

Jose Corona

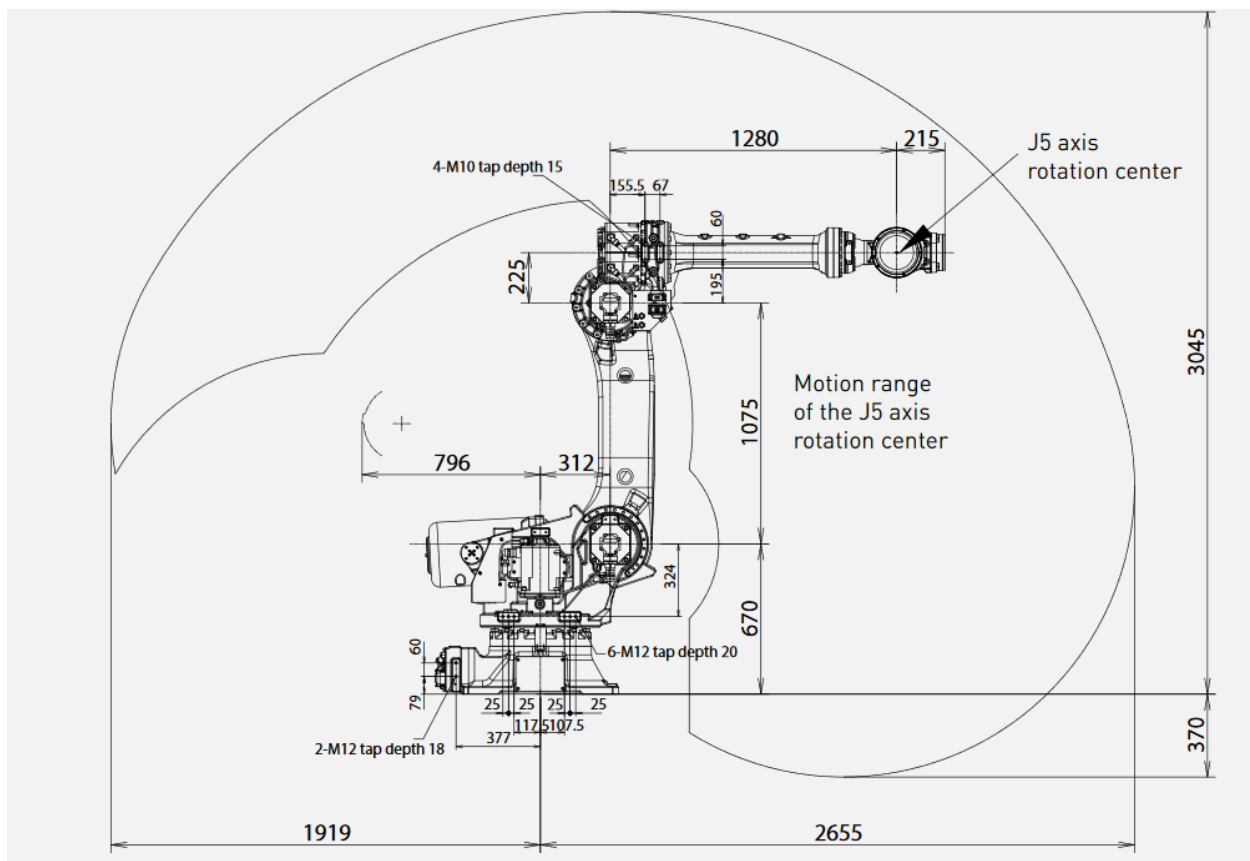
Home Task 2

FANUC R-2000iC/165F

Description of the robot.

Robot with 6 rotations and 7 links. Use a spherical wrist.

Kinematic scheme with description of the parameters.



DOF: 6

$d1 = 670 - 324 = 346$

$d2 = 324$

$d3 = 312$

$d4 = 1075$

$d5 = 225$

d6=1280

d7=215

Formulas of forward kinematics solution.

$T = T_z(d1) * R_z(q1) * T_z(d2) * T_x(d3) * R_y(q2) * T_x(d4) * R_y(q3) * T_z(d5) * T_x(d6) * R_x(q4) * R_y(q5) * R_z(q6) * T_x(d7)$

```
FK_Fanuc= FK_FANUC_200ic_165(q1,q2,q3,q4,q5,q6,d1,d2,d3,d4,d5,d6,d7) ;
```

Step by step explanation of inverse kinematics solution.

For the numerical implementation, we use the Jacobian, evaluated in the previous instant time, for the joint variables.

$$\mathbf{q}(t_{k+1}) = \mathbf{q}(t_k) + \mathbf{J}^{-1}(\mathbf{q}(t_k)) \mathbf{v}_e(t_k) \Delta t.$$

To overcome the problem of the end-effector pose is different than the corresponding, we could use an operational space error formula.

$$\mathbf{e} = \mathbf{x}_d - \mathbf{x}_e$$

$$\dot{\mathbf{e}} = \dot{\mathbf{x}}_d - \dot{\mathbf{x}}_e$$

$$\dot{\mathbf{e}} = \dot{\mathbf{x}}_d - \mathbf{J}_A(\mathbf{q}) \dot{\mathbf{q}}.$$

And to get the final position in the coordinate system we could use the next formula where delta_q refers to a small increment in the joints. q_0 refers to the initial position in the joints.

$$T(q_0 + \text{delta_q}) = T(q_0) + \text{Jacobian} * \text{delta_q}$$

A singularity happens when the effector try to reach a point that it is in the self-robot links or is out of the space tasks.

Singularities: Case 1

Case 1 $C_3 = 0$

$$J = \begin{bmatrix} s_2 & 0 & 0 & 0 & s_4 & c_4 s_5 \\ 0 & 1 & 1 & 0 & -c_4 & s_4 s_5 \\ -c_2 & 0 & 0 & 1 & 0 & -c_5 \\ -l c_2 & m & 0 & 0 & n c_4 & -n s_4 s_5 \\ -m c_2 & 0 & 0 & 0 & n s_4 & n c_4 s_5 \\ -l s_2 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

- Zero pitch wrench reciprocal to all joint screws
- Line intersects all six joint axes
- Rows 1, 5, and 6 are dependent
- It is not possible to effect the twist $[n l s_2, 0, 0, 0, -l s_2, n s_2 + m c_2]^T$

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Singularities: Case 2

Case 2 $S_5 = 0$

$$J = \begin{bmatrix} s_{23} & 0 & 0 & 0 & s_4 & 0 \\ 0 & 1 & 1 & 0 & -c_4 & 0 \\ -c_{23} & 0 & 0 & 1 & 0 & -1 \\ -l c_{23} & m s_3 & 0 & 0 & n c_4 & 0 \\ -m c_2 & 0 & 0 & 0 & n s_4 & 0 \\ -l s_{23} & -m c_3 & 0 & 0 & 0 & 0 \end{bmatrix}$$

- Axes 4 and 6 are dependent
- Joints 4 and 6 have the same instantaneous motions
- The end effector loses a degree of freedom

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Singularities: Case 3

Case 3 $n S_{23} + m C_2 = 0$

$$J = \begin{bmatrix} -\frac{m}{n} C_2 & 0 & 0 & 0 & s_4 & c_4 s_5 \\ 0 & 1 & 1 & 0 & -c_4 & s_4 s_5 \\ -c_{23} & 0 & 0 & 1 & 0 & -c_5 \\ -l c_{23} & m s_3 & 0 & 0 & n c_4 & -n s_4 s_5 \\ -m c_2 & 0 & 0 & 0 & n s_4 & n c_4 s_5 \\ \frac{lm}{n} C_2 & -m c_3 & 0 & 0 & 0 & 0 \end{bmatrix}$$

- Point of concurrence of axes 4, 5, and 6 lies on the plane defined by axes 1 and 2
- Zero pitch wrench reciprocal to all the joint screws
- Line intersects or is parallel to all joint axes
- Rows 1 and 5 are dependent
- The end effector cannot move along the twist: $\{-n, 0, 0, 0, 1, 0\}^T$

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To run the program we have to introduce the initial value

```
q0 = [0.2,0.2,0.2,0.2,0.2,0.2]'; %inicial position for the joints
```

Choose a point to get with the ik.

```
td=[0.4,0.5,0.4]' %position we want to get coordinates
Td=[0,0,0,td(1);0,0,0,td(2);0,0,0,td(3);0,0,0,1]; %position we want to get coordinates
```

The we could calculate de IK.

```
q = IK_FANUC_200ic_165(Td, q0, only_position,d_1,d_2,d_3,d_4,d_5,d_6,d_7); %vector of joint
```

We get the a column vector $q = [q1 \ q2 \ q3 \ q4 \ q5 \ q6]^T$ with the joints position. So we cold calculate again the FK and compare that are the same.

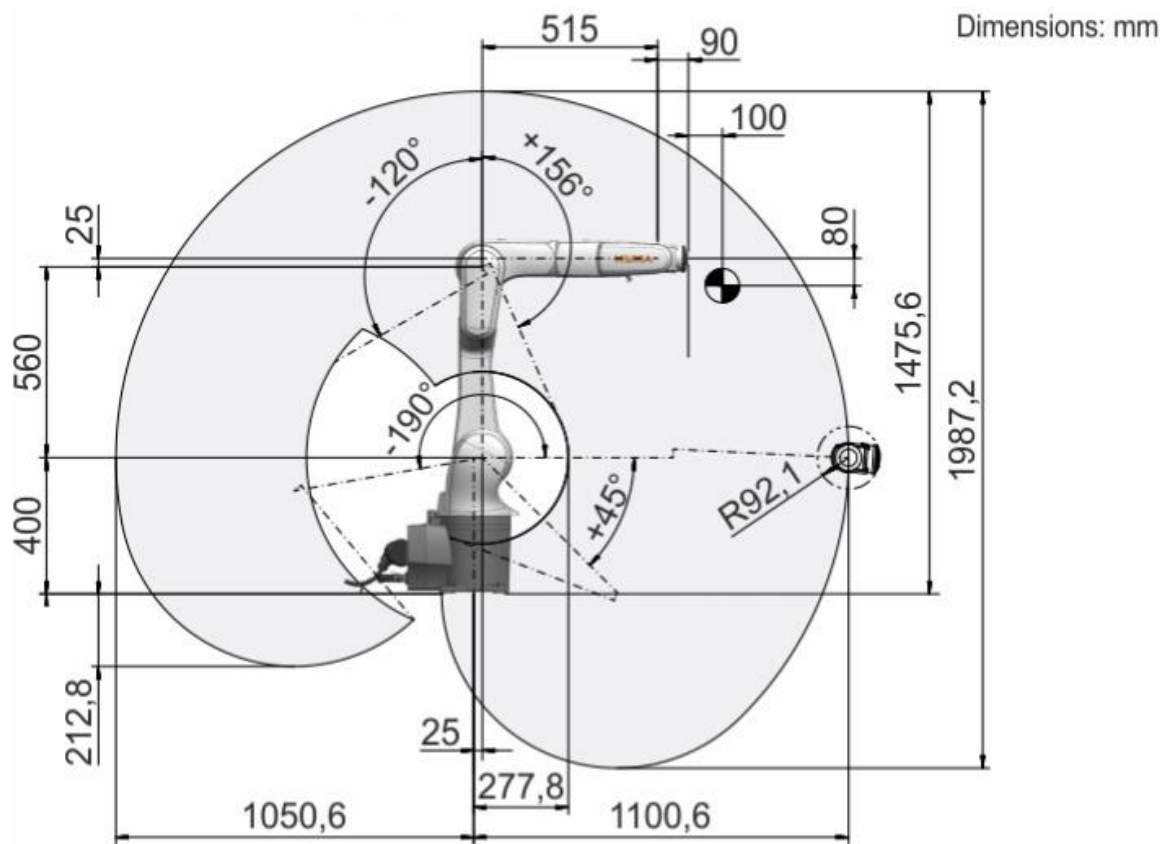
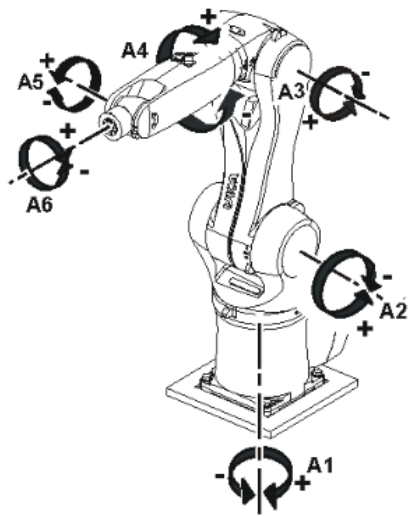
```
T = FK_FANUC_200ic_165(q(1),q(2),q(3),q(4),q(5),q(6),d_1,d_2,d_3,d_4,d_5,d_6,d_7);
```

KUKA KR 10 R1100-2

Description of the robot.

Robot with 6 rotations and 8 links. The origin is in the base of the robot, and for the forward kinematics we take the pose when the robot is completely open in the ground.

Kinematic scheme with description of the parameters



DOF: 6

$d1=400/2=200$

$d2=200$

$d3=25$

$d4=560$

d5=25

d6=277.8

d7=515-277.8 =237.2

d8=90

Formulas of forward kinematics solution.

$$T = T_z(d1) * R_z(q1) * T_z(d2) * T_x(d3) * R_y(q2) * T_x(d4) * R_y(q3) * T_z(d5) * \\ T_x(d6) * R_x(q4) * T_x(d7) * R_y(q5) * T_x(d8) * R_x(q6)$$

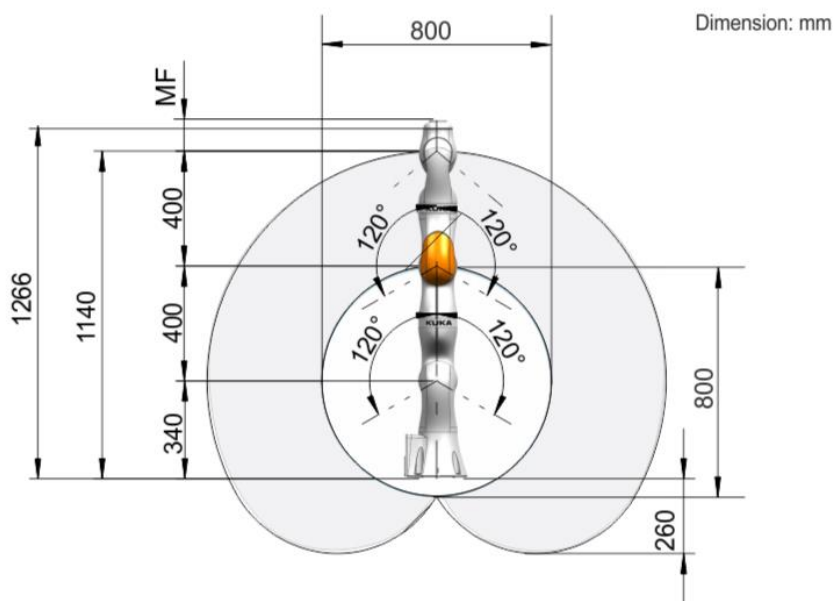
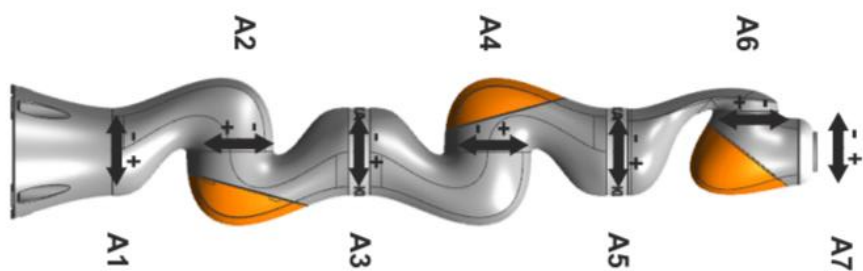
Step by step explanation of inverse kinematics solution.

KUKA LBR iiwa 14 R820 (fix third joint for simplification)

Description of the robot.

Robot with 6 rotations and 6 links.

Kinematic scheme with description of the parameters



	Range of motion	Maximum torque	Maximum velocity
J1	$\pm 170^\circ$	320Nm	$85^\circ/\text{s}$
J2	$\pm 120^\circ$	320Nm	$85^\circ/\text{s}$
J3	$\pm 170^\circ$	176Nm	$100^\circ/\text{s}$
J4	$\pm 120^\circ$	176Nm	$75^\circ/\text{s}$
J5	$\pm 170^\circ$	110Nm	$130^\circ/\text{s}$
J6	$\pm 120^\circ$	40Nm	$135^\circ/\text{s}$
J7	$\pm 175^\circ$	40Nm	$135^\circ/\text{s}$

DOF: 6

$$d1 = 360/2 = 180$$

$$d2 = 360 - d1 = 180$$

$$d3 = 400$$

$$d4 = 200$$

d5=200

d6=126

Formulas of forward kinematics solution.

$$T = T_z(d1) * R_z(q1) * T_z(d2) * R_y(q2) * T_x(d3) * R_y(q3) * T_x(d4) * \\ R_x(q4) * T_x(d5) * R_y(q5) * T_x(d6) * R_x(q6)$$

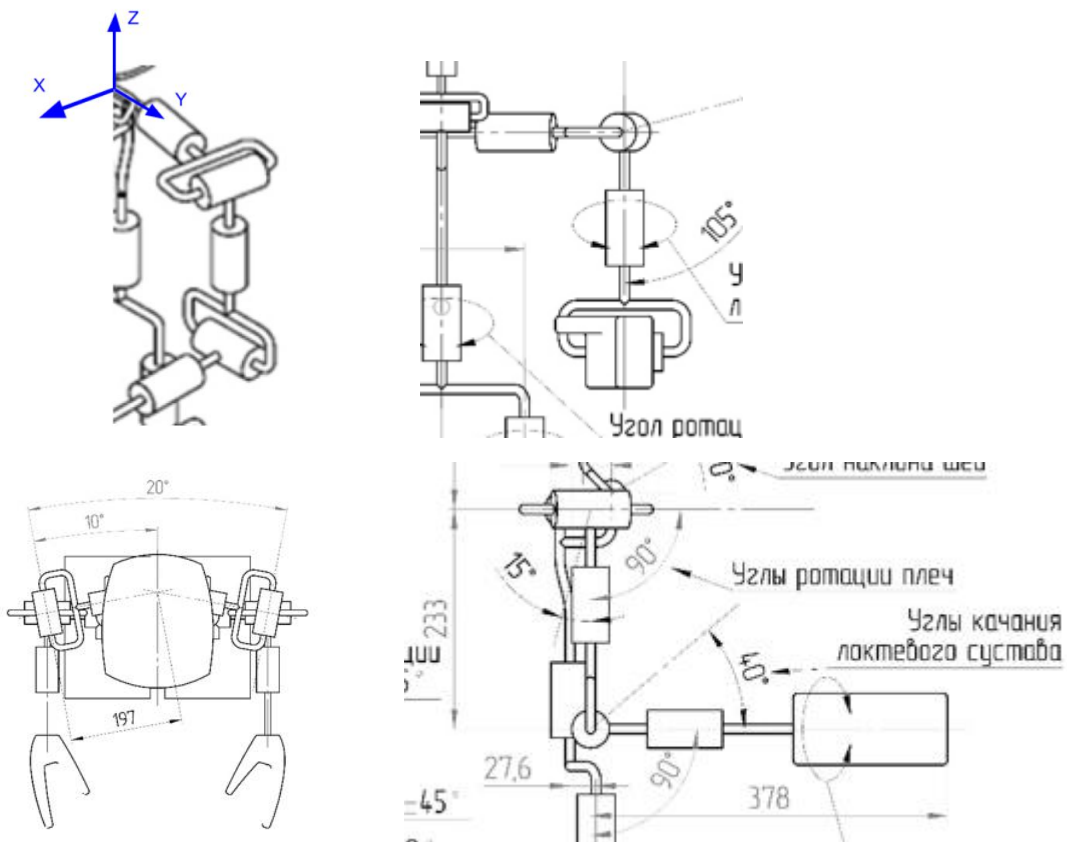
Step by step explanation of inverse kinematics solution.

AR601 arm

Description of the robot.

Robot with 5 rotations and 3 links.

Kinematic scheme with description of the parameters



DOF: 5

$d1=387/2=193.5$

$d2=223$

$d3=378$

$\alpha1=10$ degrees

Formulas of forward kinematics solution.

$T=R_y(q1)*T_y(d1)*R_z(\alpha1)*R_x(q2)*R_z(q3)*T_z(-d2)*R_y(q4)*T_x(d3)*R_x(q5)$

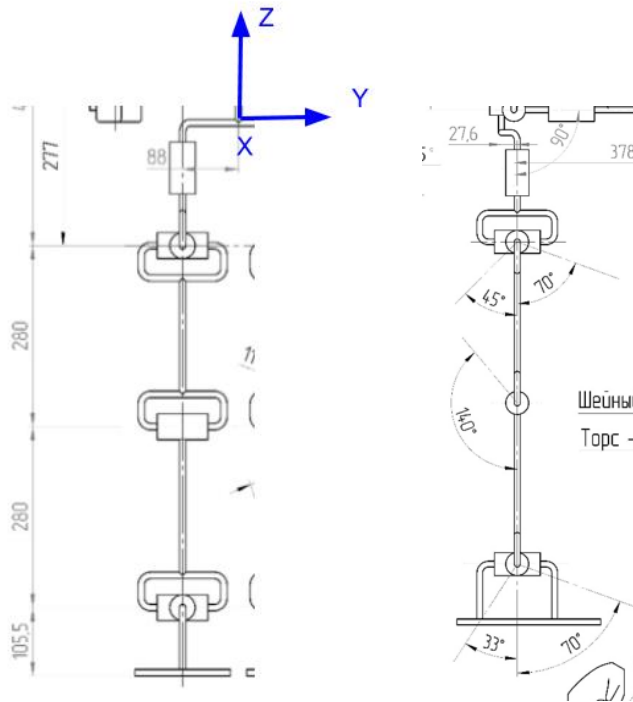
Step by step explanation of inverse kinematics solution.

AR601 leg

Description of the robot.

Robot with 6 rotations and 6 links.

Kinematic scheme with description of the parameters



DOF: 6

d1=88

d2=27.6

d3=462-233=229

d4=280

d5=280

d6=105.5

Formulas of forward kinematics solution.

$$T = T_y(-d1) * T_x(d2) * R_z(q1) * T_z(-d3) * R_y(q2) * R_x(q3) * T_z(-d4) * R_y(q4) * T_z(-d5) * R_y(q5) * R_x(q6) * T_z(-d6)$$

Step by step explanation of inverse kinematics solution.

Link to the project on git hub.

<https://github.com/Jose-R-Corona/Home-Task2>