



Big O Notation

Web Development Boot Camp
Lesson 11.5





Welcome to... Computer Science Fundamentals!

Remember...

Computer science fundamentals



Fundamentals aren't the "easy" computer science stuff.



Rather, they are the fundamental concepts that underlie all of the work we've been doing to date.



The biggest takeaway is to understand that there are different tools to increase computational efficiency.

Fundamentals

Remember this stuff? Yeah, me neither.

Stokes Theorem

$$\oint_C \vec{F} \cdot d\vec{r} = \iint_S \text{curl } \vec{F} \cdot d\vec{A}$$



S smooth oriented surface

C piecewise smooth oriented boundary

\vec{F} smooth vectorfield defined on S and C .



Be Wary of Imposter Syndrome

Don't let the hard stuff scare you.

Why Cover This?

01

These concepts sometimes appear in coding interviews.

02

When inheriting large codebases, you might be tasked to optimize code efficiency.

03

The computational challenges in this lesson force you to deepen your understanding.

Bottom Line

My goal is to give you the terminology and the concepts.



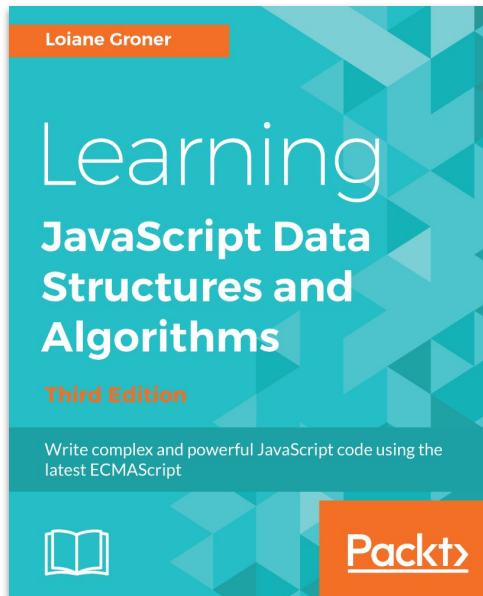
I want to give you enough insight so you can understand the context of interview questions that come your way.



And to encourage those of you who are into math to take a second look!

Going Deep

For those who dare dive deeper

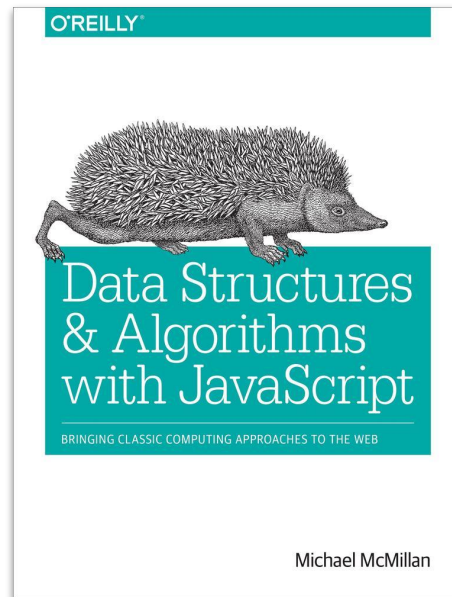


Learning JavaScript Data Structures and Algorithms—Third Edition

by Loiane Groner

Publisher: Packt Publishing

Release Date: April 2018



Data Structures and Algorithms with JavaScript

by Michael McMillan

Publisher: O'Reilly Media, Inc.

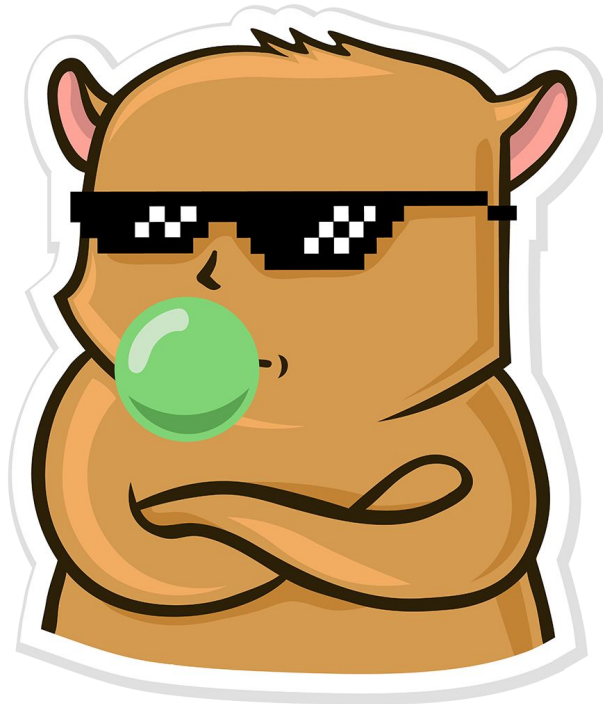
Release Date: March 2014

Efficiency

Activities 1 & 2

What does “Efficient” Mean?

We talk a lot about efficiency. But what exactly does “efficient” mean?



What's a Step?



A step is an instruction to the computer.



All computations boil down to a handful of basic steps.



Arithmetic (+, *, etc.)



Assignment (`var x = 42;`)



Boolean tests (`x === 42`)



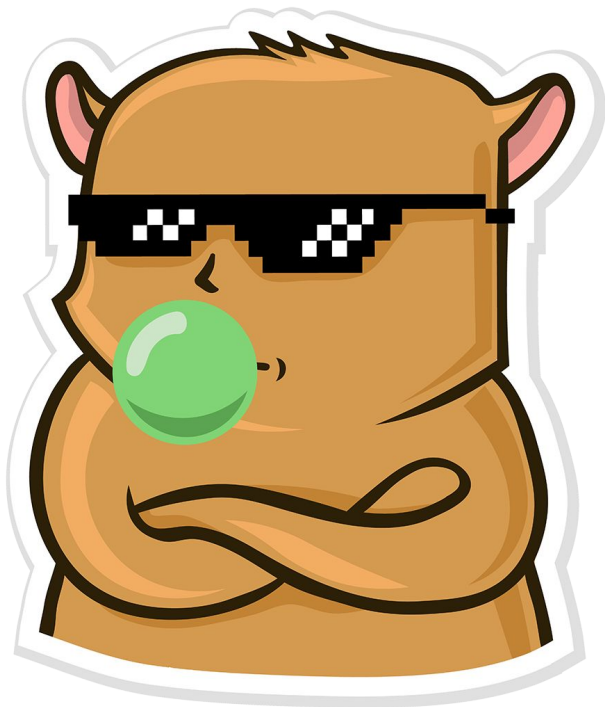
Reading from memory



Writing from memory

What's a Step?

Each of these counts as a step.



Some Common Sorting Algorithms

Activity 3

Time Complexity



Time complexity =
the rate at which algorithm
slows as input **grows**.

Big O Notation

Big O



Big O Notation lets us describe how running time scales when we increase the input size (n).



It is denoted with a big O and the growth factor in parentheses.

Examples:



$O(1)$ Grows like “1” (i.e., running time never grows)



$O(n)$ Grows like “ n ” (i.e., gets bigger as n gets bigger)



$O(n^2)$ Grows like “ n^2 ” (i.e., grows as square n as n gets bigger)



$O(\lg(n))$ Grows like “ $\log(n)$ ” (i.e., grows as $\log_2(n)$ as n gets bigger)

Big O

2 nested for loops ~ $O(n^2)$



NOT COINCIDENCE!

3 nested for loops $\sim O(n^3)$

Etc.



Big O:
One More...

Activity:

Binary search this array by hand, for 3, then 9.
Count the steps.

```
// Ready for binary search!  
var sorted = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10];
```



Activity:

Binary search this array by hand, for 3, then 9.
Count the steps.

```
// Ready for binary search!  
var sorted = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10];
```

Answer: 3 Steps



Add the digits 11–20. Repeat.

Add the digits 11–20. Repeat.

Answer: 4 Steps (!)



Much faster than linear.

Big O

$(\text{input size})^2 \sim 2x \text{ running time}$

$(\text{input size})^3 \sim 3x \text{ running time}$

Etc.

This is called $O(\lg n)$.

Big O

$\lg n$ = how many times do I divide n
by 2 to get to 1?

Logarithm Example

What is $\lg 8$?

Logarithm Example

$$8 / 2 = 4 \text{ (1)}$$

$$4 / 2 = 2 \text{ (2)}$$

$$2 / 2 = 1 \text{ (**3**)}$$

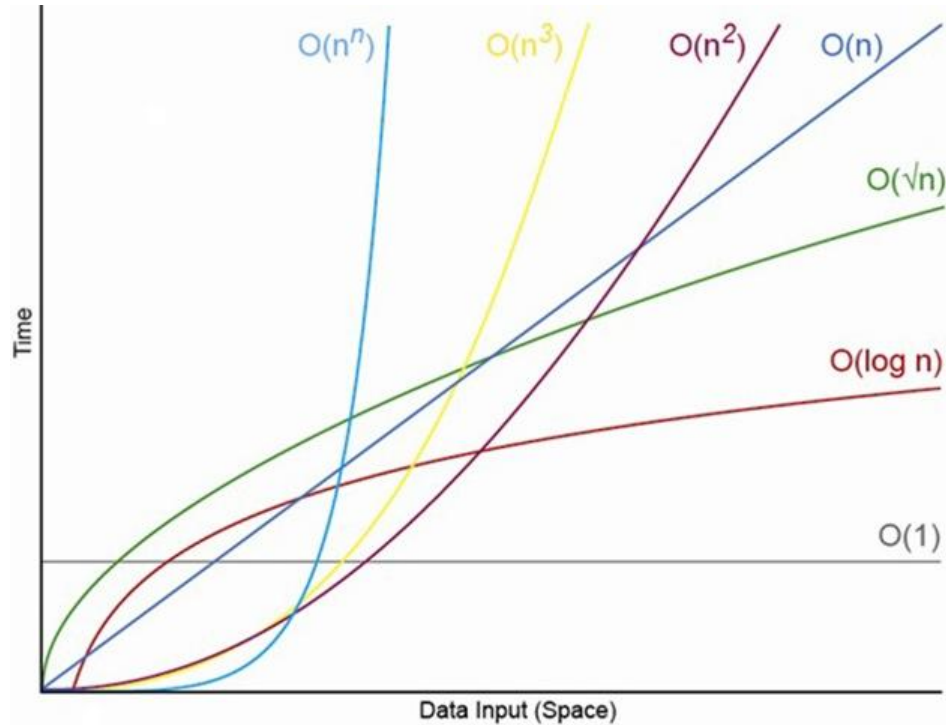
Logarithm Example

$$\lg 8 = 3$$

But if this is confusing...

Don't worry about it.

Big O Comparisons



Asymptotic Analysis

Examine the Code Base	The function should exist and be observable.
Count the Steps	Remember what counts as a step? (Slide 11)
Identify the maximum growth term	Which step grew the fastest as input size changes?
Simplify	Remove any constants or coefficients.

Activity 4

Big O Review

Calculation1.js ~ $O(1)$	Grows like "1" (i.e., 2x input size -> 1x running time)
Calculation2.js ~ $O(n)$	Grows like "n" (i.e., 2x input size -> 2x running time)
Calculation3.js ~ $O(n^2)$	Grows like " n^2 " (i.e., 2x input size -> 4x running time)
Calculation4.js ~ $O(\lg n)$	Grows like " $\lg n$ " (i.e, (input size) ² -> 2x running time)



Questions?

Activity 5



Back to Projects!