

VSC faults: generalization to multiple converters

CITCEA

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1 Development

We present a fundamental scheme in Figure 1, from where we will extend the system. The goal here is to show a scalable procedure to solve the circuit for all possible faults. The analysis is performed in the *abc* natural frame of reference, where the constraints are set. Then, voltages are expressed in symmetrical components and the optimization function is called. The grid equivalent is depicted as a Norton equivalent for greater simplicity in the analysis.

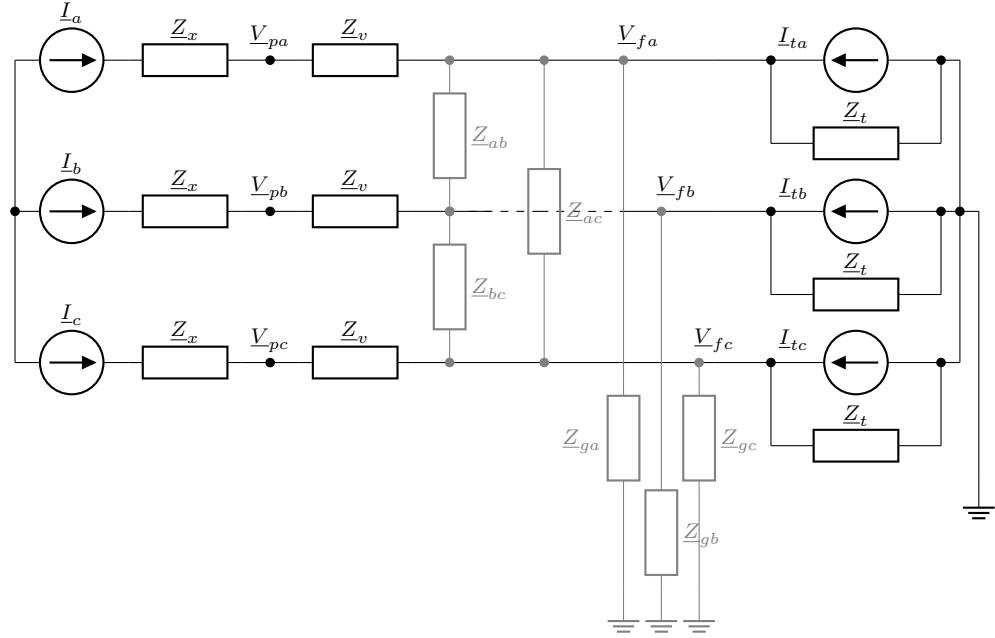


FIGURE 1. General *abc* scheme to analyze faults

In matricial form, the equations that define the system depicted in 1 become:

$$\begin{pmatrix} \underline{I}_a \\ \underline{I}_b \\ \underline{I}_c \\ \underline{I}_{ta} \\ \underline{I}_{tb} \\ \underline{I}_{tc} \end{pmatrix} = \begin{pmatrix} \underline{Y}_v & 0 & 0 & -\underline{Y}_v & 0 & 0 \\ 0 & \underline{Y}_v & 0 & 0 & -\underline{Y}_v & 0 \\ 0 & 0 & \underline{Y}_v & 0 & 0 & -\underline{Y}_v \\ -\underline{Y}_v & 0 & 0 & \underline{Y}_{f,11} & \underline{Y}_{f,12} & \underline{Y}_{f,13} \\ 0 & -\underline{Y}_v & 0 & \underline{Y}_{f,21} & \underline{Y}_{f,22} & \underline{Y}_{f,23} \\ 0 & 0 & -\underline{Y}_v & \underline{Y}_{f,31} & \underline{Y}_{f,32} & \underline{Y}_{f,33} \end{pmatrix} \begin{pmatrix} \underline{V}_{pa} \\ \underline{V}_{pb} \\ \underline{V}_{pc} \\ \underline{V}_{fa} \\ \underline{V}_{fb} \\ \underline{V}_{fc} \end{pmatrix}, \quad (1)$$

where the admittances, denoted by \underline{Y} , are the inverse of the corresponding impedances \underline{Z} . The elements

of the form $\underline{Y}_{f,ij}$ form the matrix $\underline{\mathbf{Y}}_f$, which turns out to be:

$$\underline{\mathbf{Y}}_f = \begin{pmatrix} \underline{Y}_{ab} + \underline{Y}_{ac} + \underline{Y}_{ga} + \underline{Y}_t + \underline{Y}_v & -\underline{Y}_{ab} & -\underline{Y}_{ac} \\ -\underline{Y}_{ba} & \underline{Y}_{ba} + \underline{Y}_{bc} + \underline{Y}_{gb} + \underline{Y}_t + \underline{Y}_v & -\underline{Y}_{bc} \\ -\underline{Y}_{ca} & -\underline{Y}_{cb} & \underline{Y}_{ca} + \underline{Y}_{cb} + \underline{Y}_{gc} + \underline{Y}_t + \underline{Y}_v \end{pmatrix}. \quad (2)$$

With this approach, the solution to the system is rather straightforward. Solving for the vector formed by \underline{V}_p and \underline{V}_f involves moving to the left hand side of the equation the second summand found in Equation 1, calculating the inverse of the admittances matrix that multiplies the unknowns and computing the final product.

The advantage of attacking the problem this way, and not in the previous manner where we developed the particular expressions for each fault, is found in its flexibility. Each type of fault can be simulated, and even, simultaneous faults can be calculated. It also makes sense to develop the problem in this way due to the fact that including another converter does not add much complexity. We are now going to add another converter, which we will call VSC2; VSC1 is supposed to be the already present converter shown in Figure 1. This new converter remains connected to the point where the fault takes place. Our goal is to obtain the necessary equations to compute the particular voltages at the PCC of each branch together with the voltage at the faulted point. Just for clarification purposes, Figure 2 shows the single-phase representation of the system with the two converters added to the faulted grid.

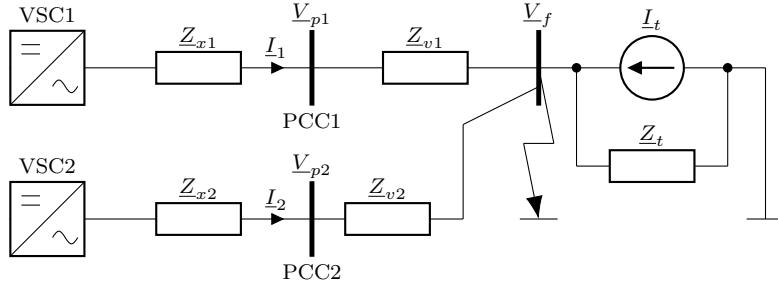


FIGURE 2. Single-phase representation of the simple system under a fault

Similarly to the single converter scenario, the Kirchoff equations in compact form are:

$$\begin{pmatrix} \mathbf{I}_1 \\ \mathbf{I}_2 \\ \mathbf{I}_t \end{pmatrix} = \begin{pmatrix} \underline{\mathbf{Y}}_{v1} & \mathbf{0} & -\underline{\mathbf{Y}}_{v1} \\ \mathbf{0} & \underline{\mathbf{Y}}_{v2} & -\underline{\mathbf{Y}}_{v2} \\ -\underline{\mathbf{Y}}_{v1} & -\underline{\mathbf{Y}}_{v2} & \underline{\mathbf{Y}}_f \end{pmatrix} \begin{pmatrix} \underline{\mathbf{V}}_{p1} \\ \underline{\mathbf{V}}_{p2} \\ \underline{\mathbf{V}}_f \end{pmatrix}, \quad (3)$$

where the vectors \mathbf{I}_1 and \mathbf{I}_2 denote the abc currents injected by the associated converter; $\underline{\mathbf{Y}}_{v1}$ and $\underline{\mathbf{Y}}_{v2}$ are matrices full of zeros expect for the elements \underline{Y}_{v1} and \underline{Y}_{v2} placed on the diagonal; $\underline{\mathbf{Y}}_f$ is the matrix shown in Equation 2, where \underline{Y}_v would be the sum of \underline{Y}_{v1} and \underline{Y}_{v2} in this case; $\underline{\mathbf{V}}_{p1}$ and $\underline{\mathbf{V}}_{p2}$ are the abc voltages at the point of common coupling of each branch; $\underline{\mathbf{V}}_t$ is the diagonal matrix with \underline{Y}_t terms; and $\underline{\mathbf{V}}_t$ is the voltage imposed by the grid, in the abc frame.

Adding more converters to the grid would not suppose a challenge from the point of view of solving the system since the general structure of the equations would take the same form. A more general case could consist of adding a grid between the point where the converters are connected and the Thevenin equivalent. The approach we suggest here would be the same as the one shown in Equation 3, where the complete matrices are formed by concatenating 3×3 block matrices. At this stage, the block matrices are formed by inspection, but the positive aspect of employing admittance matrices is that their construction can be easily programmed. Thus, we believe that the procedure shown here is meant to be adaptable to an n converter case with a full grid, as Figure 3 tries to illustrate. For now, we will suppose the grid to be fully passive, in the sense that there are no power loads or generator

units connected to it. Consequently, it can be described by only an admittance matrix, which causes the development of the equations to be considerably simpler.

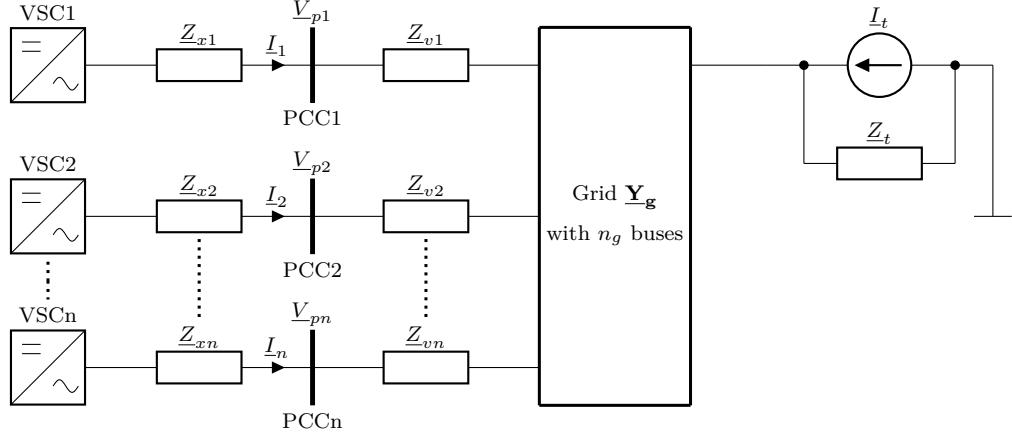


FIGURE 3. Single-phase representation of a complete system

As follows, the equations to solve the system in matricial form are presented below:

$$\begin{pmatrix} \underline{I}_1 \\ \underline{I}_2 \\ \vdots \\ \underline{I}_n \\ \underline{I}_t \end{pmatrix} = \begin{pmatrix} \underline{Y}_{v1} & \mathbf{0} & \dots & \mathbf{0} & -\underline{Y}'_{v1} \\ \mathbf{0} & \underline{Y}_{v2} & \dots & \mathbf{0} & -\underline{Y}'_{v2} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \mathbf{0} & \mathbf{0} & \dots & \underline{Y}_{vn} & -\underline{Y}'_{vn} \\ -\underline{Y}'_{v1} & -\underline{Y}'_{v2} & \dots & -\underline{Y}'_{vn} & \underline{Y}_g \end{pmatrix} \begin{pmatrix} \underline{V}_{p1} \\ \underline{V}_{p2} \\ \vdots \\ \underline{V}_{pn} \\ \underline{V}_g \end{pmatrix}, \quad (4)$$

where matrices of the form \underline{Y}'_x differ from \underline{Y}'_x in the sense that they are not 3×3 matrices but instead are constituted by null elements except for the ones that symbolize the connection between a generic bus with the associated \underline{V}_{px} voltage and the grid. Besides, the matrix \underline{Y}_g includes the \underline{Y}_t admittance and the admittances of the form \underline{Y}_{vk} .

2 Two converters case study

2.1 Balanced fault

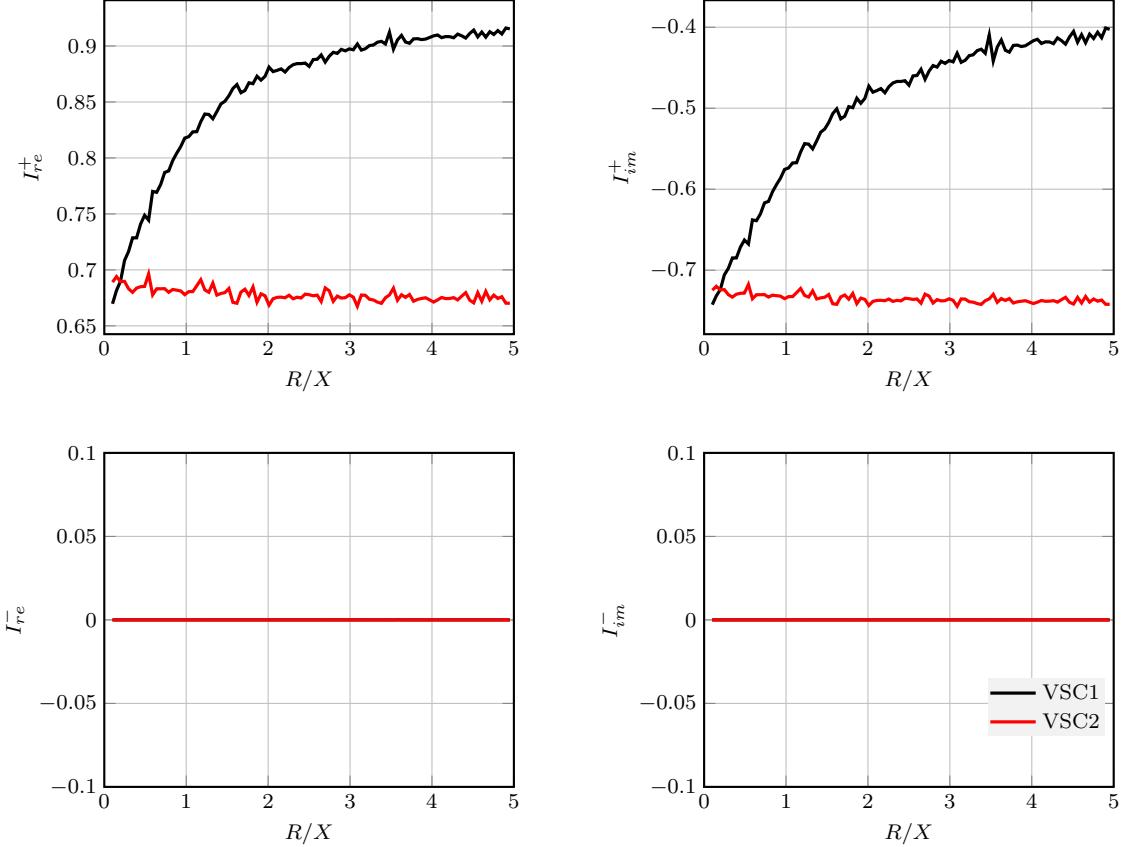


FIGURE 4. Influence of the currents on the objective function for the balanced fault with $\underline{Y}_{xg} = 15$

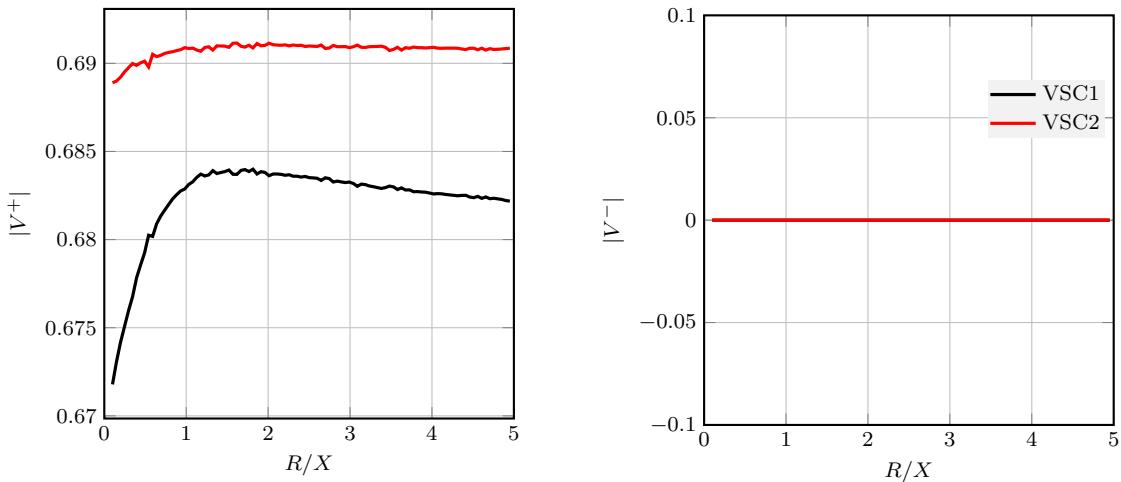


FIGURE 5. Influence of the R/X ratio on the voltages for the balanced fault with $\underline{Y}_{xg} = 15$

2.2 Line to ground fault

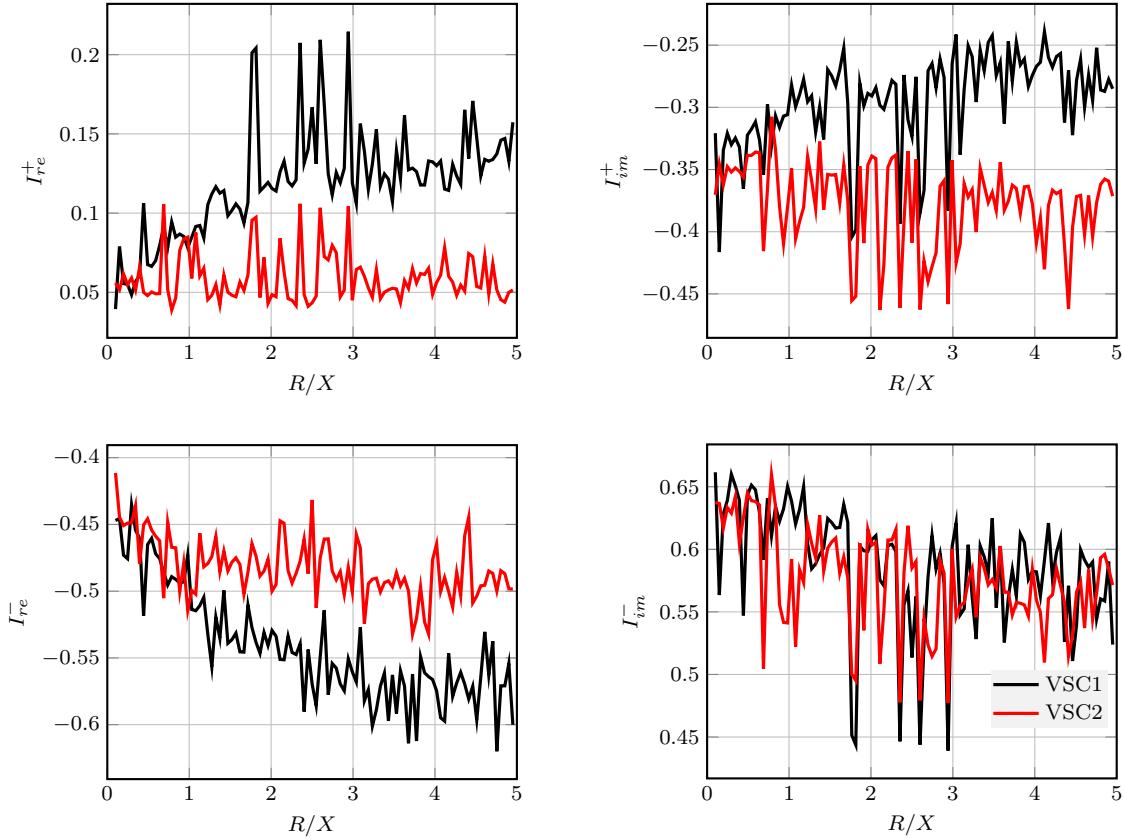


FIGURE 6. Influence of the currents on the objective function for the line to ground fault with $\underline{Y}_{ag} = 15$

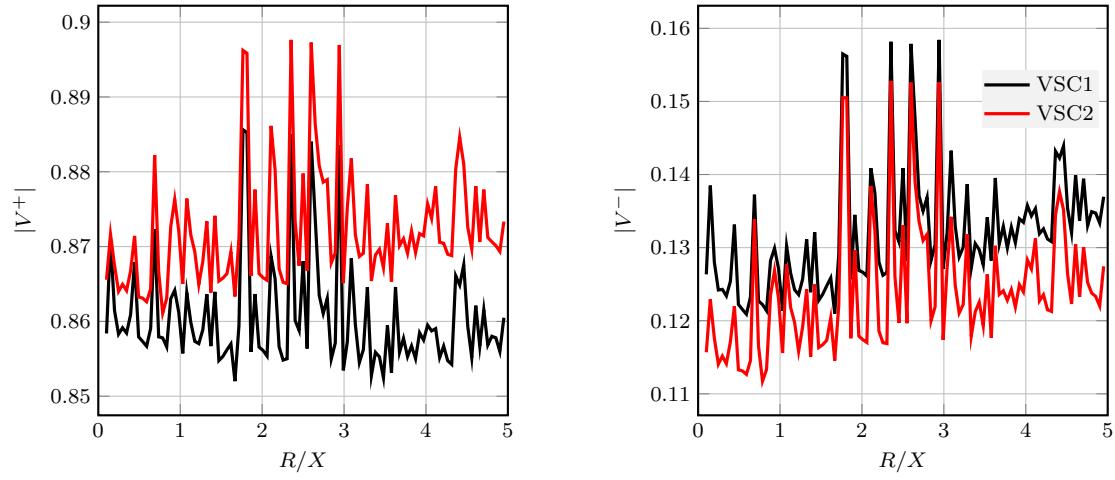


FIGURE 7. Influence of the R/X ratio on the voltages for the line to ground fault with $\underline{Y}_{ag} = 15$

2.3 Line to line fault

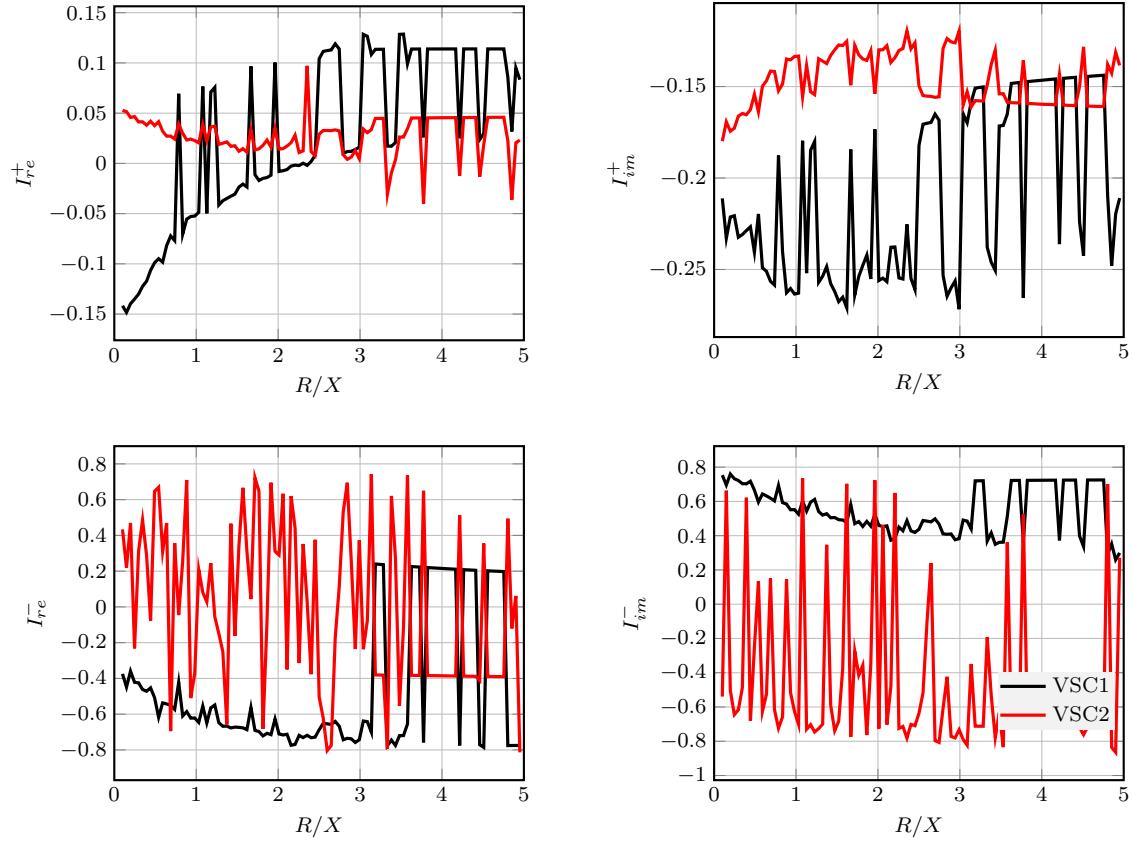


FIGURE 8. Influence of the currents on the objective function for the line to line fault with $\underline{Y}_{ab} = 2$

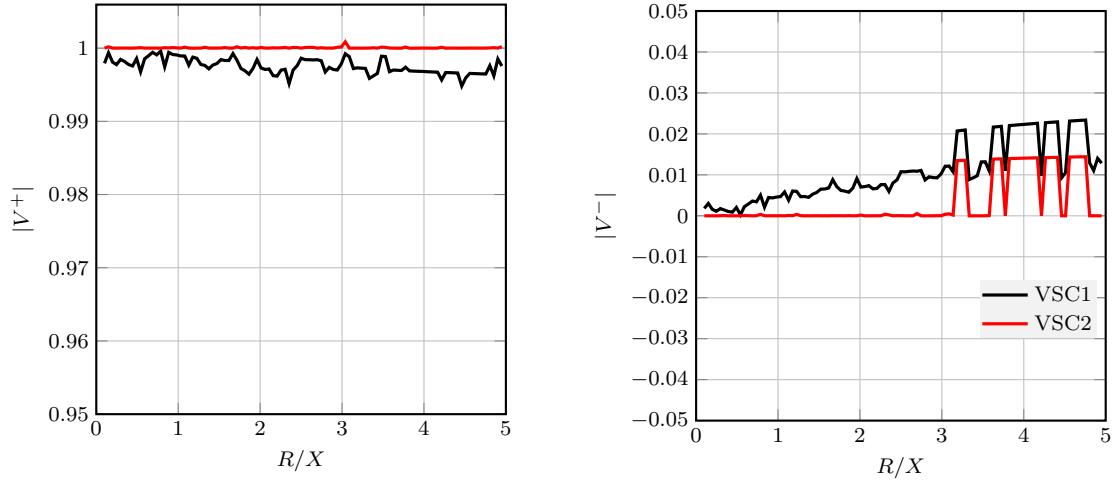


FIGURE 9. Influence of the R/X ratio on the voltages for the line to line fault with $\underline{Y}_{ab} = 2$

2.4 Double line to ground fault

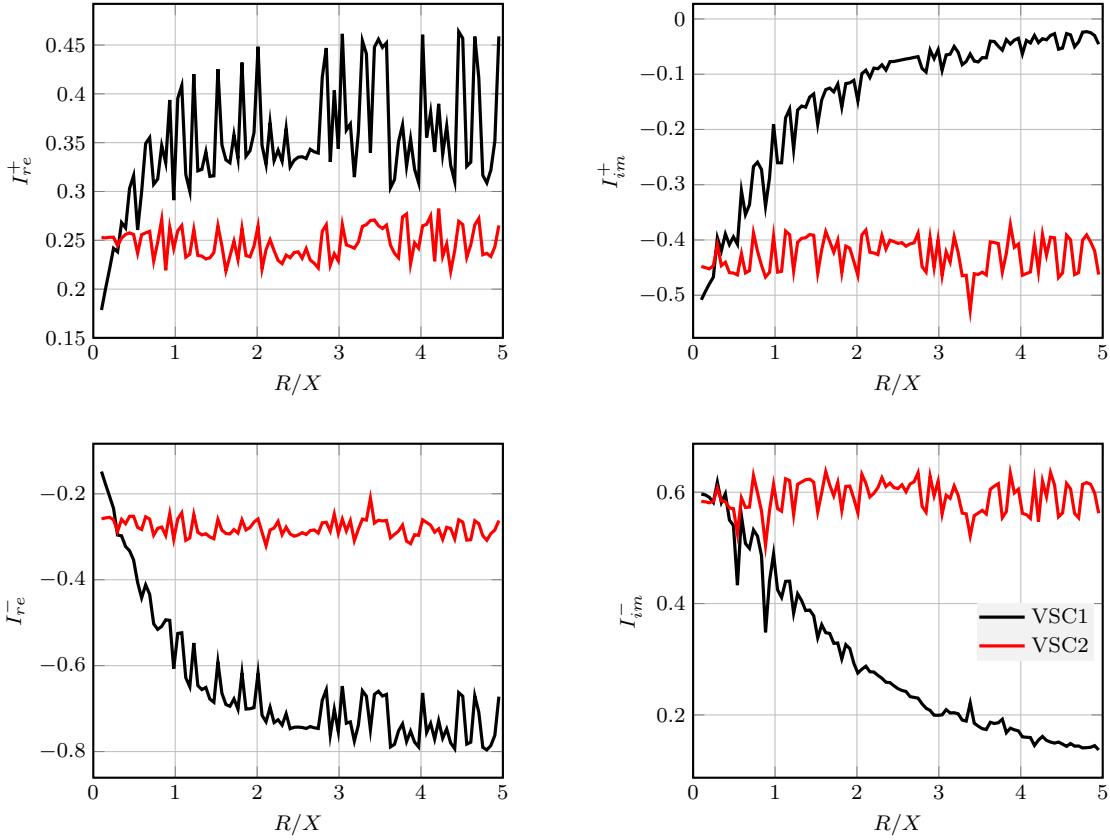


FIGURE 10. Influence of the currents on the objective function for the line to line fault with $\underline{Y}_{ab} = 100$ and $\underline{Y}_{ag} = 1$

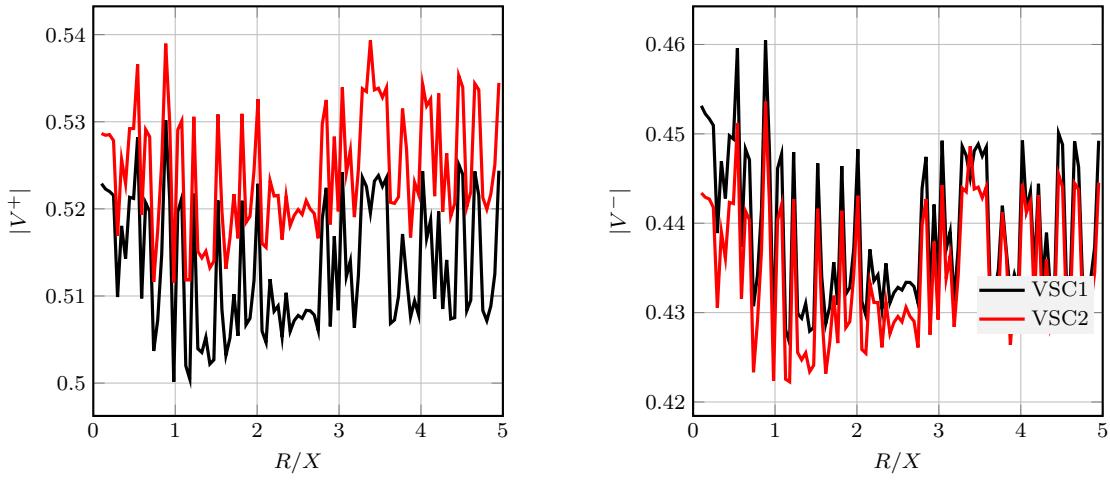


FIGURE 11. Influence of the R/X ratio on the voltages for the line to line fault with $\underline{Y}_{ab} = 100$ and $\underline{Y}_{ag} = 1$