



# **Circuit Theory and Electronics Fundamentals**

Department of Electrical and Computer Engineering, Técnico, University of Lisbon

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## **Laboratory Assignment - T1**

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# 1 Introduction

The objective of this laboratory assignment is to study a circuit containing:

- seven resistors ( $R_1$ - $R_7$ )
- one voltage source ( $V_a$ )
- one current source ( $I_d$ )
- one voltage-controlled current source ( $I_b$ )
- one current-controlled voltage source ( $V_c$ )

Circuit T1 is presented in Figure 1. All components, including nodes ( $N1$ - $N8$ ) and ground ( $GND$  or 0), are identified with their respective names. Note that  $I_b$  is also referred to as  $G_1$  and  $V_c$  as  $H_1$  (explanation can be found in Subsection 3.1). Furthermore, the existence of  $N6$  and  $N7$  is also explained in Subsection 3.1, however, consider the voltages in both nodes to be equal.

In Section 2, a theoretical analysis (using two distinct methods) of the circuit is presented. In Section 3, the circuit is analysed by simulation, and the results are compared to the theoretical results obtained in Section 2. The conclusions of this study are outlined in Section 4.

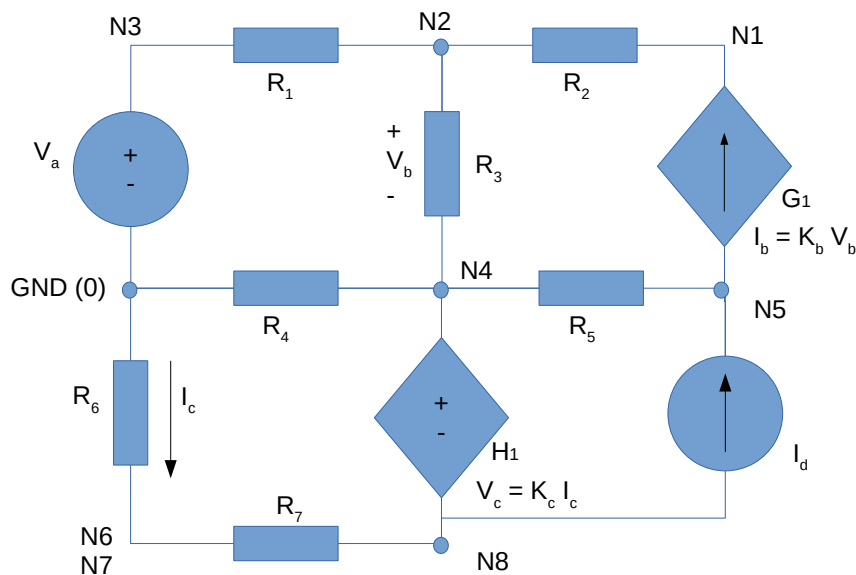


Figure 1: Circuit T1

For this laboratory assignment, the values considered for all the variables can be found on Table 1. They were obtained through a Python script that generates random values.

Name	Value
$R_1$	1.00359089673
$R_2$	2.04298963569
$R_3$	3.02503141993
$R_4$	4.05647775356
$R_5$	3.07781188185
$R_6$	2.01277040929
$R_7$	1.01993304256
$V_a$	5.11402517827
$I_d$	1.03896393154
$K_b$	7.23768458527
$K_c$	8.33526265782

Table 1: Values provided by the Python script. Units for the values: kOhm, V, mA and mS

## 2 Theoretical Analysis

In this section, the circuit in Figure 1 is analysed theoretically.

Two methods were used and both will be presented and explained. In Subsection 2.1 the application of the mesh method and its results are shown. In Subsection 2.2 the same is done with the node method.

### 2.1 Mesh method

Name	Value [A or V]
$V_b$	-4.752955e+00
$V_c$	7.657904e+00
@ $I_b$	-2.957272e-01
@ $I_c$	9.187358e-01
@ $I_d$	1.038964e+00

Table 2: Values computed by Octave. Variables identified with a '@' have a corresponding value in Ampere (A). The others are expressed in Volts (V).

### 2.2 Node method

## 3 Simulation Analysis

In this section, Circuit T1 is reproduced with the help of Ngspice.

Name	Value [A or V]
$V_{N1}$	4.226624e+00
$V_{N2}$	4.830792e+00
$V_{N3}$	5.114025e+00
$V_{N4}$	4.871651e+00
$V_{N5}$	8.979579e+00
$V_{N6}$	-1.849204e+00
$V_{N8}$	-2.786253e+00
$V_b$	4.085937e-02
$V_c$	7.657904e+00
@ $I_b$	2.957272e-04
@ $I_c$	9.187358e-04
@ $I_{H1}$	-1.202281e-04

Table 3: Values computed by Octave. Variables identified with a '@' have a corresponding value in Ampere (A). The others are expressed in Volts (V).

Firstly, the outcome of the simulation is shown, as well as a brief explanation on how it was achieved. Afterwards, a comparison is done between those values and the ones attained in Section 2.

### 3.1 Simulated results

Ngspice is a simulator for electronic circuits that can output a variety of results. This emulator computes the voltages in every node, as well as the potential difference between two given nodes. Apart from that, the group made use of the command *.options savecurrents* which also enables the output of the currents that pass through all branches.

With the limitation that Ngspice only provides the current in the components and not through the nodes, an additional voltage source ( $V_{aux}$ ) was added so that the current in  $R_6$  ( $I_c$ ) is known. This source (not displayed in Figure 1) as a voltage of 0V and it was implemented between  $R_6$  and  $R_7$ . Therefore an additional node had to be added (node  $N7$ ).

As previously stated,  $I_b$  is referred to as  $G_1$ . This is because, in Ngspice, a voltage-controlled current source is identified with capital 'g' (G). In the case of  $V_c$ , all current-controlled voltage source are identified with H.

Table 4 shows the simulated operating point results for Circuit T1.

### 3.2 Comparison

By comparing both Tables, we confirm that all the absolute values displayed in Table 4 are identical to the ones shown in Table 3, including all decimal digits.

All the voltages in every node match with high precision. Moreover,  $V_b$  and  $V_c$  are equal to the simulated values, which are presented in Table 4 as  $v(n2, n4)$  and  $v(n4, n8)$ , respectively. Finally, theoretical  $I_d$  is also the same as the one obtained via Ngspice ('@g1[i]').

It is also worth noting that all theoretical calculations consider every element of the circuit to be ideal (without energy loss nor self-inductance nor any other phenomena that could alter the results). Similarly, Ngspice also considers all components to be ideal. Therefore every source of discrepancies between theoretical and simulated results are removed (apart from the small limitations concerning calculations and the rounding of values).

Name	Value [A or V]
i(vaux)	9.187358e-04
i(h1)	1.202281e-04
@g1[i]	-2.95727e-04
@id[current]	1.038964e-03
@r1[i]	-2.82220e-04
@r2[i]	-2.95727e-04
@r3[i]	1.350709e-05
@r4[i]	-1.20096e-03
@r5[i]	-1.33469e-03
@r6[i]	9.187358e-04
@r7[i]	-9.18736e-04
n1	4.226624e+00
n2	4.830792e+00
n3	5.114025e+00
n4	4.871651e+00
n5	8.979579e+00
n6	-1.84920e+00
n7	-1.84920e+00
n8	-2.78625e+00
v(n4,n2)	4.085937e-02
v(n4,n8)	7.657904e+00

Table 4: Values provided by Ngspice. Variables identified with a '@' or are of the type  $i(...)$  have a corresponding value in Ampere (A). The others are expressed in Volts (V).

## 4 Conclusion

For this laboratory assignment, we were given a circuit composed by 7 resistors, 1 independent voltage source, 1 independent current source, 1 current-dependent voltage source, 1 voltage-dependent current source and had the objective of analyzing and simulating it, which we did successfully.

Static analyses were performed theoretically and by circuit simulation, using the Octave math tool and Ngspice tool, respectively. The simulation results matched the theoretical results very precisely, despite the circuit having dependent voltage and current sources (which could have caused some discrepancies in the results).