> with (Student [Linear Algebra]): with (Linear Algebra) [&x, Add, Adjoint, BackwardSubstitute, BandMatrix, Basis, BezoutMatrix, BidiagonalForm, **(1)** BilinearForm, CARE, CharacteristicMatrix, CharacteristicPolynomial, Column, ColumnDimension, ColumnOperation, ColumnSpace, CompanionMatrix, CompressedSparseForm, ConditionNumber, ConstantMatrix, ConstantVector, Copy, CreatePermutation, CrossProduct, DARE, DeleteColumn, DeleteRow, Determinant, Diagonal, Diagonal Matrix, Dimension, Dimensions, Dot Product, Eigen Condition Numbers, Eigenvalues, Eigenvectors, Equal, ForwardSubstitute, FrobeniusForm, FromCompressedSparseForm, From SplitForm, Gaussian Elimination, Generate Equations, Generate Matrix, Generic, GetResultDataType, GetResultShape, GivensRotationMatrix, GramSchmidt, HankelMatrix, HermiteForm, HermitianTranspose, HessenbergForm, HilbertMatrix, HouseholderMatrix, IdentityMatrix, IntersectionBasis, IsDefinite, IsOrthogonal, IsSimilar, IsUnitary, JordanBlockMatrix, JordanForm, KroneckerProduct, LA Main, LUDecomposition, LeastSquares, LinearSolve, LyapunovSolve, Map, Map2, MatrixAdd, MatrixExponential, MatrixFunction, MatrixInverse, MatrixMatrixMultiply, MatrixNorm, MatrixPower, MatrixScalarMultiply, MatrixVectorMultiply, MinimalPolynomial, Minor, Modular, Multiply, NoUserValue, Norm, Normalize, NullSpace, OuterProductMatrix, Permanent, Pivot, PopovForm, ProjectionMatrix, QRDecomposition, RandomMatrix, RandomVector, Rank, RationalCanonicalForm, ReducedRowEchelonForm, Row, RowDimension, RowOperation, RowSpace, ScalarMatrix, ScalarMultiply, ScalarVector, SchurForm, SingularValues, SmithForm, SplitForm, StronglyConnectedBlocks, SubMatrix, SubVector, SumBasis, SylvesterMatrix, SylvesterSolve, ToeplitzMatrix, Trace, Transpose, TridiagonalForm, UnitVector, VandermondeMatrix, VectorAdd, VectorAngle, VectorMatrixMultiply, VectorNorm, *VectorScalarMultiply*, *ZeroMatrix*, *ZeroVector*, *Zip*]

> A := Matrix([[0, -2, 0], [1, -2, 0], [0, 0, -2]])

$$A := \begin{bmatrix} 0 & -2 & 0 \\ 1 & -2 & 0 \\ 0 & 0 & -2 \end{bmatrix}$$
 (2)

> Determinant(A) -4 (3)

> A^(−1)

$$\begin{bmatrix}
-1 & 1 & 0 \\
-\frac{1}{2} & 0 & 0 \\
0 & 0 & -\frac{1}{2}
\end{bmatrix}$$
(4)

CharacteristicPolynomial(A, r)

 \rightarrow Column(P, 3)·lam[3]

$$\begin{bmatrix} -2 \\ -1 - I \\ 0 \end{bmatrix} \tag{15}$$

 $\supset J := DiagonalMatrix(lam)$

$$J := \begin{bmatrix} -2 & 0 & 0 \\ 0 & -1 + I & 0 \\ 0 & 0 & -1 - I \end{bmatrix}$$
 (16)

> P

$$\begin{bmatrix} 0 & 1+I & 1-I \\ 0 & 1 & 1 \\ 1 & 0 & 0 \end{bmatrix}$$
 (17)

 $P \cdot J \cdot P^{(-1)}$

$$\begin{bmatrix} 0 & -2 & 0 \\ 1 & -2 & 0 \\ 0 & 0 & -2 \end{bmatrix}$$
 (18)

 \rightarrow MatrixExponential($t \cdot A$)

$$\begin{bmatrix} e^{-t}\cos(t) + e^{-t}\sin(t) & -2e^{-t}\sin(t) & 0 \\ e^{-t}\sin(t) & e^{-t}\cos(t) - e^{-t}\sin(t) & 0 \\ 0 & 0 & e^{-2t} \end{bmatrix}$$
(19)

 \rightarrow MatrixExponential $(t \cdot J)$

$$\begin{bmatrix} e^{-2t} & 0 & 0 \\ 0 & e^{-t}\cos(t) + I e^{-t}\sin(t) & 0 \\ 0 & 0 & e^{-t}\cos(t) - I e^{-t}\sin(t) \end{bmatrix}$$
 (20)

Map(limit, MatrixExponential($t \cdot A$), t = infinity)

$$\begin{bmatrix}
0 & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & 0
\end{bmatrix}$$
(21)

> P := Matrix([[1, 0, 3, 14], [5, 6, 7, 28], [9, 10, 11, 142], [0, 0, 0, 1]])

$$P := \begin{bmatrix} 1 & 0 & 3 & 14 \\ 5 & 6 & 7 & 28 \\ 9 & 10 & 11 & 142 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
 (22)

> Determinant(P)

$$J := Diagonal Matrix([2, 2, -1, 0])$$

$$J := \begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A := P \cdot J \cdot P^*(-1)$$

$$A := \begin{bmatrix} -\frac{1}{4} & -\frac{45}{8} & \frac{27}{8} & -\frac{1273}{4} \\ -\frac{21}{4} & -\frac{89}{8} & \frac{63}{8} & -\frac{2933}{4} \\ -\frac{33}{4} & -\frac{165}{8} & \frac{115}{8} & -\frac{5393}{4} \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A := -8 \cdot A$$

$$A := \begin{bmatrix} 2 & 45 & -27 & 2546 \\ 42 & 89 & -63 & 5866 \\ 66 & 165 & -115 & 10786 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\Rightarrow solve(1 - x^2 = 0, x)$$

$$-1, 1$$

$$\Rightarrow eq := diff(x(t), t) = 1 - x(t)^2$$

$$eq := \frac{d}{dt} x(t) = 1 - x(t)^2$$

$$\Rightarrow ic := x(0) = -2$$

$$\Rightarrow sol := dsolve(\{eq, ie\}, x(t)\})$$

$$sol := x(t) = coth(-arctanh(\frac{1}{2}) + t)$$

$$\Rightarrow sol := rhs(sol)$$

$$sol := coth(-arctanh(\frac{1}{2}) + t)$$

$$\Rightarrow fl := convert(convert(sol, exp), exp)$$

$$fl := \frac{e^{2t} + 3}{e^{2t} - 3}$$

$$\Rightarrow ic := x(0) = 0$$

ic := x(0) = 0

(33)

| >
$$sol := dsolve(\{eq, ic\}, x(t))$$
 | $sol := x(t) = tanh(t)$ | (34)
| > $sol := rhs(sol)$ | $sol := tanh(t)$ | (35)
| > $f2 := convert(sol, exp)$ | $f2 := \frac{e' - e^{-t}}{e' + e^{-t}}$ | (36)
| > $ic := x(0) = -1$ | $ic := x(0) = -1$ | (37)
| > $sol := dsolve(\{eq, ic\}, x(t))$ | $sol := x(t) = -1$ | (38)
| > $ic := x(0) = 1$ | $ic := x(0) = 1$ | (39)
| > $sol := dsolve(\{eq, ic\}, x(t))$ | $sol := x(t) = 1$ | (40)
| > $sol := asolve(\{eq, ic\}, x(t))$ | $sol := x(t) = 1$ | (41)
| > $sol := asolve(\{eq, ic\}, x(t))$ | $sol := asolve(\{eq, ic\}, x(t))$ |

plot(fl)





