Time Series Analysis & Forecasting Using R

1. Introduction to tsibbles



Photo by Max Bender on Unsplash



Outline

- 1 Time series data and tsibbles
- 2 Example: Australian prison population
- 3 Example: Australian pharmaceutical sales
- 4 Lab Session 1
- 5 Time plots
- 6 Lab Session 2

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Tidyverts packages

tidyverts.org



Tidyverts developers





Time series data

- Four-yearly Olympic winning times
- Annual Google profits
- Quarterly Australian beer production
- Monthly rainfall
- Weekly retail sales
- Daily IBM stock prices
- Hourly electricity demand
- 5-minute freeway traffic counts
- Time-stamped stock transaction data

Class packages

```
# Data manipulation
library(dplyr)
# Plotting functions
library(ggplot2)
# Time and date manipulation
library(lubridate)
# Time series class
library(tsibble)
# Tidy time series data
library(tsibbledata)
# Time series graphics and statistics
library(feasts)
# Forecasting functions
library(fable)
```

Class packages

```
# Data manipulation
library(dplyr)
# Plotting functions
library(ggplot2)
# Time and date manipulation
library(lubridate)
# Time series class
library(tsibble)
# Tidy time series data
library(tsibbledata)
# Time series graphics and statistics
library(feasts)
# Forecasting functions
library(fable)
```

All of the above library(fpp3)

global_economy

```
# A tsibble: 15,150 x 6 [1Y]
# Kev:
      Country [263]
   Year Country
                          GDP Imports Exports Population
  <dbl> <fct>
                        <dbl>
                                <dbl>
                                       <dbl>
                                                 <dbl>
   1960 Afghanistan 537777811. 7.02 4.13
                                               8996351
   1961 Afghanistan 548888896. 8.10 4.45
                                                9166764
   1962 Afghanistan 546666678. 9.35
                                        4.88
                                                9345868
   1963 Afghanistan 751111191.
                                16.9
                                        9.17
                                               9533954
   1964 Afghanistan 800000044.
                                18.1
                                        8.89
                                               9731361
   1965 Afghanistan 1006666638.
                                21.4
                                       11.3
                                                9938414
   1966 Afghanistan 139999967.
                                18.6
                                        8.57
                                               10152331
   1967 Afghanistan 1673333418.
                                14.2
                                        6.77
                                               10372630
   1968 Afghanistan 1373333367.
                                15.2
                                        8.90
                                               10604346
   1969 Afghanistan 1408888922.
                                15.0
                                       10.1
                                               10854428
# i 15,140 more rows
```

global_economy

```
# A tsibble: 15,150 x 6 [1Y]
# Kev:
      Country [263]
   Year Country
                GDP Imports Exports Population
   Index <fct>
                        <dbl>
                               <dbl>
                                       <dbl>
                                                 <dbl>
   1960 Afghanistan 537777811. 7.02 4.13
                                               8996351
   1961 Afghanistan 548888896. 8.10 4.45
                                               9166764
   1962 Afghanistan 546666678. 9.35
                                       4.88
                                               9345868
   1963 Afghanistan 751111191.
                               16.9
                                       9.17
                                               9533954
   1964 Afghanistan 800000044.
                               18.1
                                       8.89
                                               9731361
   1965 Afghanistan 1006666638.
                               21.4
                                       11.3
                                               9938414
   1966 Afghanistan 139999967.
                               18.6
                                       8.57
                                              10152331
   1967 Afghanistan 1673333418.
                               14.2
                                       6.77
                                              10372630
   1968 Afghanistan 1373333367.
                               15.2
                                       8.90
                                              10604346
   1969 Afghanistan 1408888922.
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                                       10.1
                                              10854428
# i 15,140 more rows
```

global_economy

```
# A tsibble: 15,150 x 6 [1Y]
# Kev:
            Country [263]
   Year Country
                           GDP Imports Exports Population
   Index Kev
                         <dbl>
                                <dbl>
                                        <dbl>
                                                  <dbl>
   1960 Afghanistan 537777811. 7.02 4.13
                                                8996351
   1961 Afghanistan 548888896. 8.10 4.45
                                                9166764
   1962 Afghanistan 546666678.
                                 9.35
                                         4.88
                                                9345868
   1963 Afghanistan 751111191.
                                16.9
                                         9.17
                                                9533954
   1964 Afghanistan 800000044.
                                18.1
                                         8.89
                                                9731361
   1965 Afghanistan 1006666638.
                                21.4
                                        11.3
                                                9938414
   1966 Afghanistan 139999967.
                                18.6
                                        8.57
                                               10152331
   1967 Afghanistan 1673333418.
                                14.2
                                         6.77
                                               10372630
   1968 Afghanistan 1373333367.
                                15.2
                                         8.90
                                               10604346
   1969 Afghanistan 1408888922.
                                15.0
                                        10.1
                                               10854428
# i 15,140 more rows
```

8

global_economy

```
# A tsibble: 15,150 x 6 [1Y]
# Kev:
           Country [263]
   Year Country
                          GDP Imports Exports Population
   Index Kev
                     Measured variables
   1960 Afghanistan 537777811.
                                 7.02
                                        4.13
                                                8996351
   1961 Afghanistan 548888896. 8.10
                                        4.45
                                                9166764
   1962 Afghanistan 546666678. 9.35
                                        4.88
                                                9345868
   1963 Afghanistan 751111191.
                                16.9
                                        9.17
                                                9533954
   1964 Afghanistan 800000044.
                                18.1
                                        8.89
                                                9731361
   1965 Afghanistan 1006666638.
                                21.4
                                        11.3
                                                9938414
   1966 Afghanistan 139999967.
                                18.6 8.57
                                               10152331
   1967 Afghanistan 1673333418.
                                14.2
                                        6.77
                                               10372630
   1968 Afghanistan 1373333367.
                                15.2
                                        8.90
                                               10604346
   1969 Afghanistan 1408888922.
                                15.0
                                        10.1
                                               10854428
# i 15,140 more rows
```

tourism

```
# A tsibble: 24,320 x 5 [10]
# Kev:
            Region, State, Purpose [304]
  Ouarter Region State Purpose
                                  Trips
     <qtr> <chr> <chr> <chr>
                                  <dbl>
 1 1998 Q1 Adelaide SA
                         Business
                                   135.
 2 1998 O2 Adelaide SA
                         Business 110.
3 1998 O3 Adelaide SA
                         Business 166.
 4 1998 O4 Adelaide SA
                         Business 127.
 5 1999 Q1 Adelaide SA
                         Business
                                   137.
 6 1999 O2 Adelaide SA
                         Business
                                   200.
 7 1999 03 Adelaide SA
                         Business
                                   169.
 8 1999 O4 Adelaide SA
                         Business 134.
 9 2000 Q1 Adelaide SA
                         Business 154.
  2000 Q2 Adelaide SA
                         Business 169.
# i 24,310 more rows
```

tourism

```
# A tsibble: 24,320 x 5 [10]
# Kev:
            Region, State, Purpose [304]
  Quarter Region State Purpose
                                  Trips
          <chr> <chr> <chr>
   Index
                                  <dbl>
 1 1998 Q1 Adelaide SA
                         Business
                                   135.
 2 1998 O2 Adelaide SA
                         Business 110.
 3 1998 O3 Adelaide SA
                         Business
                                   166.
 4 1998 O4 Adelaide SA
                         Business 127.
 5 1999 Q1 Adelaide SA
                         Business
                                   137.
 6 1999 O2 Adelaide SA
                         Business
                                   200.
 7 1999 03 Adelaide SA
                         Business
                                   169.
 8 1999 O4 Adelaide SA
                         Business 134.
 9 2000 Q1 Adelaide SA
                         Business 154.
  2000 Q2 Adelaide SA
                         Business
                                  169.
# i 24,310 more rows
```

tourism

```
# A tsibble: 24,320 x 5 [10]
# Kev:
             Region, State, Purpose [304]
   Ouarter Region State Purpose
                                   Trips
   Index
           Keys
                                   <dbl>
 1 1998 Q1 Adelaide SA
                          Business
                                    135.
 2 1998 O2 Adelaide SA
                          Business
                                    110.
 3 1998 O3 Adelaide SA
                          Business
                                    166.
 4 1998 O4 Adelaide SA
                          Business 127.
 5 1999 Q1 Adelaide SA
                          Business
                                    137.
 6 1999 O2 Adelaide SA
                          Business
                                    200.
 7 1999 03 Adelaide SA
                          Business
                                    169.
 8 1999 O4 Adelaide SA
                          Business 134.
 9 2000 Q1 Adelaide SA
                          Business 154.
  2000 Q2 Adelaide SA
                          Business
                                   169.
# i 24,310 more rows
```

A tsibble: 24,320 x 5 [10]

tourism

```
# Kev:
            Region, State, Purpose [304]
  Ouarter Region State Purpose
                                  Trips
   Index
           Keys
                                  Measure
1 1998 Q1 Adelaide SA
                          Business
                                    135.
2 1998 O2 Adelaide SA
                          Business
                                   110.
3 1998 O3 Adelaide SA
                          Business 166.
4 1998 O4 Adelaide SA
                          Business 127.
5 1999 Q1 Adelaide SA
                          Business
                                   137.
6 1999 O2 Adelaide SA
                          Business
                                   200.
7 1999 03 Adelaide SA
                          Business
                                   169.
8 1999 O4 Adelaide SA
                          Business 134.
9 2000 Q1 Adelaide SA
                          Business 154.
  2000 Q2 Adelaide SA
                          Business
                                   169.
# i 24,310 more rows
```

- A tsibble allows storage and manipulation of multiple time series in R.
- It contains:
 - An index: time information about the observation
 - Measured variable(s): numbers of interest
 - Key variable(s): optional unique identifiers for each series
- It works with tidyverse functions.

Example

```
mydata <- tsibble(</pre>
 year = 2012:2016,
 y = c(123, 39, 78, 52, 110),
 index = year
mydata
# A tsibble: 5 x 2 [1Y]
  year
  <int> <dbl>
1 2012
        123
  2013
        39
  2014
        78
        52
  2015
   2016
          110
```

For observations more frequent than once per year, we need to use a time class function on the index.

Z

5 2019 May

For observations more frequent than once per year, we need to use a time class function on the index.

```
z |>
 mutate(Month = yearmonth(Month)) |>
 as_tsibble(index = Month)
# A tsibble: 5 x 2 [1M]
     Month Observation
     <mth> <dbl>
1 2019 Jan
                     50
2 2019 Feb
                     23
3 2019 Mar
                     34
4 2019 Apr
                     30
```

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Common time index variables can be created with these functions:

Frequency	Function
Annual	start:end
Quarterly	yearquarter()
Monthly	yearmonth()
Weekly	yearweek()
Daily	<pre>as_date(), ymd()</pre>
Sub-daily	as_datetime()

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Australian prison population



prison <- readr::read_csv("data/prison_population.csv")</pre>

```
# A tibble: 3,072 x 6
  date
           state gender legal indigenous count
  <date> <chr> <chr> <chr> <chr>
                                           <dbl>
1 2005-03-01 ACT Female Remanded ATSI
2 2005-03-01 ACT Female Remanded Other
3 2005-03-01 ACT Female Sentenced ATSI
4 2005-03-01 ACT Female Sentenced Other
5 2005-03-01 ACT Male Remanded ATSI
6 2005-03-01 ACT Male Remanded Other
                                              58
7 2005-03-01 ACT Male Sentenced ATSI
8 2005-03-01 ACT Male Sentenced Other
9 2005-03-01 NSW Female Remanded ATSI
                                              51
10 2005-03-01 NSW Female Remanded Other
                                             131
# i 3.062 more rows
```

```
prison <- readr::read_csv("data/prison_population.csv") |>
  mutate(Quarter = yearquarter(date))
```

```
# A tibble: 3,072 x 7
  date
            state gender legal indigenous count Quarter
  <date> <chr> <chr> <chr> <chr>
                                            <dbl> <qtr>
1 2005-03-01 ACT Female Remanded ATSI
                                               0 2005 Q1
2 2005-03-01 ACT Female Remanded Other
                                               2 2005 01
3 2005-03-01 ACT Female Sentenced ATSI
                                               0 2005 01
4 2005-03-01 ACT Female Sentenced Other
                                               0 2005 Q1
5 2005-03-01 ACT
                  Male Remanded ATSI
                                               7 2005 01
6 2005-03-01 ACT
                  Male Remanded Other
                                               58 2005 01
7 2005-03-01 ACT
                  Male Sentenced ATSI
                                               0 2005 Q1
8 2005-03-01 ACT
                  Male Sentenced Other
                                               0 2005 01
9 2005-03-01 NSW Female Remanded ATSI
                                               51 2005 01
10 2005-03-01 NSW Female Remanded Other
                                              131 2005 01
# i 3.062 more rows
```

```
prison <- readr::read_csv("data/prison_population.csv") |>
  mutate(Quarter = yearquarter(date)) |>
  select(-date)
```

```
# A tibble: 3,072 x 6
  state gender legal indigenous count Ouarter
  <chr> <chr> <chr>
                        <chr>
                                   <dbl> <atr>
1 ACT
        Female Remanded ATSI
                                       0 2005 Q1
2 ACT
        Female Remanded Other
                                       2 2005 01
3 ACT
        Female Sentenced ATST
                                       0 2005 01
4 ACT
        Female Sentenced Other
                                       0 2005 Q1
5 ACT
        Male
               Remanded ATSI
                                       7 2005 01
6 ACT
        Male
               Remanded Other
                                      58 2005 01
7 ACT
        Male
               Sentenced ATSI
                                       0 2005 01
8 ACT
        Male
               Sentenced Other
                                       0 2005 01
9 NSW
        Female Remanded ATSI
                                      51 2005 01
10 NSW
        Female Remanded Other
                                     131 2005 01
# ÷ 2 002 -----
```

```
prison <- readr::read csv("data/prison population.csv") |>
 mutate(Quarter = yearquarter(date)) |>
  select(-date) |>
  as tsibble(
   index = Quarter,
   kev = c(state, gender, legal, indigenous)
# A tsibble: 3,072 x 6 [10]
            state, gender, legal, indigenous [64]
# Kev:
  state gender legal indigenous count Quarter
  <chr> <chr> <chr> <chr> <chr> <chr> <chr> <dbl> <gtr>
        Female Remanded ATSI
 1 ACT
                                       0 2005 Q1
2 ACT
        Female Remanded ATSI
                                       1 2005 02
```

0 2005 03

0 2005 04

5 ACT Female Remanded ATSI 1 2006 Q1 6 ACT Female Remanded ATSI 1 2006 Q2

Female Remanded ATSI

Female Remanded ATSI

3 ACT

4 ACT

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Australian Pharmaceutical Benefits Scheme



Australian Pharmaceutical Benefits Scheme

The **Pharmaceutical Benefits Scheme** (PBS) is the Australian government drugs subsidy scheme.

Australian Pharmaceutical Benefits Scheme

The **Pharmaceutical Benefits Scheme** (PBS) is the Australian government drugs subsidy scheme.

- Many drugs bought from pharmacies are subsidised to allow more equitable access to modern drugs.
- The cost to government is determined by the number and types of drugs purchased. Currently nearly 1% of GDP.
- The total cost is budgeted based on forecasts of drug usage.
- Costs are disaggregated by drug type (ATC1 x15 / ATC2 84), concession category (x2) and patient type (x2), giving 84 × 2 × 2 = 336 time series.

PBS

```
# A tsibble: 67,596 x 9 [1M]
# Kev:
            Concession, Type, ATC1, ATC2 [336]
     Month Concession Type
                               ATC1 ATC1 desc ATC2 ATC2 desc Scripts Cost
      <mth> <chr>
                        <chr> <chr> <chr> <chr>
                                                <chr> <chr>
                                                                  <dbl> <dbl>
1 1991 Jul Concessional Co-pay~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  18228 67877
2 1991 Aug Concessional Co-pay~ A
                                     Alimenta~ A01
                                                      STOMATOL~
                                                                  15327 57011
 3 1991 Sep Concessional Co-pay~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  14775 55020
4 1991 Oct Concessional Co-pay~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  15380 57222
5 1991 Nov Concessional Co-pay~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  14371 52120
6 1991 Dec Concessional Co-pay~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  15028 54299
7 1992 Jan Concessional Co-pay~ A
                                      Alimenta~ A01
                                                                  11040 39753
                                                      STOMATOL~
8 1992 Feb Concessional Co-pay~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  15165 54405
9 1992 Mar Concessional Co-pay~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  16898 61108
10 1992 Apr Concessional Co-pav~ A
                                      Alimenta~ A01
                                                      STOMATOL~
                                                                  18141 65356
# i 67,586 more rows
```

PBS |>

We can use the filter() function to select rows.

```
filter(ATC2 == "A10")
# A tsibble: 816 x 9 [1M]
# Key: Concession, Type, ATC1, ATC2 [4]
     Month Concession Type ATC1 ATC1 desc ATC2 ATC2 desc Scripts Cost
     <mth> <chr>
                  <chr> <chr> <chr> <chr> <chr>
                                                               <dbl> <dbl>
1 1991 Jul Concessional Co-pa~ A
                                   Alimenta~ A10
                                                   ANTIDIAB~
                                                              89733 2.09e6
2 1991 Aug Concessional Co-pa~ A Alimenta~ A10
                                                   ANTIDIAB~
                                                              77101 1.80e6
3 1991 Sep Concessional Co-pa~ A
                                   Alimenta~ A10
                                                   ANTIDIAB~
                                                              76255 1.78e6
4 1991 Oct Concessional Co-pa~ A
                                   Alimenta~ A10
                                                   ANTIDIAB~
                                                              78681 1.85e6
5 1991 Nov Concessional Co-pa~ A
                                    Alimenta~ A10
                                                   ANTIDIAB~
                                                               70554 1.69e6
6 1991 Dec Concessional Co-pa~ A
                                    Alimenta~ A10
                                                   ANTIDIAB~
                                                              75814 1.84e6
 7 1992 Jan Concessional Co-pa~ A
                                    Alimenta~ A10
                                                   ANTIDIAB~
                                                               64186 1.56e6
8 1992 Feb Concessional Co-pa~ A
                                    Alimenta~ A10
                                                   ANTIDIAB~
                                                              75899 1.73e6
9 1992 Mar Concessional Co-pa~ A
                                    Alimenta~ A10
                                                   ANTTDTAR~
                                                              89445 2.05e6
10 1992 Apr Concessional Co-pa~ A
                                    Alimenta~ A10
                                                   ANTTDTAR~
                                                               97315 2.23e6
```

We can use the select() function to select columns.

```
PBS I>
  filter(ATC2 == "A10") |>
  select(Month, Concession, Type, Cost)
# A tsibble: 816 x 4 [1M]
       Concession, Type [4]
# Kev:
     Month Concession Type
                                     Cost
     <mth> <chr>
                  <chr>
                                     <dbl>
 1 1991 Jul Concessional Co-payments 2092878
2 1991 Aug Concessional Co-payments 1795733
 3 1991 Sep Concessional Co-payments 1777231
4 1991 Oct Concessional Co-payments 1848507
5 1991 Nov Concessional Co-payments 1686458
6 1991 Dec Concessional Co-payments 1843079
 7 1992 Jan Concessional Co-payments 1564702
8 1992 Feb Concessional Co-payments 1732508
 9 1992 Mar Concessional Co-nayments 2046102
```

We can use the summarise() function to summarise over keys.

```
PBS |>
  filter(ATC2 == "A10") |>
  select(Month, Concession, Type, Cost) |>
  summarise(total_cost = sum(Cost))
```

```
# A tsibble: 204 x 2 [1M]
      Month total cost
      <mth>
                <dbl>
1 1991 Jul 3526591
2 1991 Aug
             3180891
3 1991 Sep
              3252221
4 1991 Oct
              3611003
5 1991 Nov
              3565869
6 1991 Dec
              4306371
7 1992 Jan
              5088335
8 1992 Feb
              2814520
9 1992 Mar
              2985811
```

We can use the mutate() function to create new variables.

```
PBS |>
  filter(ATC2 == "A10") |>
  select(Month, Concession, Type, Cost) |>
  summarise(total_cost = sum(Cost)) |>
  mutate(total_cost = total_cost / 1e6)
```

```
# A tsibble: 204 x 2 [1M]
     Month total_cost
     <mth>
               <dbl>
1 1991 Jul 3.53
2 1991 Aug 3.18
3 1991 Sep 3.25
4 1991 Oct 3.61
5 1991 Nov
               3.57
6 1991 Dec
               4.31
7 1992 Jan
               5.09
8 1992 Feb
                2.81
```

Working with tsibble objects

We can use the mutate() function to create new variables.

```
PBS |>
  filter(ATC2 == "A10") |>
  select(Month, Concession, Type, Cost) |>
  summarise(total_cost = sum(Cost)) |>
  mutate(total_cost = total_cost / 1e6) -> a10
```

```
# A tsibble: 204 x 2 [1M]
    Month total_cost
     <mth>
              <dbl>
1 1991 Jul 3.53
2 1991 Aug 3.18
3 1991 Sep 3.25
4 1991 Oct 3.61
5 1991 Nov
              3.57
6 1991 Dec
               4.31
7 1992 Jan
               5.09
8 1992 Feb
               2.81
```

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Lab Session 1

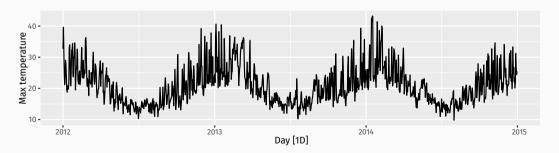
- Download tourism.xlsx from
 http://robjhyndman.com/data/tourism.xlsx, and read it
 into R using read_excel() from the readxl package.
- Create a tsibble which is identical to the tourism tsibble from the tsibble package.
- Find what combination of Region and Purpose had the maximum number of overnight trips on average.
- Create a new tsibble which combines the Purposes and Regions, and just has total trips by State.

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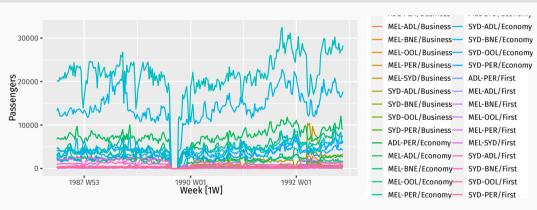
Time plots

```
maxtemp <- vic_elec |>
  index_by(Day = date(Time)) |>
  summarise(Temperature = max(Temperature))
maxtemp |>
  autoplot(Temperature) +
  labs(y = "Max temperature")
```

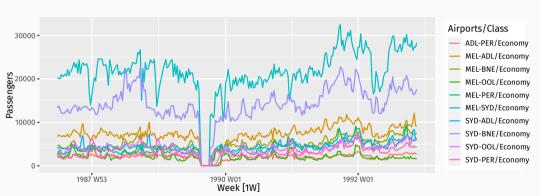




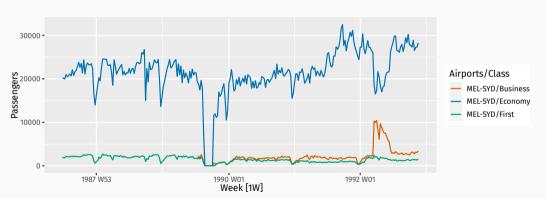
```
ansett |>
  autoplot(Passengers)
```



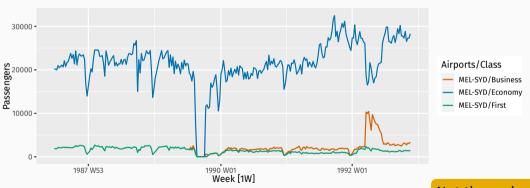
```
ansett |>
  filter(Class == "Economy") |>
  autoplot(Passengers)
```



```
ansett |>
  filter(Airports == "MEL-SYD") |>
  autoplot(Passengers)
```



```
ansett |>
  filter(Airports == "MEL-SYD") |>
  autoplot(Passengers)
```



Not the real data! Or is it?

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Lab Session 2

- Create time plots of the following four time series:
 - Bricks from aus_production
 - 2 Lynx from pelt
 - 3 Close **from** gafa_stock
 - Demand from vic_elec
- Use help() to find out about the data in each series.
- For the last plot, modify the axis labels and title.