

> 1 + 2

3

(1)

> eq1 := diff(u(x), x\$2) + 5\*diff(u(x), x) - 7\*u(x) = x^2 + 5\*x - 7

$$eq1 := \frac{d^2}{dx^2} u(x) + 5 \frac{d}{dx} u(x) - 7 u(x) = x^2 + 5x - 7$$

(2)

> eq1 := dsolve(eq1, u(x))

$$eq1 := u(x) = e^{\frac{(-5+\sqrt{53})x}{2}} c_2 + e^{-\frac{(5+\sqrt{53})x}{2}} c_1 - \frac{x^2}{7} - \frac{45x}{49} + \frac{104}{343}$$

(3)

> eq1

$$u(x) = e^{\frac{(-5+\sqrt{53})x}{2}} c_2 + e^{-\frac{(5+\sqrt{53})x}{2}} c_1 - \frac{x^2}{7} - \frac{45x}{49} + \frac{104}{343}$$

(4)

> eq1 := rhs(eq1)

$$eq1 := e^{\frac{(-5+\sqrt{53})x}{2}} c_2 + e^{-\frac{(5+\sqrt{53})x}{2}} c_1 - \frac{x^2}{7} - \frac{45x}{49} + \frac{104}{343}$$

(5)

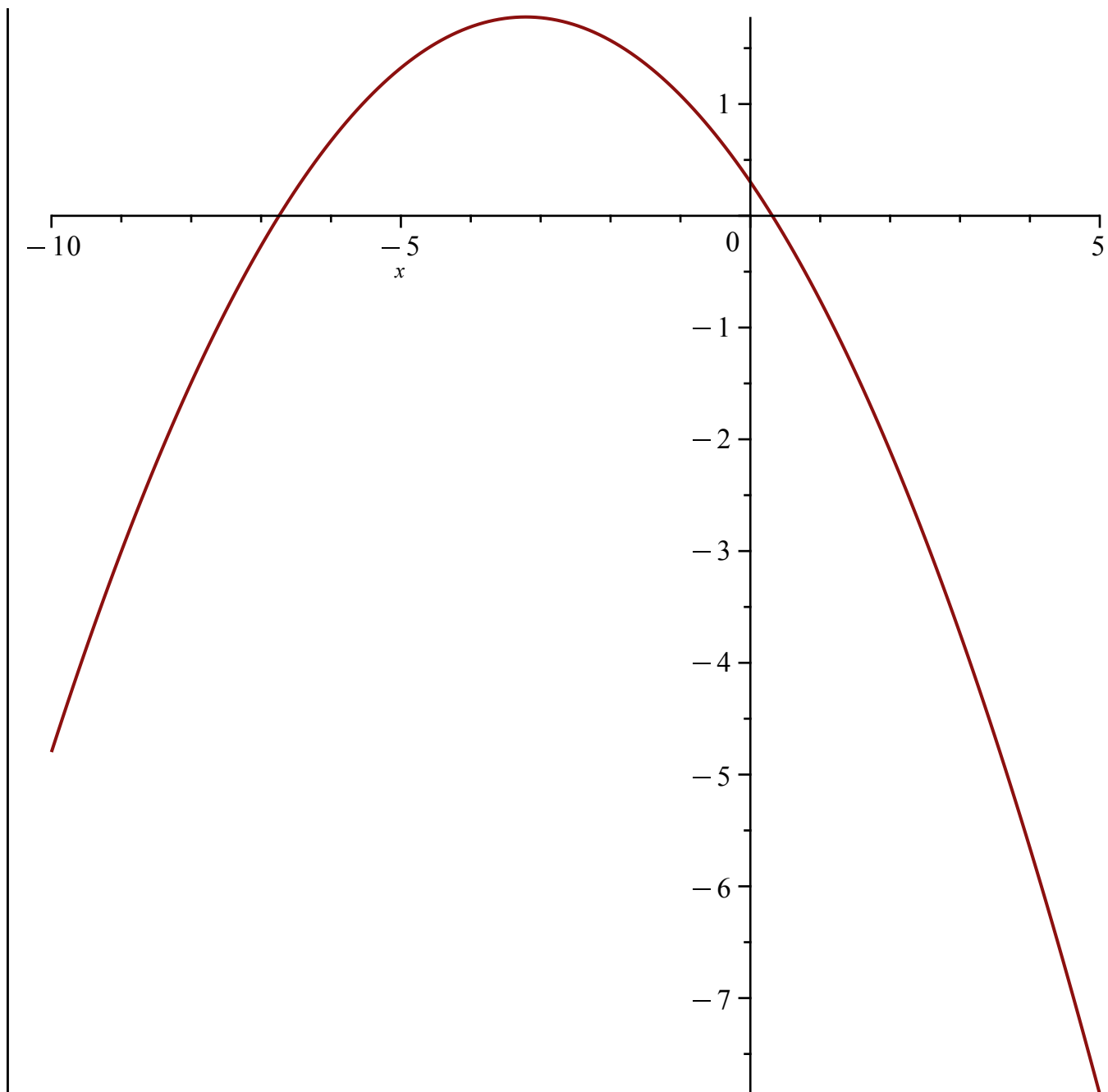
>

> eq1 := -\frac{x^2}{7} - \frac{45x}{49} + \frac{104}{343}

$$eq1 := -\frac{1}{7} x^2 - \frac{45}{49} x + \frac{104}{343}$$

(6)

> plot(eq1, x=-10..5)




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>  $f := x \mapsto -\frac{1}{7}x^2 - \frac{45}{49}x + \frac{104}{343}$

$f := x \mapsto -\frac{1}{7} \cdot x^2 - \frac{45}{49} \cdot x + \frac{104}{343}$  (7)

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>  $f(x)$

$-\frac{1}{7}x^2 - \frac{45}{49}x + \frac{104}{343}$  (8)

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>  $f(1)$

$-\frac{260}{343}$  (9)

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>  $val := \text{Pi} \cdot \text{sqrt}(2)$

$$val := \pi \sqrt{2} \quad (10)$$

>  $f(val)$

$$-\frac{2\pi^2}{7} - \frac{45\pi\sqrt{2}}{49} + \frac{104}{343} \quad (11)$$

>  $eval(f(x), x = val)$

$$-\frac{2\pi^2}{7} - \frac{45\pi\sqrt{2}}{49} + \frac{104}{343} \quad (12)$$

>  $f(2)$

$$-\frac{722}{343} \quad (13)$$

>  $f(\text{sqrt}(2))$

$$\frac{6}{343} - \frac{45\sqrt{2}}{49} \quad (14)$$

>  $f(val)$

$$-\frac{2\pi^2}{7} - \frac{45\pi\sqrt{2}}{49} + \frac{104}{343} \quad (15)$$

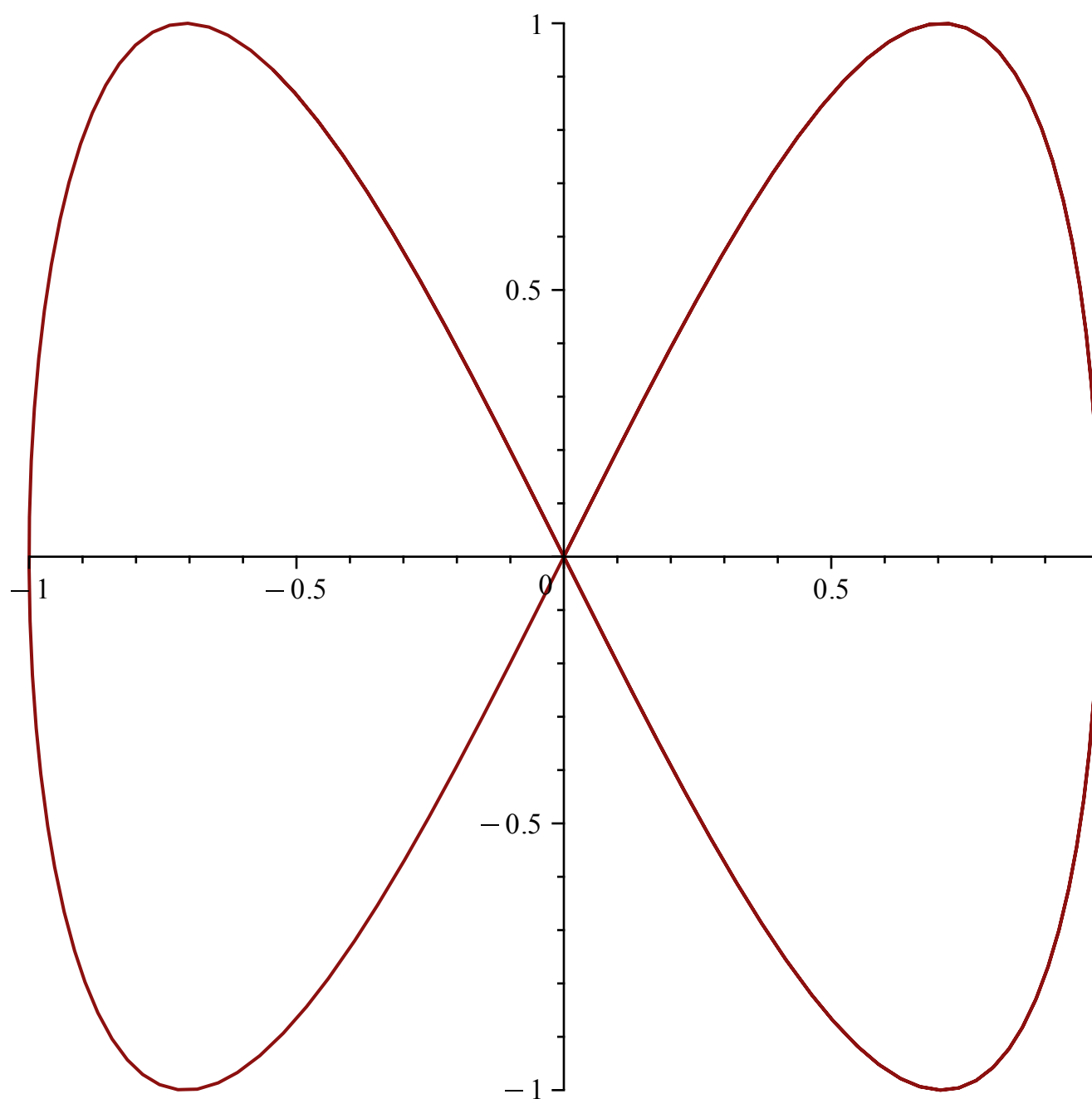
>  $evalf(f(val))$

$$-6.596878591 \quad (16)$$

>  $evalf(D(f)(val))$

$$-2.187762472 \quad (17)$$

>  $plot([\sin(t), \sin(2t), t = 0..10])$



```
> diff(sin(t), t)
cos(t) (18)
```

```
> with(LinearAlgebra) : with(VectorCalculus)
[&x, `*`, `+`, `^`, `.` , <, >, <|>, About, AddCoordinates, ArcLength, BasisFormat, Binormal, (19)
ConvertVector, CrossProduct, Curl, Curvature, D, Del, DirectionalDiff, Divergence,
DotProduct, Flux, GetCoordinateParameters, GetCoordinates, GetNames, GetPVDDescription,
GetRootPoint, GetSpace, Gradient, Hessian, IsPositionVector, IsRootedVector, IsVectorField,
Jacobian, Laplacian, LineInt, MapToBasis, ∇, Norm, Normalize, PathInt, PlotPositionVector,
PlotVector, PositionVector, PrincipalNormal, RadiusOfCurvature, RootedVector,
ScalarPotential, SetCoordinateParameters, SetCoordinates, SpaceCurve, SurfaceInt,
```

*TNBFrame, TangentLine, TangentPlane, TangentVector, Torsion, Vector, VectorField, VectorPotential, VectorSpace, Wronskian, diff, eval, evalVF, int, limit, series ]*

>  $A := \text{Matrix}([[-7, 0], [1, 7]])$

$$A := \begin{bmatrix} -7 & 0 \\ 1 & 7 \end{bmatrix} \quad (20)$$

>  $\text{Determinant}(A)$

$$-49 \quad (21)$$

>  $\text{Eigenvalues}(A)$

$$\begin{bmatrix} 7 \\ -7 \end{bmatrix} \quad (22)$$

>  $\text{MatrixExponential}(t \cdot A)$

$$\begin{bmatrix} e^{-7t} & 0 \\ \frac{e^{7t}}{14} - \frac{e^{-7t}}{14} & e^{7t} \end{bmatrix} \quad (23)$$

>  $eq1 := x - 17 \cdot y + 3 \cdot y^2 - 2 \cdot x \cdot y = 0$

$$eq1 := -2xy + 3y^2 + x - 17y = 0 \quad (24)$$

>  $eq2 := 17 \cdot x + y = 0$

$$eq2 := 17x + y = 0 \quad (25)$$

>  $\text{solve}(\{eq1, eq2\}, \{x, y\})$

$$\{x=0, y=0\}, \left\{x = -\frac{290}{901}, y = \frac{290}{53}\right\} \quad (26)$$

>  $f1 := (x, y) \mapsto x - 17 \cdot y + 3 \cdot y^2 - 2 \cdot x \cdot y$

$$f1 := (x, y) \mapsto x + (-17 \cdot y) + 3 \cdot y^2 + (-2 \cdot x \cdot y) \quad (27)$$

>  $f2 := (x, y) \mapsto 17 \cdot x + y$

$$f2 := (x, y) \mapsto 17 \cdot x + y \quad (28)$$

>  $Jm := \text{Jacobian}([f1(x, y), f2(x, y)], [x, y])$

$$Jm := \begin{bmatrix} -2y + 1 & -2x + 6y - 17 \\ 17 & 1 \end{bmatrix} \quad (29)$$

>  $A := \text{subs}([x=0, y=0], Jm)$

$$A := \begin{bmatrix} 1 & -17 \\ 17 & 1 \end{bmatrix} \quad (30)$$

>  $\text{Eigenvalues}(A)$

$$\begin{bmatrix} 1 + 17I \\ 1 - 17I \end{bmatrix} \quad (31)$$

>  $eq1 := 0.002 \cdot x \cdot (100 - x) = 0$

$$eq1 := 0.002x(100 - x) = 0 \quad (32)$$

```
|> solve(eq1,x)  
=  
|>
```

0., 100.

**(33)**