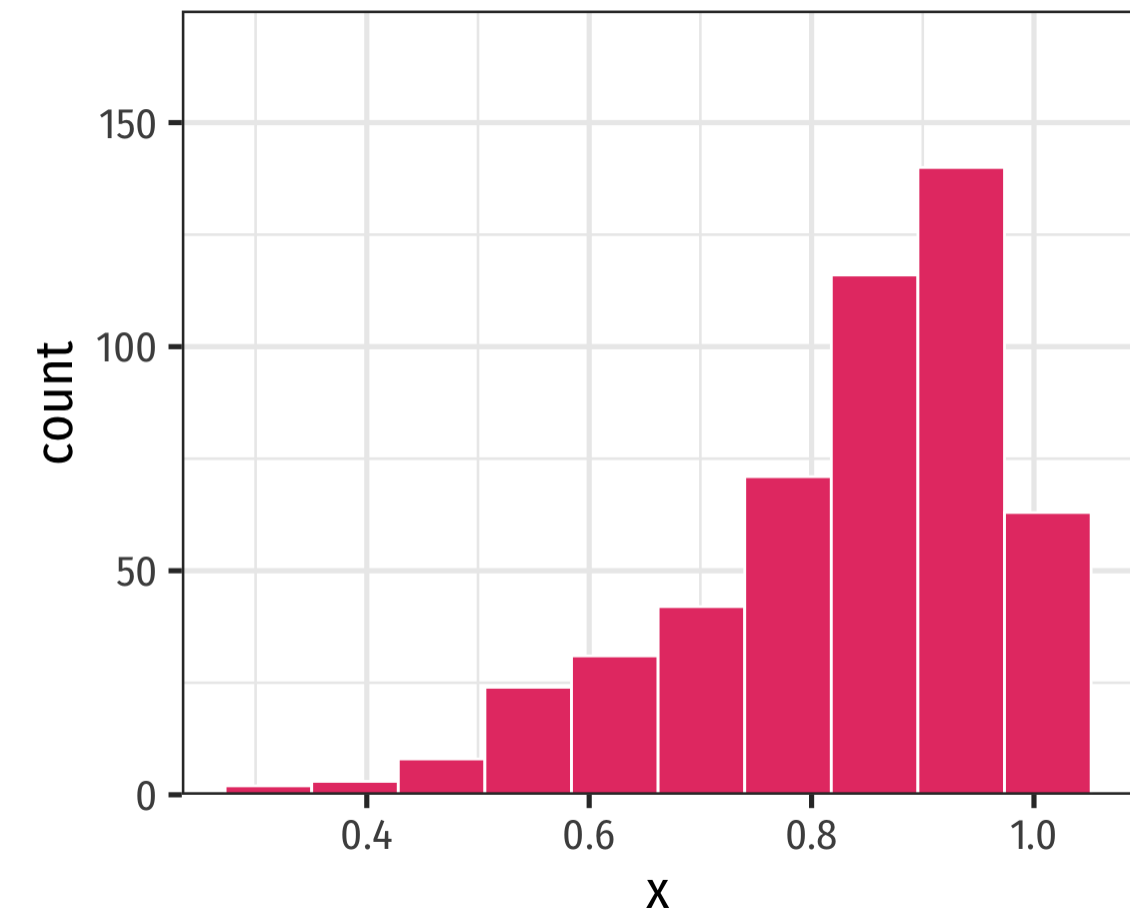
Symmetry and Skew I

- A distribution is **symmetric** if it looks roughly the same on either side of the “center”
- The thinner ends (far left and far right) are called the **tails** of a distribution



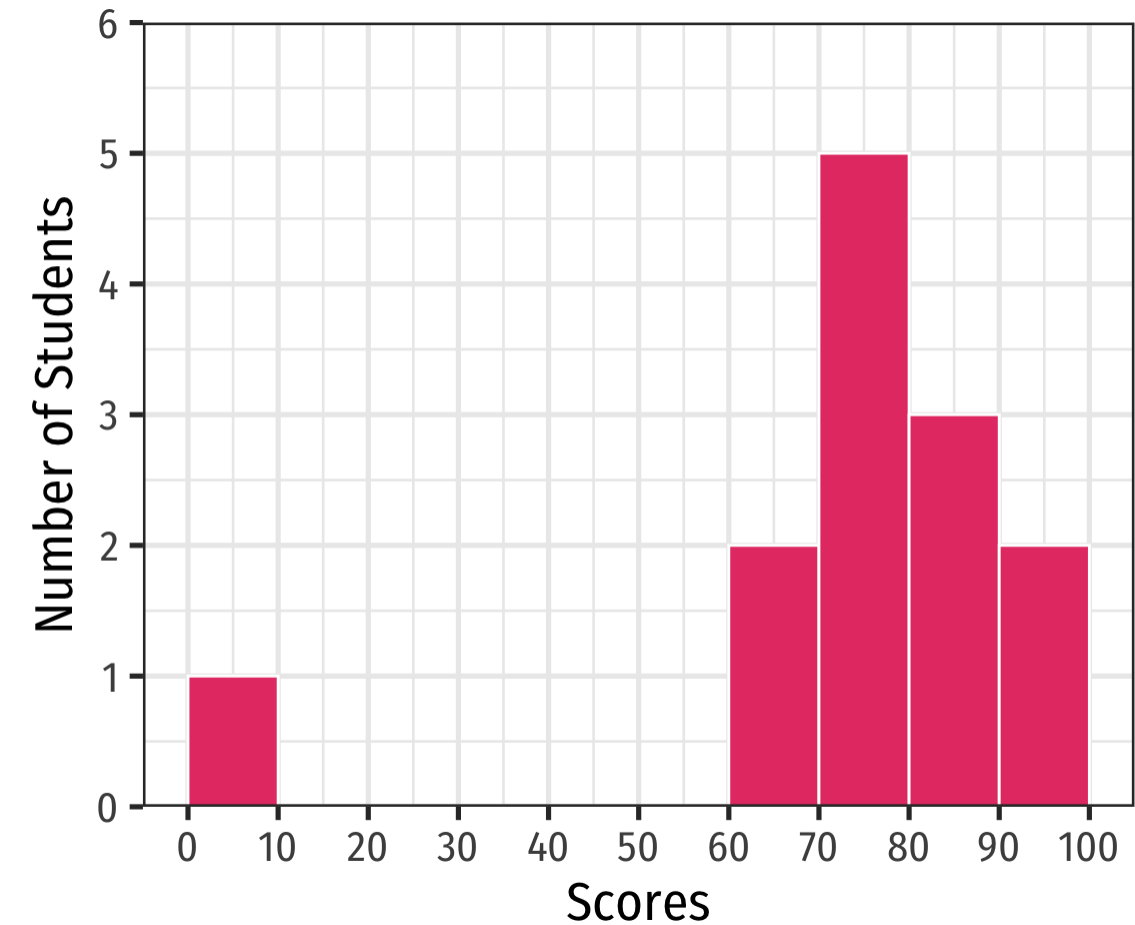
Symmetry and Skew I

- If one tail stretches farther than the other, distribution is **skewed** in the direction of the longer tail
 - In this example, skewed to the **left**



Outliers

- **Outlier**: “extreme” value that does not appear part of the general pattern of a distribution
- Can strongly affect descriptive statistics
- Might be the most informative part of the data
- Could be the result of errors
- Should always be explored and discussed!



Arithmetic Mean (Population)

- The natural measure of the center of a *population's* distribution is its “average” or **arithmetic mean μ**

$$\mu = \frac{x_1 + x_2 + \dots + x_N}{N} = \frac{1}{N} \sum_{i=1}^N x_i$$

- For N values of variable x , “mu” is the sum of all individual x values (x_i) from 1 to N , divided by the N number of values¹
- See **today's appendix** for more about the **summation operator**, \sum , it'll come up again!

¹ Note the mean need not be an actual value of the data!



Arithmetic Mean (Sample)

- When we have a *sample*, we compute the **sample mean \bar{x}**

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

- For n values of variable x , “x-bar” is the sum of all individual x values (x_i) divided by the n number of values



Arithmetic Mean (Sample)

Example

{0, 62, 66, 71, 71, 74, 76, 79, 83, 86, 88, 93, 95}

$$\bar{x} = \frac{1}{13}(0 + 62 + 66 + 71 + 71 + 74 + 76 + 79 + 83 + 86 + 88 + 93 + 95)$$

$$\bar{x} = \frac{944}{13}$$

$$\bar{x} = 72.62$$

```
1 quizzes %>%
2   summarize(mean = mean(scores))
```

```
# A tibble: 1 × 1
  mean
<dbl>
1  72.6
```



Arithmetic Mean: Affected by Outliers

- If we drop the outlier (0)

Example

{62, 66, 71, 71, 74, 76, 79, 83, 86, 88, 93, 95}

$$\begin{aligned}\bar{x} &= \frac{1}{12}(62 + 66 + 71 + 71 + 74 + 76 + 79 + 83 + 86 + 88 + 93 + 95) \\ &= \frac{944}{12} \\ &= 78.67\end{aligned}$$

```
1 quizzes %>%
2   filter(scores > 0) %>%
3   summarize(mean = mean(scores))
```

```
# A tibble: 1 × 1
  mean
  <dbl>
1  78.7
```



Median

$\{0, 62, 66, 71, 71, 74, \mathbf{76}, 79, 83, 86, 88, 93, 95\}$

- The **median** is the midpoint of the distribution
 - 50% to the left of the median, 50% to the right of the median
- Arrange values in numerical order
 - For odd n : median is middle observation
 - For even n : median is average of two middle observations



Mean, Median, and Outliers



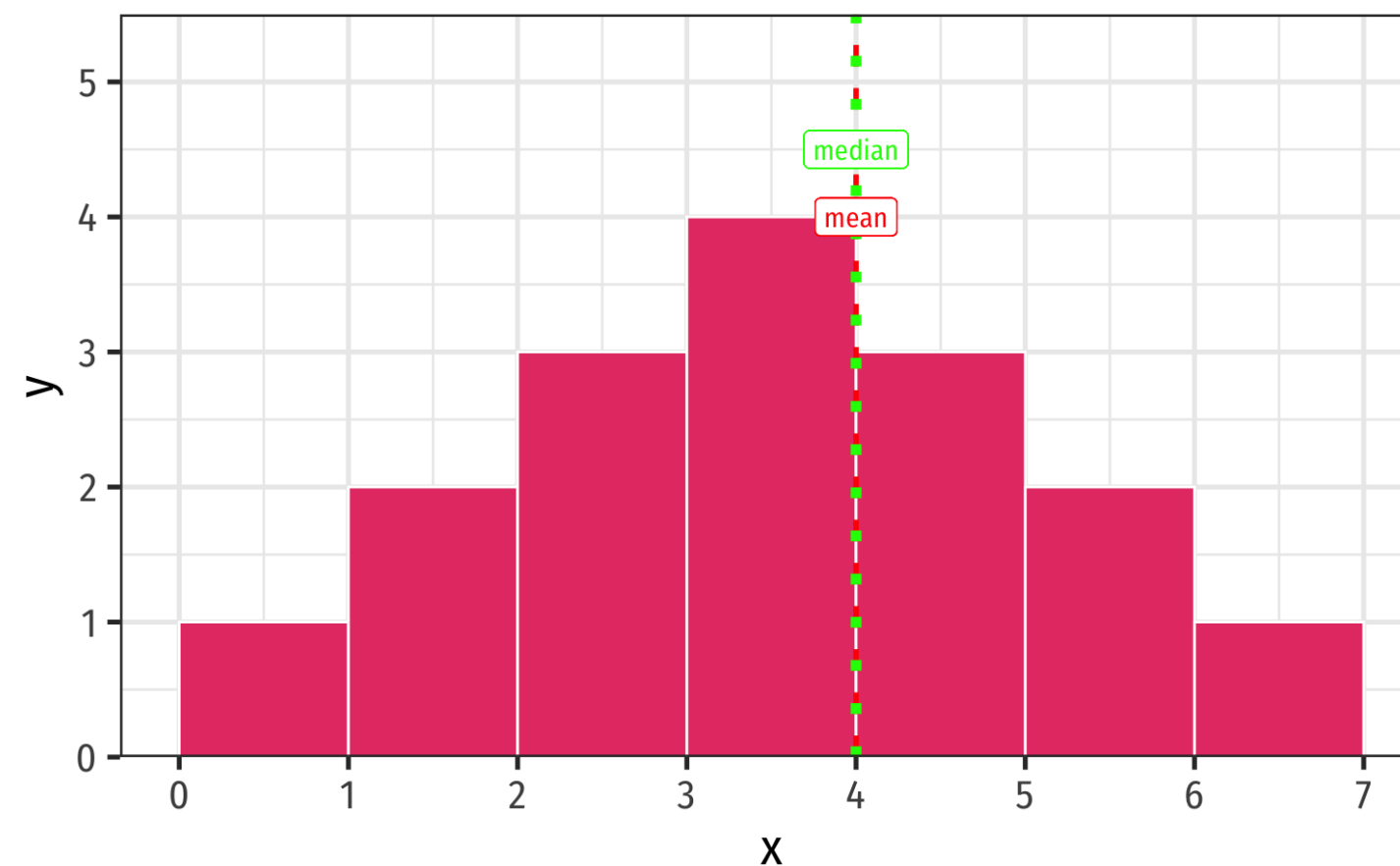
Mean, Median, Symmetry, & Skew I

- Symmetric distribution: mean \approx median

```
1 symmetric %>%
2   summarize(mean = mean(x),
3             median = median(x))
```

A tibble: 1 × 2

	mean	median
	<dbl>	<dbl>
1	4	4



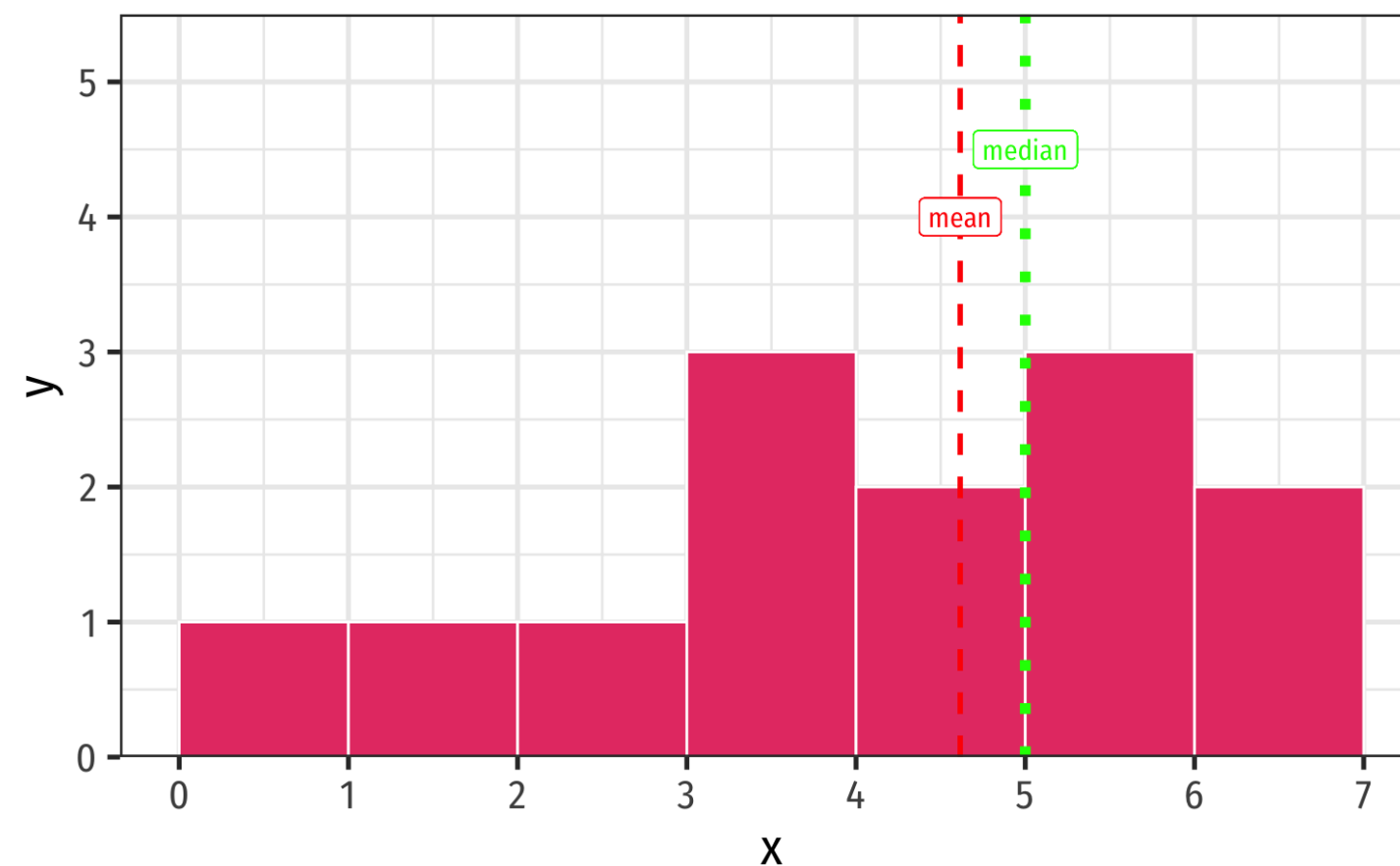
Mean, Median, Symmetry, & Skew II

- Left-skewed: $\text{mean} < \text{median}$

```
1 leftskew %>%
2   summarize(mean = mean(x),
3             median = median(x))
```

A tibble: 1 × 2

	mean	median
	<dbl>	<dbl>
1	4.62	5



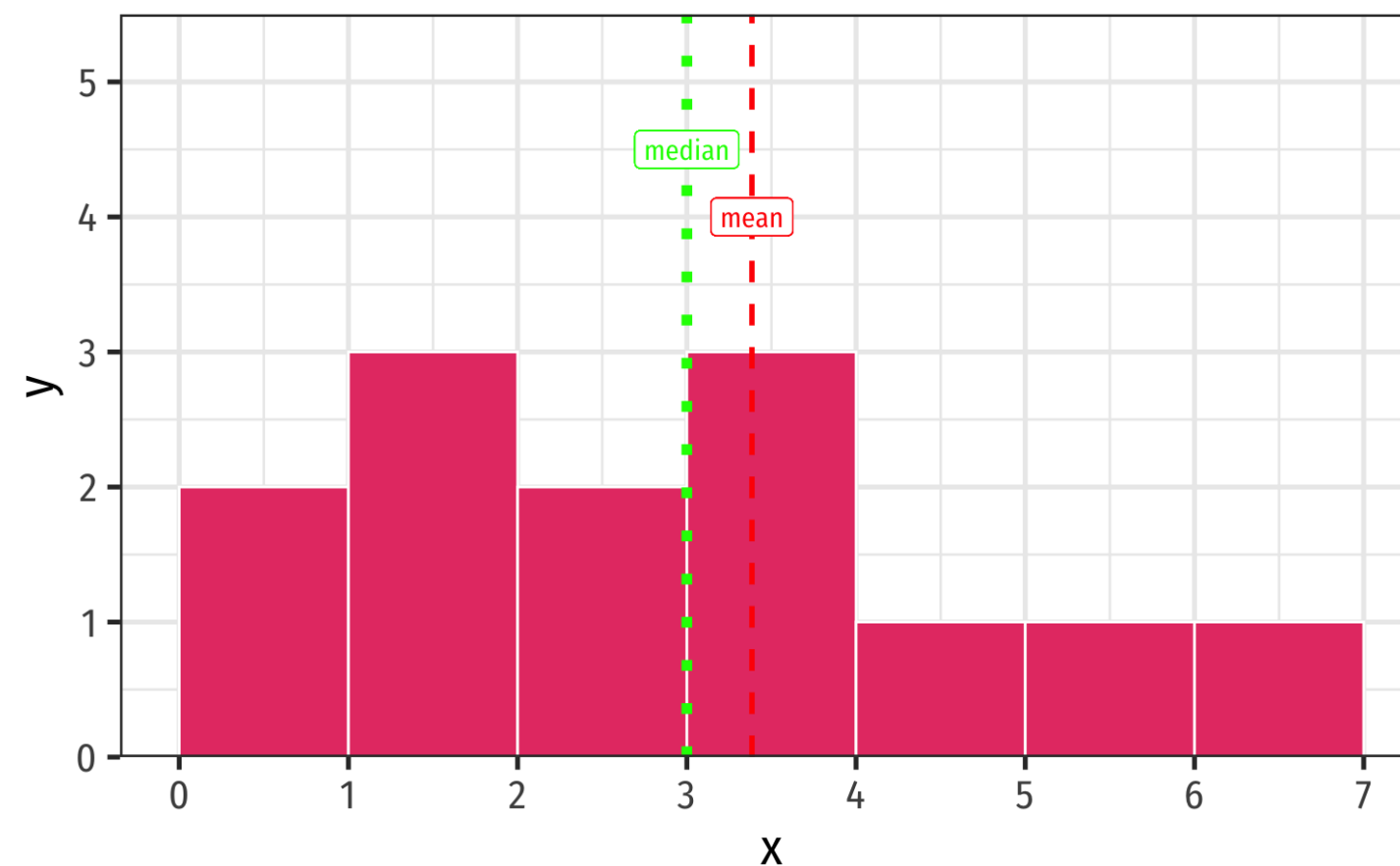
Mean, Median, Symmetry, & Skew III

- Right-skewed: $\text{mean} > \text{median}$

```
1 rightskew %>%
2   summarize(mean = mean(x),
3             median = median(x))
```

A tibble: 1 × 2

	mean	median
	<dbl>	<dbl>
1	3.38	3



Measures of Dispersion



Range

- The more *variation* in the data, the less helpful a measure of central tendency will tell us
- Beyond just the center, we also want to measure the spread
- Simplest metric is **range** = $\text{max} - \text{min}$



Five Number Summary I

- Common set of summary statistics of a distribution: **“five number summary”**:

1. Minimum value
2. 25th percentile (Q_1 , median of first 50% of data)
3. 50th percentile (median, Q_2)
4. 75th percentile (Q_3 , median of last 50% of data)
5. Maximum value

```
1 # Base R summary command (includes Mean)
2 summary(quizzes$scores)
```

```
      Min. 1st Qu.  Median    Mean 3rd Qu.
Max.
 0.00   71.00   76.00   72.62   86.00
95.00
```

```
1 quizzes %>% # dplyr
2   summarize(Min = min(scores),
3             Q1 = quantile(scores, 0.25),
4             Median = median(scores),
5             Q3 = quantile(scores, 0.75),
6             Max = max(scores))
```

```
# A tibble: 1 × 5
   Min    Q1 Median    Q3    Max
<dbl> <dbl> <dbl> <dbl> <dbl>
1     0    71    76    86    95
```



Five Number Summary II

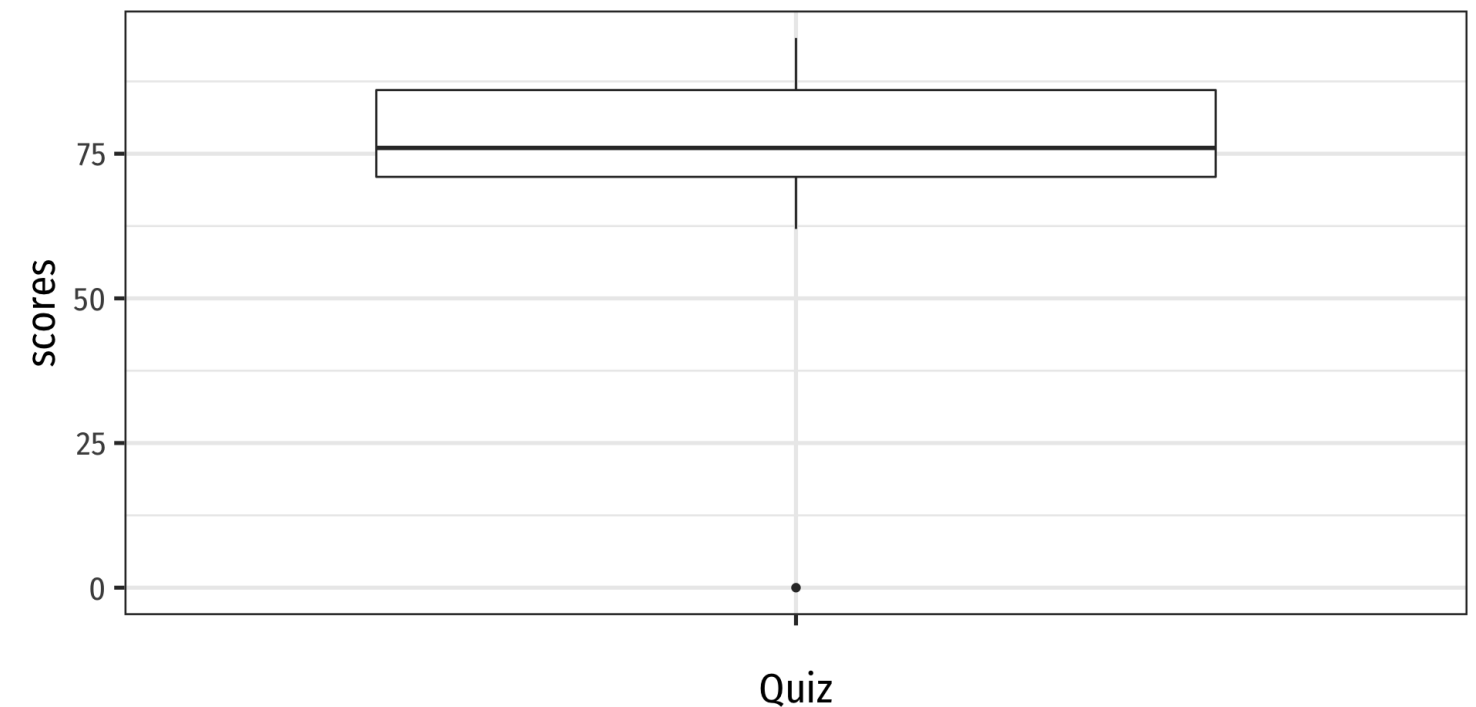
- The n^{th} **percentile** of a distribution is the value that places n percent of values beneath it

```
1 quizzes %>%  
2   summarize("37th percentile" = quantile(scores,0.37))  
  
# A tibble: 1 × 1  
  `37th percentile`  
      <dbl>  
1             72.3
```



Boxplot I

- **Boxplots** are a great way to visualize the 5 number summary
- **Height of box:** Q_1 to Q_3 (known as **interquartile range (IQR)**, middle 50% of data)
- **Line inside box:** median (50th percentile)
- **“Whiskers”** identify data within $1.5 \times IQR$
- Points *beyond* whiskers are **outliers**
 - common definition: Outlier $> 1.5 \times IQR$



Boxplot Comparisons I

- Boxplots (and five number summaries) are great for comparing two distributions

Example

Quiz 1 : {0, 62, 66, 71, 71, 74, 76, 79, 83, 86, 88, 93, 95}

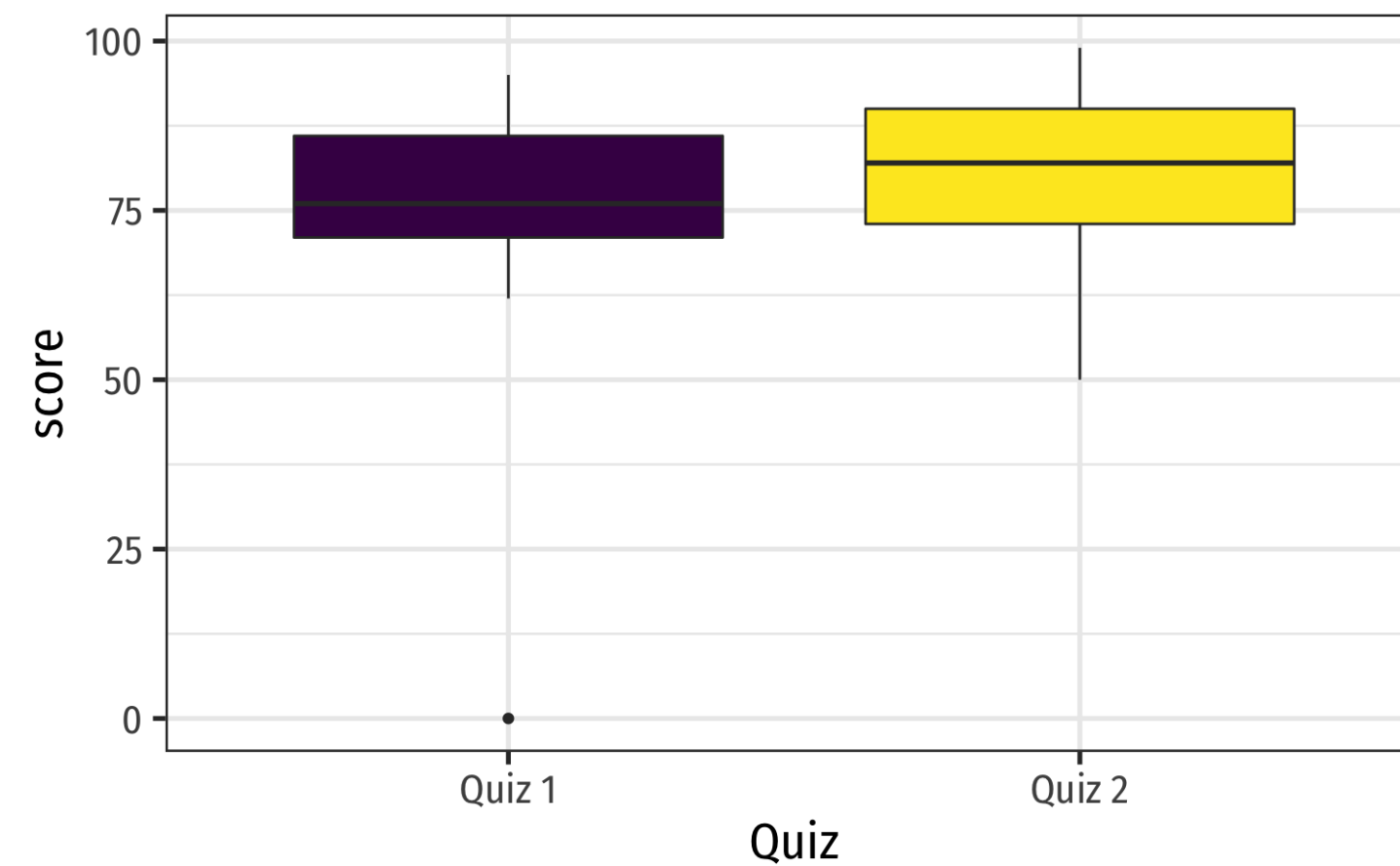
Quiz 2 : {50, 62, 72, 73, 79, 81, 82, 82, 86, 90, 94, 98, 99}



Boxplot Comparisons II

```
1 quizzes_new %>% summary()
```

student	quiz_1	quiz_2
Min. : 1	Min. : 0.00	Min. : 50.00
1st Qu.: 4	1st Qu.: 71.00	1st Qu.: 73.00
Median : 7	Median : 76.00	Median : 82.00
Mean : 7	Mean : 72.62	Mean : 80.62
3rd Qu.: 10	3rd Qu.: 86.00	3rd Qu.: 90.00
Max. : 13	Max. : 95.00	Max. : 99.00



Aside: Making Nice Summary Tables I

- I don't like the options available for printing out summary statistics
 - So I wrote my own R function called `summary_table()` that makes nice summary tables (it uses `dplyr` and `tidyr`!). To use:
1. Download the `summaries.R` file from the website¹ and move it to your working directory/project folder
 2. Load the function with the `source()` command:²

```
1 source("summaries.R")
```

1. One day I'll make this part of a package I'll write.

2. If it was a package, then you'd load with `library()`. But you can run a single R script with `source()`.



Aside: Making Nice Summary Tables II

3. The function has at least 2 arguments: the `data.frame` (automatically piped in if you use the pipe!) and then all variables you want to summarize, separated by commas¹

```
1 mpg %>%
2   summary_table(hwy, cty, cyl)
```

A tibble: 3 × 9

	Variable	Obs	Min	Q1	Median	Q3	Max	Mean	Std. Dev.
	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	cty	234	9	14	17	19	35	16.9	4.26
2	cyl	234	4	4	6	8	8	5.89	1.61
3	hwy	234	12	18	24	27	44	23.4	5.95

1. There is one restriction: No variable name can have an underscore (`_`) in it. You will have to rename them or else you will break the function!



Aside: Making Nice Summary Tables III

4. When rendered in Quarto, it looks nicer:

```
1 mpg %>%
2   summary_table(hwy, cty, cyl) %>%
3   knitr::kable(., format="html")
```

Variable	Obs	Min	Q1	Median	Q3	Max	Mean	Std. Dev.
cty	234	9	14	17	19	35	16.86	4.26
cyl	234	4	4	6	8	8	5.89	1.61
hwy	234	12	18	24	27	44	23.44	5.95



Measures of Dispersion: Deviations

- Every observation i **deviates** from the mean of the data:

$$deviation_i = x_i - \mu$$

- There are as many deviations as there are data points (n)
- We can measure the *average* or **standard deviation** of a variable from its mean
- Before we get there...



Variance (Population)

- The **population variance σ^2** of a *population* distribution measures the average of the *squared* deviations from the *population* mean (μ)

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2$$

- Why do we square deviations?
- What are these units?



Standard Deviation (Population)

- Square root the variance to get the **population standard deviation** σ , the average deviation from the population mean (in same units as x)

$$\sigma = \sqrt{\sigma^2} = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2}$$



Variance (Sample)

- The **sample variance** s^2 of a *sample* distribution measures the average of the *squared* deviations from the *sample* mean (\bar{x})

$$s^2 = \frac{1}{n - 1} \sum_{i=1}^n (x_i - \bar{x})^2$$

- Why do we divide by $n - 1$?



Standard Deviation (Sample)

- Square root the sample variance to get the **sample standard deviation s** , the average deviation from the *sample* mean (in same units as x)

$$s = \sqrt{s^2} = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$



Sample Standard Deviation: Example

Example

Calculate the sample standard deviation for the following series:

$\{2, 4, 6, 8, 10\}$

```
1 sd(c(2,4,6,8,10))
```

```
[1] 3.162278
```



The Steps to Calculate `sd()`, Coded I

```
1 # first let's save our data in a tibble
2 sd_example <- tibble(x = c(2,4,6,8,10))
```

```
1 # first find the mean (just so we know)
2
3 sd_example %>%
4   summarize(mean(x))
```

```
# A tibble: 1 × 1
  `mean(x)`
  <dbl>
1         6
```

```
1 # now let's make some more columns:
2 sd_example <- sd_example %>%
3   mutate(deviations = x - mean(x), # take deviations from mean
4          deviations_sq = deviations^2) # square them
```



The Steps to Calculate `sd()`, Coded II

```
1 sd_example # see what we made
```

```
# A tibble: 5 × 3
```

	x	deviations	deviations_sq
	<dbl>	<dbl>	<dbl>
1	2	-4	16
2	4	-2	4
3	6	0	0
4	8	2	4
5	10	4	16



The Steps to Calculate `sd()`, Coded III

```

1 sd_example %>%
2   # sum the squared deviations
3   summarize(sum_sq_devs = sum(deviations_sq),
4             # divide by n-1 to get variance
5             variance = sum_sq_devs/(n()-1),
6             # square root to get sd
7             std_dev = sqrt(variance))

```

```

# A tibble: 1 × 3
  sum_sq_devs variance std_dev
    <dbl>      <dbl>   <dbl>
1         40         10     3.16

```



Sample Standard Deviation: You Try

Example

Calculate the sample standard deviation for the following series:

$\{1, 3, 5, 7\}$

```
1 sd(c(1, 3, 5, 7))
```

```
[1] 2.581989
```



Descriptive Statistics: Populations vs. Samples

Population parameters

- **Population size:** N

- **Mean:** μ

- **Variance:** $\sigma^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2$

- **Standard deviation:** $\sigma = \sqrt{\sigma^2}$

Sample statistics

- **Population size:** n

- **Mean:** \bar{x}

- **Variance:** $s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$

- **Standard deviation:** $s = \sqrt{s^2}$

