

# Circuit Theory and Electronics Fundamentals

Department of Electrical and Computer Engineering, Técnico, University of Lisbon

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## Laboratory Assignment - T1

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### Group nº59

José Miguel Goulão - 95814

Lourenço Pacheco - 95817

André Gomes - 96352

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# 1 Introduction

The objective of this laboratory assignment is to study a circuit containing:

- seven resistors ( $R_1$ - $R_7$ )
- one voltage source ( $V_a$ )
- one current source ( $I_d$ )
- one voltage-controlled current source ( $I_b$ )
- one current-controlled voltage source ( $V_c$ )

Circuit T1 is presented in Figure 1. All components, including nodes ( $N1$ - $N8$ ) and ground ( $GND$  or 0), are identified with their respective names. Note that  $I_b$  is also referred to as  $G_1$  and  $V_c$  as  $H_1$  (explanation can be found in Subsection 3.1). Furthermore, the existence of  $N6$  and  $N7$  is also explained in Subsection 3.1, however, consider the voltages in both nodes to be equal.

In Section 2, a theoretical analysis (using two distinct methods) of the circuit is presented. In Section 3, the circuit is analysed by simulation, and the results are compared to the theoretical results obtained in Section 2. The conclusions of this study are outlined in Section 4.

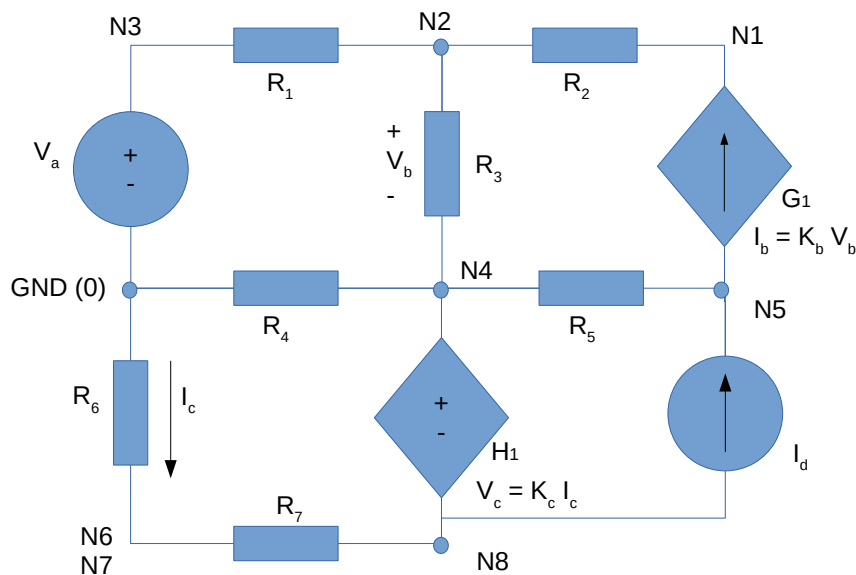


Figure 1: Circuit T1

For this laboratory assignment, the values considered for all the variables can be found on Table 1. They were obtained through a Python script that generates random values.

Name	Value
$R_1$	1.00359089673
$R_2$	2.04298963569
$R_3$	3.02503141993
$R_4$	4.05647775356
$R_5$	3.07781188185
$R_6$	2.01277040929
$R_7$	1.01993304256
$V_a$	5.11402517827
$I_d$	1.03896393154
$K_b$	7.23768458527
$K_c$	8.33526265782

Table 1: Values provided by the Python script. Units for the values: kOhm, V, mA and mS

## 2 Theoretical Analysis

In this section, the circuit in Figure 1 is analysed theoretically.

Two methods were used and both will be explained and presented. In Subsection 2.1 the application of the mesh method and its results are shown. In Subsection 2.2 the same is done with the node method.

In both of these methods, three important equations were used: both Kirchhoff's laws (Kirchhoff's current law (KCL) - eq.(1) and Kirchhoff's voltage law (KVL)- eq.(2)); Ohm's law (eq.(3)).

The algebraic sum of all the currents in any given node is zero:

$$\sum I_i = 0 \quad (1)$$

The algebraic sum of all the voltages in any given closed-loop circuit (mesh) is zero:

$$\sum V_i = 0 \quad (2)$$

The potential difference between the two nodes connected to a resistor is equal to the current that passes through the resistor multiplied by the its resistance.

$$V_i = R_i I_i \quad (3)$$

### 2.1 Mesh method

To correctly use the mesh method, firstly, four currents must be considered, one for each simple mesh. They were identified as follows:  $I_1$  - associated with the top left mesh;  $I_2$  - associated with the top right mesh;  $I_3$  - associated with the bottom left mesh;  $I_4$  - associated with the bottom right mesh. Every one of these currents is assumed to run counter clockwise.

Afterwards, eq. 2 needs to be applied in the meshes not containing any type of current sources (eq.(4) and eq.(5)). Moreover, it is essential to relate the remaining mesh current with those created by the current sources (eq.(6) and eq.(7)). Likewise, eq.(8) is also obtained.

$$V_a = I_1(R_1 + R_3 + R_4) - I_2(R_3) - I_3(R_4) \quad (4)$$

$$-V_c = I_3(R_4 + R_6 + R_7) - I_1(R_4) \quad (5)$$

$$I_2 = -I_b \quad (6)$$

$$I_4 = -I_d \quad (7)$$

$$I_3 = -I_c \quad (8)$$

Further relations need to be made in order to solve the circuit. We must not forget the two equations from the linear dependent sources (eq.(9) and eq.(10)). In addition, by making use of eq.(3), one more equation is acquired, eq. 11.

$$I_b = K_b V_b \quad (9)$$

$$V_c = K_c I_b \quad (10)$$

$$I_1(R_3) - I_2(R_3) = V_b \quad (11)$$

With eight equations and eight unknown variables, the system can be solved. The results were computed by Octave and organized in Table 2

Name	Value [A or V]
@I <sub>1</sub>	2.820335e-04
@I <sub>2</sub>	2.955316e-04
@I <sub>3</sub>	9.189620e-04
@I <sub>4</sub>	-1.038964e-03
V <sub>b</sub>	-4.083234e-02
V <sub>c</sub>	-7.658750e+00
@I <sub>b</sub>	-2.955316e-04
@I <sub>c</sub>	-9.189620e-04

Table 2: Values computed by Octave. Variables identified with a '@' have a corresponding value in Ampere (A). The others are expressed in Volts (V).

## 2.2 Node method

Similarly to the previous subsection, for the node method, ground was considered to be where it is identified in Figure 1. In addition, assume  $V_{Ni}$  to be the voltage in node  $Ni$  (every node position can also be found in Figure 1).

The results were computed by Octave and organized in Table 3

## 3 Simulation Analysis

In this section, Circuit T1 is reproduced with the help of Ngspice.

Firstly, the outcome of the simulation is shown, as well as a brief explanation on how it was achieved. Afterwards, a comparison is done between those values and the ones attained in Section 2.

Name	Value [A or V]
$V_{N1}$	4.226624e+00
$V_{N2}$	4.830792e+00
$V_{N3}$	5.114025e+00
$V_{N4}$	4.871651e+00
$V_{N5}$	8.979579e+00
$V_{N6}$	-1.849204e+00
$V_{N8}$	-2.786253e+00
$V_b$	4.085937e-02
$V_c$	7.657904e+00
@ $I_b$	2.957272e-04
@ $I_c$	9.187358e-04
@ $I_{H1}$	-1.202281e-04

Table 3: Values computed by Octave. Variables identified with a '@' have a corresponding value in Ampere (A). The others are expressed in Volts (V).

### 3.1 Simulated results

Ngspice is a simulator for electronic circuits that can output a variety of results. This emulator computes the voltages in every node, as well as the potential difference between two given nodes. Apart from that, the group made use of the command `.options savecurrents` which also enables the output of the currents that pass through all branches.

With the limitation that Ngspice only provides the current in the components and not through the nodes, an additional voltage source ( $V_{aux}$ ) was added so that the current in  $R_6$  ( $I_c$ ) is known. This source (not displayed in Figure 1) as a voltage of 0V and it was implemented between  $R_6$  and  $R_7$ . Therefore an additional node had to be added (node  $N7$ ).

As previously stated,  $I_b$  is referred to as  $G_1$ . This is because, in Ngspice, a voltage-controlled current source is identified with capital 'g' ( $G$ ). In the case of  $V_c$ , all current-controlled voltage source are identified with  $H$ .

Table 4 shows the simulated operating point results for Circuit T1.

### 3.2 Comparison

By comparing both Tables, we confirm that all the absolute values displayed in Table 4 are identical to the ones shown in Section 2, including all decimal digits.

All the voltages in every node match with high precision. Moreover,  $V_b$  and  $V_c$  are equal to the simulated values, which are presented in Table 4 as  $v(n2, n4)$  and  $v(n4, n8)$ , respectively. Finally, theoretical  $I_d$  is also the same as the one obtained via Ngspice ('@g1[i]').

It is also worth noting that all theoretical calculations consider every element of the circuit to be ideal (without energy loss nor self-inductance nor any other phenomena that could alter the results). Similarly, Ngspice also considers all components to be ideal. Therefore every source of discrepancies between theoretical and simulated results are removed (apart from the small limitations concerning calculations and the rounding of values).

Name	Value [A or V]
i(vaux)	9.187358e-04
i(h1)	1.202281e-04
@g1[i]	-2.95727e-04
@id[current]	1.038964e-03
@r1[i]	-2.82220e-04
@r2[i]	-2.95727e-04
@r3[i]	1.350709e-05
@r4[i]	-1.20096e-03
@r5[i]	-1.33469e-03
@r6[i]	9.187358e-04
@r7[i]	-9.18736e-04
n1	4.226624e+00
n2	4.830792e+00
n3	5.114025e+00
n4	4.871651e+00
n5	8.979579e+00
n6	-1.84920e+00
n7	-1.84920e+00
n8	-2.78625e+00
v(n4,n2)	4.085937e-02
v(n4,n8)	7.657904e+00

Table 4: Values from Ngspice. Variables identified with a '@' or are of the type  $i(...)$  have a corresponding value in Ampere (A). The others are expressed in Volts (V).

## 4 Conclusion

For this laboratory assignment, we were given a circuit composed by 7 resistors, 1 independent voltage source, 1 independent current source, 1 current-dependent voltage source, 1 voltage-dependent current source and had the objective of analyzing and simulating it, which we did successfully.

Static analyses were performed theoretically and by circuit simulation, using the Octave math tool and Ngspice tool, respectively. The simulation results matched the theoretical results very precisely, despite the circuit having dependent voltage and current sources (which could have caused some discrepancies in the results).