

Calc III Notes Day 36

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Decide which test should work (and then use that test!) to decide convergence for:

1

$$\sum_{n=1}^{\infty} \frac{n^2}{e^n}$$

Do terms approach 0? yes

sign is all positive

Trying ROOT test:

ANSWER: Root test

nth power makes it likely a root test most of the time root and ratio test work interchangeably

Another (awful) possible solution: integral test (but awful)

2

$$\sum_{n=3}^{\infty} \frac{\cos(n)^2}{n^2 \ln(n)}$$

Solutions: Comparison (cos is always ≤ 1)

3

$$\sum_{n=8}^{\infty} \frac{\sqrt{n} + 1}{n^2 - 1}$$

Solution: Limit Comparison Test

4

$$\sum_{n=1}^{\infty} \frac{5^n}{3^n + 4^n}$$

5

$$\sum_{n=1}^{\infty} \frac{(-3)^n n^2}{n!}$$

solution: can't use AST (derivative part) because factorial

6

diverges

7

Integral test $u = \frac{1}{x}$

LCT $\frac{1}{n^2}$