Course: Deep Learning

Unit 2: Computer Vision

Fundamentals of image processing and object recognition

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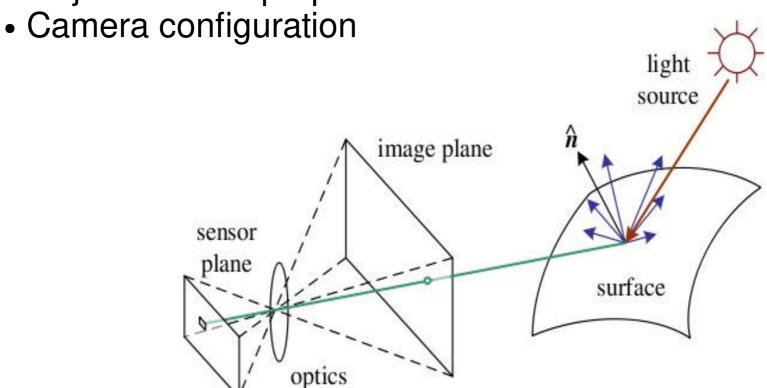
Fundamentals of Imge processing and Object Recognition

- 1. Introduction to image processing
 - Image formation
 - Convolution
 - Gradient and Laplacian of an image
- 2. Shallow object recognition approach
 - Bag of words

Image formation

Image gray levels depend on:

- Illumination
- Scene geometry
- Object surface properties



Digital image

Let \mathcal{F} be the set of image **rows** and \mathcal{C} the set of **colums**

$$\mathcal{F} = \{0,\dots,f-1\} \qquad f \times c \ \text{ is the spatial resolution}.$$

$$\mathcal{C} = \{0,\dots,c-1\}$$

A digital image is a function

$$\mathtt{I}:\mathcal{F} imes\mathcal{C} o\mathcal{D}$$

where

$$\mathcal{D} = \{0, \dots, d-1\}$$

is the image digital resolution, typically

$$d = 256$$

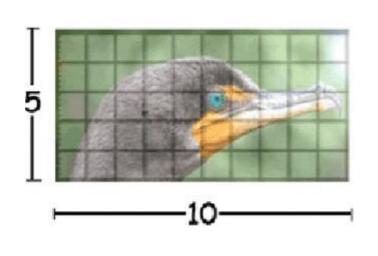
Colour digital image

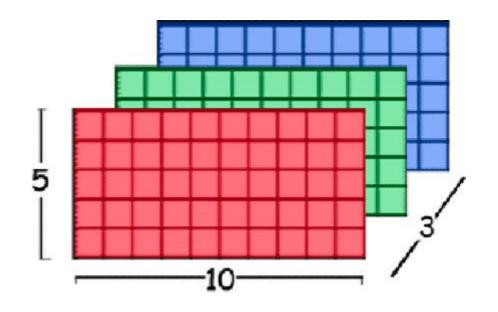
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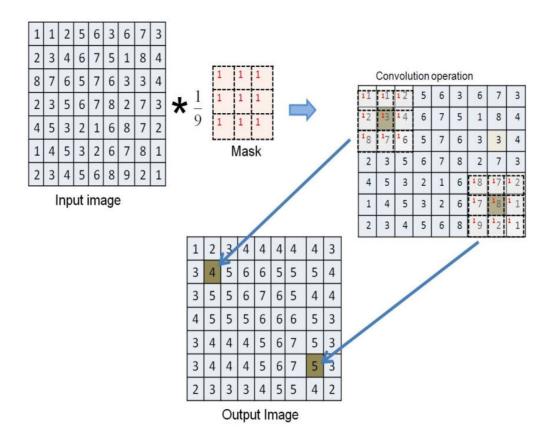
A colour digital image is a function $I: \mathcal{F} \times \mathcal{C} \to \mathcal{D}^3$





Discrete convolution

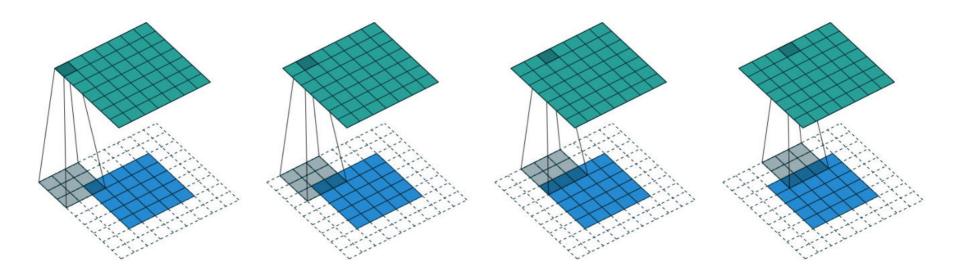
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$$o(r,t) = \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} h(i,j)e_e[r+i-(m-1),t+j-(n-1)]$$



Discrete convolution with padding

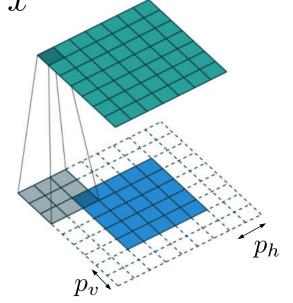
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Let p_x be the **padding** amount in dimension x where $x \in \{h, v\}$, o is a function of dimension

$$M + 2p_v - m + 1 \times N + 2p_v - n + 1$$

in this case, $p_h = m-1$, $p_v = n-1$. termed full / strict padding



Discrete convolution / correlation

Half padding convolution

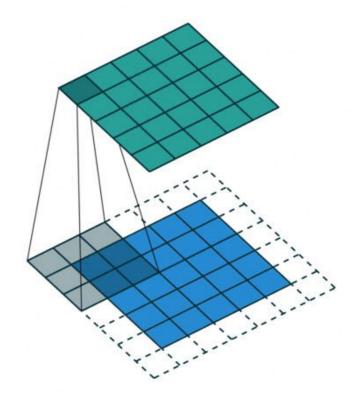
$$o(r,t) = \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} h(i,j)e_e[r+i-(m-1)/2,t+j-(n-1)/2]$$

where o has dimension $M \times N$.

In the case of half padding

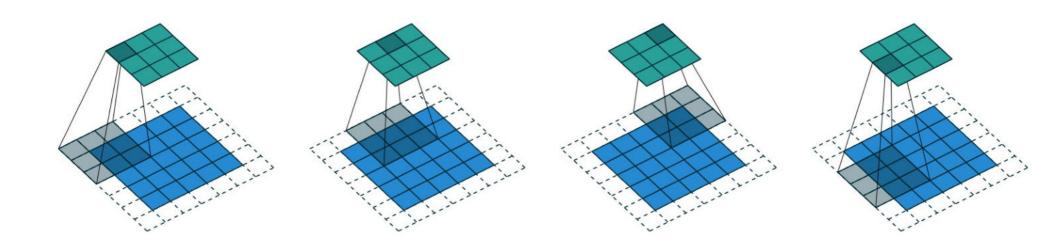
$$p_h = \frac{m-1}{2}, \qquad p_v = \frac{n-1}{2}$$
 $M + 2p_h - m + 1 = M$
 $N + 2p_v - n + 1 = N$

half padding / same convolution



Strided convolution / correlation
 Skip s positions in the input signal when convolving the kernel.
 Half padding strided convolution

$$o(r,t) = \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} h(i,j)e_e[sr+i-(m-1)/2, st+j-(n-1)/2]$$



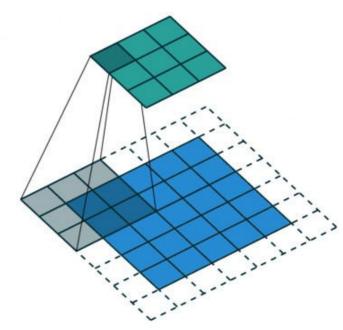
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$$o(r,t) = \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} h(i,j)e_e[sr+i-(m-1)/2, st+j-(n-1)/2]$$

$$\frac{M+2p-m}{s}+1$$

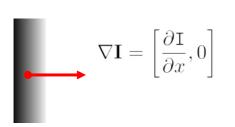
If half padded and $s=2\,$ the ouput is half the input

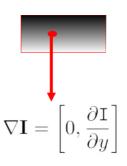
$$\frac{M-1}{2} + 1 \times \frac{N-1}{2} + 1$$

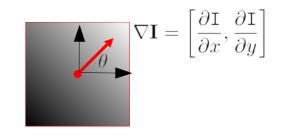


Gradient filter

The image gradient at pixel I(x,y) is a vector $[I_x,I_y]$ pointing in the direction of maximum growth in the image gray value







$$|\bar{\nabla}\mathbf{I}| = \sqrt{\mathbf{I}_x^2 + \mathbf{I}_y^2}$$

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 $\theta = \arctan\left(\frac{\mathbf{I}_y}{\mathbf{I}_x}\right)$

Gradient filter

How do I compute the gradient of an image?

$$\frac{\partial I(x,y)}{\partial x} \equiv I_x \approx \frac{I(x+\delta x,y) - I(x-\delta x,y)}{2\delta x}$$

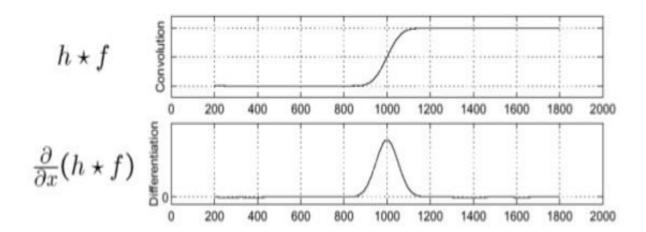
$$\mathbf{I}_x \approx \frac{1}{2} \left[\mathbf{I}(x+1,y) - \mathbf{I}(x-1,y) \right] = h_{dx} * \mathbf{I}$$

$$h_{dx} = \frac{1}{2} \begin{bmatrix} 1 & 0 & -1 \end{bmatrix} h_{dy} = \frac{1}{2} \begin{bmatrix} 1 & 0 \\ -1 & -1 \end{bmatrix}$$

Then
$$I_x = h_{dx} * I$$
 and $I_y = h_{dy} * I$

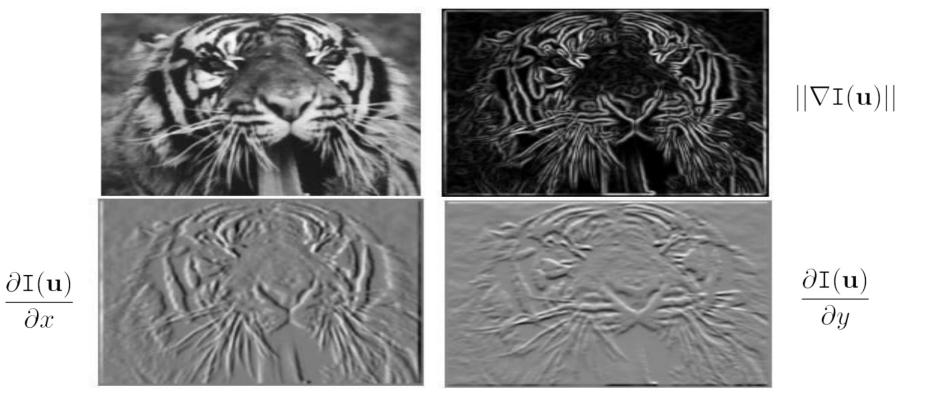
Gradient filter

The gradient of an image border



Gradient filter

Results of gradient estimation



Laplacian filter

The Laplacian of digital image I(x, y) is given by the scalar

$$\Delta I = \frac{\partial^2 I}{\partial x^2} + \frac{\partial^2 I}{\partial y^2}$$

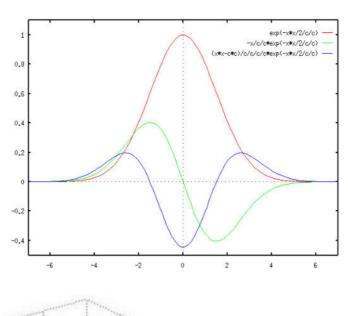
How do we compute it?

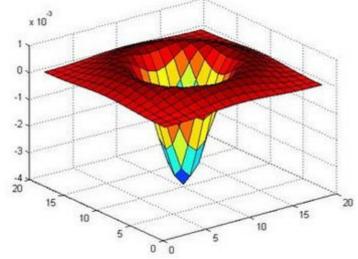
$$I_x \approx I(x+1,y) - I(x,y) = [1 \ -1] * I$$

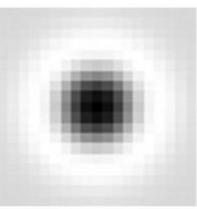
$$I_{xx} \approx [1 \ -1] * [1 \ -1] * I = [1 \ -2 \ 1] * I$$

$$\Delta \mathbf{I} = \left(\begin{bmatrix} 1 & -2 & 1 \end{bmatrix} + \begin{bmatrix} 1 \\ -2 \\ 1 \end{bmatrix} \right) * \mathbf{I} = \mathbf{h}_{l_a} = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

Laplacian filter. The Laplacian of Gaussian filter:

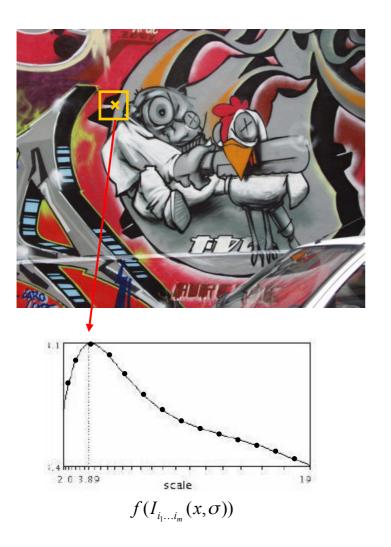


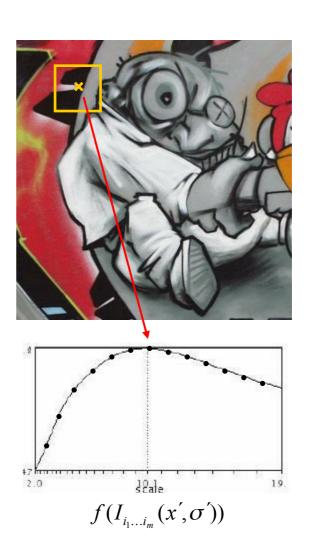




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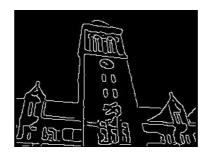
Response at different scales



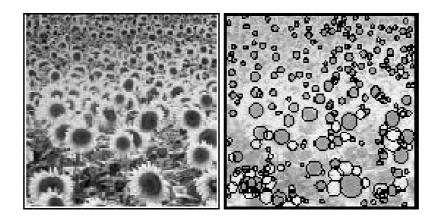


- Why are we interested in gradients and laplacians?
 - Gradients are useful for image description
 Image edges are invariant to illumination changes





- Laplacians are useful for detecting image structures (blobs)
 - → Local maxima mark blob centers
 - → Variance represent blob size



Object recognition

Problem statement

We want to recognize objects inspite of the large variability of object clases, changes in appearance caused by illumination, geometry, deformation, etc.





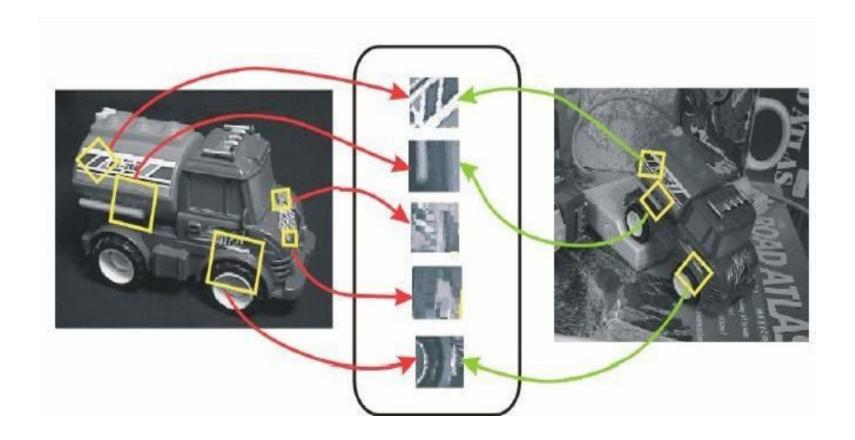


An appropriate image description invariant to most of those variations will be the key to success.

How to describe?

General approach

Image content represented by local models of appearance



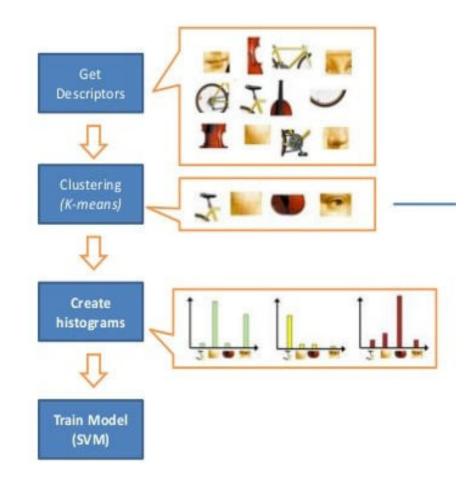
Shallow object recognition approach

1. Low-level features

2. Mid-level representation

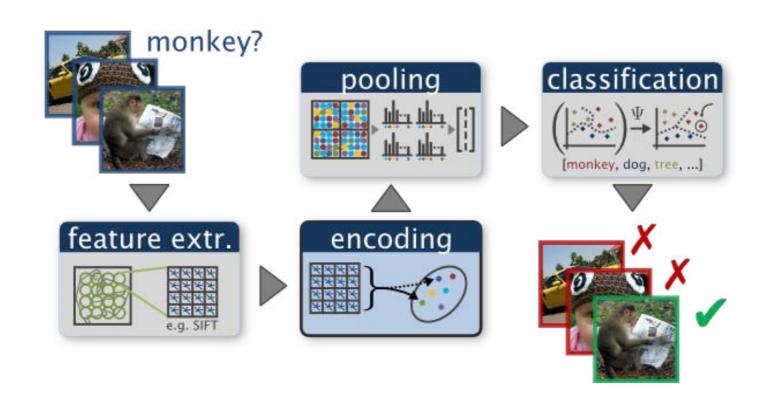
3. Pooling/aggregation

4. Classification



Shallow object recognition approach

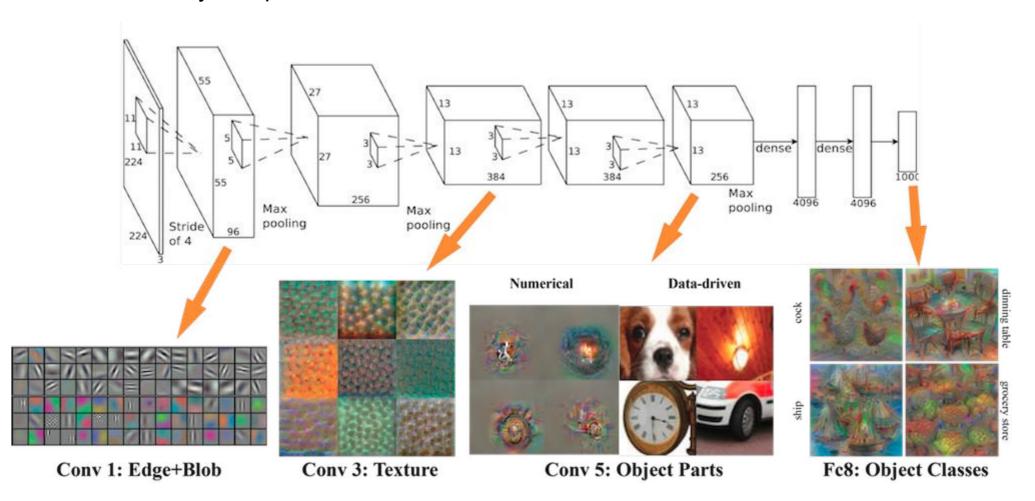
- 1. Extract low-level features
- 2. Compute mid-level representation (quantification)
- 3. Pool/aggregate spatial information
- 4. Classify



Deep object recognition approach

Trainable hierarchical representations (Krizhevsky, 2012)

Image content represented by the agreggation of local features into a hierarchy of representations AUTOMATICALLY trained.



Object recognition challenges

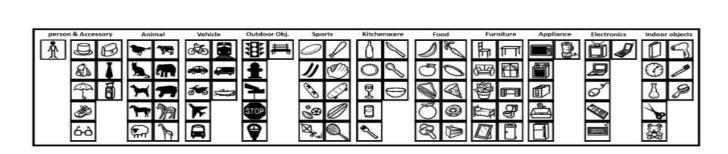
Early challenges

Caltech 101 (2004), Caltech 256 (2007), Pascal VOC (2006-2012), .

- Image Large Scale Visual Recognition Challenge
 - 1000 categories
 - 1.4 M images
 - ~ 3 instances per image



- 15.000 visual categories10 M labeled images
- ~ 700 images/category
- Common Objects in Context (Microsoft)
 - 91 categories, 328 k images
 - 2.5 M instances (~ 7.7 per image)
 - Every instance fully segmented







Deep object recognition approach

Image Large Scale Visual Recognition Contest (ILSVRC)

