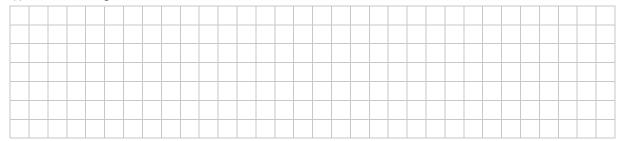
(Suggested maximum time: 10 minutes)

- (a) A bus company increases the price of all of its tickets by 6%.Before the increase, the price of a ticket from Cork to Dublin was €17·00.
 - (i) Find the price of this ticket after the increase.

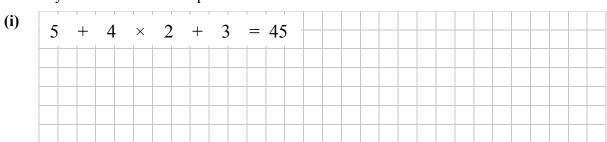


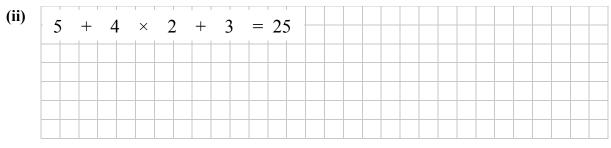
Six months later, the company reduces the price of this ticket back to €17.00.

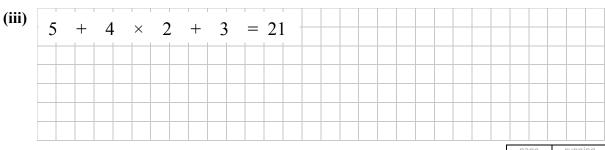
(ii) Find the **percentage decrease** in the price of this ticket. Give your answer correct to one decimal place.



(b) Insert brackets into each of the following statements to make them true. You may need more than one pair of brackets in some of the statements.

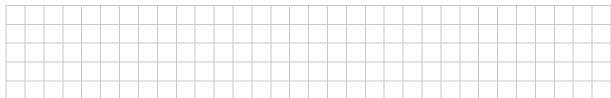




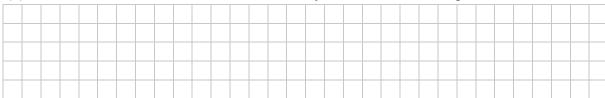


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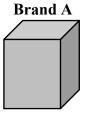
(a) (i) Write 20 cent as a **fraction** of €20. Give your answer in its simplest form.



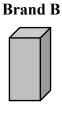
(ii) Write 0.5 cm as a **fraction** of 2 m. Give your answer in its simplest form.



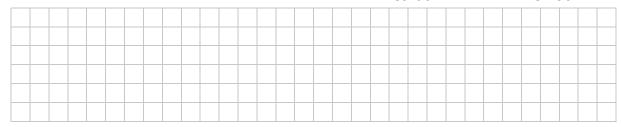
- (b) A shop sells two brands of orange juice, **Brand A** and **Brand B**, as shown.
 - (i) Find which brand, A or B, is cheaper per litre.Show all of your working out.







750 ml €1·50



Samantha needs to buy at least 5 litres of orange juice.

(ii) Find the **lowest price** that she could pay to do this, by buying **Brand A**, **Brand B**, or a **combination** of both. Justify your answer fully.



(Suggested maximum time: 5 minutes)

Conor carries out a survey on all of the 25 students in his class (U). He asks each student if they own a pet (P), and if they own a bicycle (Q).

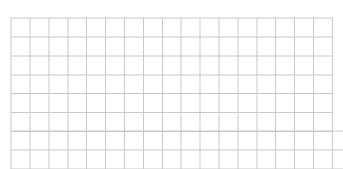
U

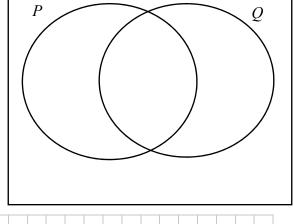
6 students own **neither** a pet **nor** a bicycle.

28% of the students own **both** a pet and a bicycle.

The ratio $\#(P \setminus Q) : \#(Q \setminus P) = 2 : 1$.

Use this information to fill in the Venn diagram.





Question 4

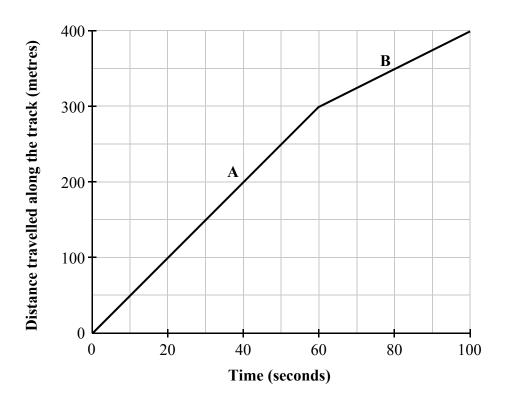
(Suggested maximum time: 5 minutes)

Put a tick (\checkmark) in the correct box in each row of the table below to show whether each statement is always true, sometimes true, or never true, for three **different** sets A, B, and C.

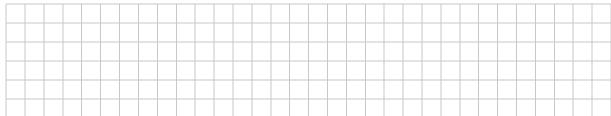
Statement	Tick one	box only, for each st	tatement
Statement	Always true	Sometimes true	Never true
$A \cap B = B \cap A$			
$A \cup B = B \cup C$			
$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$			
$A \cup C = A \cap C$			
$A \setminus B = \{ \}$			

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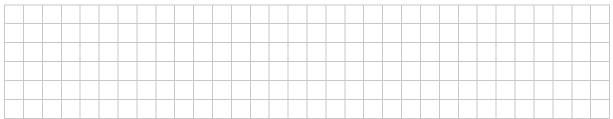
(a) The graph below shows the distance travelled along a track by Ann over the course of a race. The graph is in two sections, labelled **A** and **B**.



(i) Show that Ann's speed in section A is 5 metres per second.

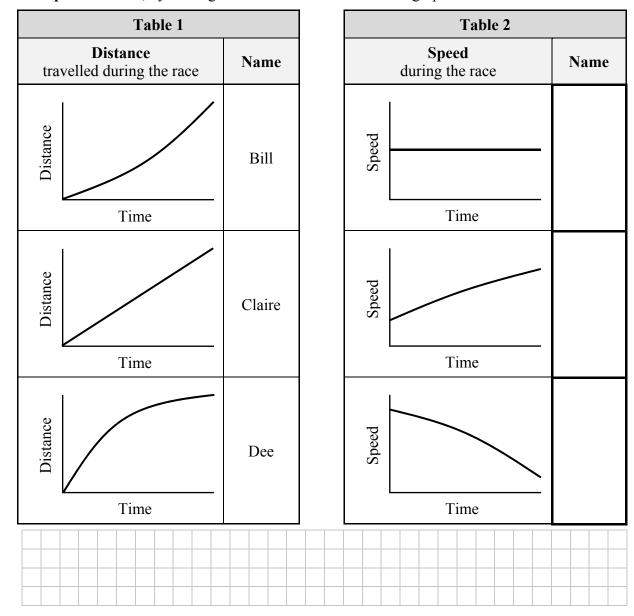


(ii) Find Ann's speed in section **B**, in metres per second.

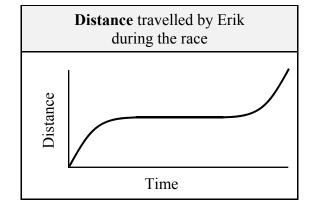


(b) Table 1 shows graphs of the **distance** travelled along the track by Bill, Claire, and Dee during the same race. Each person's name is written next to their graph.

Table 2 shows graphs of the **speed** of Bill, Claire, and Dee during the race. **Complete Table 2**, by writing the correct name next to each graph.



(c) The graph below shows the distance Erik travelled along the track during the same race. **Sketch** the graph of Erik's **speed** during the race on the axes below.



	Erik's speed during the race							
Speed								
Time								

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(Suggested maximum time: 10 minutes)

Write the following four numbers in order, from the smallest to the biggest.





Put a tick (\checkmark) in the correct box in each row of the table below to show whether each number **(b)** is rational or irrational. Give a reason for each answer.

Number	Tick one for each	box only, number	Reason										
	Rational	Irrational											
$\sqrt{10}$													
3·14													

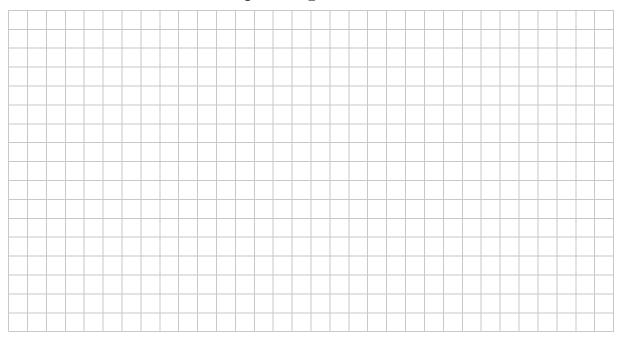
How many digits does the number 3.14×10^{100} have, when it is written out fully? Justify your answer.

	Ans	SW	er:	_																				
	Justification:																							
٠.	us	ווווי	cai.	IOII	•																			

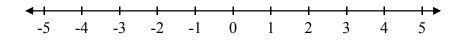
(Suggested maximum time: 5 minutes)

(a) Solve the following equation.

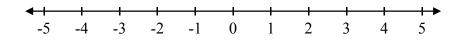
$$\frac{2x+4}{3} - \frac{5x-7}{2} = 5$$



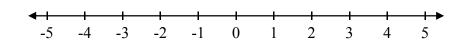
- **(b)** Graph each of the following inequalities on the number line given.
 - (i) x < 4, where $x \in \mathbb{N}$.



(ii) x < 4, where $x \in \mathbb{Z}$.



(iii) x < 4, where $x \in \mathbb{R}$.

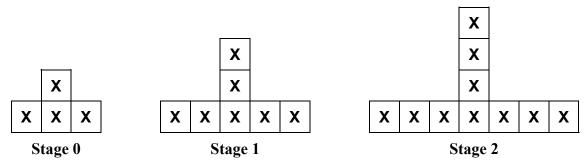


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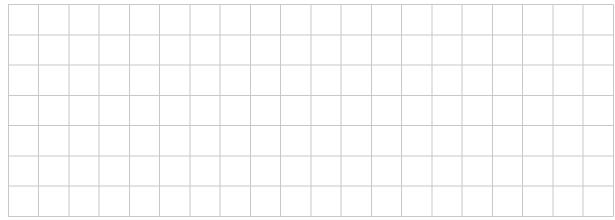
(Suggested maximum time: 15 minutes)

John makes a sequence where each stage is made up of a certain number of **X**s arranged in a pattern. The first three stages of John's sequence are shown below.

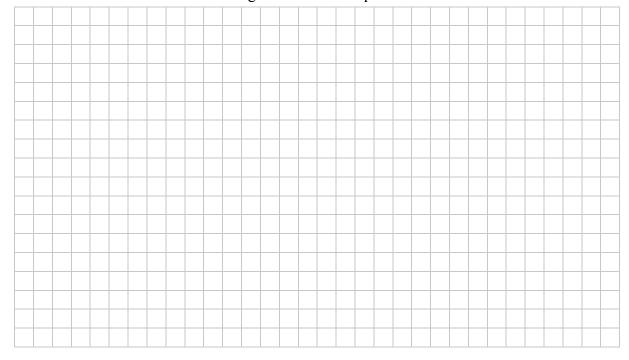
The sequence starts at **stage 0**.



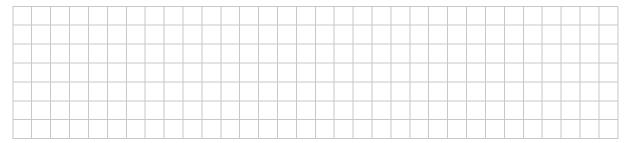
(a) Draw the next stage of John's sequence.



(b) Using a table, a graph, or otherwise, write a **formula** to express N in terms of S, where N is the number of X s in stage S of John's sequence.



(c) There are exactly 130 Xs in stage k of John's sequence. Find the value of k.



(d) Yoko is also making a sequence, with each stage made up of a certain number of Xs arranged in a pattern. In Yoko's sequence, the relationship between N and S is given by the formula:

$$N = 1 + 2S$$
,

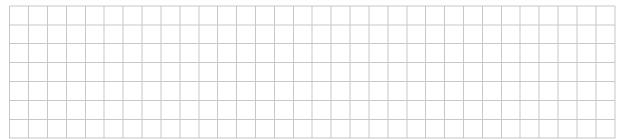
where N is the number of \mathbf{X} s in stage S of the sequence (starting at stage 0).

(i) **Draw** one possible example of the first three stages of Yoko's sequence in the table below.

	Yoko's sequence													
Stage 0	Stage 1	Stage 2												

(ii) p represents the number of Xs in stage y of Yoko's sequence.

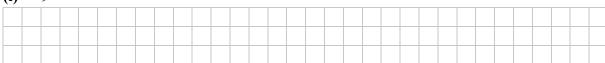
Write down the number of Xs in stage y + 3 of Yoko's sequence. Give your answer in terms of p.



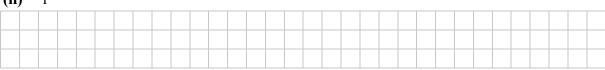
(Suggested maximum time: 5 minutes)

(a) Write each of the following numbers in the form 3^k , where $k \in \mathbb{Q}$.

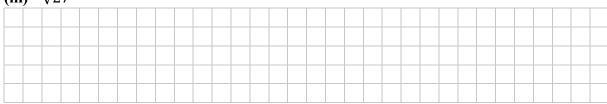
(i) (i)



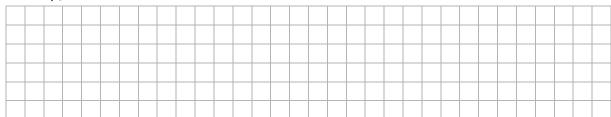
(ii)



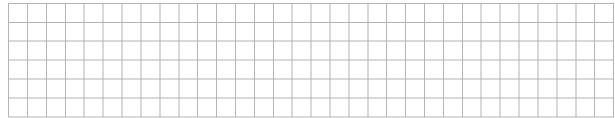
(iii) $\sqrt{27}$



(iv) $\frac{1}{\sqrt[3]{3}}$



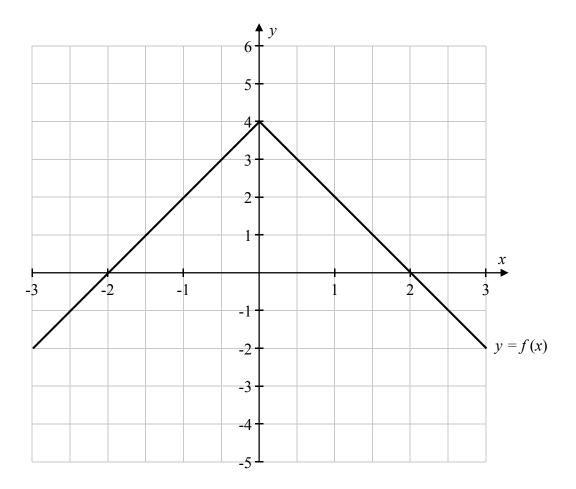
(b) Write $(-2n)^4$ in the form an^b , where $a, b \in \mathbb{Z}$.



(c) x and $\sqrt{x^2}$ are **not** always equal.

Give an example of a value of x, and the corresponding value of $\sqrt{x^2}$, which are **not** equal.

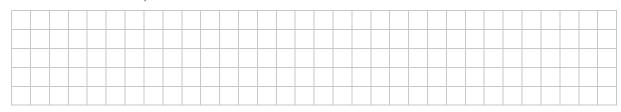
(a) The graph of the function y = f(x) is shown on the co-ordinate diagram below, for $-3 \le x \le 3$, $x \in \mathbb{R}$. The graph is made up of two line segments.



(i) Fill in the table below to show the value of f(x) and the value of f(x) - 2 for each of the given values of x.

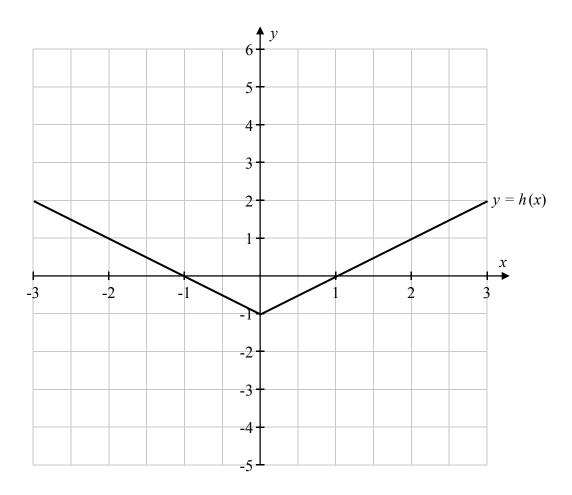
x	-3	-2	-1	0	1	2	3
f(x)							
f(x)-2							

(ii) Hence, or otherwise, **draw** the graph of y = f(x) - 2 on the co-ordinate diagram above, for $-3 \le x \le 3$, $x \in \mathbb{R}$.



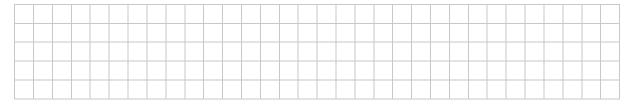
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(b) The graph of a different function, y = h(x), is shown on the co-ordinate diagram below, for $-3 \le x \le 3$, $x \in \mathbb{R}$. The graph is made up of two line segments.



(i) Fill in the table below to show the value of h(x) for each of the given values of x.

x	-3	-2	-1	0	1	2	3
h(x)							



(ii) Hence, or otherwise, **draw** the graph of $y = [h(x)]^2$ on the co-ordinate diagram above, for $-3 \le x \le 3$, $x \in \mathbb{R}$.

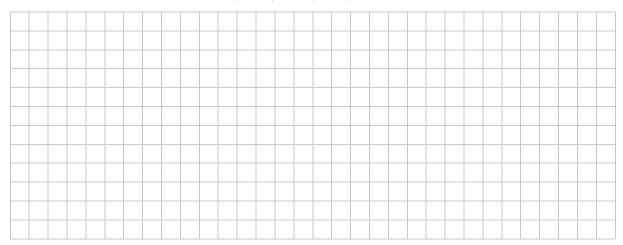
(Suggested maximum time: 10 minutes)

(a) (i) Multiply out and simplify $(x+5)^2$.



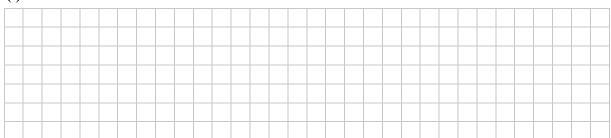
(ii) Hence, or otherwise, show that the following expression is always divisible by 4.

$$(x+5)^2 - (x-5)^2$$

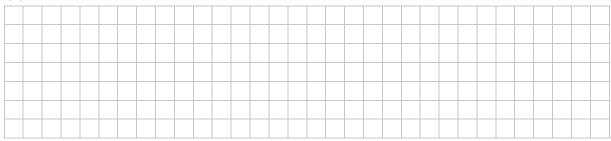


(b) Factorise each of the following expressions.

(i)
$$25x^2 - 49n^2$$



(ii)
$$2x^2 - 9x - 18$$



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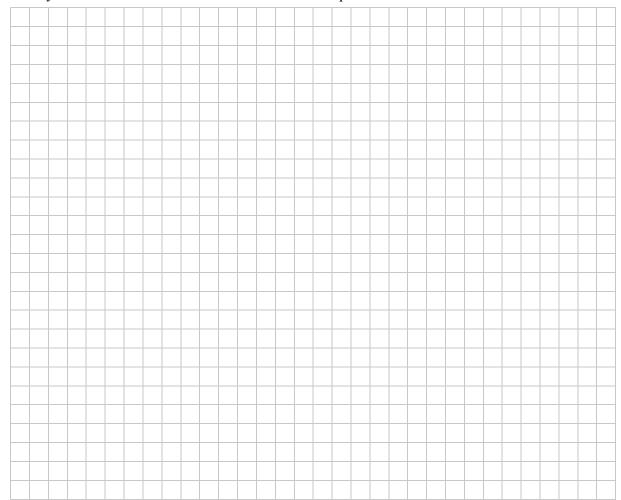
(Suggested maximum time: 10 minutes)

Three bags are shown in the table below. The mass of each bag (in kg) is also shown.

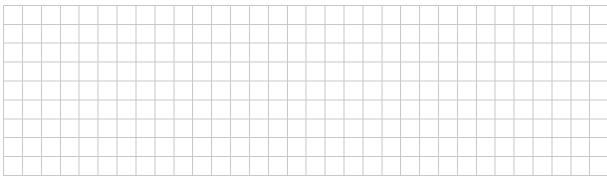
Bag	THE PARTY OF THE P		And the state of t
Mass, in kg $(y \in \mathbb{R})$	y + 5	19	$2y^2 + 1$

Two of the bags have the same mass (in kg).

(a) Find the **three** possible positive values of y. Give your irrational answer correct to two decimal places.



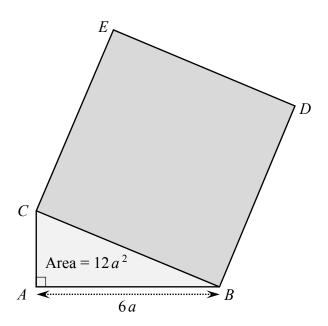
(b) Explain why all three bags can **not** have the same mass (in kg).



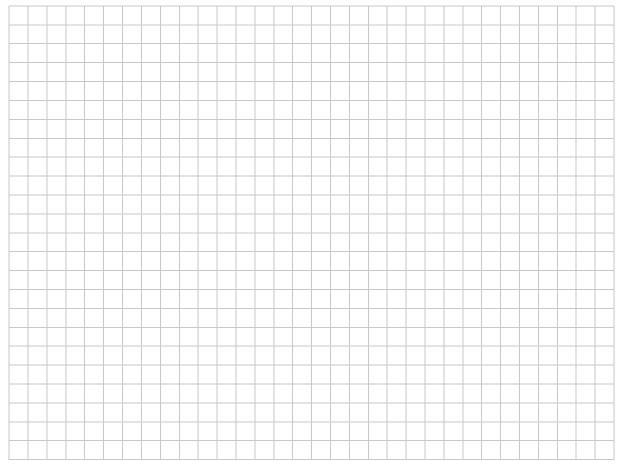
(Suggested maximum time: 10 minutes)

The right-angled triangle ABC is shown in the diagram below. The square BDEC is placed on the hypotenuse of this triangle.

The **area** of the **triangle** ABC is $12a^2$ square units, where $a \in \mathbb{R}$. The **length** of the side [AB] is 6a units.



Find the area of the square BDEC, in terms of a^2 .



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The function h(x) below gives the approximate height of the water at Howth Harbour on a particular day, from 12 noon to 5 p.m.

$$h(x) = 10x^2 - 50x + 130$$
,

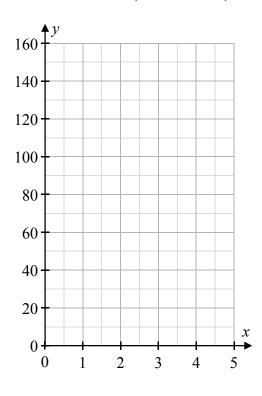
where h(x) is the height of the water in centimetres, and x is the time in hours after 12 noon.

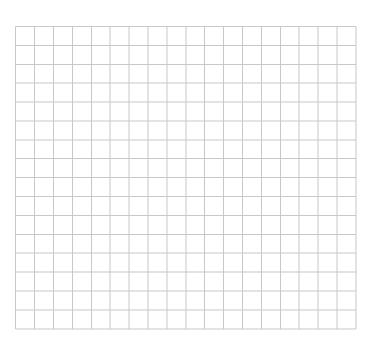
(a) Draw the graph of the function $h(x) = 10x^2 - 50x + 130$ on the axes below, for $0 \le x \le 5$, $x \in \mathbb{R}$.

(Suggested maximum time: 20 minutes)

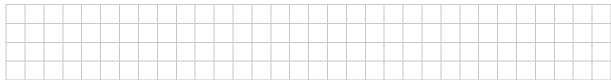


Source: www.theirishlandscape.com. Altered.

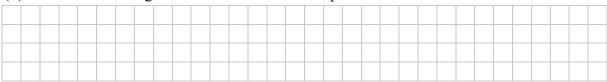




- **(b)** Use your graph in part **(a)** to answer the following questions.
 - (i) Find the height of the water at 12 noon.



(ii) Estimate the height of the water at its lowest point.



(iii) After 12 noon, how long did it take before the water was at its lowest point?

The graph on the right shows the approximate height of the water in centimetres at Crookhaven on a different day, from 12 noon to 6 p.m. The graph is symmetrical.

On this day, the height of the water at 12 noon was 180 cm, and the height of the water at the lowest point on the graph was 0 cm.

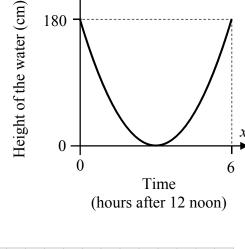
Taking x as the time in hours after 12 noon, this graph is given by the function

$$g(x) = ax^2 + bx + c,$$

where $a, b, c \in \mathbb{Z}$, and $x \in \mathbb{R}$.

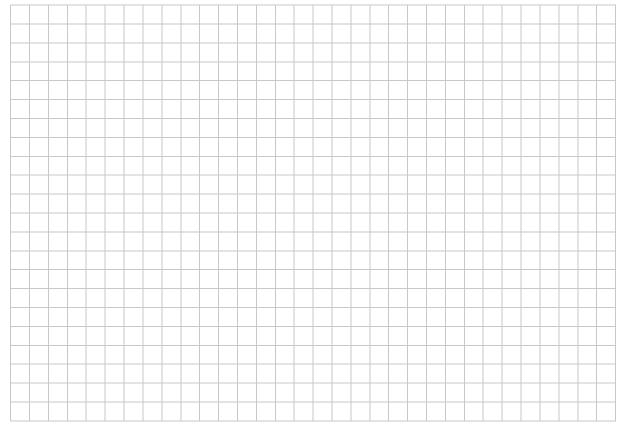
Find the value of c.

(i)



Crookhaven

- Hence, or otherwise, find the value of a and the value of b. (ii)



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