

¡Felicitaciones! ¡Aprobaste!

Calificación recibida 100 % Para Aprobar 80 % o más

Ir al siguiente elemento

Problem Set #1

C	alificación de la entrega más reciente: 100 $\%$	
1.	3-way-Merge Sort: Suppose that instead of dividing in half at each step of Merge Sort, you divide into thirds, sort each third, and finally combine all of them using a three-way merge subroutine. What is the overall asymptotic running time of this algorithm? (Hint: Note that the merge step can still be implemented in $O(n)$ time.)	1 / 1 punto
	$lacksquare$ $n \log(n)$	
	$\bigcap n(\log(n))^2$	
	\bigcirc n	
	$\bigcap n^2 \log(n)$	
	Correcto That's correct! There is still a logarithmic number of levels, and the overall amount of work at each level is still linear.	
2.	You are given functions f and g such that $f(n) = O(g(n))$. Is $f(n) * log_2(f(n)^c) = O(g(n) * log_2(g(n)))$? (Here c is some positive constant.) You should assume that f and g are nondecreasing and always bigger than 1.	1/1 punto
	igcirc Sometimes yes, sometimes no, depending on the constant c	
	○ False	
	igcirc Sometimes yes, sometimes no, depending on the functions f and g	
	● True	
	Correcto That's correct! Roughly, because the constant c in the exponent is inside a logarithm, it becomes part of the leading constant and gets suppressed by the big-Oh notation.	
3.	Assume again two (positive) nondecreasing functions f and g such that $f(n) = O(g(n))$. Is $2^{f(n)} = O(2^{g(n)})$? (Multiple answers may be correct, you should check all of those that apply.)	1/1 punto
	Always	
	□ Never	
	$lacksquare$ Yes if $f(n) \leq g(n)$ for all sufficiently large n	
	○ Correcto	
	lacksquare Sometimes yes, sometimes no (depending on f and g)	
	○ Correcto	

 $\textbf{4.} \quad \text{k-way-Merge Sort. Suppose you are given } k \text{ sorted arrays, each with } n \text{ elements, and you want to combine them into a single array of } k n \text{ elements. Consider the following}$ $approach. \ Using the merge subroutine taught in lecture, you merge the first 2 arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the first two arrays, then merge the 3^{rd} given array with this merged version of the 5^{rd} given array with the first two arrays are the 3^{rd} given array with the 3^{rd} given array with this merged version of the 5^{rd} given array with the 3^{rd} given array wit$ merge the 4^{th} given array with the merged version of the first three arrays, and so on until you merge in the final (k^{th}) input array. What is the running time taken by this successive merging algorithm, as a function of k and n? (Ontional: can you think of a faster way to do the k-way merge procedure?)

1/1 punto

$\bigcap \theta(n\log(k))$	
\bigcap $\theta(nk)$	
\bigcirc $ heta(n^2k)$	
$lack egin{array}{c} heta(nk^2) \end{array}$	
\odot Correcto That's correct! For the upper bound, the merged list size is always $O(kn)$, merging is linear in the size of the larger array, and there are k iterations. For the lower bound, each of the last $k/2$ merges takes $\Omega(kn)$ time.	
Assume the following functions in increasing evelor of growth rate (with $g(y)$ following $f(y)$ in your list if and only if $f(y) = O(g(y))$)	
_	1/1 pu
$\mathfrak{b})10^n$	
c) $n^{1.5}$	
$\mathrm{d} i 2^{\sqrt{\log(n)}}$	
e) $n^{5/3}$	
Write your 5-letter answer, i.e., the sequence in lower case letters in the space provided. For example, if you feel that the answer is a->b->c->d->e (from smallest to largest), then type abcde in the space provided without any spaces before / after / in between the string.	
You can assume that all logarithms are base 2 (though it actually doesn't matter).	
WARNING: this question has multiple versions, you might see different ones on different attempts!	
daceb Please note: Each of the following will be interpreted as a single variable, not as a product of variables: daceb. To multiply variables, please use * (e.g. enter x*y to multiply variables x and y).	
daceb	
Correcto One approach is to graph these functions for large values of n. Once in a while this can be misleading, however. Another useful trick is to take logarithms and see what happens (though again be careful, as in Question 3).	
C C C C C C C C C C C C C C C C C C C	$\theta(nk)$ $\theta(nk)$ $\theta(nk^2)$