

Paper 1: Marking Scheme 2016

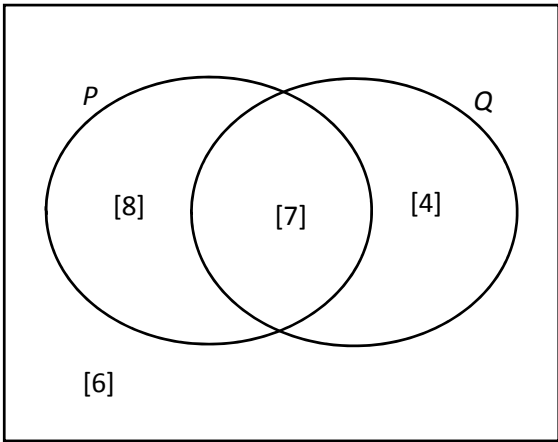
The Left Side shows the solution.

The Right Side shows how marks were awarded.

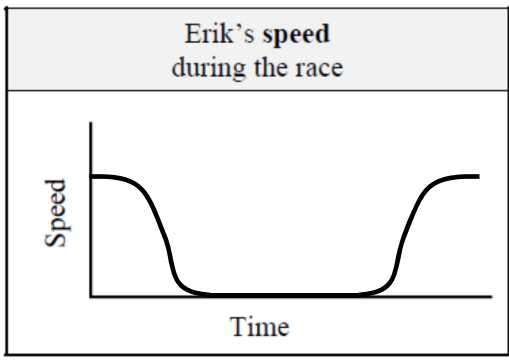
Q1	Model Solution – 30 Marks	Marking Notes
(a)(i)	$17 \times 1.06 = \text{€}18.02$ OR $6\% = \text{€}1.02$ $106\% = \text{€}17 + \text{€}1.02$ $= \text{€}18.02$	Scale 10B (0, 4, 10) Accept correct answer without work. Accept answer without € sign. <i>Partial Credit</i> <ul style="list-style-type: none"> Shows understanding of percentages e.g. 0.06, $\frac{3}{50}$, 94% Finds increase (i.e. 1.02) <i>Full Credit –1</i> <ul style="list-style-type: none"> Subtracts $\text{€}1.02$ (i.e. finds decrease instead of increase)
(a)(ii)	$\frac{18.02 - 17}{18.02} \times 100$ $= \frac{1.02}{18.02} \times 100$ $= 5.66\ldots$ $= 5.7\% [1 \text{ DP}]$ OR $100 - \left(\frac{17}{18.02} \times 100 \right)$ $= 5.7\% [1 \text{ DP}]$	Scale 5C (0, 2, 4, 5) Accept correct answer without work. <i>No Credit</i> <ul style="list-style-type: none"> Answer of 6% with no supporting work <i>Low Partial Credit</i> <ul style="list-style-type: none"> One relevant operation, e.g. $17/18.02$, $18.02 - 17$, etc. One relevant operation with $\text{€}17$ as the base price, e.g. $18.02/17$, etc. <i>High Partial Credit</i> <ul style="list-style-type: none"> $1.02/18.02$ $(17/18.02) \times 100$ Finds reduction as a percentage of $\text{€}17$ (i.e. answer of 6%) with supporting work
(b)	(i) $(5 + 4) \times (2 + 3) = 45$ (ii) $5 + 4 \times (2 + 3) = 25$ (iii) $(5 + 4) \times 2 + 3 = 21$	Scale 15C (0, 5, 12, 15) Accept correct answer without work. <i>Low Partial Credit</i> <ul style="list-style-type: none"> One part correct Calculations that imply correct brackets in one part, e.g. $9 \times 5 = 45$ in (i) <i>High Partial Credit</i> <ul style="list-style-type: none"> Two parts correct

Q2	Model Solution – 20 Marks	Marking Notes
(a)	<p>(i) $\frac{0.20}{20} = \frac{1}{100}$</p> <p>(ii) $\frac{0.5}{200} = \frac{1}{400}$</p>	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept correct answer without work.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> One conversion correct e.g. €20 = 2000c Makes fraction with relevant numbers e.g. 20/20 or 0.5/2 <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> One part correct Both conversions correct <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Answer as a percentage or a decimal
(b)(i)	<p>Brand A is cheaper.</p> <p>Brand A: $3.60/2 = €1.80$ per litre</p> <p>Brand B: $1.50/0.75 = €2.00$ per litre</p> <p style="text-align: center;">OR</p> <p>Brand A: $3.60/8 = €0.45$ per 250ml</p> <p>Brand B: $1.50/3 = €0.50$ per 250ml</p> <p style="text-align: center;">OR</p> <p>Brand A: $(3.60/8) \times 3 = €1.35$ per 750ml</p> <p style="text-align: center;">OR</p> <p>Brand B: $(1.50/3) \times 8 = €4$ per 2 litre</p> <p style="text-align: center;">OR</p> <p>Brand A: $2/3.60 = 0.55...$ litre per €</p> <p>Brand B: $0.75/1.50 = 0.5$ litre per €</p>	<p>Scale 10B (0, 4, 10)</p> <p>Accept cost per same amount for both brands, e.g. per 250 ml, per 2 litres, etc. This may require only 1 conversion (A or B).</p> <p><i>Partial Credit</i></p> <ul style="list-style-type: none"> One relevant calculation Some correct conversion Correct answer with no work <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Working out fully correct, but no statement or incorrect statement

Q2	Model Solution – 20 Marks	Marking Notes
(b)(ii)	<p>Lowest price = €9·60</p> <p>$3 \times A = €10·80$</p> <p>$(2 \times A) + (2 \times B) = €10·20$</p> <p>$(1 \times A) + (4 \times B) = €9·60$</p> <p>$7 \times B = €10·50$</p>	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept answer without € sign.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Price of one combination worked out (not necessarily ≥ 5 litres) • Uses price per litre from b(i) • States: 1 Brand A and 4 Brand B <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Price of two correct combinations worked out • Correct answer with no other work <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> • €9·60 given as answer, and the price of one other relevant combination found • Price of all four combinations worked out, lowest not identified

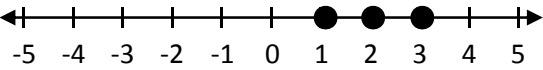
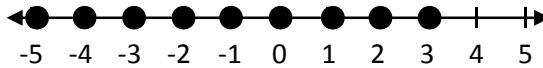
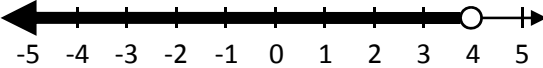
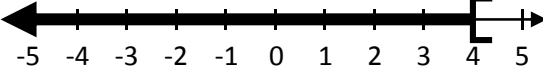
Q3	Model Solution – 10 Marks	Marking Notes
		<p>Scale 10C (0, 3, 8, 10)</p> <p>Accept correct answer without work.</p> <p>Treat solution as requiring three steps:</p> <p>Step 1: Finds $\#(P \cap Q)$</p> <p>Step 2: Splits value in the ratio 2 : 1</p> <p>Step 3: Fill in the Venn diagram ($\#U$ must equal 25, and [6] must be correct)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Relevant work in any step • 1 step correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Any 2 steps correct (excluding case where $\#(P \setminus Q) = 2$ and $\#(Q \setminus P) = 1$)

Q4	Model Solution – 5 Marks	Marking Notes
	<ol style="list-style-type: none"> 1. Always true 2. Sometimes true 3. Always true 4. Never true 5. Sometimes true 	<p>Scale 5D (0, 2, 3, 4, 5)</p> <p>Accept correct answer without work.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Relevant work on a Venn diagram • 1 correct <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • 2 correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • 4 correct

Q5	Model Solution – 25 Marks	Marking Notes
(a)	<p>(i) $\frac{\text{Distance}}{\text{Time}} = \frac{300}{60} = 5 \text{ m/s}$</p> <p>(ii) $\frac{\text{Distance}}{\text{Time}} = \frac{100}{40} = \frac{5}{2}$ or 2.5 m/s</p>	<p>Scale 10C (0, 3, 8, 10)</p> <p>Accept correct answer without units.</p> <p>In (i) accept $\frac{300}{60}$ or similar (i.e. unsimplified)</p> <p>In (ii) accept correct answer without work.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • A correct relevant formula • Correct distance or time for either (i) or (ii) • Relevant work on graph <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • (i) or (ii) correct <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> • (i) correct and answer not fully simplified in (ii)
(b)	<p>1. Claire</p> <p>2. Bill</p> <p>3. Dee</p>	<p>Scale 10C (0, 3, 8, 10)</p> <p>Accept correct answer without work.</p> <p><i>No Credit</i></p> <ul style="list-style-type: none"> • Same answer in all 3 boxes <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • 1 part correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • 2 parts correct
(c)		<p>Scale 5B (0, 2, 5)</p> <p>Accept correct answer without work.</p> <p><i>Partial Credit</i></p> <ul style="list-style-type: none"> • 1 section of graph correct (speed decreasing or speed = 0 or speed increasing) • Graph touches the time axis when Erik has stopped • Indicates an understanding of speed on the given distance/time graph

Q6	Model Solution – 20 Marks	Marking Notes
(a)	$3 \cdot 14, \pi, \frac{22}{7}, \sqrt{10}$ OR $3 \cdot 14, 3 \cdot 141..., 3 \cdot 142..., 3 \cdot 16...$	<p>Scale 10C (0, 3, 8, 10)</p> <p>Accept correct answer without work.</p> <p>Accept correct answer in decimal form (as long as values are distinguishable).</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Any two consecutive numbers in the correct increasing order. A relevant approximation of any one of the numbers. <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> Three numbers in increasing order with supporting work. Numbers not ordered, but π and $\frac{22}{7}$ to at least 3 decimal places and $\sqrt{10}$ to at least 2 decimal places. <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Numbers in decreasing order.
(b)	<p>$\sqrt{10}$: Irrational</p> <p>It cannot be written as a fraction using only integers or It goes on forever without repeating as a decimal or any other equivalent reason</p> <p>$3 \cdot 14$: Rational</p> <p>It can be written as a fraction using only integers [e.g. $\frac{314}{100}$] or It doesn't go on forever without repeating as a decimal or any other equivalent reason</p>	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept "It can/cannot be written as a fraction" or "It does/doesn't go on forever as a decimal", as appropriate.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> 1 part (tick or reason) correct Defines a rational or irrational number Both correctly identified but no reason or incorrect reasons given <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> 1 tick and corresponding reason correct

Q6	Model Solution – 20 Marks	Marking Notes
(c)	<p>Answer: 101</p> <p>Justification: $3 \cdot 14 \times 10^2 = 314$, so power = 2 \Rightarrow 2+1 = 3 digits or any other valid justification</p>	<p>Scale 5B (0, 2, 5)</p> <p><i>Partial Credit</i></p> <ul style="list-style-type: none"> • Correct answer (i.e. 101) • Relevant example • Shows understanding of scientific notation

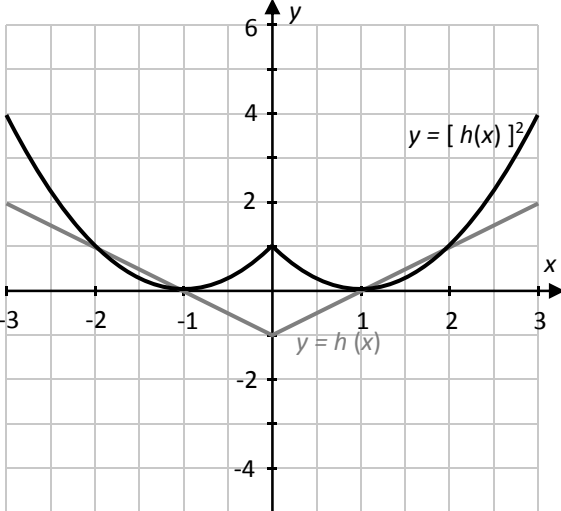
Q7	Model Solution – 15 Marks	Marking Notes
(a)	$\frac{2(2x+4)}{6} - \frac{3(5x-7)}{6} = 5$ $\Rightarrow \frac{4x+8-15x+21}{6} = 5$ $\Rightarrow \frac{-11x+29}{6} = 5$ $\Rightarrow -11x + 29 = 30$ $\Rightarrow -11x = 1$ $\Rightarrow x = -\frac{1}{11} \text{ or equivalent}$	<p>Scale 10D (0, 2, 4, 8, 10)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Any work of merit, e.g. 3(2), 6 (or any multiple of 6), 2(2x+4), 3(5x-7) <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • $\frac{2(2x+4)-3(5x-7)}{6} = 5$ • $\frac{2(2x+4)}{6} - \frac{3(5x-7)}{6} = 5$ • $\frac{6(2x+4)}{3} - \frac{6(5x-7)}{2} = 6(5)$ <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Correct linear equation without fractions and with brackets distributed. • $4x + 8 - 15x + 21 = 30$, or equivalent. • Correct answer without work.
(b)	<p>(i)</p>  <p>(ii)</p>  <p>(iii)</p>  <p style="text-align: center;">OR</p> 	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept 0 as an element in (i). Accept correct answer without work.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • One graph correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Two graphs correct <p><i>Full Credit – 1</i></p> <ul style="list-style-type: none"> • 4 included in one or more solutions, otherwise all parts fully correct

Q8	Model Solution – 30 Marks	Marking Notes																																													
(a)	<div><table><tr><td></td><td></td><td></td><td></td><td>X</td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>X</td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>X</td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>X</td><td></td><td></td><td></td><td></td></tr><tr><td>X</td><td>X</td><td>X</td><td>X</td><td>X</td><td>X</td><td>X</td><td>X</td><td>X</td></tr></table></div>					X									X									X									X					X	X	X	X	X	X	X	X	X	<p>Scale 10B (0, 4, 10)</p> <p>Accept diagram with boxes, or X s, or both.</p> <p><i>Partial Credit</i></p> <ul style="list-style-type: none">Similar shape to previous stages, as long as the sequence is increasing
				X																																											
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X	X	X	X	X	X	X	X	X																																							
(b)	<p>$N = 4 + 3 S$</p> <p>OR</p> <table><tr><th>Stage(S)</th><th>Number(N)</th></tr><tr><td>0</td><td>$4 + 0(3)$</td></tr><tr><td>1</td><td>$4 + 1(3)$</td></tr><tr><td>2</td><td>$4 + 2(3)$</td></tr><tr><td>3</td><td>$4 + 3(3)$</td></tr><tr><td>.</td><td>.</td></tr><tr><td>.</td><td>.</td></tr><tr><td>S</td><td>$4 + 3(S)$</td></tr></table> <p>$N = 4 + 3 S$</p>	Stage(S)	Number(N)	0	$4 + 0(3)$	1	$4 + 1(3)$	2	$4 + 2(3)$	3	$4 + 3(3)$	S	$4 + 3(S)$	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept correct answer without work.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none">Number of Xs written down for any stage from 0 to 3 or beyond.Identifies common differenceIdentifies the first termAny linear graph or formula, or mentions ‘linear’Relevant formula, e.g. $T_n = a + (n - 1)d$, or $y = mx + c$ <p><i>High Partial Credit</i></p> <ul style="list-style-type: none">Starts with $T_1 = 4$, finishes correctly (i.e. $N = 1 + 3 S$, or equivalent)$y = 1 + 3x$Formula in the correct form with either the constant term or the coefficient of S correct i.e. $N = 4 + pS$ or $N = q + 3S$ <p><i>Full Credit –1</i></p> <ul style="list-style-type: none">Swaps N and S (i.e. $S = 4 + 3 N$)Uses different variables, without defining them e.g. $y = 4 + 3x$$4 + 3S$																													
Stage(S)	Number(N)																																														
0	$4 + 0(3)$																																														
1	$4 + 1(3)$																																														
2	$4 + 2(3)$																																														
3	$4 + 3(3)$																																														
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S	$4 + 3(S)$																																														

Q8	Model Solution – 30 Marks	Marking Notes
(c)	$4 + 3k = 130$ $3k = 126$ $k = 42$	Scale 10B (0, 4, 10) Accept correct answer without work <i>Partial Credit</i> <ul style="list-style-type: none"> • Some attempt at trial and error • Extends sequence towards 130 • Substitutes values into formula • Sets answer from (b) equal to 130
(d)	(i) <i>Any configuration where the number of Xs is 1, 3, and 5, respectively.</i> (ii) $p + 6$	Scale 5C (0, 2, 4, 5) Accept correct answer without work. <i>Low Partial Credit</i> <ul style="list-style-type: none"> • Any 3 terms of a linear sequence with common difference of 2 • Any one stage correct in (i) • Indicates that the first difference is 2 • Work of merit in (ii) <i>High Partial Credit</i> <ul style="list-style-type: none"> • (i) or (ii) correct (patterns must be drawn in (i) for it to be taken as correct)

Q9	Model Solution – 20 Marks	Marking Notes
(a)	(i) 3^2 (ii) 3^0 (iii) $3^{3/2}$ (iv) $3^{-1/3}$	Scale 10D (0, 2, 4, 8, 10) Accept correct answer without work. <i>Low Partial Credit</i> <ul style="list-style-type: none"> Any work of merit e.g. $3\sqrt{3}$, $3^{\frac{1}{3}}$, 3×3, $3^{\frac{2}{3}}$ 1 part correct <i>Mid Partial Credit</i> <ul style="list-style-type: none"> 2 parts correct <i>High Partial Credit</i> <ul style="list-style-type: none"> 3 parts correct
(b)	$16n^4$	Scale 5B (0, 2, 5) Accept correct answer without work <i>Partial Credit</i> <ul style="list-style-type: none"> Any work of merit e.g. n^4, ± 16, $(-2n)(-2n)$ or -2^4
(c)	$x = -1$ and $\sqrt{x^2} = 1$ <i>or any other negative value of x, with the corresponding value of $\sqrt{x^2} = x$.</i>	Scale 5B (0, 2, 5) Accept a description in place of an example, e.g. "if x is a negative number, then $\sqrt{x^2}$ is the positive of that" <i>Partial Credit</i> <ul style="list-style-type: none"> x = any negative value and no work or incorrect work on $\sqrt{x^2}$ x = any non-negative value and $\sqrt{x^2}$ = the same non-negative value

Q10	Model Solution – 15 Marks	Marking Notes																								
(a)	<p>(i)</p> <table><tr><td>x</td><td>-3</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>$f(x)$</td><td>-2</td><td>0</td><td>2</td><td>4</td><td>2</td><td>0</td><td>-2</td></tr><tr><td>$f(x) - 2$</td><td>-4</td><td>-2</td><td>0</td><td>2</td><td>0</td><td>-2</td><td>-4</td></tr></table> <p>(ii)</p>	x	-3	-2	-1	0	1	2	3	$f(x)$	-2	0	2	4	2	0	-2	$f(x) - 2$	-4	-2	0	2	0	-2	-4	<p>Scale 10C (0, 3, 8, 10)</p> <p>Accept correct answer (i.e. table and graph fully correct) without work.</p> <p>Treat solution as requiring three steps:</p> <p>Step 1. Completing $f(x)$ row</p> <p>Step 2. Completing $f(x) - 2$ row</p> <p>Step 3. Plotting the graph of $f(x) - 2$</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none">• 4 values of $f(x)$ filled in correctly• 1 correct value for $f(x) - 2$• Graph in correct shape without work• One step correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none">• Two steps correct• Correct graph (as per solution) without work <p><i>Full Credit –1</i></p> <ul style="list-style-type: none">• All correct except one value from table or graph• Table and graph fully correct for $f(x) + k$, where $k \neq -2$
x	-3	-2	-1	0	1	2	3																			
$f(x)$	-2	0	2	4	2	0	-2																			
$f(x) - 2$	-4	-2	0	2	0	-2	-4																			

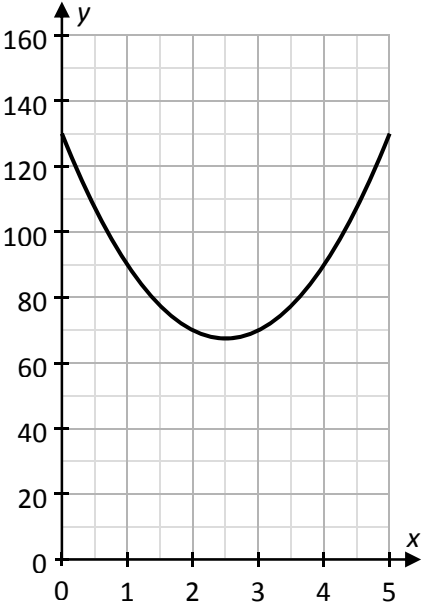
Q10	Model Solution – 15 Marks	Marking Notes																
(b)	<p>(i)</p> <table><tr><td>x</td><td>-3</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>$h(x)$</td><td>2</td><td>1</td><td>0</td><td>-1</td><td>0</td><td>1</td><td>2</td></tr></table> <p>(ii)</p> 	x	-3	-2	-1	0	1	2	3	$h(x)$	2	1	0	-1	0	1	2	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept correct answer (i.e. table and graph fully correct) without work.</p> <p>No credit for graph from work of no merit</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none">• 4 values of $h(x)$ filled in correctly• 1 correct value for $[h(x)]^2$ calculated <p><i>High Partial Credit</i></p> <ul style="list-style-type: none">• 4 values of $[h(x)]^2$ calculated, for the given x values• 4 points correctly plotted and joined, as per solution• All 7 points correctly plotted as per solution, but not joined or joined incorrectly <p><i>Full Credit –1</i></p> <ul style="list-style-type: none">• All correct except one value from table or graph
x	-3	-2	-1	0	1	2	3											
$h(x)$	2	1	0	-1	0	1	2											

Q11	Model Solution – 25 Marks	Marking Notes									
(a)(i)	$(x+5)(x+5)$ $= x^2 + 5x + 5x + 25$ $= x^2 + 10x + 25$ <p style="text-align: center;">OR</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td></td><td>x</td><td>$+5$</td></tr> <tr> <td>x</td><td>x^2</td><td>$5x$</td></tr> <tr> <td>$+5$</td><td>$5x$</td><td>25</td></tr> </table> $x^2 + 10x + 25$		x	$+5$	x	x^2	$5x$	$+5$	$5x$	25	<p>Scale 5B (0, 2, 5)</p> <p>Accept correct answer without work.</p> <p><i>Partial Credit</i></p> <ul style="list-style-type: none"> Any correct relevant multiplication $x(x+5) + 5(x+5)$ or grid set up properly Shows understanding of distribution <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> $x^2 + 5x + 5x + 25$ or grid filled in correctly
	x	$+5$									
x	x^2	$5x$									
$+5$	$5x$	25									
(a)(ii)	$x^2 + 10x + 25 - (x^2 - 10x + 25)$ $= x^2 + 10x + 25 - x^2 + 10x - 25$ $= 20x$ $= 4(5x)$ <p style="text-align: center;">OR</p> $(x+5+x-5)(x+5-(x-5))$ $= (2x)(10)$ $= 20x, \text{ which is divisible by 4.}$	<p>Scale 5C (0, 2, 4, 5)</p> <p>Oversimplification because of incorrect work in (a)(i) merits <i>Low Partial Credit</i> at most</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Any correct relevant multiplication Substitutes some value for x and shows the result is divisible by 4 Indicates or shows understanding of difference of 2 squares $2x$ or 10 calculated correctly <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> All terms correctly multiplied, including signs $(2x)(10)$ <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Failure to make final statement Getting to the line $20x$. 									
(b)(i)	$(5x)^2 - (7n)^2$ $= (5x+7n)(5x-7n)$ <p style="text-align: center;">OR</p> $(-5x-7n)(7n-5x)$	<p>Scale 10C (0, 3, 8, 10)</p> <p>Accept correct answer without work.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Indicates or shows understanding of difference of 2 squares $5x$ or $7n$ appears 5 and 7 appear <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> Correct, other than sign errors $(5x)^2 - (7n)^2$ $5x+7n$ or $5x-7n$ 									

Q11	Model Solution – 25 Marks	Marking Notes									
(b)(ii)	$(2x + 3)(x - 6)$ <p style="text-align: center;">OR</p> <p>Guide Number = $2 \times (-18) = -36$</p> $2x^2 - 12x + 3x - 18$ $= 2x(x - 6) + 3(x - 6)$ $= (2x + 3)(x - 6)$ <p style="text-align: center;">OR</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td></td><td style="text-align: center;">$2x$</td><td style="text-align: center;">$+3$</td></tr> <tr> <td style="text-align: center;">x</td><td style="border: 1px solid black; padding: 5px;">$2x^2$</td><td style="border: 1px solid black; padding: 5px;">$3x$</td></tr> <tr> <td style="text-align: center;">-6</td><td style="border: 1px solid black; padding: 5px;">$-12x$</td><td style="border: 1px solid black; padding: 5px;">-18</td></tr> </table> $(2x + 3)(x - 6)$		$2x$	$+3$	x	$2x^2$	$3x$	-6	$-12x$	-18	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept correct answer without work.</p> <p><i>No Credit</i></p> <ul style="list-style-type: none"> • () () <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Some work of merit, e.g. factorises $2x^2$ or 18 or finds / factorises 36 • Any correct substitution into the quadratic formula <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • $2x(x - 6) + 3(x - 6)$ • $x(2x + 3) - 6(2x + 3)$ • Answer given multiplies out to give two correct terms (including signs) • Solves correctly $2x^2 - 9x - 18 = 0$ (i.e. $x = 6$ and $x = -\frac{3}{2}$)
	$2x$	$+3$									
x	$2x^2$	$3x$									
-6	$-12x$	-18									

Q12	Model Solution – 25 Marks	Marking Notes
(a) E1&E2	E1: $y + 5 = 19$ $y = 14$ E2: $2y^2 + 1 = 19$ $2y^2 = 18$ $y^2 = 9$ $y = 3$ [as $y > 0$]	Scale 15D (0, 4, 9, 13, 15) Accept correct answers without work <i>Low Partial Credit</i> <ul style="list-style-type: none"> Sets up one equation <i>Mid Partial Credit</i> <ul style="list-style-type: none"> Sets up two equations Solves E1 <i>High Partial Credit</i> <ul style="list-style-type: none"> Solves E2 Solves E1 and work of merit in solving E2 (must make at least one correct transposition)
(a) E3	E3: $2y^2 + 1 = y + 5$ $2y^2 - y - 4 = 0$ $y = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(2)(-4)}}{2(2)}$ $= \frac{1 \pm \sqrt{33}}{4}$ $= 1.686... \text{ [as } y > 0]$ $= 1.69 \text{ [2 DP]}$	Scale 5D (0, 2, 3, 4, 5) Accept “1.69” verified in both relevant expressions or subbed into E3 Consider solution as requiring 4 steps: Step 1. Sets up the equation with LHS = 0 Step 2. Writes down the quadratic formula or identifies a , b , and c Step 3. Correct substitution into the quadratic formula Step 4. Evaluates to 2 decimal places <i>Low Partial Credit</i> <ul style="list-style-type: none"> 1 step correct <i>Mid Partial Credit</i> <ul style="list-style-type: none"> 2 steps correct <i>High Partial Credit</i> <ul style="list-style-type: none"> 3 steps correct (assume steps 1 and 2 are done if step 3 is correct) <i>Full Credit –1</i> <ul style="list-style-type: none"> Answer left in surd form, i.e. $\frac{1 \pm \sqrt{33}}{4}$, or rounded incorrectly
(b)	If 1st bag = 19 kg, then $y = 14$ so 3rd bag $\neq 19$ kg or any other valid explanation	Scale 5A(0, 5) Accept: “All three y values are different”, “If two weights are the same, the other must be different”, etc.

Q13	Model Solution – 15 Marks	Marking Notes
	$\text{Area } ABC = 12a^2$ $\Rightarrow \frac{1}{2}(6a) \cdot AC = 12a^2$ $\Rightarrow AC = 4a$ $\begin{aligned} \text{Area of square} &= BC ^2 \\ &= AB ^2 + AC ^2 \quad [\text{Pyth Thm}] \\ &= (6a)^2 + (4a)^2 \\ &= 36a^2 + 16a^2 \\ &= 52a^2 \end{aligned}$	<p>Scale 15D (0, 4, 9, 13, 15)</p> <p>Accept correct answer without work. Treat solution as requiring four steps:</p> <p>Step 1. Formula for the area of a triangle Step 2. Finding AC Step 3. Substitution into Pythagoras' Thm Step 4. Finish to find the area of BDEC</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • 1 step correct • Relevant formula: Pythagoras Theorem, area of a square, area of a rectangle <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • 2 steps correct (if Step 2 is done then assume Step 1 is also done) <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • 3 steps correct (if Step 3 is done then assume Step 1 & Step 2 are also done)

Q14	Model Solution – 45 Marks	Marking Notes
(a)		<p>Scale 15D (0, 4, 9, 13, 15)</p> <p>Accept correct graph without work.</p> <p>Award a linear graph at most <i>Low Partial Credit</i>.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Some work of merit, e.g. some correct substitution for x in $h(x)$. <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> $h(x)$ evaluated correctly for any three values of $x \in \{0,1,2,3,4,5\}$ (Accept points shown on the graph) <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> 6 points on the graph of $h(x)$ plotted correctly. 5 points on the graph of $h(x)$ plotted and joined correctly <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Curve with a flat bottom, otherwise correct
(b)	<p>(i) 130 cm</p> <p>(ii) 67.5 cm</p> <p>(iii) 2.5 hours</p>	<p>Scale 15C (0, 5, 12, 15)</p> <p>Accept correct answers without work.</p> <p>Accept answers taken from either the graph or the function</p> <p>In (ii), tolerance of ± 3 units on y-axis, but not in next box up or down.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> 1 part correct Relevant line on graph (either a vertical line from the lowest point or a horizontal line from the lowest point) <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> 2 parts correct <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Unit(s) incorrect or omitted, otherwise fully correct

Q14	Model Solution – 45 Marks	Marking Notes
(c) (i)&(ii)	<p>Method 1</p> <p><i>Part (i)</i></p> <p>(0, 180):</p> $a(0)^2 + b(0) + c = 180 \quad [\text{E1}]$ $\Rightarrow c = 180$ <p><i>Part (ii)</i></p> <p>(3, 0):</p> $a(3)^2 + b(3) + 180 = 0 \quad [\text{E2}]$ $\Rightarrow 9a + 3b = -180$ $\Rightarrow 3a + b = -60$ <p>(6, 180):</p> $a(6)^2 + b(6) + 180 = 180 \quad [\text{E3}]$ $\Rightarrow 36a + 6b = 0$ $\Rightarrow 6a + b = 0$ <p>E3 – E2:</p> $\Rightarrow 3a = 60$ $\Rightarrow a = 20$ <p>E2: $b = -60 - 3(20)$</p> $\Rightarrow b = -120$ <p style="text-align: center;">OR</p> <p>Method 2</p> <p>Quadratic has 2 roots at $x = 3$</p> $\Rightarrow g(x) = a(x - 3)^2$ $= a(x^2 - 6x + 9)$ $= ax^2 - 6ax + 9a$ <p>(0, 180):</p> $a(0)^2 - 6a(0) + 9a = 180$ $\Rightarrow a = 20$ $\Rightarrow g(x) = 20x^2 - 120x + 180$ <p>i.e. $a = 20, b = -120, c = 180$</p> <p style="text-align: center;">OR</p>	<p>15D (0, 4, 9, 13, 15)</p> <p>Accept correct answers without work.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Work of merit, e.g. identifies (0,180), (3,0), or (6,180); relevant substitution in $g(x)$; relates c to y-intercept; attempt at relevant shifting of graph; <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • Finds $c = 180$ • Finds E1 and E2 and E3 • Finds $a = 20$ • $(x - 3)^2$ <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Finds c and E2 and E3 • $20(x - 3)^2$ • Finds a or b, having found c

Q14	Model Solution – 45 Marks	Marking Notes
(c) (i)&(ii) cntd	<p>Method 3</p> <p>The shifted quadratic graph through (0,0) and (3,180) is of the form $y = ax^2$</p> $\Rightarrow a(3)^2 = 180$ $\Rightarrow a = 20$ <p>Shift quadratic 3 units back to the right:</p> $\begin{aligned}\Rightarrow g(x) &= 20(x - 3)^2 \\ &= 20(x^2 - 6x + 9) \\ &= 20x^2 - 120x + 180\end{aligned}$ <p>i.e. $a = 20, b = -120, c = 180$</p>	See previous page.