Research project meeting summary: Trajectory Module for Launcher MDAO

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November 7, 2020

Plan:



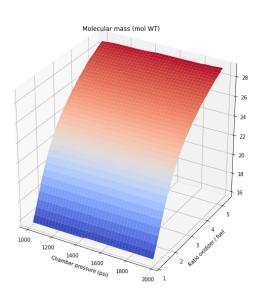
Review of previous work

2 Key points discussed

3 Future actions

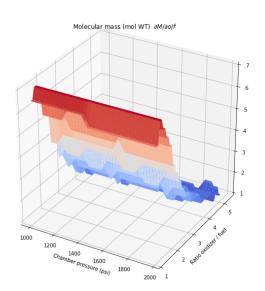
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Linear interpolation of Rocket CEA outputs



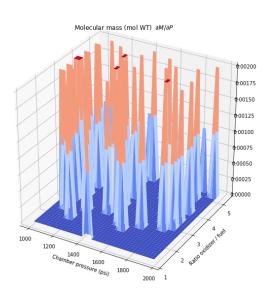


Linear interpolation of Rocket CEA outputs



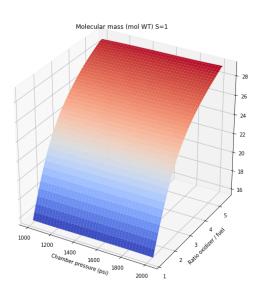
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Linear interpolation of Rocket CEA outputs



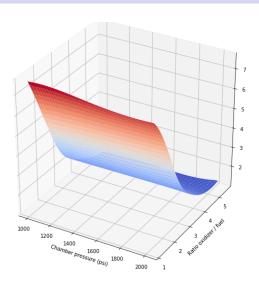


Bivariate Spline for comparisson



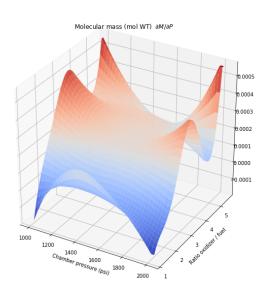
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Bivariate Spline for comparisson



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Bivariate Spline for comparisson





Error in I_{sp} calculation

$$Isp = \lambda_n \cdot \frac{C^*}{g_0} \left(\gamma_t \sqrt{\left(\frac{2}{\gamma_t - 1}\right) \cdot \left(\frac{2}{\gamma_t + 1}\right)^{\frac{\gamma_t + 1}{\gamma_t - 1}}} \sqrt{1 - \frac{Pe}{Pc}}^{\frac{\gamma_t - 1}{\gamma_t}} + \frac{\epsilon}{Pc} (Pe - P_a) \right)$$

Figure: I_{sp} as a function of C_f used in LAST from Dr. Balesdent's thesis

$$\begin{split} C_F &= \frac{F}{p_1 A_t} = \frac{v_2^2 A_2}{p_1 A_t V_2} + \frac{p_2 A_2}{p_1 A_t} - \frac{p_3 A_2}{p_1 A_t} \\ &= \sqrt{\frac{2k^2}{k-1} \left(\frac{2}{k+1}\right)^{(k+1)/(k-1)} \left[1 - \left(\frac{p_2}{p_1}\right)^{(k-1)/k}\right]} + \frac{p_2 - p_3}{p_1} \frac{A_2}{A_t} \end{split}$$

Figure: C_f as in Sutton - Rocket Propulsion Elements

• $1 \le C_f \le 2$, according to Sutton

Key points discussed



Proposal to further decompose the calculation of $I_{\rm sp_{\rm vac}}$

In order to compare results against the literature I think it would be convenient to further divide the calculation of $I_{\rm sp_{\rm vac}}$ like this

- Calculate effective exhaust velocity at vacuum: c_{vac}
- ${\color{red} 2}$ Calculate thrust coefficient at vacuum: $C_{f_{\rm vac}} = \frac{c_{\rm vac}}{c^{\star}}$
- **3** Calculate $I_{\rm sp_{\rm vac}} = \lambda_{\rm n} * \frac{c^{\star}}{g_0} * C_{\rm f_{\rm vac}}$

Key points discussed



Convergence problems

- Right now the values of nozzle exit area and exit pressure behave as expected when running the optimization
- Still, there as some convergence problems as the optimizer fails to satisfy inequality constraints
- I'm trying to use Linux to have accesss to more performant open source optimizers as IPOPT and PyOptSparse's SLSQP. Dr. Urbano suggests to use a virtual machine.
- Dr. URbano suggest to use previous code (without propulsion optimization) with inputs taken from the unconverged simulations.
- it would be good to separate λ_n into eta_{c^*} and eta_{C_f}

Future actions



• Keep trying with the propulsion optimization based on the things discussed during this meeting