

Chapter 4

Fisher LDA [5 pts] Given the following data points:

| # | Data points (A_1, A_2) | Class |
|---|-------------------------------|-------|
| 1 | (4,2.9) | 1 |
| 2 | (3.6,4) | 1 |
| 3 | (2.5,1) | 0 |
| 4 | (2,2.15) | 0 |

- [1 pt] Compute means μ_1 and μ_0 , and the between-class scatter matrix S_B
- [1 pt] Compute SC_1 and SC_0 , the within-class scatter matrices and their sum S_W
- [1 pt] Find the optimal vector \bar{w} that discriminates between the classes
- [1 pt] Having found discriminant vector \bar{w} , find the point on \bar{w} that best separates the two classes.
- [1 pt] Classify the point (3.8, 5)

Perceptron [3 pts] . Apply the perceptron learning algorithm for the following pattern set until convergence. Start with 0-weight vector

$$\bar{w} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$$

For simplicity of computation use $\eta = 1$. Apply the learning algorithm to data points in the given order cyclically. For each step of perceptron learning write down the classification result of a data point with the current weight vector, indicator if update is needed, and computation of vector update if necessary. The dataset consist of datapoints a, b, c, d :

| | X_1 | X_2 | X_3 | Y |
|------|-------|-------|-------|-----|
| $a.$ | 4 | 3 | 6 | -1 |
| $b.$ | 2 | -2 | 3 | 1 |
| $c.$ | 1 | 0 | -3 | 1 |
| $d.$ | 4 | 2 | 3 | -1 |