2017 Paper 1 Marking Scheme

The Left Side is the solution.

The Right Side is a breakdown of how the marks were awared

Q1	Model Solution – 25 Marks	Marking Notes
(a)	(i) BMI = $\frac{77.5}{(1.63)^2}$ = 29.169 = 29.2 [1 D.P.] (ii) $w = BMI \times h^2$ = 24 × (1.63) ² = 63.76 = 63.8 [kg] [1 D.P.]	Scale 15D (0, 7, 9, 12, 15) Accept correct answers without work. Accept correct answer without units in (ii). Low Partial Credit Work of merit in one part, for example: some correct substitution into either (i) or (ii). Mid Partial Credit (i) correct. Work of merit in both (i) and (ii). High Partial Credit Swaps 77·5 and 1·63 but finishes correctly. (ii) correct. (ii) correct and work of merit in (ii). Full Credit -1 Apply a * to incorrect rounding the first time it
(b)	Answer: less than Jo's Justification – accept: Alex is dividing the same top line as Jo by a bigger number. OR $\frac{w}{(h+0\cdot10)^2} < \frac{w}{h^2}$	Scale 10C (0, 5, 7, 10) Low Partial Credit Correct answer. Work of merit in justification, for example: attempts to substitute in particular values to check. High Partial Credit Correct answer with work of merit in justification.
	or any valid justification	 Justification fully correct. Full Credit -1 Apply a * if answer given as "Jo's BMI is greater than Alex's"

Q2	Model Solution – 20 Marks	Marking Notes
(a)	Profit = $49 - 25 = €24$	Scale 15D (0, 7, 9, 12, 15)
		Accept correct answers without work.
	(i) Mark up $=\frac{24}{25} \times 100 = 96 [\%]$	Accept correct answer without % sign (96 and 49).
	(ii) Margin $=\frac{24}{49} \times 100$ = 48.9 = $49 [\%]$ [nearest $\%$]	 Low Partial Credit Work of merit in either (i) or (ii), for example: 49 − 25; or something × 100.
		 Mid Partial Credit Work of merit in both (i) and (ii). Either (i) or (ii) correct.
		 High Partial Credit One part correct and work of merit in the other. Both correct as decimals rather than percentages (0.96 and 0.49). Calculates Margin in (i) and Mark up in (ii).
		Full Credit −1Apply a * for incorrect rounding in (ii)
(b)	Markup = $50\% = 0.5 = \frac{\text{Profit}}{\text{Cost}}$ $\Rightarrow P = 0.5C$ $\Rightarrow \text{ Selling Price (S)} = C + P = 1.5C$ $\Rightarrow \text{ Margin} = \frac{P}{S} = \frac{0.5C}{1.5C} = \frac{1}{3}$ = 33[%] [nearest %] OR $\frac{\frac{x}{2}}{x + \frac{x}{2}} \times 100 = \frac{1}{3} \times 100$ $= 33\frac{1}{3}$	Scale 5C (0, 2, 3, 5) Accept correct answer without work. Accept correct answer without % sign (33). Accept justification using particular values. Low Partial Credit Makes relevant use of 50%, for example: 150%, or 1·5, or $C = 2P$. High Partial Credit Table 1, or 0·33, or 0·3 Full Credit -1 Apply 2 * for incorrect rounding, if not
	= 33[%][nearest %]	 Apply a * for incorrect rounding, if not already applied in (a)(ii)

Q3	Model Solution – 15 Marks	Marking Notes
(a)	$868 \text{ million} = 868 \times 10^{6}$ $= 8.68 \times 10^{2} \times 10^{6}$ $= 8.68 \times 10^{8}$	Scale 5C (0, 2, 3, 5) Accept correct answer without work. Low Partial Credit Some work of merit, for example: 1 000 000, or 8.68. High Partial Credit Correct value but not in correct form, for example: 868 000 000, or 868× 10 ⁶ 8.68 × 10 ² or 8.68 × 10 ⁶
(b), (c)	(b) $1.3 \text{ secs} \rightarrow 380\ 000 \text{ km}$ $1 \text{ sec} \rightarrow \frac{380\ 000}{1.3} \text{ km}$ $1 \text{ min} \rightarrow 60 \times \frac{380\ 000}{1.3} \text{ km}$ $= 1.75 \times 10^7 \text{ [km/min]} \text{ [2 D.P.]}$ (c) $\frac{8.68 \times 10^8}{1.75 \times 10^7} = 49.6 \text{ [minutes]}$	Scale 10D (0, 4, 6, 8, 10) Accept correct answers without units. Low Partial Credit Some relevant calculation in either (b) or (c). Mid Partial Credit (b) or (c) correct Some relevant calculation in both (b) and (c). High Partial Credit One part correct and some relevant
		 calculation in the other Correct answers with no supporting work in (c) Full Credit -1 Apply a * for incorrect rounding in (b). Apply a * in (c) if candidate uses values in (c) other than their answer from (b).

Q4	Model Solution – 15 Marks	Marking Notes
(a), (b)(i)	(a) £0.7241 = £1.00 £1 = £ $\frac{1}{0.7241}$ £380 = £ $\frac{380}{0.7241}$ = £524.789 = [£]524.79 [2 D.P.] (b)(i) 3 + 7 = 10 ⇒ Juice in Fruitex = $\frac{3}{10} \times 20$ = 6 [litres]	Scale 10D (0, 4, 6, 8, 10) Accept correct answers without work. Accept correct answers without units. Low Partial Credit Some relevant calculation in either (a) or (b). Mid Partial Credit Either (a) or (b) correct. Some relevant calculation in both (a) and (b). High Partial Credit Either (a) or (b) correct, and some relevant calculation in the other part. Full Credit -1 Apply a * for incorrect rounding in (a). Apply a * in (b)(i) if the amount of water is found (14 litres), or if 6 and 14 are found but answer is not identified.
(b)(ii)	$7+8=15$ ⇒ Juice in mix $=\frac{7}{15} \times 60$ $=28$ litres ⇒ Juice in Juicy $=28-6=22$ litres ⇒ Water in Juicy $=40-22=18$ litres ⇒ Ratio of juice to water in Juicy $=22:18$ $=11:9$ OR $7:8=15$ [Ratio in mixture] ⇒ $28:32=60$ [Litres in mixture] $-6:14$ [Litres in Fruitex] $=22:18$ [Ratio in Juicy] $=11:9$. [Ratio in Juicy]	Scale 5C (0, 2, 3, 5) Low Partial Credit Work of merit using the correct ratio, for example: 7 + 8 High Partial Credit Finds 22 litres or 18 litres Correct answer without work Full Credit -1 Apply a * for ratio not in simplest form.

Q5	Model Solution – 25 Marks	Marking Notes
(a),	(a)(i) $20 + (5 \times 12) = [€] 80$	Scale 15C (0, 8, 11, 15)
(b)		Accept correct answers without work.
	(a)(ii) [€] 20 + 12 <i>n</i>	Accept correct answers without units.
		Low Partial Credit
	(b) [€] $15 + 6n$	Work of merit in one of the three parts,
		for example:
		in (a)(i): one relevant calculation; in (a)(ii): $7 + 12n$ (coefficient of n
		correct), or $20 + 9n$ (constant correct)
		High Partial Credit
		Work of merit in (a)(ii) and (b)
		• (a)(ii) or (b) correct

Mathematics

Higher Level

Q5 Model Solution - 25 Marks **Marking Notes** Interpretation 1, Method 1: (c) Scale 10D (0, 4, 6, 8, 10) $\frac{1}{4}(12n+20) + \frac{2}{3}(6n+15) = 200$ Accept correct answer without units. Accept solution using interpretation 1 or 3n + 5 + 4n + 10 = 200interpretation 2. 7n + 15 = 200If using trial and improvement, must have 7n = 185supporting work to show that the given $n = \frac{185}{7} = 26.4 \dots$ answer is the smallest number of weeks that is sufficient. i.e. 27 [weeks] OR Consider the solution as having 4 steps: **Step 1**: Sets up correct expression for Interpretation 1, Method 2: either Pete or Maeve. Starts with 5, plus 3 each week Pete: **Step 2**: Sets up correct expressions for Maeve: Starts with 10, plus 4 each week Pete and Maeve; OR Solves correctly for In total: They start with 15, plus 7 each either Pete or Maeve. week **Step 3**: Distributes the fractions correctly $\frac{200-15}{7} = 26.4 \dots$ in equation(s). Step 4: Solves equation(s). i.e. 27 [weeks] OR Low Partial Credit Interpretation 2, Method 1: • 1 step correct. Pete: $\frac{1}{4}(12n + 20) = 200$ • 12n + 20 + 6n + 15 = 200 solved correctly. 12n + 20 = 800• 12n + 20 = 200 and 6n + 15 = 200n = 65 [weeks] both solved correctly. Maeve: $\frac{2}{3}(6n+15) = 200$ Mid Partial Credit • 2 steps correct. 12n + 30 = 600High Partial Credit n = 47.5 3 steps correct. i.e. 48 [weeks] Correct answer, but without supporting OR work to show that it is the smallest **Interpretation 2, Method 2:** number of weeks that is sufficient. Starts with 5, plus 3 each week Pete: Full Credit -1 $\frac{200-5}{2} = 65$ [weeks] Apply * for incorrect / no rounding. • Apply * if $\frac{1}{4}$ and $\frac{2}{3}$ swapped. Maeve: Starts with 10, plus 4 each week $\frac{200-10}{4} = 47.5$ i.e. 48 [weeks] OR **Either Interpretation, Method 3:** Solution via trial and improvement.

Q6	Model Solution – 35 Marks	Marking Notes
(a)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Scale 15C (0, 8, 11, 15) Accept correct answer without work. Low Partial Credit 2 regions correct High Partial Credit 4 regions correct, which must include one of W only or S only, in terms of x
(b)	36 + 10 + 16 + (30 - x) = 80 $92 - x = 80$ $x = 12$	 Scale 5B (0, 2, 5) Accept correct answer without work. Partial Credit Work of merit, for example: some relevant use of 80 or x, or solves an incorrect linear equation correctly
(c)	 S1: 8 students have all 3 apps, or equivalent S2: 24 = #(I ∩ S) S3: 10 students have Instagram only, or equivalent S4: #S > #W 	Scale 15D (0, 7, 9, 12, 15) Low Partial Credit Work of merit in one of the four statements. Mid Partial Credit 2 statements correct. High Partial Credit 3 statements correct. Full Credit -1 Apply a * for a missing #, at most once.

Q7	Model Solution – 5 Marks	Marking Notes
(a), (b)	(a) Any two sets A and B for which $A \subset B$, for example: $A = \{1,2,3\}; B = \{1,2,3\}$ OR $A \qquad \qquad b \qquad \qquad b$ or any other valid example (b) Any two sets P and Q for which $P \cap Q = \{\}$, for example: $P = \{1,2,3,4\}; Q = \{5,6,7,8\}$ OR $P \qquad \qquad Q$ or any other valid example	Scale 5D (0, 2, 3, 4, 5) Low Partial Credit Work of merit in either (a) or (b), for example: in (a), indication of a set fully inside a larger set; in (b), indication of mutually exclusive sets, or some explanation of what's left in P after taking away Q Mid Partial Credit (a) or (b) correct. Work of merit in both (a) and (b). High Partial Credit (a) or (b) correct, and work of merit in the other part.

Q8	Model Solution – 30 Marks	Marking Notes
(a),	(a)	Scale 15D (0, 7, 9, 12, 15)
(b)	Answer: <i>Lecky</i>	Accept 0, 1000 and 50, 325 in (b)
	Reason: Cuts y -axis at $(0,0)$	Low Partial Credit
	OR	Work of merit in either (a) or (b), for a properties (a) are properties.
	b(x) starts at 50	for example: in (a), answer or reason correct; in (b), domain or range correct
	or any other valid reason	but in the wrong box; or a pair of values
		in either box with minimum or maximum
	(b)	correct.
	Domain: $0 \le x \le 1000$	Mid Partial Credit
	Range: $50 \le l(x) \le 325$	Work of merit in both (a) and (b)Either (a) or (b) correct
		High Partial Credit
		Either (a) or (b) correct, and work of merit in the other part.
		Full Credit –1
		Apply a * to 275 given as the range in (b)
(c)	(i) $100 < x < 800$	Scale 5D (0, 2, 3, 4, 5)
	OR	Accept tolerance of ± 20 in (i)
	"Between 100 and 800"	Note that answer to (i) must be in a valid form.
	OR	Low Partial Credit
	(100,800)	Work of merit in either (i) or (ii), for example:
	(ii) "Buzz is cheaper if the number of	in (i), 100 or 800 identified on graph;
	units used is between these two	or relevant region of graph identified;
	values."	in (ii), explanation of some merit.
	or any other valid explanation	Mid Partial CreditEither (i) or (ii) correct.
		 Either (i) or (ii) correct. Work of merit in both (i) and (ii).
		High Partial Credit
		Either (i) or (ii) correct, and work of merit in the other part.
		ment management part.

Q8	Model Solution – 30 Marks	Marking Notes
(d)	(i) Slope $=\frac{325-50}{1000-0}$ $=\frac{275}{1000}$ or 0.275 or $\frac{11}{40}$ (ii) "The cost of electricity rises by $\notin 0.275$ for every one unit increase of usage." or any other valid explanation	 Scale 10D (0, 4, 6, 8, 10) Accept: "each unit costs €0·275", or equivalent, in (ii) Low Partial Credit Work of merit in either (i) or (ii), for example: in (i), uses diagram to show understanding of slope; or Rise Rum with some substitution; or 11/20; in (ii), explanation of some merit. Mid Partial Credit Either (i) or (ii) correct. Work of merit in both (i) and (ii). High Partial Credit Either (i) or (ii) correct, and work of merit in the other part.

Q9	Model Solution – 25 Marks	Marking Notes
(a)	$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(-4)}}{2(1)}$ $x = \frac{2 \pm \sqrt{20}}{2}$ $x = 1 \pm \sqrt{5}$	Scale 10C (0, 5, 7, 10) Accept " $1 + \sqrt{5}$ and $1 - \sqrt{5}$ ". Consider the solution as having 3 steps: Step 1: Identifies a , or b , or c . Step 2: Full correct substitution into the quadratic formula. Step 3: Evaluates the quadratic formula.
(b)	$(c + \sqrt{d})^{2}$ $= (c + \sqrt{d}) \cdot (c + \sqrt{d})$ $= c^{2} + c\sqrt{d} + c\sqrt{d} + (\sqrt{d})^{2}$	Low Partial Credit • 1 step High Partial Credit • 2 steps • Correct answer without work Full Credit -1 • Apply a * for the correct answer not in surd form $(-1.236 \dots \text{ and } 3.236 \dots)$ Scale 5C (0, 2, 3, 5) Low Partial Credit • $(c + \sqrt{d}) \cdot (c + \sqrt{d})$ • c^2
	$= c^2 + 2c\sqrt{d} + d$	• $c\sqrt{d}$ High Partial Credit • $c^2 + c\sqrt{d} + c\sqrt{d} + \left(\sqrt{d}\right)^2$
(c)	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Scale 10D (0, 4, 6, 8, 10) Note that 12 answers are required. Low Partial Credit 4 answers correct Mid Partial Credit 1 row or 1 column fully correct High Partial Credit 2 rows or 2 columns fully correct

Q10	Model Solution – 10 Marks	Marking Notes
(a)	$2^{3+5+10} = 2^{18}$	Scale 5B (0, 2, 5) Accept correct answer without work. No Credit Evaluates the given number. Partial Credit Work of merit involving indices, for example: 18, 28, 213, 215
(b), (c)	(b) $8^{25} = (2^3)^{25} = 2^{75}$	Scale 5D (0, 2, 3, 4, 5) Accept correct answer without work for both parts.
(6)	(c) $\sqrt{8} = (2^3)^{\frac{1}{2}} = 2^{\frac{3}{2}}$ or $2^{1\cdot 5}$	 No Credit Evaluates the given number. Low Partial Credit Work of merit in either (b) or (c) involving indices, for example: 8 written as 2³ in (b) or (c); or a square root written as a power of 1/2 in (c). Mid Partial Credit Either (b) or (c) correct. Work of merit in both (b) and (c). High Partial Credit Either (b) or (c) correct, and work of merit in the other part.

Q11	Model Solution – 20 Marks	Marking Notes
(a)	$116 - 40 = 76$ $\frac{76}{4} = 19$ $40 - 19 = 21$ $40 + 19 = 59, \text{ etc.}$ Answer: 21, 40, 59, 78, 97, 116	 Scale 10C (0, 5, 7, 10) Accept correct answer without work. Low Partial Credit Applies knowledge of linear sequences, for example: 116–40, or indicates a common difference. High Partial Credit Finds or uses 19. Uses ⁷⁶/_n (for n ∈ N, n ≠ 4) and finishes correctly from one of the given values.
(b)	1st differences:	Scale 10C (0, 5, 7, 10) Accept correct answer without work. Accept correct sequence not written in answer boxes. Low Partial Credit Finds 2 first differences of given sequence. High Partial Credit Finds all 2nd differences of given sequence. Identifies 2 as the correct 2nd difference.

Q12	Model Solution – 35 Marks	Marking Notes
(a)	$(n-2)(n-9)$ OR n n n -2 $-2n$ So $(n-2)(n-9)$ OR $n^{2}-11n+18$ $= n^{2}-9n-2n+18$ $= n(n-9)-2(n-9)$ $= (n-9)(n-2)$	Scale 5C (0, 2, 3, 5) Accept correct answer without work. Low Partial Credit Work of merit, for example: $(n-2)$ or $(n-9)$, or any pair of factors of 18, or $n^2 - 9n - 2n + 18$. Some correct substitution into the quadratic formula High Partial Credit Factors which multiply to give 2 correct coefficients of the given expression, including the signs, for example: $(n+2)(n+9)$, or $(n-5)(n-6)$. $n(n-9)-2(n-9)$ Solves $n^2-11n+18=0$ (without factorising).
(b)	y(w-1) + 1(w-1) = $(w-1)(y+1)$ or $(1$ OR $w(y+1) - 1(y+1)$ = $(y+1)(w-1)$ or $(1$	 - w)(-y - 1) Low Partial Credit • Work of merit, for example: a common factor identified from given expression
(c)	$= \frac{5}{3(4)-2} - \frac{7}{6(4)-12}$ $= \frac{5}{10} - \frac{7}{12}$ $= -\frac{5}{60} = -\frac{1}{12} \text{ or } -0$	Scale 10B (0, 5, 10) Accept correct answer without work Partial Credit • $3(4) - 2$ or $6(4) - 12$
(d)	$\frac{(2e-3)(2e+3)}{(2e-3)(e+3)}$ $= \frac{(2e+3)}{(e+3)}$	Scale 5D (0, 2, 3, 4, 5) Low Partial Credit Work of merit in either numerator or denominator Mid Partial Credit Numerator or denominator factorised correctly High Partial Credit Numerator or denominator factorised correctly, and work of merit in the other

Q12	Model So	lution – 35 N	Marks		Marking Notes
(e)	Method 1	L:			Scale 10D (0, 4, 6, 8, 10)
	(x -	$-3)(ax^2+b^2$	bx + c)		Accept $2x^2 - 7x + 4$ as answer. Low Partial Credit
	$= ax^3 + bx^2 + cx - 3ax^2 - 3bx - 3c$			3bx - 3c	 Multiplication set up (Method 1) Division set up (Method 2) Array set up (Method 3) with either 2x³ or -12 placed correctly Mid Partial Credit 1 coefficient correct
	x^3 term: $a=2$ constant: $c=4$ x^2 term: $b-3a=-13$				
	x term.	b - 3a = -13 b = -13 + 3(2) = -7		-7	High Partial Credit • 2 coefficients correct
		OR Method 2:			Correct answer without work
	$2x^2 - 7x + 4$ $x - 3\sqrt{2x^3 - 13x^2 + 25x - 12}$				
	$\frac{2x^3 - 6x^2}{5x^2 + 35}$				
	$-7x^2 + 25x - 12$				
		$\frac{-7x^2 + 21x}{4x - 12}$			
	$\frac{4x-12}{4x-12}$				
	0 $\Rightarrow a = 2, b = -7, c = 4$ OR				
	Method 3:				
		$2x^2$	-7x	4	
	x	$2x^3$	$-7x^{2}$	4 <i>x</i>	
	-3	$-6x^{2}$	21 <i>x</i>	-12	
	$\Rightarrow a = 2, b = -7, c = 4$				

Q13 Model Solution – 15 Marks

Marking Notes

Scale 15D (0, 7, 9, 12, 15)

Points on y = x - 1 are (-2, -3) and (2, 1).

Low Partial Credit

4 y
3 - 2 -1 1 2 x

 Work of merit for 1 graph, for example: 1 point found, with supporting work; or y-intercept correct; or slope correct for line; or two points correct on graph.

Mid Partial Credit

- 1 correct graph **and** work of merit on 1 other graph.
- Work of merit on all 3 graphs.

High Partial Credit

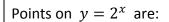
- 2 correct graphs and work of merit on 3rd
- 5 points plotted for all 3 graphs

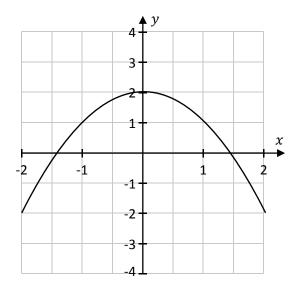
Full Credit -1

• Apply a * for one point incorrectly plotted

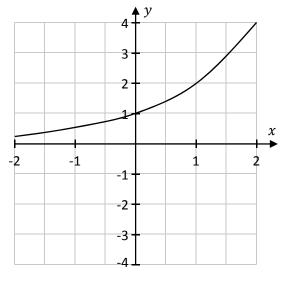
Points on $y = 2 - x^2$ are: (-2,-2); (-1,1); (0,2); (1,1); (2,-2).

-3 -





(-2,0.25); (-1,0.5); (0,1); (1,2); (2,4).



Q14	Model Solution – 20 Marks	Marking Notes
(a), (c)	(a) $360 + 180 = 540^{\circ}$ $540 + 180 = 720^{\circ}$ (c) $\frac{360}{4} = 90^{\circ}$	Scale 10D (0, 4, 6, 8, 10) Accept correct answers without units (degree symbol). Low Partial Credit 1 of the 5 values correct.
	$\frac{\frac{540}{5}}{\frac{720}{6}} = 120^{\circ}$	Mid Partial Credit • (a) or (c) correct. High Partial Credit
(b)	180(n-2) [degrees]	 (a) or (c) correct, and 1 value correct in the other part. Scale 5B (0, 2, 5)
	OR $180n-360$ [degrees]	Accept correct answer without units. Accept correct formula in words. Partial Credit Work of merit, for example: 180n, or 360n - 360.
(d)	$\frac{180(n-2)}{n} \text{ [degrees]}$ $\frac{\mathbf{OR}}{n}$ $\frac{180n-360}{n} \text{ [degrees]}$	Scale 5B (0, 2, 5) Accept correct answer without units. Accept correct formula in words. Partial Credit Work of merit, for example: $\frac{k}{n}$, $k \in \mathbb{R}$.

Q15	Model Solution – 5 Marks	Marking Notes
	Answer: C	Scale 5B (0, 2, 5)
	Reason: Some x values have more than one y value or any other valid reason	 Partial Credit C identified as answer Shows understanding of the relevant feature of a function, for example: vertical line drawn.