

# C Programming Basic – week 13

String Pattern Matching

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## Topics of this week

- String pattern matching algorithms
  - Naive algorithm
  - Knuth-Morris-Pratt algorithm
  - Boyer-Moore algorithm
- Exercises

 a
 b
 a
 c
 a
 a
 b

 1
 a
 b
 a
 c
 a
 b

 4
 3
 2

 a
 b
 a
 c
 a
 b

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## String matching problem

- Let P be a string of size m
  - A substring P[i .. j] of P is the subsequence of P consisting of the characters with ranks between i and j
  - A prefix of P is a substring of the type P[0 .. i]
  - A suffix of P is a substring of the type P[i ..m − 1]
- Given strings T (text) and P (pattern), the pattern matching problem consists of finding a substring of T equal to P
- Applications:
  - Text editors, Search engines, Biological research

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## Brute Force Matching

- The brute-force pattern matching algorithm compares the pattern P with the text T for each possible shift of P relative to T, until either
  - a match is found, or
  - all placements of the pattern have been tried
- Brute-force pattern matching runs in time O(nm)
- Example of worst case:
  - T = aaa ... ah
  - -P = aaah
  - may occur in images and DNA sequences
  - unlikely in English text

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## Algorithm

```
Algorithm BruteForceMatch(T, P)
```

```
// Input text T of size n and pattern P of size m
// Output starting index of a substring of T equal to P or
-1
if no such substring exists
  for i \( \infty \) 0 to n - m {
      test shift i of the pattern
    }
    j \( \infty \) 0
    while j < m \( \Lambda \) T[i + j] = P[j]
      j \( \infty \) j + 1
    if j = m
      return i {match at i}
    else
    break while loop {mismatch}
    return -1 {no match anywhere}</pre>
```

### Exercise 13.1

- Make a random string that has about 2000 characters consisting of a set of characters..
- For example:
  - set of characters: abcdef
  - string: abcadacaeeeffaadbfacddedcedfbeccae...
- Write the program that searches the pattern, for example "aadbf", from the string.
- Note: use Simple searching string Algorithm

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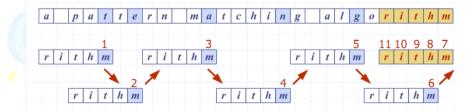
## **Boyer-Moore Heuristics**

- The Boyer-Moore's pattern matching algorithm is based on two heuristics
- Looking-glass heuristic: Compare P with a subsequence of T
- moving backwards
- Character-jump heuristic: When a mismatch occurs at T[i] = c
  - If P contains c, shift P to align the last occurrence of c in P with T[i]
  - Else, shift P to align P[0] with T[i + 1]

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## Example



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#### Last-Occurrence Function

- Boyer-Moore's algorithm preprocesses the pattern P and the alphabet  $\Sigma$  to build the last-occurrence function L mapping  $\Sigma$  to integers, where L(c) is defined as
  - the largest index i such that P[i] = c or
  - -1 if no such index exists
- Example:
  - $-\Sigma = \{a, b, c, d\}$ - P = abacab

С	a	b	С	d
L(C)	4	5	3	-1

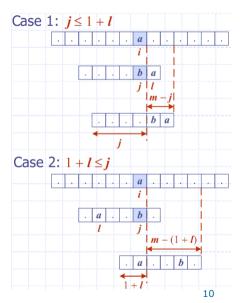
- The last-occurrence function can be represented by an array indexed by the numeric codes of the characters
- The last-occurrence function can be computed in time O(m + s), where m is the size of P and s is the size of  $\Sigma$

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## Algorithm Boyer Moore

```
Algorithm BoyerMooreMatch(T, P, \Sigma)
    L \leftarrow lastOccurenceFunction(P, \Sigma)
    i \leftarrow m - 1
    i \leftarrow m - 1
    repeat
    if T[i] = P[j]
           if j = 0
           return i { match at i }
           else
           i \leftarrow i - 1
           j \leftarrow j - 1
    else
    { character-jump }
           l \leftarrow L[T[i]]
           i \leftarrow i + m - min(j, 1 + l)
           i \leftarrow m - 1
    until i > n - 1
    return -1 { no match }
```



# Exercise 13.2: Searching string by Boyer-Moore

- Make a random string that has about 2000 characters consisting of a set of characters.
- set of characters: abcdef
- string: abcadacaeeeffaadbfacddedcedfbeccae...
- Write the program that search the pattern, for example "aadbf", from the string.
- Note: use Boyer-Moore Algorithm

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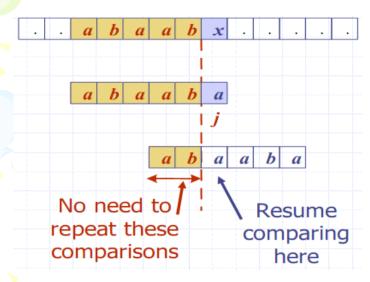
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## KMP string matching

- Knuth-Morris-Pratt's algorithm compares the pattern to the text in left-to-right, but shifts the pattern more intelligently than the bruteforce algorithm.
- When a mismatch occurs, what is the most we can shift the pattern so as to avoid redundant comparisons?
- Answer: the largest prefix of P[0..j] that is a suffix of P[1..j]

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### **KMP Failure Function**

- Knuth-Morris-Pratt's algorithm preprocesses the pattern to find matches of prefixes of the pattern with the pattern itself
- The failure function F(j) is defined as the size of the largest prefix of P[0..j] that is also a suffix of P[1..j]
- Knuth-Morris-Pratt's algorithm modifies the brute-force algorithm so that if a mismatch occurs at P[j] ≠ T[i] we set

 $j \leftarrow F(j-1)$ 

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# Example P[j]F(j)3 $a \mid a \mid b$

Algorithm failureFunction(P)

$$i \leftarrow 1$$
 $j \leftarrow 0$ 

while i < m

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 $F[0] \leftarrow 0$ if P[i] = P[j]{we have matched j + 1 chars}  $F[i] \leftarrow j + 1$  $i \leftarrow i + 1$  $j \leftarrow j + 1$ else if j > 0 then {use failure function to shift P}  $j \leftarrow F[j-1]$ else  $F[i] \leftarrow 0 \{ \text{ no match } \}$  $i \leftarrow i + 1$ 

#### Exercise 13.3

- Repeat the exercise 13.2 using the KMP algorithm.
- Calculate the number of comparisons.

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## The KMP algorithm

- The failure function can be represented by an array and can be computed in O(m) time
- At each iteration of the while-loop, either
   i increases by one, or
  - the shift amount i-j increases by at least one (observe that F(j-1) < j)
- Hence, there are no more than 2n iterations of the while-loop
- Thus, KMP's algorithm runs in optimal time O(m + n)

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```
Algorithm KMPMatch(T, P)
          F \leftarrow failureFunction(P)
          i \leftarrow 0
         j \leftarrow 0
         while i < n
                if T[i] = P[j]
                           if j = m - 1
                                     return i - j \{ match \}
                           else
                                     i \leftarrow i + 1
                                     j \leftarrow j + 1
                else
                          if j > 0
                                     j \leftarrow F[j-1]
                           else
                                     i \leftarrow i + 1
          return -1 { no match }
                                                                                               19
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```



