## R Notebook

```
library(readxl)
Tng_Ctr_Hour2 <- read_excel("C:/RBS/Business Forecasting/Group Project/Final Project/Tng_Ctr_Hour2.xlsx</pre>
View(Tng_Ctr_Hour2)
library(data.table)
library(ggplot2)
library(stringr)
library(TTR)
library(fpp)
## Loading required package: forecast
## Registered S3 method overwritten by 'quantmod':
##
     method
##
     as.zoo.data.frame zoo
## Loading required package: fma
## Loading required package: expsmooth
## Loading required package: lmtest
## Loading required package: zoo
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: tseries
library(fpp2)
## Attaching package: 'fpp2'
## The following objects are masked from 'package:fpp':
##
       ausair, ausbeer, austa, austourists, debitcards, departures,
##
##
       elecequip, euretail, guinearice, oil, sunspotarea, usmelec
```

```
library(ggplot2)
library(stats)
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:data.table':
##
##
      between, first, last
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
      intersect, setdiff, setequal, union
library(graphics)
library(ggfortify)
## Registered S3 methods overwritten by 'ggfortify':
##
    method
                           from
##
    autoplot.Arima
                           forecast
##
    autoplot.acf
                           forecast
##
    autoplot.ar
                           forecast
##
    autoplot.bats
                           forecast
    autoplot.decomposed.ts forecast
##
    autoplot.ets
                           forecast
##
    autoplot.forecast forecast
##
    autoplot.stl
                         forecast
##
    autoplot.ts
                         forecast
##
    fitted.ar
                           forecast
    fortify.ts
##
                           forecast
    residuals.ar
                           forecast
setDT(Tng_Ctr_Hour2)
Tng_Ctr_Hour2[,Quarter:=factor(Quarter)]
Tng_Ctr_Hour2[,Month:=factor(Month)]
Tng_Ctr_Hour2[,Year:=factor(Year)]
```

# Multiple Regression Analysis

```
setDT(Tng_Ctr_Hour2)
class(Tng_Ctr_Hour2)
```

```
## [1] "data.table" "data.frame"
```

```
Tng_Ctr_Hour2[,RPM:=shift(RPM, n=2)]
Tng_Ctr_Hour2[,NJURN:=shift(NJURN, n=1)]
Tng_Ctr_Hour2[,Cons_Sent:=shift(Cons_Sent, n=2)]
head(Tng_Ctr_Hour2)
```

```
##
                 Yr Quarter Month Device_Hrs DH_Prev_Year DH_YoY_Change
         Year
## 1: 2015-01 2015
                         Q1
                              Jan
                                       960.42
                                                         NA
## 2: 2015-02 2015
                         Q1
                              Feb
                                       944.08
                                                         NA
                                                                        NA
## 3: 2015-03 2015
                                                                        NA
                         Q1
                              Mar
                                      1429.12
                                                         NA
## 4: 2015-04 2015
                         Q2
                                                                        NA
                              Apr
                                      1097.00
                                                         NA
## 5: 2015-05 2015
                         02
                                                                        NA
                              May
                                       915.85
                                                         NA
## 6: 2015-06 2015
                         Q2
                              Jun
                                       783.45
                                                         NA
                                                                        NA
      DH_YoY_Ch_Per Total_Inst_Hrs Total_Inst_Hrs_Prev_Year Inst_Hrs_YoY_Change
                            1700.67
## 1:
                 NA
                                                            NA
## 2:
                 NA
                            1614.00
                                                            NA
                                                                                 NA
## 3:
                                                            NA
                 NA
                            2532.90
                                                                                 NA
## 4:
                 NA
                            2152.25
                                                            NΑ
                                                                                 NΑ
## 5:
                 NA
                            1695.43
                                                            NA
                                                                                 NA
## 6:
                 NA
                            1675.91
                                                            NΑ
                                                                                 NA
##
      Total_Inst_Hrs_YoY_Change_Per2 Cons_Sent NJURN
                                                             RPM CPIUrban CPIMedian
                                                                  234.747
## 1:
                                    NA
                                              NA
                                                     NA
                                                              NA
                                                                           1.947530
## 2:
                                    NA
                                              NA
                                                    6.8
                                                              NA
                                                                  235.342
                                                                            1.954495
                                    NA
                                                                  235.976
## 3:
                                            98.1
                                                    6.7 65975447
                                                                            2.433336
## 4:
                                    NA
                                            95.4
                                                    6.3 59784666
                                                                  236.222
                                                                            2.962651
                                                    5.8 75751609
## 5:
                                    NA
                                            93.0
                                                                  237.001
                                                                            2.501291
## 6:
                                                    6.0 73090871
                                                                  237.657
                                    NA
                                            95.9
                                                                            2.972400
```

#### head(Tng\_Ctr\_Hour2)

```
##
                 Yr Quarter Month Device_Hrs DH_Prev_Year DH_YoY_Change
         Year
## 1: 2015-01 2015
                         Q1
                              Jan
                                       960.42
                                                         NA
## 2: 2015-02 2015
                                       944.08
                         Q1
                              Feb
                                                                        NA
                                                         NA
## 3: 2015-03 2015
                         Q1
                              Mar
                                      1429.12
                                                         NA
                                                                        NA
## 4: 2015-04 2015
                         Q2
                              Apr
                                      1097.00
                                                         NA
                                                                        NA
## 5: 2015-05 2015
                         Q2
                              May
                                       915.85
                                                         NA
                                                                        NA
## 6: 2015-06 2015
                                       783.45
                         Q2
                              Jun
                                                         NA
                                                                        NA
      DH_YoY_Ch_Per Total_Inst_Hrs Total_Inst_Hrs_Prev_Year Inst_Hrs_YoY_Change
##
## 1:
                 NA
                            1700.67
                                                            NA
                                                                                 NA
## 2:
                 NA
                            1614.00
                                                            NA
                                                                                 NA
## 3:
                 NA
                            2532.90
                                                            NA
                                                                                 NA
## 4:
                 NA
                            2152.25
                                                            NA
                                                                                 NA
## 5:
                 NA
                                                            NA
                            1695.43
                                                                                 NΑ
## 6:
                            1675.91
                                                            NA
                                                                                 NA
                 NA
      Total Inst Hrs YoY Change Per2 Cons Sent NJURN
##
                                                             RPM CPIUrban CPIMedian
## 1:
                                    NA
                                              NA
                                                     NA
                                                              NA
                                                                  234.747 1.947530
## 2:
                                    NA
                                              NA
                                                    6.8
                                                              NA
                                                                  235.342 1.954495
## 3:
                                    NA
                                            98.1
                                                    6.7 65975447
                                                                  235.976
                                                                            2.433336
## 4:
                                    NA
                                            95.4
                                                    6.3 59784666
                                                                  236.222
                                                                            2.962651
## 5:
                                                                  237.001
                                    NA
                                            93.0
                                                    5.8 75751609
                                                                            2.501291
## 6:
                                    NA
                                            95.9
                                                    6.0 73090871 237.657
                                                                            2.972400
```

```
Tng_Ctr_Hour2[, Quarter := factor(Quarter, ordered = T)]
Tng_Ctr_Hour2[, Month := factor(Month, ordered = T)]
summary(Tng_Ctr_Hour2)
##
         Year
                      Yr
                                    Quarter
                                                 Month
                                                            Device_Hrs
##
   2015-01: 1
                                    Q1:21
                                                    : 7
                                                                 : 222.8
                 Length:81
                                            Apr
                                                          Min.
   2015-02: 1
                 Class :character
                                    Q2:21
                                                    : 7
                                                          1st Qu.: 899.0
##
                                            Aug
## 2015-03: 1
                 Mode :character
                                    Q3:21
                                            Feb
                                                    : 7
                                                          Median :1008.0
## 2015-04: 1
                                                                : 990.1
                                    Q4:18
                                            Jan
                                                    : 7
                                                          Mean
## 2015-05: 1
                                                    : 7
                                            Jul
                                                          3rd Qu.:1101.7
## 2015-06: 1
                                                    : 7
                                                         Max.
                                            Jun
                                                                 :1519.9
                                             (Other):39
## (Other):75
## DH_Prev_Year
                       DH_YoY_Change
                                          DH_YoY_Ch_Per
                                                              Total_Inst_Hrs
## Length:81
                                                              Min. : 504.6
                       Length:81
                                          Length:81
## Class :character
                       Class :character
                                          Class :character
                                                              1st Qu.:1937.3
##
   Mode :character
                       Mode :character
                                          Mode :character
                                                              Median :2203.2
##
                                                              Mean
                                                                    :2165.7
##
                                                              3rd Qu.:2446.8
##
                                                              Max.
                                                                     :3084.1
##
##
   Total_Inst_Hrs_Prev_Year Inst_Hrs_YoY_Change Total_Inst_Hrs_YoY_Change_Per2
##
   Length:81
                             Length:81
                                                  Length:81
##
   Class : character
                             Class : character
                                                  Class : character
   Mode :character
                             Mode :character
                                                 Mode :character
##
##
##
##
##
      Cons_Sent
                         NJURN
                                           RPM
                                                              CPIUrban
##
   Min. : 71.80
                     Min.
                            : 2.900
                                             : 2908236
                                                           Min.
                                                                  :234.7
                                      Min.
   1st Qu.: 89.45
                     1st Qu.: 4.075
                                                           1st Qu.:241.2
                                      1st Qu.: 68377378
  Median : 93.80
                     Median : 4.850
                                      Median : 77274227
                                                           Median :250.8
                           : 5.607
## Mean
         : 92.00
                     Mean
                                      Mean
                                             : 70811208
                                                           Mean
                                                                  :250.2
##
   3rd Qu.: 97.95
                     3rd Qu.: 6.225
                                      3rd Qu.: 85417423
                                                           3rd Qu.:257.4
          :101.40
                           :16.600
                                      Max.
                                                           Max.
                                                                  :274.1
##
  {\tt Max.}
                     Max.
                                             :101794185
##
  NA's
           :2
                     NA's
                                      NA's
                            :1
                                             :2
##
      CPIMedian
           :0.9755
##
  \mathtt{Min}.
  1st Qu.:2.1551
  Median :2.5922
##
## Mean
          :2.5862
##
   3rd Qu.:2.9557
## Max.
           :5.5690
##
str(Tng_Ctr_Hour2)
## Classes 'data.table' and 'data.frame':
                                            81 obs. of 17 variables:
## $ Year
                                     : Factor w/ 81 levels "2015-01", "2015-02",...: 1 2 3 4 5 6 7 8 9 10
```

: chr "2015" "2015" "2015" "2015" ...

: Ord.factor w/ 4 levels "Q1"<"Q2"<"Q3"<...: 1 1 1 2 2 2 3 3 3 4 ...

: Ord.factor w/ 12 levels "Apr"<"Aug"<"Dec"<...: 5 4 8 1 9 7 6 2 12

## \$ Yr

## \$ Quarter

## \$ Month

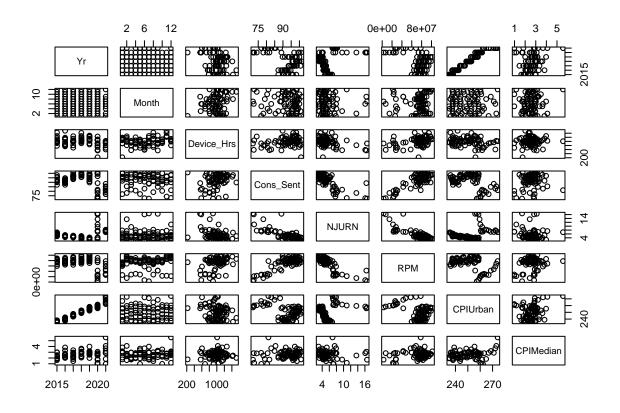
```
## $ Device Hrs
                                        960 944 1429 1097 916 ...
                                 : num
## $ DH_Prev_Year
                                 : chr
                                        "NA" "NA" "NA" "NA" ...
                                        "NA" "NA" "NA" "NA" ...
## $ DH_YoY_Change
                                 : chr
## $ DH_YoY_Ch_Per
                                        "NA" "NA" "NA" "NA" ...
                                 : chr
## $ Total_Inst_Hrs
                                 : num 1701 1614 2533 2152 1695 ...
## $ Total Inst Hrs Prev Year
                                       "NA" "NA" "NA" "NA" ...
                                 : chr
## $ Inst_Hrs_YoY_Change
                                        "NA" "NA" "NA" "NA" ...
                                  : chr
## $ Total_Inst_Hrs_YoY_Change_Per2: chr
                                        "NA" "NA" "NA" "NA" ...
## $ Cons Sent
                                  : num
                                        NA NA 98.1 95.4 93 95.9 90.7 96.1 93.1 91.9 ...
## $ NJURN
                                  : num
                                        NA 6.8 6.7 6.3 5.8 6 5.9 6.2 5.5 5.1 ...
                                  : num NA NA 65975447 59784666 75751609 ...
## $ RPM
## $ CPIUrban
                                        235 235 236 236 237 ...
                                  : num
                                  : num 1.95 1.95 2.43 2.96 2.5 ...
## $ CPIMedian
## - attr(*, ".internal.selfref")=<externalptr>
Mach1 = subset(Tng_Ctr_Hour2, select = c(Yr, Month, Device_Hrs, Cons_Sent, NJURN, RPM, CPIUrban, CPIMed
Mach1$Yr = as.numeric(Mach1$Yr)
class(Mach1$Yr)
## [1] "numeric"
str(Mach1)
## Classes 'data.table' and 'data.frame': 81 obs. of 8 variables:
              : num 2015 2015 2015 2015 2015 ...
              : Ord.factor w/ 12 levels "Apr"<"Aug"<"Dec"<...: 5 4 8 1 9 7 6 2 12 11 ...
## $ Device_Hrs: num 960 944 1429 1097 916 ...
## $ Cons_Sent : num NA NA 98.1 95.4 93 95.9 90.7 96.1 93.1 91.9 ...
## $ NJURN : num NA 6.8 6.7 6.3 5.8 6 5.9 6.2 5.5 5.1 ...
              : num NA NA 65975447 59784666 75751609 ...
## $ CPIUrban : num 235 235 236 236 237 ...
   $ CPIMedian : num 1.95 1.95 2.43 2.96 2.5 ...
## - attr(*, ".internal.selfref")=<externalptr>
summary(Mach1)
##
                     Month
                                Device_Hrs
                                                Cons_Sent
                                                                  NJURN
## Min. :2015
                      : 7
                              Min. : 222.8
                                              Min. : 71.80
                                                              Min. : 2.900
                 Apr
  1st Qu.:2016
                        : 7
                             1st Qu.: 899.0
                                              1st Qu.: 89.45
                                                              1st Qu.: 4.075
                 Aug
## Median :2018
                 Feb
                        : 7
                              Median :1008.0
                                              Median : 93.80
                                                              Median: 4.850
                        : 7
## Mean :2018
                 Jan
                             Mean : 990.1
                                              Mean : 92.00
                                                              Mean : 5.607
                        : 7
##
   3rd Qu.:2020
                 Jul
                              3rd Qu.:1101.7
                                              3rd Qu.: 97.95
                                                              3rd Qu.: 6.225
                      : 7
## Max. :2021
                  Jun
                             Max. :1519.9
                                              Max. :101.40
                                                              Max. :16.600
                                                              NA's :1
##
                  (Other):39
                                              NA's :2
        RPM
                         CPIUrban
                                      CPIMedian
                      Min. :234.7 Min. :0.9755
## Min. : 2908236
## 1st Qu.: 68377378 1st Qu.:241.2 1st Qu.:2.1551
## Median : 77274227
                      Median :250.8 Median :2.5922
## Mean : 70811208 Mean :250.2 Mean :2.5862
```

```
## 3rd Qu.: 85417423 3rd Qu.:257.4 3rd Qu.:2.9557
## Max. :101794185 Max. :274.1 Max. :5.5690
```

## NA's :2

#### TrainMach = Mach1

## pairs(TrainMach)



### TrainMach\$Yr[TrainMach\$Yr >= 2020] <- NA</pre>

## summary(TrainMach)

Median : 77274227

```
##
         Yr
                      Month
                                 Device_Hrs
                                                  Cons_Sent
                                                                      NJURN
                                      : 222.8
                                                 Min. : 71.80
##
   Min.
          :2015
                          : 7
                               Min.
                                                                  Min. : 2.900
                   Apr
                                                 1st Qu.: 89.45
##
   1st Qu.:2016
                  Aug
                          : 7
                               1st Qu.: 899.0
                                                                  1st Qu.: 4.075
   Median:2017
                          : 7
                               Median :1008.0
                                                 Median : 93.80
                                                                  Median : 4.850
##
                  Feb
   Mean
         :2017
                   Jan
                          : 7
                               Mean
                                      : 990.1
                                                 Mean
                                                       : 92.00
                                                                  Mean : 5.607
                          : 7
                                                                  3rd Qu.: 6.225
##
   3rd Qu.:2018
                               3rd Qu.:1101.7
                                                 3rd Qu.: 97.95
                   Jul
##
   Max.
          :2019
                   Jun
                          : 7
                               Max.
                                      :1519.9
                                                 Max.
                                                        :101.40
                                                                  Max.
                                                                        :16.600
          :21
                                                                  NA's
##
   NA's
                   (Other):39
                                                 NA's
                                                        :2
                                                                        :1
##
        RPM
                           CPIUrban
                                         CPIMedian
##
   Min. : 2908236
                       Min.
                              :234.7
                                       Min. :0.9755
##
   1st Qu.: 68377378
                       1st Qu.:241.2
                                       1st Qu.:2.1551
```

Median :250.8

Median :2.5922

```
## Mean
           : 70811208
                        Mean
                               :250.2
                                        Mean
                                               :2.5862
                        3rd Qu.:257.4
## 3rd Qu.: 85417423
                                        3rd Qu.:2.9557
## Max.
           :101794185
                        Max.
                               :274.1
                                        Max.
                                              :5.5690
## NA's
           :2
TrainMach = na.omit(TrainMach)
summary(TrainMach)
##
          Yr
                       Month
                                  Device_Hrs
                                                   Cons_Sent
                                                                      NJURN
  Min.
           :2015
                          : 5
                                       : 693.3
                                                       : 87.20
                                                                  Min.
                                                                         :2.900
                   Apr
                                Min.
                                                 Min.
   1st Qu.:2016
                          : 5
                                                 1st Qu.: 92.15
                                1st Qu.: 963.8
                                                                  1st Qu.:3.900
                   Aug
## Median :2017
                          : 5
                                Median :1041.0
                                                 Median : 95.80
                                                                  Median :4.500
                   Dec
                          : 5
                               Mean
## Mean
          :2017
                                       :1051.1
                                                 Mean : 95.08
                                                                  Mean
                   Jul
                                                                         :4.497
   3rd Qu.:2018
                   Jun
                          : 5
                                3rd Qu.:1139.1
                                                 3rd Qu.: 98.17
                                                                  3rd Qu.:5.075
##
  Max. :2019
                   Mar
                          : 5
                               Max.
                                       :1519.9
                                                 Max.
                                                       :101.40
                                                                  Max.
                                                                         :6.700
##
                   (Other):28
        RPM
##
                           CPIUrban
                                          CPIMedian
          : 59784666
                               :236.0
   Min.
                        Min.
                                        Min.
                                              :1.465
   1st Qu.: 74902332
                        1st Qu.:239.7
                                        1st Qu.:2.233
##
## Median : 80129218
                       Median :244.7
                                        Median :2.588
## Mean : 80977423
                        Mean :246.1
                                        Mean
                                              :2.605
## 3rd Qu.: 87364404
                        3rd Qu.:252.4
                                        3rd Qu.:2.959
## Max. :101794185
                        Max.
                              :258.2
                                        Max.
                                              :3.975
##
LM_Mach = lm(Device_Hrs ~ .-Yr, TrainMach)
summary(LM_Mach )
##
## Call:
## lm(formula = Device_Hrs ~ . - Yr, data = TrainMach)
##
## Residuals:
       Min
                 1Q
                       Median
                                    3Q
                                            Max
## -274.597 -65.467
                       -7.367
                                57.931 239.647
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.411e+03 2.004e+03 -1.203 0.23597
## Month.L
               -1.455e+02 2.274e+02
                                     -0.640
                                              0.52574
## Month.Q
               -8.353e+01
                          1.482e+02
                                      -0.564
                                             0.57610
## Month.C
               -5.199e+02 2.641e+02
                                      -1.969
                                              0.05577 .
                                      0.372 0.71182
## Month<sup>4</sup>
               4.060e+01
                          1.092e+02
## Month<sup>5</sup>
              -2.869e+02 1.689e+02
                                     -1.699 0.09688
## Month^6
               2.007e+02 2.315e+02
                                      0.867 0.39101
                                     -2.719 0.00957 **
## Month<sup>7</sup>
               -2.171e+02 7.985e+01
## Month<sup>8</sup>
              -1.228e+02 8.432e+01 -1.457 0.15284
## Month<sup>9</sup>
              1.789e+02 9.859e+01
                                      1.814 0.07693 .
```

1.730 0.09120 .

3.397e+02 1.964e+02

-1.534e+02 8.742e+01 -1.755 0.08674 .

2.953e+00 6.002e+00 0.492 0.62537

## Month<sup>10</sup>

## Month^11

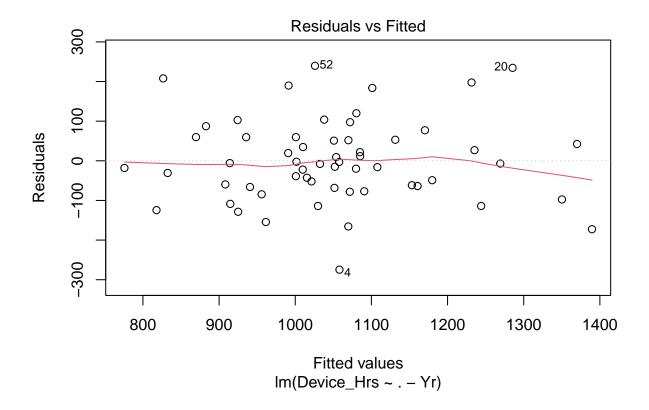
## Cons\_Sent

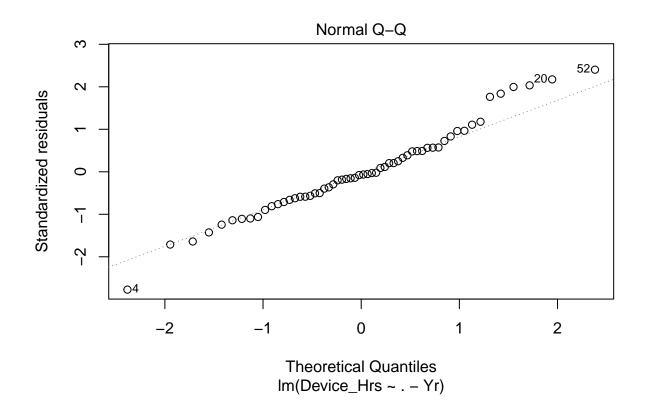
```
## NJURN
                1.245e+02
                           7.230e+01
                                       1.722
                                              0.09252 .
## RPM
                2.597e-05
                           1.893e-05
                                       1.372
                                              0.17763
                                              0.80889
  CPIUrban
                2.644e+00
                           1.086e+01
                                       0.243
               -4.993e+01
                           4.008e+01
                                      -1.246
  CPIMedian
                                              0.21996
##
## Signif. codes:
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 124.3 on 41 degrees of freedom
## Multiple R-squared: 0.6188, Adjusted R-squared: 0.4701
## F-statistic: 4.16 on 16 and 41 DF, p-value: 0.0001143
```

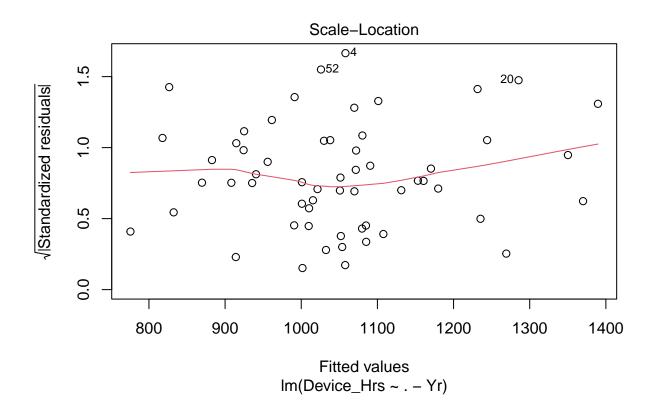
We show a relatively strong correlation between the model and Device Hours

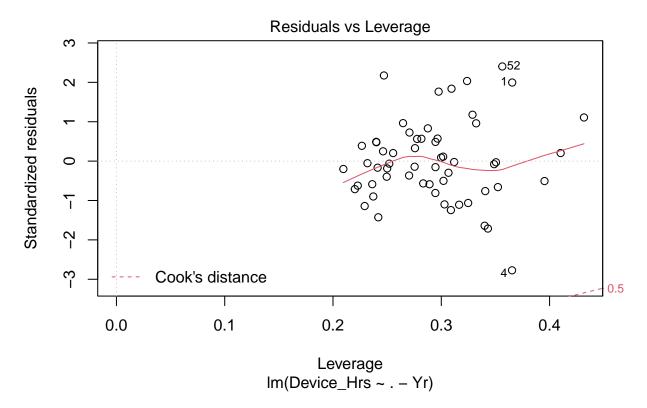
We see some correlation between Consumer Sentiment and NJ Unemployment, and Consumer Sentiment and Revenue Passenger Miles. Its possible there is some redundancy. The CPI Urban and CPI Median don't show a very strong correlation because CPI Urban is the CPI level, while CPI Median is the percentage change. That is why we're including both.

plot(LM\_Mach)





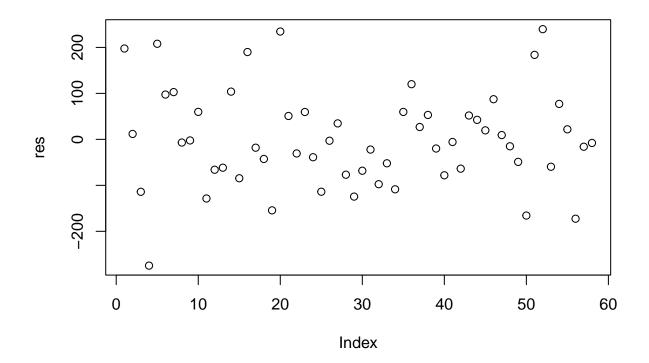




Our model looks like it is generally normal

## Let's look at the residuals

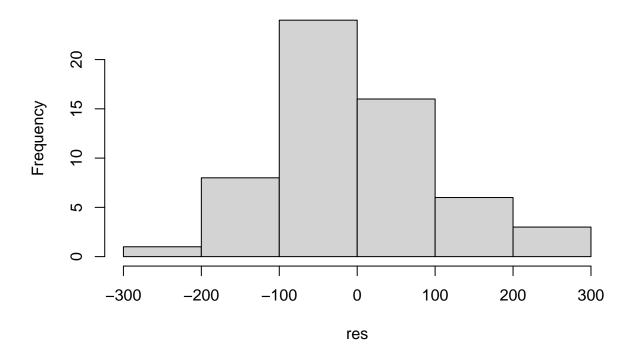
res= residuals(LM\_Mach)
plot(res)



There doesn't appear to be any pattern, which leads us to believe the model is not missing any factors. Lets take other looks at the residuals

hist(res)

# Histogram of res



This looks slightly skewed left, so not completely normal. Maybe we can get a stronger model by removing some independent variables and simplifying the model.

## Stepwise

Mach.Step = step(LM\_Mach)

Because we have multiple independent variables, it is important to run a stepwise to see if we can get a stronger model.

```
## Start: AIC=573.32
## Device_Hrs ~ (Yr + Month + Cons_Sent + NJURN + RPM + CPIUrban +
##
       CPIMedian) - Yr
##
               Df Sum of Sq
                                 RSS
##
                                        AIC
## - CPIUrban
                         916
                              634457 571.40
                1
## - Cons_Sent
                1
                        3740
                              637281 571.66
## <none>
                              633541 573.32
## - CPIMedian
                1
                       23977
                              657519 573.48
## - RPM
                1
                       29073
                              662614 573.92
## - NJURN
                1
                       45846
                              679388 575.37
## - Month
                     818714 1452255 599.43
               11
##
## Step: AIC=571.4
```

```
## Device_Hrs ~ Month + Cons_Sent + NJURN + RPM + CPIMedian
##
               Df Sum of Sq
##
                                 RSS
                                        AIC
## - Cons_Sent 1
                      5146 639603 569.87
## <none>
                              634457 571.40
## - CPIMedian 1
                       24619 659076 571.61
## - NJURN
                1
                      44968 679425 573.38
## - RPM
                       73873 708330 575.79
                1
## - Month
               11
                      983547 1618004 603.70
##
## Step: AIC=569.87
## Device_Hrs ~ Month + NJURN + RPM + CPIMedian
##
               Df Sum of Sq
                                 RSS
                                        AIC
                              639603 569.87
## <none>
## - CPIMedian 1
                       23613
                              663216 569.98
                      51057 690660 572.33
## - NJURN
                1
## - RPM
                1
                       94918 734521 575.90
## - Month
                      984794 1624397 601.93
               11
Mach.Step
##
## lm(formula = Device_Hrs ~ Month + NJURN + RPM + CPIMedian, data = TrainMach)
## Coefficients:
## (Intercept)
                    Month.L
                                  Month.Q
                                                Month.C
                                                            Month<sup>4</sup>
                                                                           Month<sup>5</sup>
   -1.949e+03
##
                -2.188e+02
                              -1.262e+02
                                             -5.971e+02
                                                           7.313e+01
                                                                        -3.253e+02
##
       Month<sup>6</sup>
                   Month<sup>7</sup>
                                 Month^8
                                               Month<sup>9</sup>
                                                           Month<sup>10</sup>
                                                                          Month<sup>11</sup>
##
     2.667e+02 -2.324e+02
                             -1.138e+02
                                             2.045e+02
                                                           3.890e+02
                                                                        -1.600e+02
##
         NJURN
                         RPM
                               CPIMedian
##
     1.279e+02
                               -4.940e+01
                  3.157e-05
summary(Mach.Step)
##
## Call:
## lm(formula = Device_Hrs ~ Month + NJURN + RPM + CPIMedian, data = TrainMach)
## Residuals:
##
        Min
                  1Q
                        Median
                                     3Q
                                              Max
## -265.886 -71.441
                        -9.159
                                 59.434 235.481
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.949e+03 1.294e+03 -1.506 0.139368
## Month.L
               -2.188e+02 1.461e+02 -1.497 0.141649
               -1.262e+02 1.144e+02 -1.104 0.275915
## Month.Q
## Month.C
               -5.971e+02 1.761e+02 -3.390 0.001506 **
## Month<sup>4</sup>
               7.313e+01 7.917e+01 0.924 0.360762
## Month<sup>5</sup>
              -3.253e+02 1.336e+02 -2.435 0.019107 *
               2.667e+02 1.646e+02 1.621 0.112353
## Month^6
```

```
## Month<sup>7</sup>
               -2.324e+02 6.424e+01 -3.618 0.000775 ***
## Month^8
               -1.138e+02 7.854e+01 -1.449 0.154609
## Month<sup>9</sup>
               2.045e+02 6.463e+01 3.164 0.002858 **
## Month<sup>10</sup>
                3.890e+02 1.423e+02
                                        2.733 0.009077 **
## Month^11
               -1.600e+02 8.506e+01 -1.881 0.066716 .
## N.JUR.N
                1.279e+02 6.906e+01
                                      1.853 0.070795 .
## RPM
                3.157e-05 1.250e-05 2.526 0.015296 *
## CPIMedian
               -4.940e+01 3.921e+01 -1.260 0.214483
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 122 on 43 degrees of freedom
## Multiple R-squared: 0.6152, Adjusted R-squared: 0.4899
## F-statistic: 4.91 on 14 and 43 DF, p-value: 2.613e-05
Test = lm(formula = Device_Hrs ~ Month + Month:RPM + Month:NJURN + Month:CPIUrban + RPM, data = Mach1)
summary(Test)
##
## Call:
## lm(formula = Device Hrs ~ Month + Month:RPM + Month:NJURN + Month:CPIUrban +
##
       RPM, data = Mach1)
## Residuals:
      Min
                10 Median
                                30
                                        Max
## -215.97 -54.94
                    -1.57
                             41.82 354.51
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      5.094e+02 2.453e+03
                                            0.208 0.836842
                     -1.775e+03 8.950e+03 -0.198 0.844113
## Month.L
## Month.Q
                     1.584e+04 6.954e+03
                                             2.278 0.029745 *
## Month.C
                     -9.461e+03 5.864e+03 -1.613 0.116774
## Month<sup>4</sup>
                     2.643e+03
                                 8.327e+03
                                             0.317 0.753024
## Month<sup>5</sup>
                     -5.298e+03 1.089e+04 -0.487 0.629938
## Month<sup>6</sup>
                     -3.839e+02 1.036e+04 -0.037 0.970669
## Month<sup>7</sup>
                     -1.258e+04 1.026e+04 -1.226 0.229346
## Month<sup>8</sup>
                     -3.852e+03 8.652e+03 -0.445 0.659292
## Month<sup>9</sup>
                     1.012e+03 6.573e+03 0.154 0.878638
## Month^10
                     7.006e+02 7.821e+03 0.090 0.929196
## Month<sup>11</sup>
                     -1.148e+03 7.190e+03 -0.160 0.874138
## R.PM
                      8.269e-06 9.542e-06
                                             0.867 0.392863
## Month.L:RPM
                     -4.383e-07
                                 3.040e-05 -0.014 0.988587
## Month.Q:RPM
                     -7.143e-05
                                 2.880e-05 -2.480 0.018766 *
## Month.C:RPM
                      3.160e-05
                                 2.511e-05
                                             1.259 0.217544
## Month<sup>4</sup>:RPM
                     -3.799e-06
                                 3.154e-05 -0.120 0.904900
## Month<sup>5</sup>:RPM
                      9.975e-06
                                 3.809e-05
                                             0.262 0.795122
## Month^6:RPM
                     -2.074e-05
                                 3.564e-05 -0.582 0.564761
## Month^7:RPM
                      4.457e-05
                                 3.772e-05
                                              1.181 0.246390
                                 3.419e-05
## Month^8:RPM
                     1.275e-05
                                             0.373 0.711685
## Month^9:RPM
                     -1.287e-05 2.874e-05 -0.448 0.657564
## Month^10:RPM
                     -2.562e-06 3.465e-05 -0.074 0.941531
```

```
## Month^11:RPM
                     3.277e-05 3.608e-05
                                            0.908 0.370761
                    -4.327e+02 1.605e+02 -2.697 0.011212 *
## MonthApr:NJURN
## MonthAug:NJURN
                     1.446e+02 3.392e+02
                                            0.426 0.672832
## MonthDec:NJURN
                                2.914e+02 -0.032 0.974359
                    -9.442e+00
## MonthFeb:NJURN
                     8.097e+01
                                3.965e+02
                                           0.204 0.839501
## MonthJan:NJURN
                     2.602e+02 7.183e+02 0.362 0.719645
## MonthJul:NJURN
                     4.718e+02 2.891e+02 1.632 0.112782
## MonthJun:NJURN
                     1.705e+01
                                1.204e+02
                                            0.142 0.888287
## MonthMar:NJURN
                     1.310e+02
                                2.010e+02 0.651 0.519584
## MonthMay:NJURN
                    -2.656e+01
                                2.490e+01 -1.067 0.294253
## MonthNov:NJURN
                     1.908e+02
                                3.980e+02
                                           0.479 0.635031
## MonthOct:NJURN
                    -3.457e+02
                                7.831e+02 -0.441 0.661924
## MonthSep:NJURN
                    -1.302e+02
                                1.447e+02 -0.900 0.375278
## MonthApr:CPIUrban -4.202e+01
                                9.738e+00 -4.316 0.000151 ***
                                           0.497 0.622675
## MonthAug:CPIUrban 3.036e+00
                                6.107e+00
## MonthDec:CPIUrban
                     2.874e+00
                                1.002e+01
                                            0.287 0.776258
## MonthFeb:CPIUrban 4.448e+00
                                9.477e+00
                                            0.469 0.642158
## MonthJan:CPIUrban 1.619e+01
                                2.330e+01
                                            0.695 0.492353
## MonthJul:CPIUrban 4.556e+00
                                8.447e+00
                                          0.539 0.593473
## MonthJun:CPIUrban 5.835e+00
                                1.121e+01
                                            0.521 0.606342
## MonthMar:CPIUrban -1.151e+01 1.247e+01 -0.923 0.363114
## MonthMay:CPIUrban 1.072e+01
                                7.642e+00
                                           1.403 0.170677
## MonthNov:CPIUrban 1.154e+01
                                2.416e+01
                                            0.477 0.636395
## MonthOct:CPIUrban -2.551e+01
                                4.828e+01 -0.528 0.600939
## MonthSep:CPIUrban 4.517e+00 5.424e+00
                                            0.833 0.411320
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 150.2 on 31 degrees of freedom
     (2 observations deleted due to missingness)
## Multiple R-squared: 0.804, Adjusted R-squared: 0.5069
## F-statistic: 2.706 on 47 and 31 DF, p-value: 0.002178
Test.Step = step(Test)
## Start: AIC=813.94
## Device_Hrs ~ Month + Month:RPM + Month:NJURN + Month:CPIUrban +
##
      RPM
##
##
                   Df Sum of Sq
                                    RSS
                                           AIC
## <none>
                                 698922 813.94
## - Month:NJURN
                   12
                         295569
                                 994491 817.80
## - Month:RPM
                         383682 1082604 826.51
                   11
## - Month: CPIUrban 12
                         546495 1245417 835.58
Test.Step
##
## Call:
## lm(formula = Device_Hrs ~ Month + Month:RPM + Month:NJURN + Month:CPIUrban +
##
      RPM, data = Mach1)
##
## Coefficients:
```

```
Month.L
##
           (Intercept)
                                                             Month.Q
                                                                                    Month.C
                                  -1.775e+03
##
             5.094e+02
                                                          1.584e+04
                                                                                -9.461e+03
##
               Month<sup>4</sup>
                                      Month<sup>5</sup>
                                                             Month<sup>6</sup>
                                                                                    Month<sup>7</sup>
##
             2.643e+03
                                   -5.298e+03
                                                         -3.839e+02
                                                                                -1.258e+04
##
               Month<sup>8</sup>
                                      Month<sup>9</sup>
                                                           Month<sup>10</sup>
                                                                                  Month<sup>11</sup>
            -3.852e+03
                                                          7.006e+02
##
                                    1.012e+03
                                                                                -1.148e+03
##
                    RPM
                                 Month.L:RPM
                                                        Month.Q:RPM
                                                                               Month.C:RPM
##
             8.269e-06
                                  -4.383e-07
                                                         -7.143e-05
                                                                                 3.160e-05
##
          Month<sup>4</sup>:RPM
                                 Month<sup>5</sup>:RPM
                                                        Month<sup>6</sup>:RPM
                                                                               Month<sup>7</sup>:RPM
##
           -3.799e-06
                                    9.975e-06
                                                         -2.074e-05
                                                                                 4.457e-05
##
          Month<sup>8</sup>:RPM
                                 Month<sup>9</sup>:RPM
                                                       Month<sup>10:RPM</sup>
                                                                              Month^11:RPM
##
             1.275e-05
                                  -1.287e-05
                                                         -2.562e-06
                                                                                 3.277e-05
##
       MonthApr:NJURN
                                                    MonthDec: NJURN
                                                                           MonthFeb: NJURN
                             MonthAug: NJURN
##
                                                         -9.442e+00
            -4.327e+02
                                    1.446e+02
                                                                                 8.097e+01
##
       MonthJan: NJURN
                              MonthJul: NJURN
                                                                           MonthMar: NJURN
                                                    MonthJun: NJURN
##
             2.602e+02
                                    4.718e+02
                                                           1.705e+01
                                                                                 1.310e+02
##
       MonthMay: NJURN
                              MonthNov: NJURN
                                                    MonthOct:NJURN
                                                                           MonthSep: NJURN
##
            -2.656e+01
                                    1.908e+02
                                                         -3.457e+02
                                                                                -1.302e+02
   MonthApr:CPIUrban
##
                          MonthAug: CPIUrban
                                                 MonthDec:CPIUrban
                                                                       MonthFeb:CPIUrban
            -4.202e+01
                                    3.036e+00
                                                           2.874e+00
                                                                                 4.448e+00
##
   MonthJan: CPIUrban
                          MonthJul:CPIUrban
                                                 MonthJun: CPIUrban
                                                                       MonthMar: CPIUrban
             1.619e+01
                                    4.556e+00
                                                           5.835e+00
                                                                                -1.151e+01
## MonthMay:CPIUrban
                          MonthNov:CPIUrban MonthOct:CPIUrban
                                                                       MonthSep:CPIUrban
             1.072e+01
                                    1.154e+01
                                                         -2.551e+01
                                                                                 4.517e+00
```

#### summary(Test.Step)

```
##
   Call:
   lm(formula = Device_Hrs ~ Month + Month:RPM + Month:NJURN + Month:CPIUrban +
##
       RPM, data = Mach1)
##
##
   Residuals:
                  1Q
                                    3Q
##
       Min
                      Median
                                            Max
   -215.97
             -54.94
                       -1.57
                                41.82
                                        354.51
##
   Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    2.453e+03
                                                  0.208 0.836842
                        5.094e+02
## Month.L
                       -1.775e+03
                                     8.950e+03
                                                 -0.198 0.844113
## Month.Q
                        1.584e+04
                                     6.954e+03
                                                  2.278 0.029745 *
## Month.C
                       -9.461e+03
                                     5.864e+03
                                                 -1.613 0.116774
## Month<sup>4</sup>
                        2.643e+03
                                     8.327e+03
                                                  0.317 0.753024
## Month<sup>5</sup>
                                     1.089e+04
                                                 -0.487 0.629938
                       -5.298e+03
## Month<sup>6</sup>
                       -3.839e+02
                                     1.036e+04
                                                 -0.037 0.970669
## Month<sup>7</sup>
                       -1.258e+04
                                     1.026e+04
                                                 -1.226 0.229346
## Month<sup>8</sup>
                        -3.852e+03
                                     8.652e+03
                                                 -0.445 0.659292
## Month<sup>9</sup>
                                     6.573e+03
                                                  0.154 0.878638
                        1.012e+03
## Month<sup>10</sup>
                        7.006e+02
                                     7.821e+03
                                                  0.090 0.929196
                                                 -0.160 0.874138
## Month<sup>11</sup>
                       -1.148e+03
                                     7.190e+03
## RPM
                        8.269e-06
                                     9.542e-06
                                                  0.867 0.392863
## Month.L:RPM
                       -4.383e-07
                                     3.040e-05
                                                 -0.014 0.988587
## Month.Q:RPM
                                     2.880e-05
                       -7.143e-05
                                                 -2.480 0.018766 *
## Month.C:RPM
                        3.160e-05
                                    2.511e-05
                                                  1.259 0.217544
```

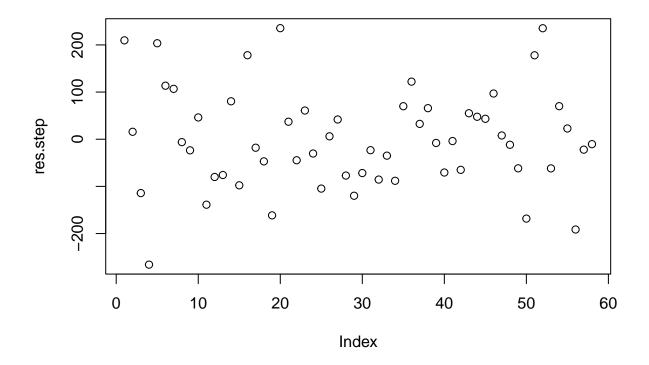
```
## Month<sup>4</sup>:RPM
                     -3.799e-06
                                 3.154e-05
                                             -0.120 0.904900
## Month<sup>5</sup>:RPM
                      9.975e-06
                                 3.809e-05
                                              0.262 0.795122
                                 3.564e-05
## Month^6:RPM
                     -2.074e-05
                                             -0.582 0.564761
## Month^7:RPM
                                 3.772e-05
                      4.457e-05
                                              1.181 0.246390
## Month^8:RPM
                      1.275e-05
                                 3.419e-05
                                              0.373 0.711685
## Month^9:RPM
                     -1.287e-05
                                 2.874e-05
                                             -0.448 0.657564
## Month^10:RPM
                     -2.562e-06
                                 3.465e-05
                                             -0.074 0.941531
## Month^11:RPM
                      3.277e-05
                                 3.608e-05
                                              0.908 0.370761
## MonthApr:NJURN
                     -4.327e+02
                                 1.605e+02
                                             -2.697 0.011212 *
## MonthAug:NJURN
                      1.446e+02
                                 3.392e+02
                                              0.426 0.672832
## MonthDec:NJURN
                     -9.442e+00
                                 2.914e+02
                                             -0.032 0.974359
## MonthFeb:NJURN
                      8.097e+01
                                 3.965e+02
                                              0.204 0.839501
## MonthJan:NJURN
                      2.602e+02
                                 7.183e+02
                                              0.362 0.719645
## MonthJul:NJURN
                      4.718e+02
                                 2.891e+02
                                              1.632 0.112782
## MonthJun:NJURN
                      1.705e+01
                                 1.204e+02
                                              0.142 0.888287
## MonthMar:NJURN
                      1.310e+02
                                 2.010e+02
                                              0.651 0.519584
                                             -1.067 0.294253
## MonthMay:NJURN
                                 2.490e+01
                     -2.656e+01
## MonthNov:NJURN
                      1.908e+02
                                 3.980e+02
                                              0.479 0.635031
## MonthOct:NJURN
                     -3.457e+02
                                 7.831e+02
                                             -0.441 0.661924
## MonthSep:NJURN
                     -1.302e+02
                                 1.447e+02
                                             -0.900 0.375278
## MonthApr:CPIUrban -4.202e+01
                                 9.738e+00
                                            -4.316 0.000151 ***
## MonthAug:CPIUrban
                     3.036e+00
                                 6.107e+00
                                             0.497 0.622675
## MonthDec:CPIUrban
                      2.874e+00
                                 1.002e+01
                                              0.287 0.776258
## MonthFeb:CPIUrban 4.448e+00
                                 9.477e+00
                                              0.469 0.642158
## MonthJan:CPIUrban 1.619e+01
                                 2.330e+01
                                              0.695 0.492353
## MonthJul:CPIUrban 4.556e+00
                                 8.447e+00
                                              0.539 0.593473
## MonthJun:CPIUrban 5.835e+00
                                 1.121e+01
                                              0.521 0.606342
## MonthMar:CPIUrban -1.151e+01
                                 1.247e+01
                                             -0.923 0.363114
## MonthMay:CPIUrban 1.072e+01
                                 7.642e+00
                                              1.403 0.170677
## MonthNov:CPIUrban 1.154e+01
                                 2.416e+01
                                              0.477 0.636395
## MonthOct:CPIUrban -2.551e+01
                                 4.828e+01
                                             -0.528 0.600939
## MonthSep:CPIUrban 4.517e+00
                                 5.424e+00
                                              0.833 0.411320
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 150.2 on 31 degrees of freedom
     (2 observations deleted due to missingness)
## Multiple R-squared: 0.804, Adjusted R-squared: 0.5069
## F-statistic: 2.706 on 47 and 31 DF, p-value: 0.002178
```

Stepwise reveals that the best way to predict training hours is to use the month and the Revenue Passenger Miles. The other variables were not strong predictors.

This model has a decently strong Adjusted R2, a high F-statistic, and a very low p-value.

#### Lets look at the residuals of the new model.

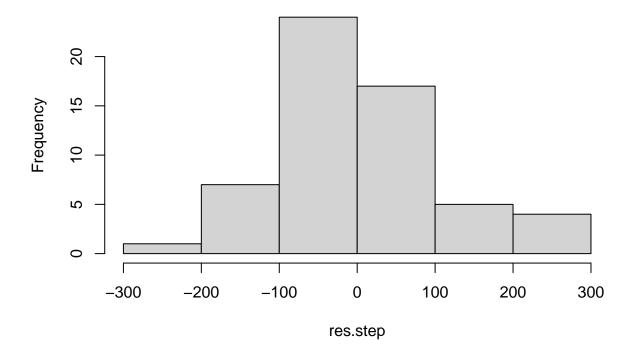
```
res.step= residuals(Mach.Step)
plot(res.step)
```



This also looks normally distributed.

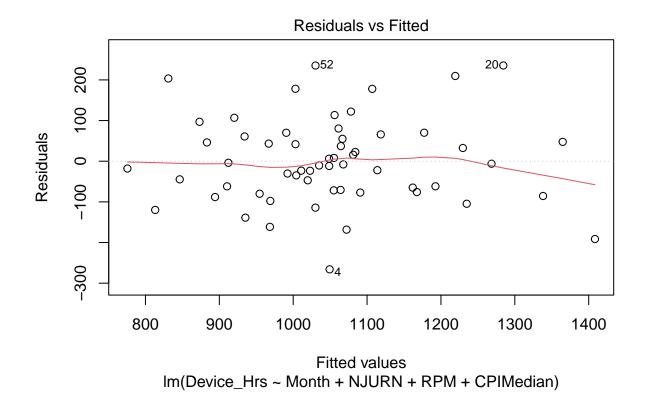
hist(res.step)

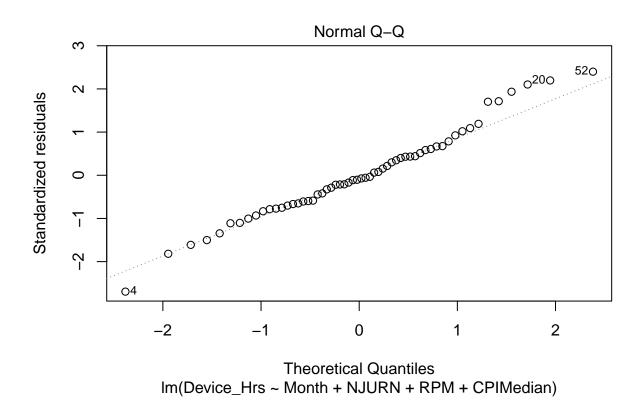
# Histogram of res.step

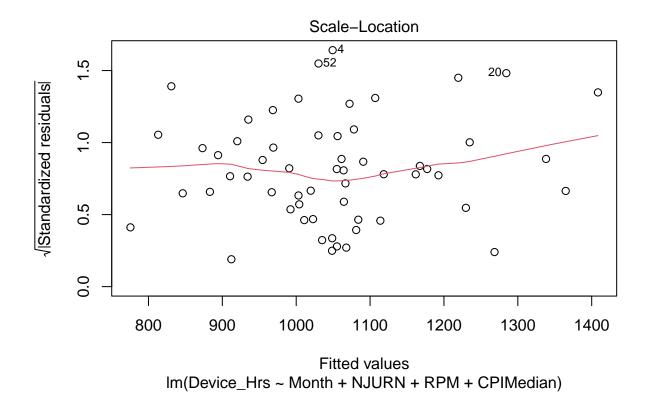


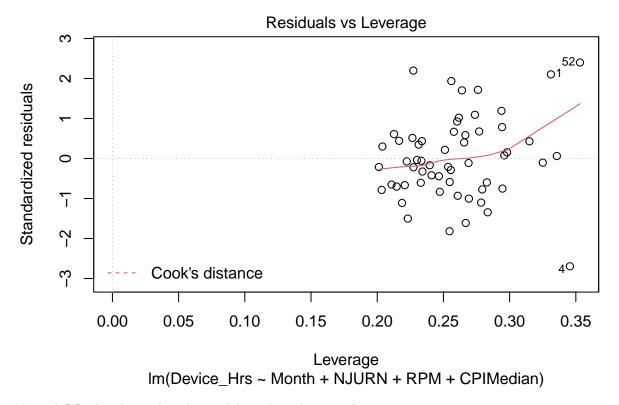
this looks to be more normally distributed, though it still slightly skewed to the left. Final residual check.

plot(Mach.Step)





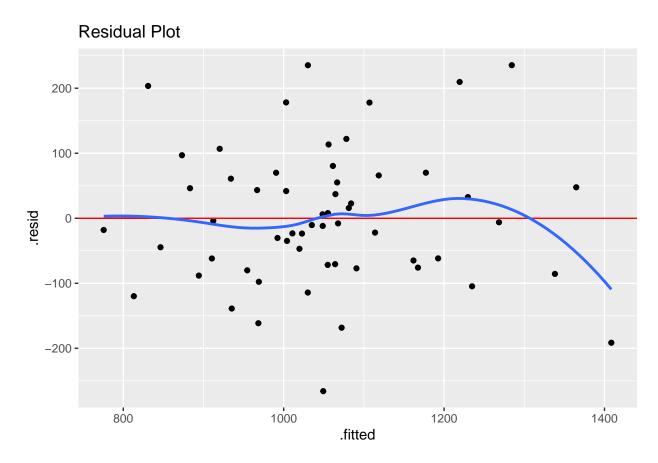




Normal QQ plot shows that the model is relatively normal.

```
p1= ggplot(Mach.Step) +
  aes(x=.fitted, y=.resid)+
  geom_point() + geom_abline(intercept = 0, slope = 0, color="red") + geom_smooth(method = "loess", se
  labs(title= "Residual Plot")
p1
```

## 'geom\_smooth()' using formula 'y ~ x'



We show some skewedness at the right side of the graph, but generally it appears strong..