Campos Transversales y Longitudinales

November 30, 2020

1 MODO TE_{10}

1.1 Arriba de la frecuencia de corte:

$$E_x^{\pm}(x, y, z, t) = 0 \tag{1}$$

$$E_y^{\pm}(x, y, z, t) = E_{y,0}^{\pm} \sin\left(\frac{\pi x}{0.00625}\right) \cos\left((2\pi 2.8 * 10^{-8})t \mp (5.03 * 10^2)z\right)$$
 (2)

$$H_x^{\pm}(x, y, z, t) = H_{x,0}^{\pm} \sin\left(\frac{\pi x}{0.00625}\right) \cos\left((2\pi 2.8 * 10^{-8})t \mp (5.03 * 10^2)z\right)$$
(3)

$$H_y^{\pm}(x, y, z, t) = 0$$
 (4)

$$H_z^{\pm}(x,y,z,t) = H_{z,0}^{\pm} \cos\left(\frac{\pi x}{0.00625}\right) \cos\left((2\pi 2.8*10^{-8})t \mp (5.03*10^2)z\right) \quad (5)$$

1.2 Debajo de la frecuencia de corte:

$$E_x^{\pm}(x, y, z, t) = 0 \tag{6}$$

$$E_y^{\pm}(x, y, z, t) = E_{y,0}^{\pm} e^{\alpha_0 z} \sin\left(\frac{\pi x}{0.008838}\right) \cos\left((2\pi 1.8 * 10^{-8})t\right)$$
 (7)

$$H_x^{\pm}(x, y, z, t) = H_{x,0}^{\pm} e^{\alpha_0 z} \sin\left(\frac{\pi x}{0.008838}\right) \cos\left((2\pi 1.8 * 10^{-8})t\right)$$
(8)

$$H_y^{\pm}(x,y,z,t) = 0 \tag{9}$$

$$H_z^{\pm}(x, y, z, t) = H_{z,0}^{\pm} e^{\alpha_0 z} \cos\left(\frac{\pi x}{0.008838}\right) \cos\left((2\pi 1.8 * 10^{-8})t\right) \tag{10}$$

$2 \quad MODO TM_{11}$

2.1 Arriba de la frecuencia de corte:

$$E_{x}^{\pm}(x,y,z,t) = E_{x,1}^{\pm} \cos\left(\frac{\pi x}{0.008838}\right) \sin\left(\frac{\pi x}{0.008838}\right) \cos\left((2\pi 2.8*10^{-8})t \mp (7.11*10^{2})z\right)$$

$$E_{y}^{\pm}(x,y,z,t) = E_{y,1}^{\pm} \sin\left(\frac{\pi x}{0.008838}\right) \cos\left(\frac{\pi x}{0.008838}\right) \cos\left((2\pi 2.8*10^{-8})t \mp (7.11*10^{2})z\right)$$

$$(12)$$

$$\begin{split} E_z^\pm(x,y,z,t) &= E_{z,1}^\pm \sin\big(\frac{\pi x}{0.008838}\big) \sin\big(\frac{\pi x}{0.008838}\big) \cos\big((2\pi 2.8*10^{-8})t \mp (7.11*10^2)z\big) \\ &\qquad \qquad (13) \\ H_x^\pm(x,y,z,t) &= H_{x,1}^\pm \sin\big(\frac{\pi x}{0.008838}\big) \cos\big(\frac{\pi x}{0.008838}\big) \cos\big((2\pi 2.8*10^{-8})t \mp (7.11*10^2)z\big) \\ &\qquad \qquad (14) \\ H_y^\pm(x,y,z,t) &= H_{y,1}^\pm \cos\big(\frac{\pi x}{0.008838}\big) \sin\big(\frac{\pi x}{0.008838}\big) \cos\big((2\pi 2.8*10^{-8})t \mp (7.11*10^2)z\big) \\ &\qquad \qquad (15) \end{split}$$

2.2 Debajo de la frecuencia de corte:

$$E_{x}^{\pm}(x,y,z,t) = E_{x,1}^{\pm}\cos\left(\frac{\pi x}{0.008838}\right)\sin\left(\frac{\pi x}{0.008838}\right)\cos\left((2\pi 1.8*10^{-8})t\mp(7.11*10^{2})z\right)$$

$$(16)$$

$$E_{y}^{\pm}(x,y,z,t) = E_{y,1}^{\pm}\sin\left(\frac{\pi x}{0.008838}\right)\cos\left(\frac{\pi x}{0.008838}\right)\cos\left((2\pi 1.8*10^{-8})t\mp(7.11*10^{2})z\right)$$

$$(17)$$

$$E_{z}^{\pm}(x,y,z,t) = E_{z,1}^{\pm}\sin\left(\frac{\pi x}{0.008838}\right)\sin\left(\frac{\pi x}{0.008838}\right)\cos\left((2\pi 1.8*10^{-8})t\mp(7.11*10^{2})z\right)$$

$$(18)$$

$$H_{x}^{\pm}(x,y,z,t) = H_{x,1}^{\pm}\sin\left(\frac{\pi x}{0.008838}\right)\cos\left(\frac{\pi x}{0.008838}\right)\cos\left((2\pi 1.8*10^{-8})t\mp(7.11*10^{2})z\right)$$

$$(19)$$

$$H_{y}^{\pm}(x,y,z,t) = H_{y,1}^{\pm}\cos\left(\frac{m\pi x}{0.008838}\right)\sin\left(\frac{n\pi x}{0.008838}\right)\cos\left((2\pi 1.8*10^{-8})t\mp(7.11*10^{2})z\right)$$

$$(20)$$

3 MODO TE₂₁

3.1 Arriba de la frecuencia de corte:

Propagación:

$$E_{x}^{\pm}(x,y,z,t) = E_{x,2}^{\pm}\cos\left(\frac{2\pi x}{0.03125}\right)\sin\left(\frac{\pi x}{0.03125}\right)\cos\left((2\pi 2.8*10^{-8})t\mp(5.03*10^{2})z\right)$$

$$(21)$$

$$E_{y}^{\pm}(x,y,z,t) = E_{y,2}^{\pm}\sin\left(\frac{2\pi x}{0.03125}\right)\cos\left(\frac{\pi x}{0.03125}\right)\cos\left((2\pi 2.8*10^{-8})t\mp(5.03*10^{2})z\right)$$

$$(22)$$

$$H_{x}^{\pm}(x,y,z,t) = H_{x,2}^{\pm}\sin\left(\frac{2\pi x}{0.03125}\right)\cos\left(\frac{n\pi x}{0.03125}\right)\cos\left((2\pi 2.8*10^{-8})t\mp(5.03*10^{2})z\right)$$

$$(23)$$

$$H_{y}^{\pm}(x,y,z,t) = H_{y,2}^{\pm}\sin\left(\frac{m\pi x}{0.03125}\right)\cos\left(\frac{n\pi x}{0.03125}\right)\sin\left((2\pi 2.8*10^{-8})t\mp(5.03*10^{2})z\right)$$

$$(24)$$

$$H_{z}^{\pm}(x,y,z,t) = H_{z,2}^{\pm}\cos\left(\frac{2\pi x}{0.03125}\right)\cos\left(\frac{\pi x}{0.03125}\right)\cos\left((2\pi 2.8*10^{-8})t\mp(5.03*10^{2})z\right)$$

3.2 Debajo de la frecuencia de corte:

$$E_x^{\pm}(x,y,z,t) = E_{x,2}^{\pm} e^{\alpha_2 z} \cos\left(\frac{2\pi x}{0.03125}\right) \sin\left(\frac{\pi x}{0.03125}\right) \cos\left((2\pi 1.8 * 10^{-8})t\right) (26)$$

$$E_y^{\pm}(x,y,z,t) = E_{y,2}^{\pm} e^{\alpha_2 z} \sin\left(\frac{2\pi x}{0.03125}\right) \cos\left(\frac{\pi x}{0.03125}\right) \cos\left((2\pi 1.8 * 10^{-8})t\right) (27)$$

$$H_x^{\pm}(x,y,z,t) = H_{x,2}^{\pm} e^{\alpha_2 z} \sin\left(\frac{2\pi x}{0.03125}\right) \cos\left(\frac{\pi x}{0.03125}\right) \cos\left((2\pi 1.8*10^{-8})t\right) \ (28)$$

$$H_y^{\pm}(x,y,z,t) = H_{y,2}^{\pm} e^{\alpha_2 z} \cos{(\frac{2\pi x}{0.03125})} \sin{(\frac{\pi x}{0.03125})} \cos{((2\pi 1.8*10^{-8})t)}$$
(29)

$$H_z^{\pm}(x,y,z,t) = H_{z,2}^{\pm} e^{\alpha_2 z} \cos{(\frac{2\pi x}{0.03125})} \cos{(\frac{\pi x}{0.03125})} \cos{((2\pi 1.8*10^{-8})t)}$$
(30)